

## Positron Annihilation Spectroscopy - A non-destructive method for material testing -

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# Positron Annihilation Spectroscopy

## - A non-destructive method for material testing -

M. Butterling, W. Anwand, K. Potzger, A. Wagner

- Basics about Positron Annihilation Spectroscopy (PAS)
  - The Positron
  - Utility of positrons for spectroscopy
- Measurements
  - Positron lifetime
  - Doppler broadening
  - Depth-resolved defect profiling
- Technical hints of PAS
- First measurements within the DETI.2 project



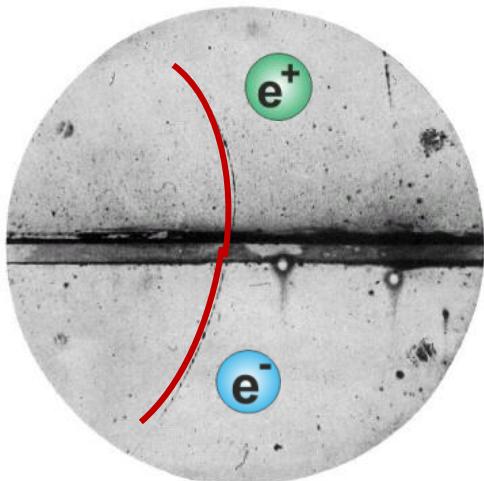
# The Positron

antiparticle of the electron:

- same mass  $m_e$
- spin  $\frac{1}{2}$
- opposite electric charge  $+e$
- annihilation with an electron by emitting photons



P.A.M Dirac (1928) and C.D. Anderson (1932)



MARCH 15, 1933

PHYSICAL REVIEW

VOLUME 43

## The Positive Electron

CARL D. ANDERSON, *California Institute of Technology, Pasadena, California*

(Received February 28, 1933)

Out of a group of 1300 photographs of cosmic-ray tracks in a vertical Wilson chamber 15 tracks were of positive particles which could not have a mass as great as that of the proton. From an examination of the energy-loss and ionization produced it is concluded that the charge is less than twice, and is probably exactly equal to, that of the proton. If these particles carry unit positive charge the

curvatures and ionizations produced require the mass to be less than twenty times the electron mass. These particles will be called positrons. Because they occur in groups associated with other tracks it is concluded that they must be secondary particles ejected from atomic nuclei.

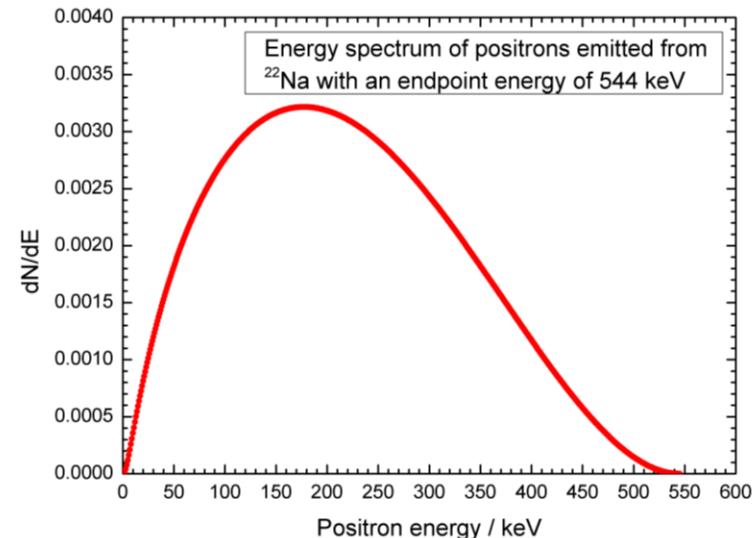
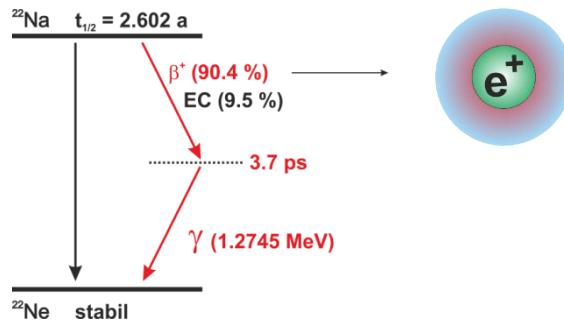
*Editor*



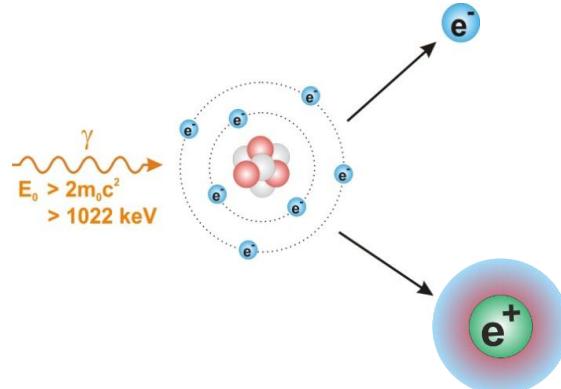
# The Positron

## Generation methods

### $\beta^+$ decay of $^{22}\text{Na}$



### pair production



$$E_{\text{gamma}} \rightarrow (m_{\text{elec}}c^2 + E_{\text{kin,positron}}) + (m_{\text{pos}}c^2 + E_{\text{kin,electron}})$$

$$E_{\text{gamma}} \geq 2 \cdot m_0 c^2 \geq 2 \cdot 511 \text{ keV}$$

# The Positron

## Thermalization and Diffusion

### Thermalization

- energy transfer to target atoms/molecules via inelastic scattering
- within a few ps
- leads to an energy dependent penetration depth profile
  
- in metals: excitation of conduction electrons
- in semiconductors: excitation of electron-hole pairs with  $E >$  bandgap width

### Diffusion

- behaviour of charged particles
- repelled from the nuclei
- largest position probability in interstitial regions



# Utility of positron for spectroscopy

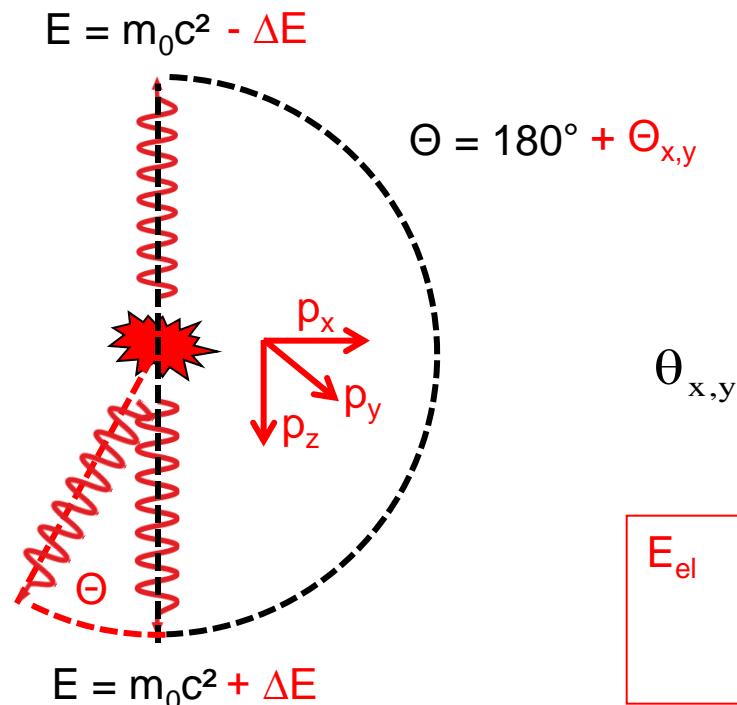
## Annihilation of positrons – information from annihilation photons

$$\Delta E = \frac{(p_z^{\text{el}} + p_z^{\text{pos}}) \cdot c}{2}$$

Positron is thermalized:

$$E_{\text{pos}} = k_B T$$

~ 26 meV at 300 K  
 $\ll E_{\text{el}}$



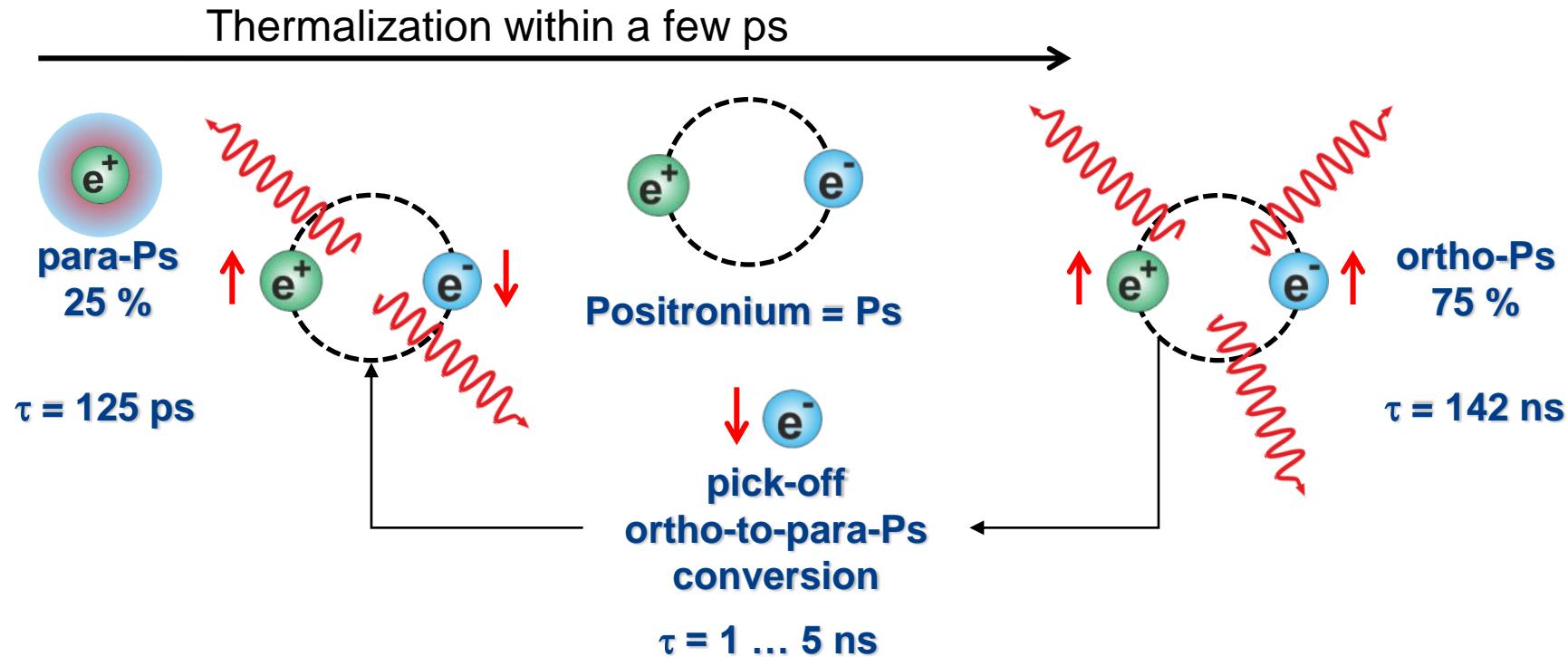
$$\theta_{x,y} = \frac{p_{x,y}^{\text{el}}}{m_0 c}$$

$$\boxed{E_{\text{el}} = 10 \text{ eV}} \\ \rightarrow \Delta E = 1.6 \text{ keV} \\ \rightarrow \Phi = 6 \text{ mrad}}$$

- electron momentum influences energy and emission angle of annihilation photons

# The Positron

## Bound states

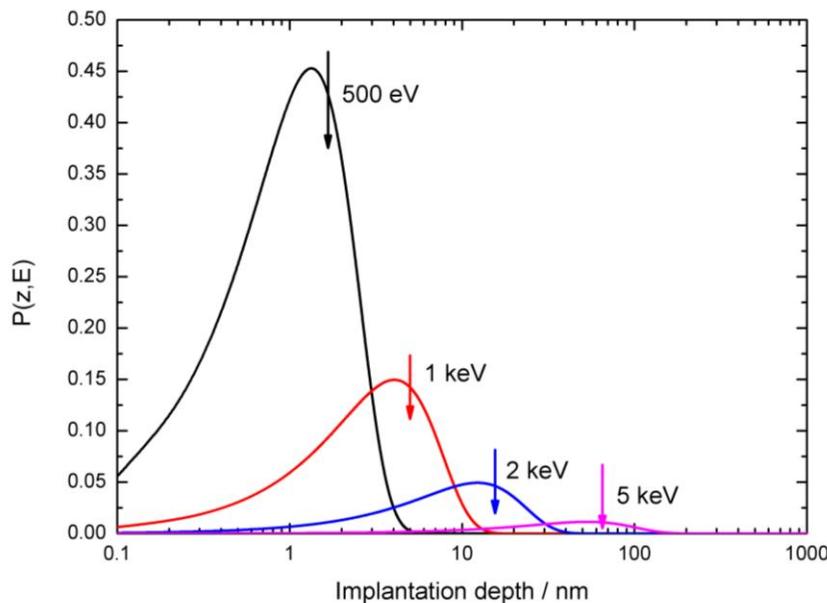


Ore (1949) „Positronium generation in solids if“:

$$\Delta E_{\text{pos}} = E_{\text{max}} - E_{\text{min}} = E_{\text{excite}} - (E_{\text{ion}} - 6.8 \text{ eV})$$

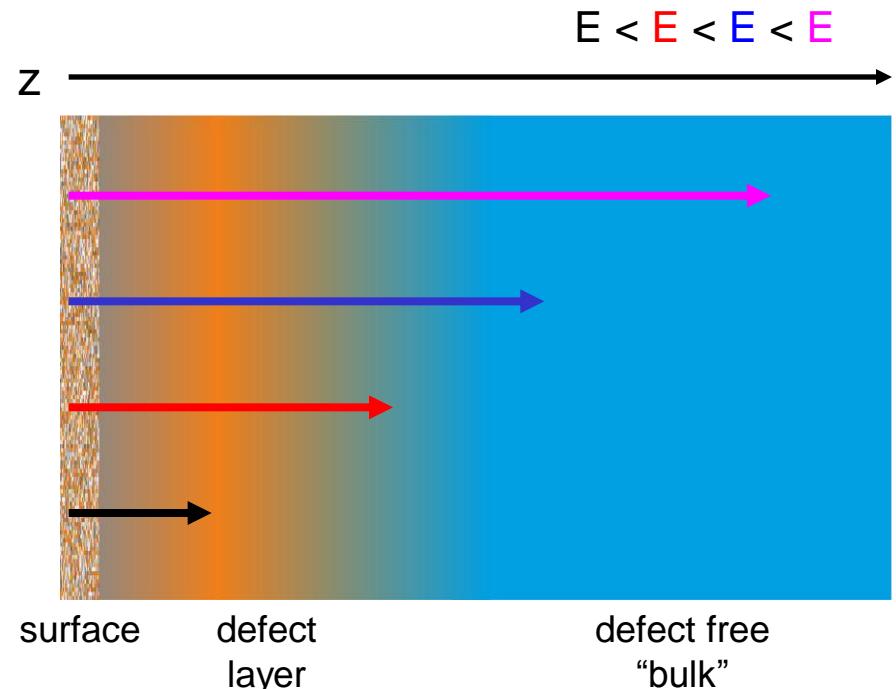
# Utility of positron for spectroscopy

## Implantation profiles for solids



$$\bar{z} = \frac{A \cdot E^r}{\rho}$$

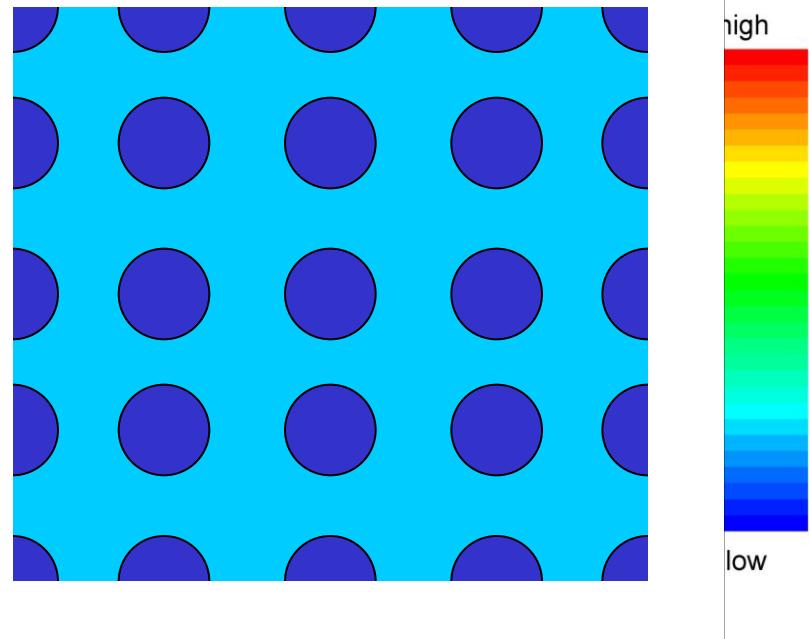
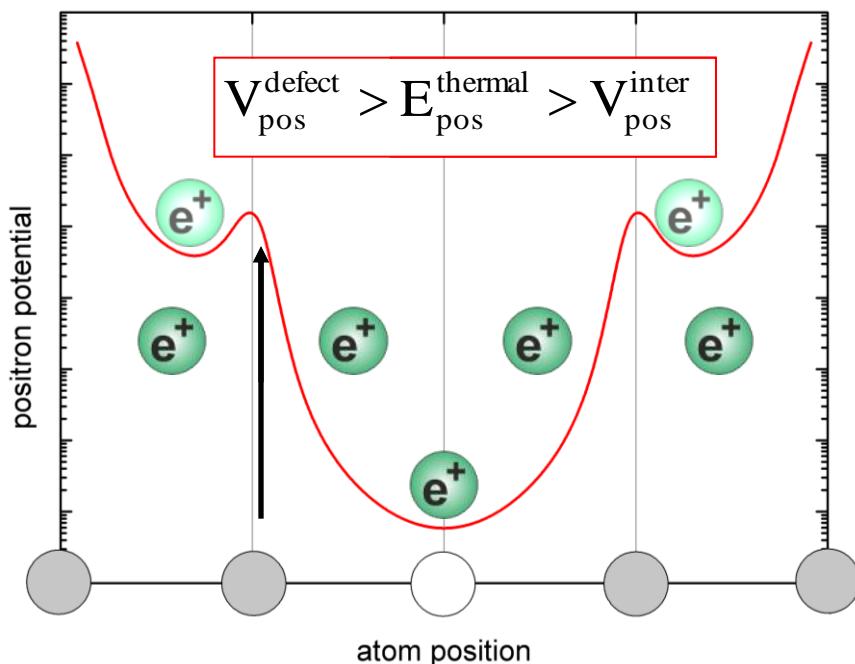
mean positron implantation depth  
(with empirical parameters A and r)



- **Implantation profile (Makhovian profile)** is result of the thermalization process
- smearing with increasing energy: limit in energy necessary

# Utility of positron for spectroscopy

## Trapping in negatively charged defects

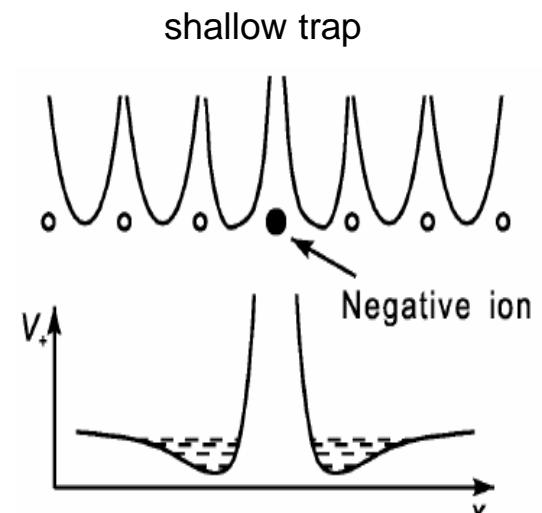
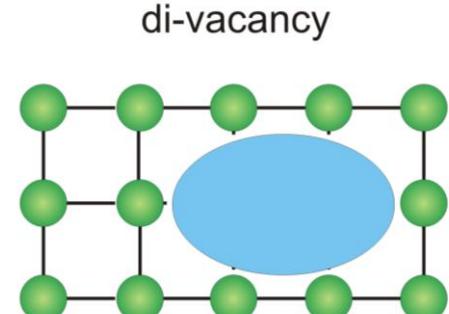
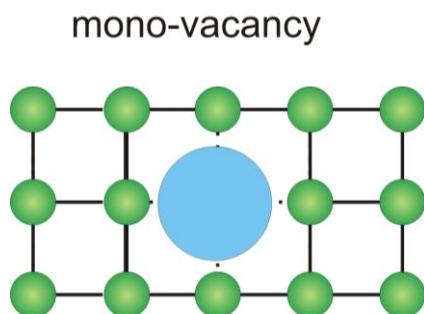
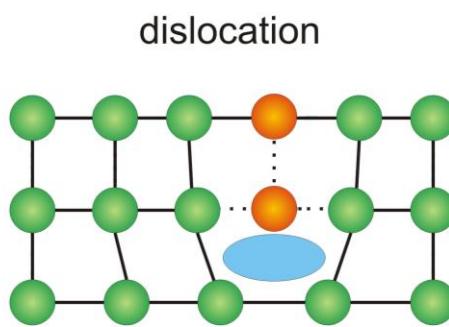
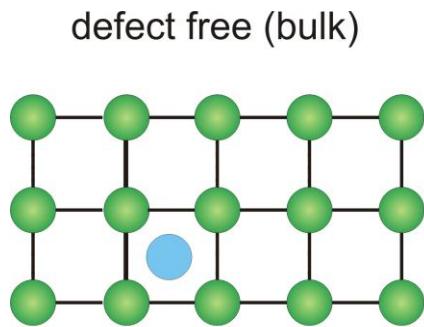


- missing positive repelling charge
- reduction of the ground potential for positrons
- trap for positrons
- positrons are suitable for detecting atomic defects

- positive vacancies repell positrons

# Utility of positron for spectroscopy

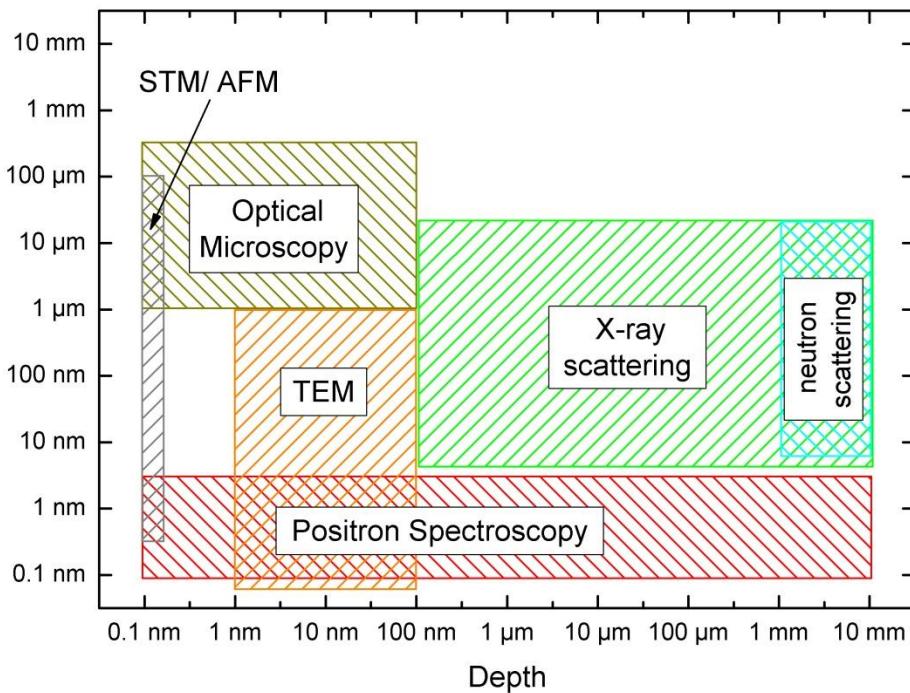
## Variety of defects



a “shallow trap” has a small positron binding energy

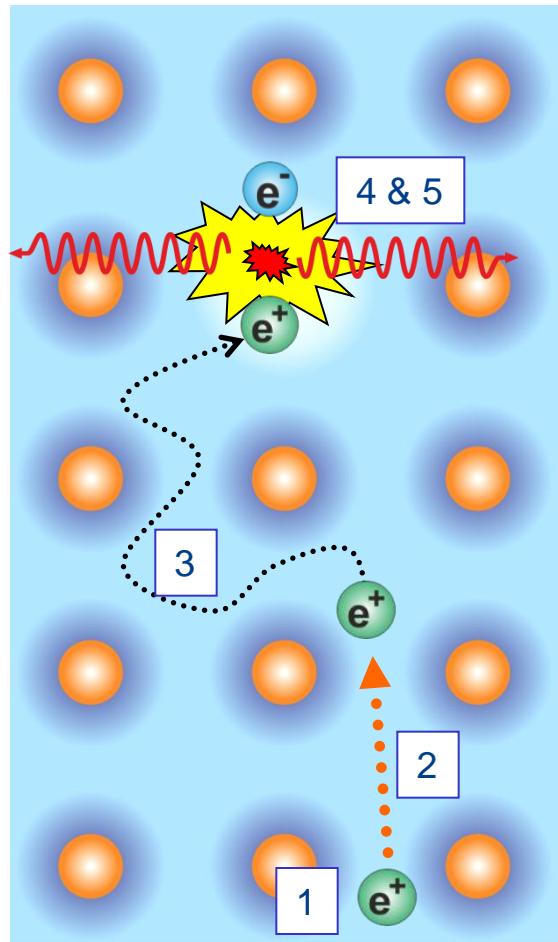
- acceptor-type impurities
- dopants (p doped Si)
- negative antisite defects  $\text{Si}_{\text{Ga}}$

# Utility of positron for spectroscopy



- non destructive method
- sensitive to atomic defects (even single dislocations or mono-vacancies are detectable)
- lowest concentrations detectable: 1 vacancy per  $10^6 \dots 10^3$  atoms
- elemental sensitivity
- depth profiling possible

# Summary – Fate of positrons in solid matter



lattice of a solid with a single vacancy

## 1) Positron generation & implantation in the solid

- $\beta^+$  decay of  $^{22}\text{Na}$
- pair production

## 2) Thermalization – reducing energy

- $\sim 10 \text{ ps}$

## 3) Diffusion through the lattice

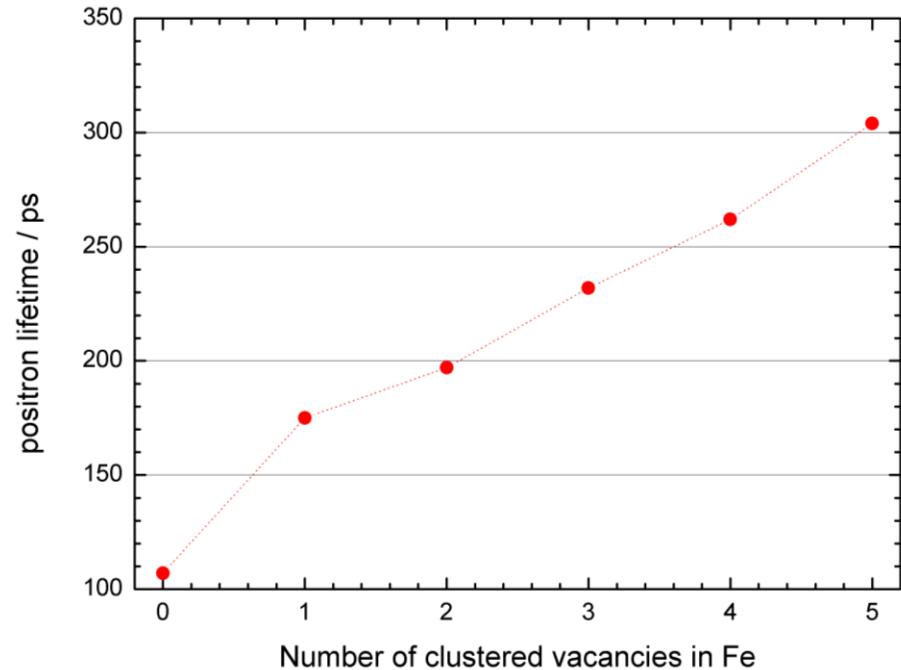
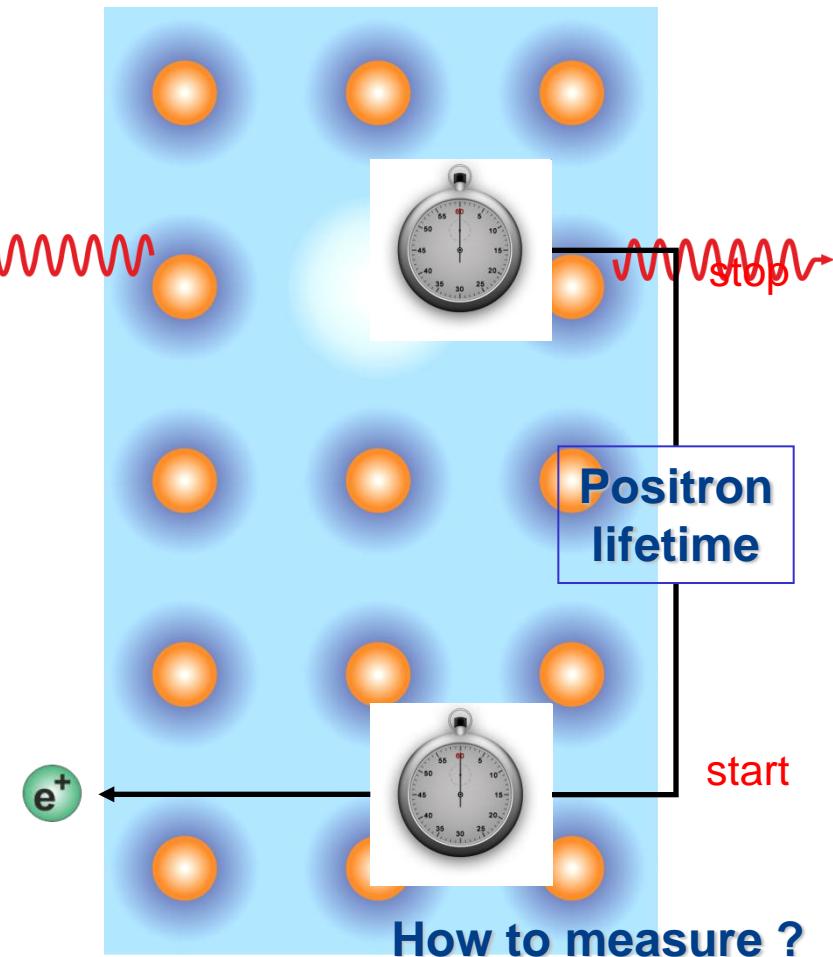
- $\sim 100 \text{ nm}$

## 4) Trapping in defects

## 5) Annihilation with an electron

- emission of two photons in metals/ semiconductors
- angle and energy depend on momentum of electron

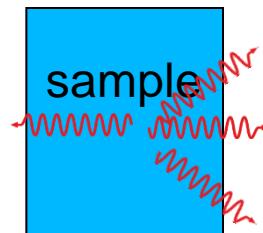
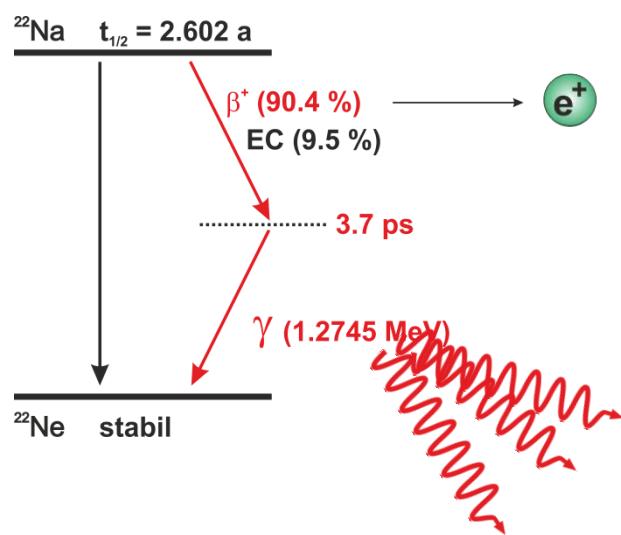
# Measurement – positron lifetime



identification and concentration of  
open-volume defects

# Measurement – positron lifetime

## Start signal – with radio-isotope $^{22}\text{Na}$



stop

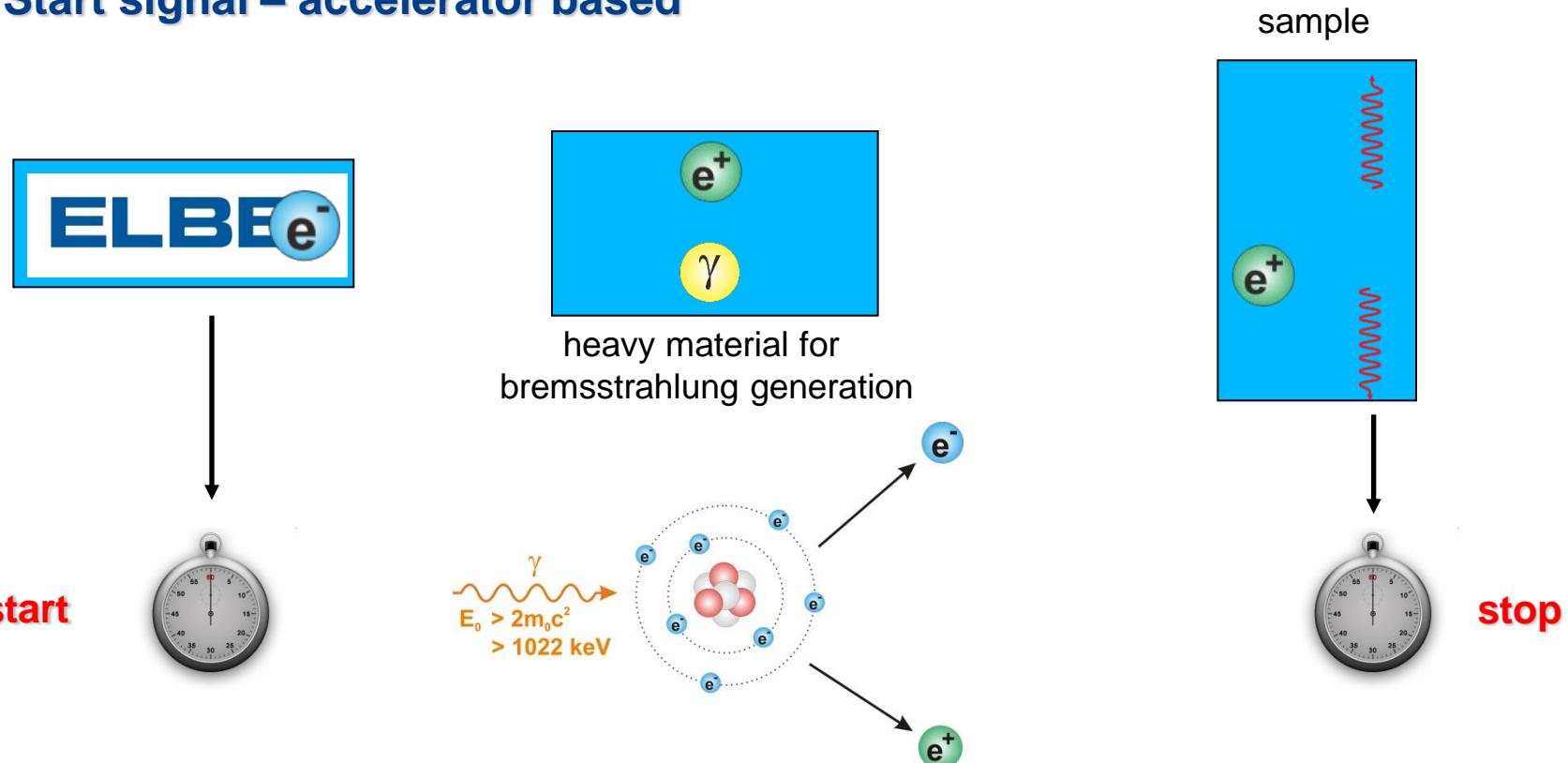
Problem: low probability of detecting both rays

Solution: increase efficiency of start signal



# Measurement – positron lifetime

## Start signal – accelerator based



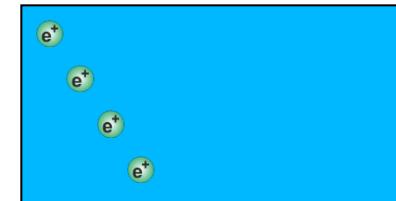
condition:  
at ELBE:      electron pulse short in time → sharp time signal for the start  
                  ~ 5 ps width → possible to use

# Measurement – positron lifetime

## Positron generation methods and consequences

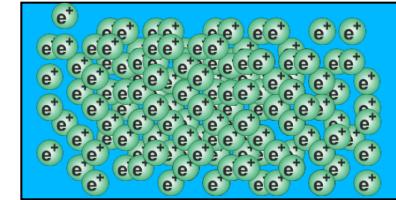
### Implantation of positrons

- + adjustable energy → adjustable implantation depth
- limited implantation depth of a few  $\mu\text{m}$

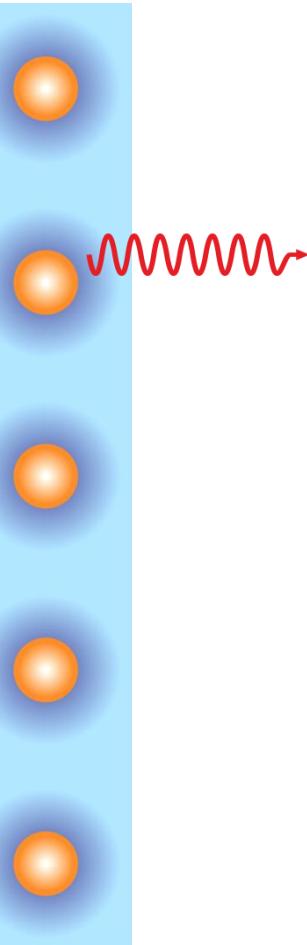


### Pair production inside sample

- + information from the entire sample volume
- no depth information

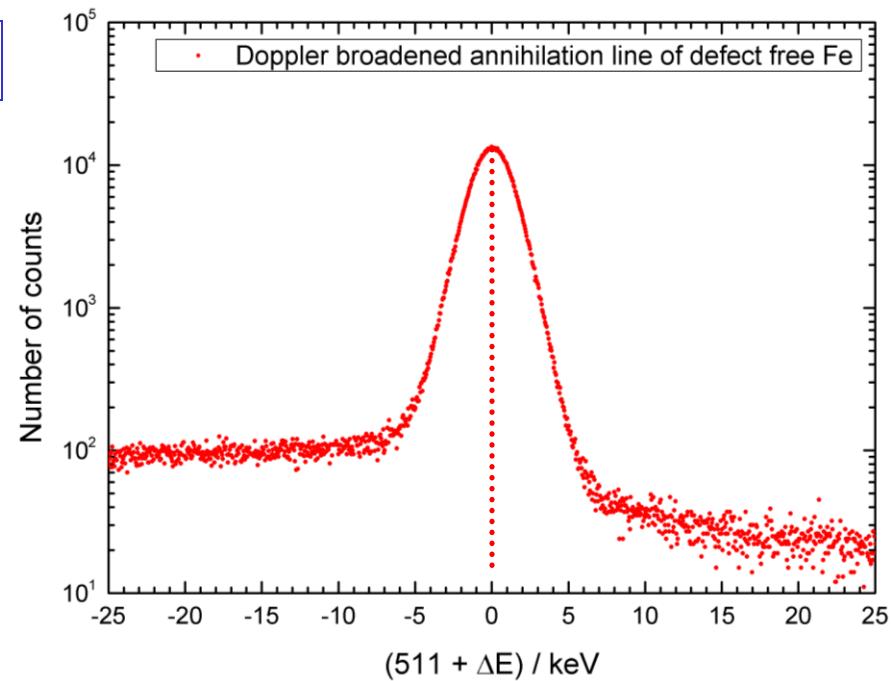


# Measurement – Doppler broadening



## Doppler broadening

energy deviation  
from 511 keV

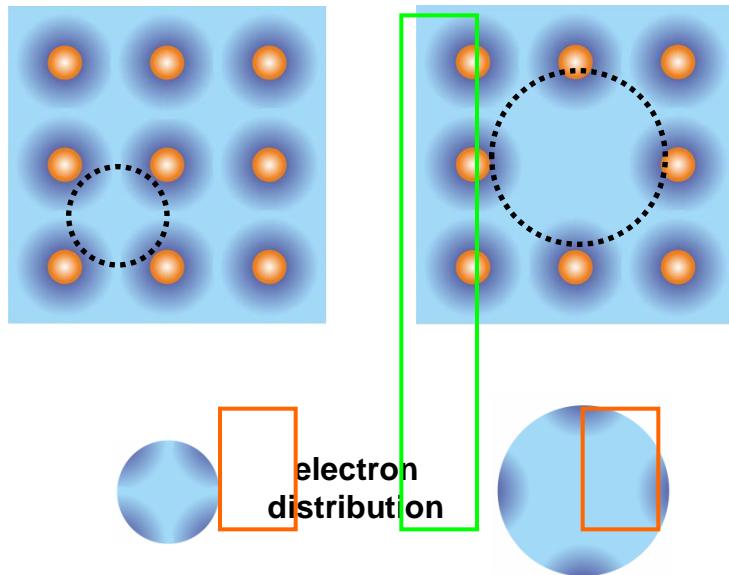


Doppler broadening of the 511 keV line due to the **kinetic energy** of the annihilated electron (positron is in the ground state)

Example:  $E_{\text{kin}} = 10 \text{ eV} \rightarrow \Delta E = 1.6 \text{ keV}$

# Measurement – Doppler broadening

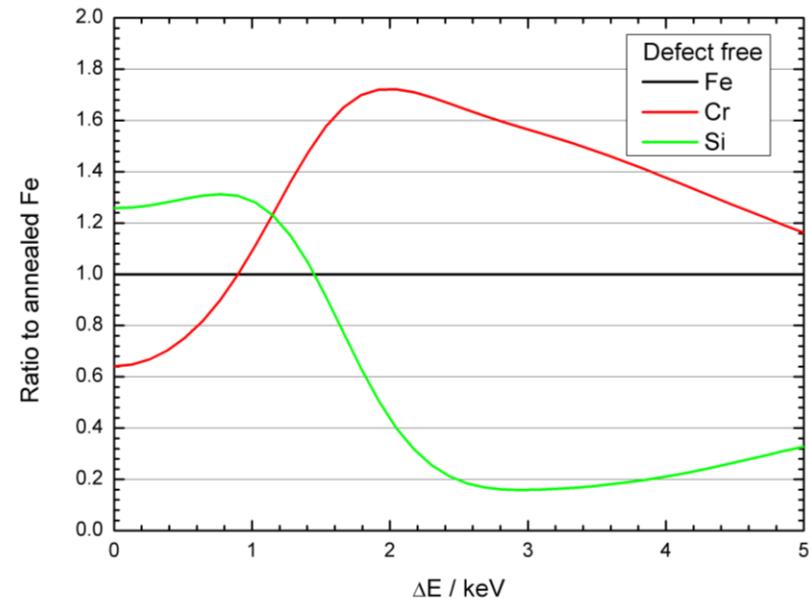
## From electronic structure to the defect situation



$$S = \frac{A_{\text{Peak}}}{A_{\text{All}}} \quad \begin{array}{l} \text{core} \\ \text{valence} \end{array}$$

Sensitive to size and concentration of open-volume defects

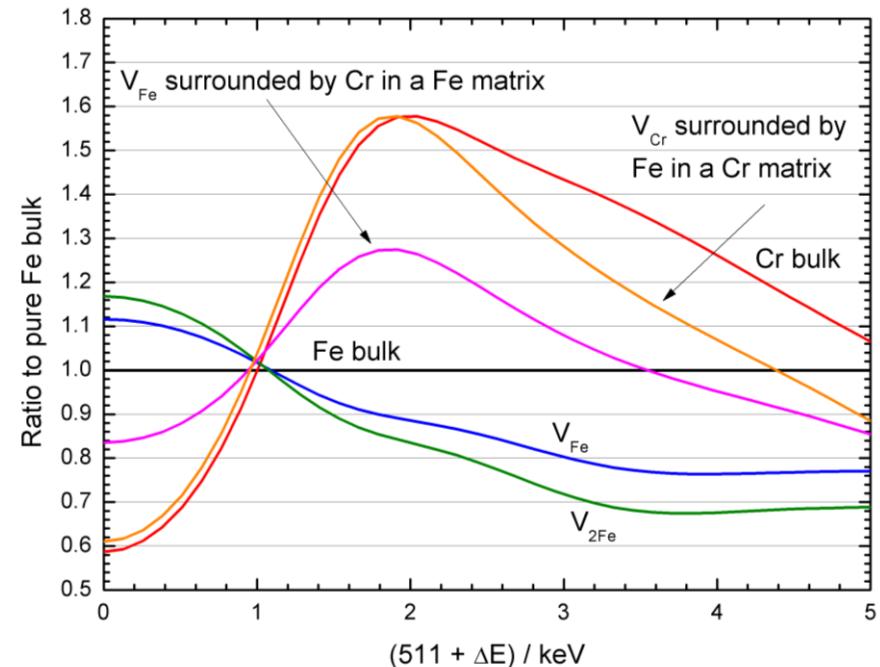
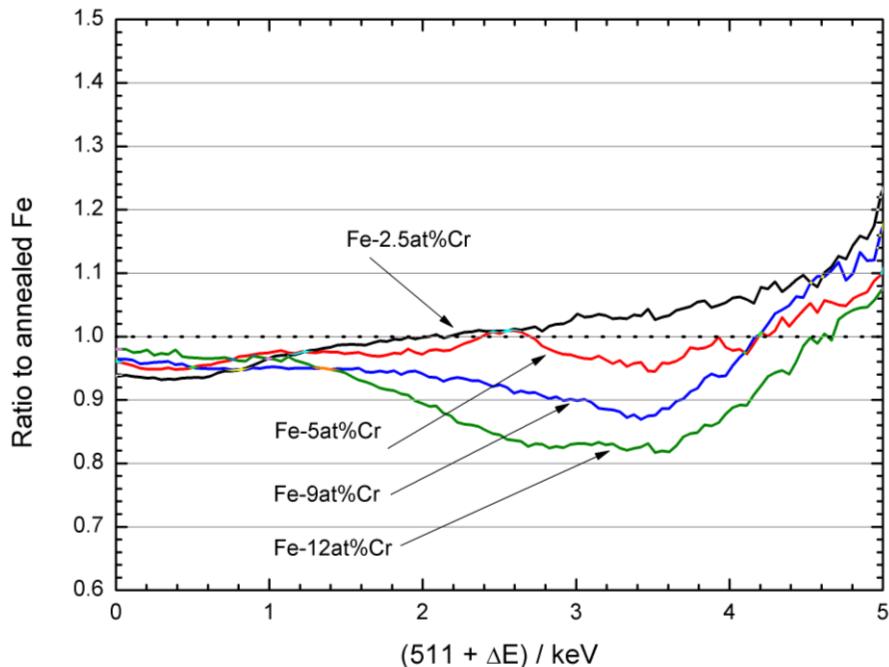
$$W = \frac{W_1 + W_2}{W_{\text{All}}}$$



sensitive to the chemical surrounding (elements) of the annihilation site

# Measurement – Doppler broadening

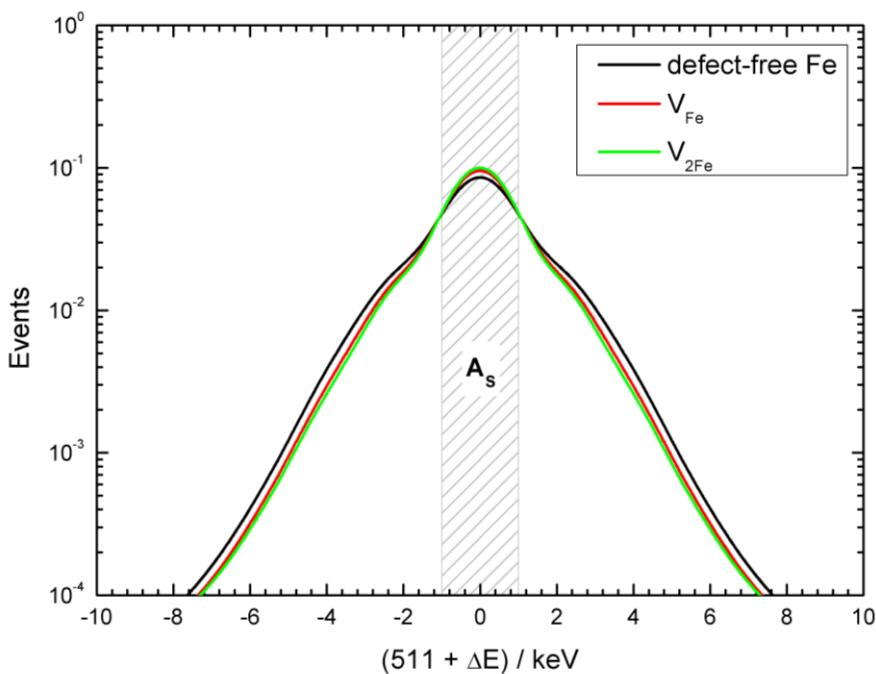
## Chemical surrounding investigated by positrons



- $\alpha'$  phase with Cr rich precipitates for more than 9% Cr
- Cr precipitates repel vacancies
- Cr content < 9%:  $V_{\text{Fe}}$  and  $V_{\text{Fe}}$  - Cr defects
- Cr content > 9%:  $\alpha'$  phase  $\rightarrow V_{\text{Fe}}$  and Cr precipitates (invisible)

# Depth-resolved defect profiling

## Calculation of S for series

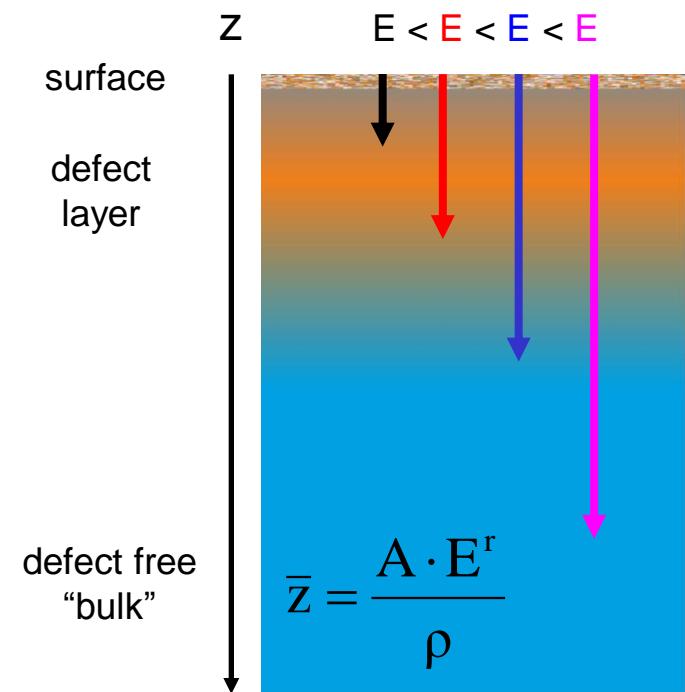
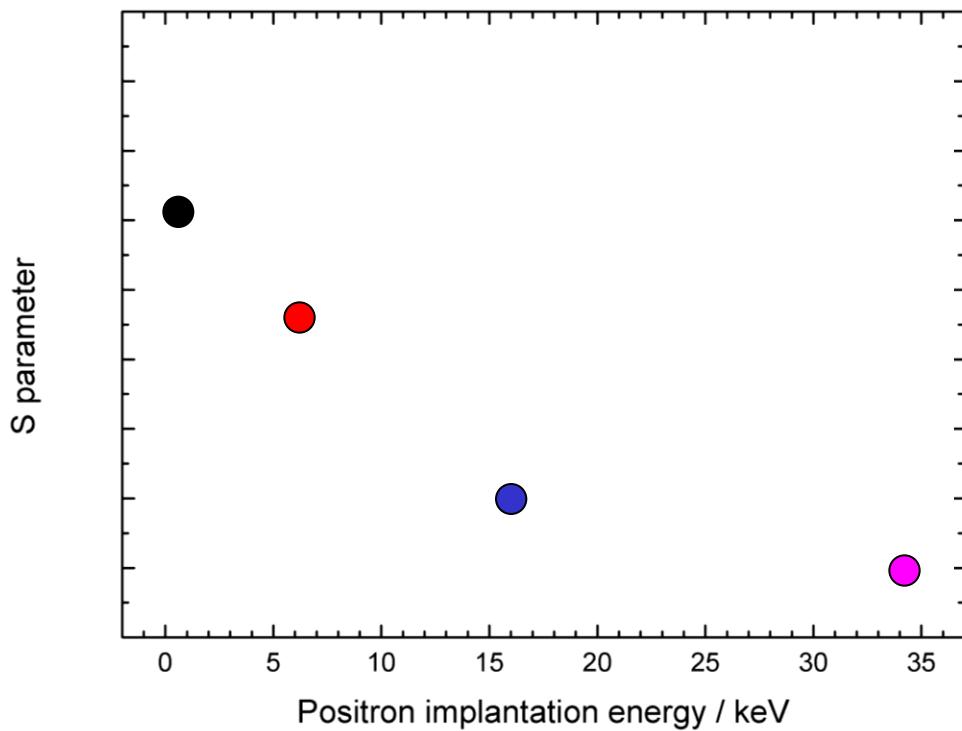


$$S = \frac{A_s}{A_{\text{All}}}$$

- $S \sim 0.5$  for the reference
- same limits then for each following annihilation line
- (set reference parameter as 1)
- relative changes in  $S$  visible for different implantation positron energies/ implantation depths

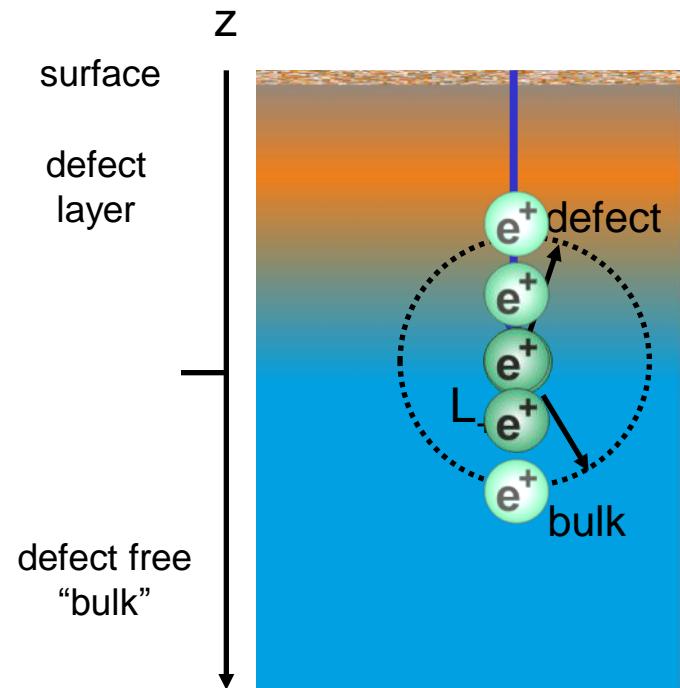
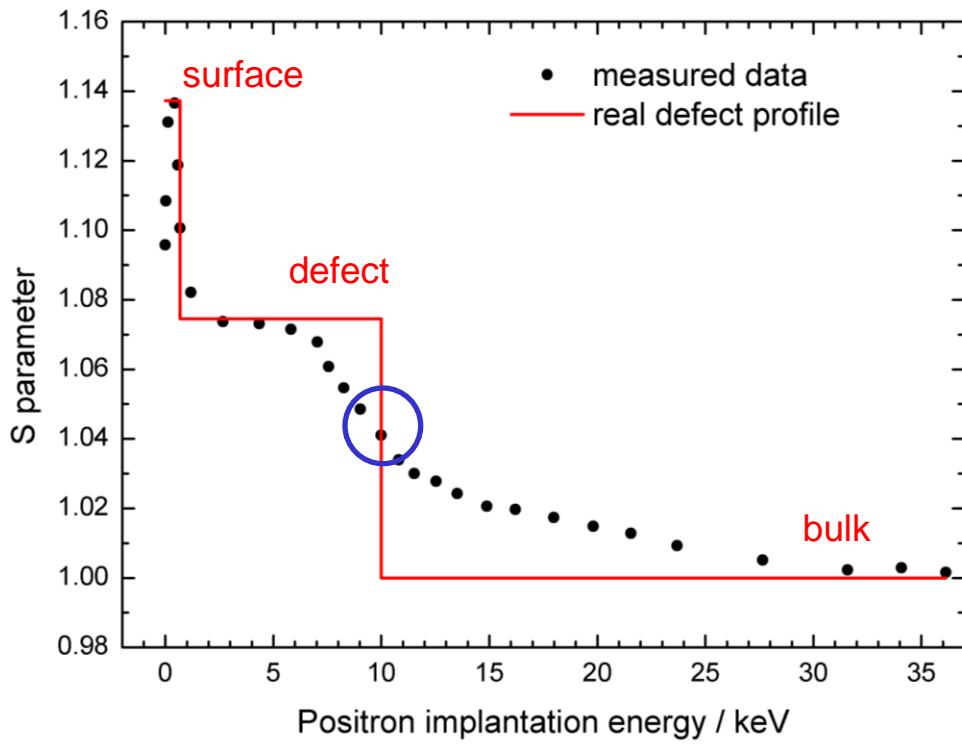
# Depth-resolved defect profiling

## Depth-resolved S parameter



# Depth-resolved defect profiling

## Smearing of profile information – thermalization & diffusion

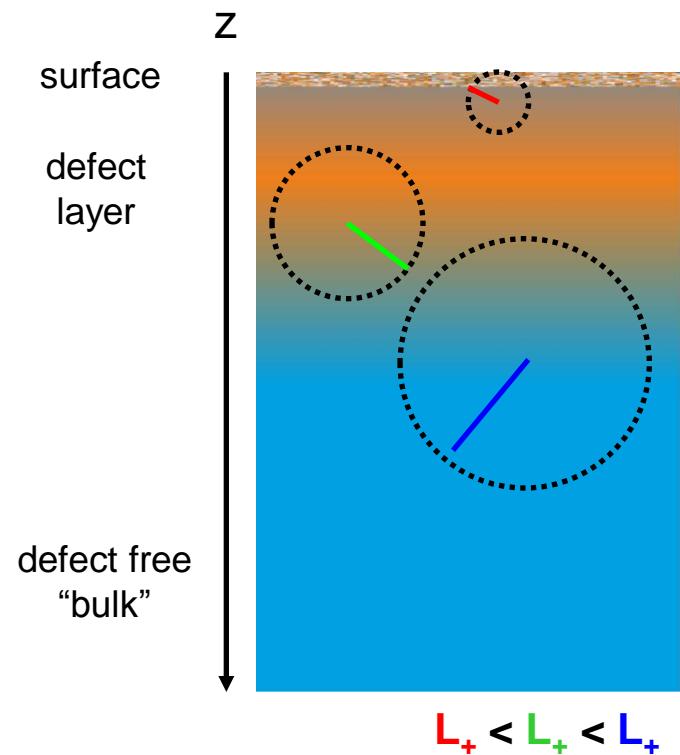
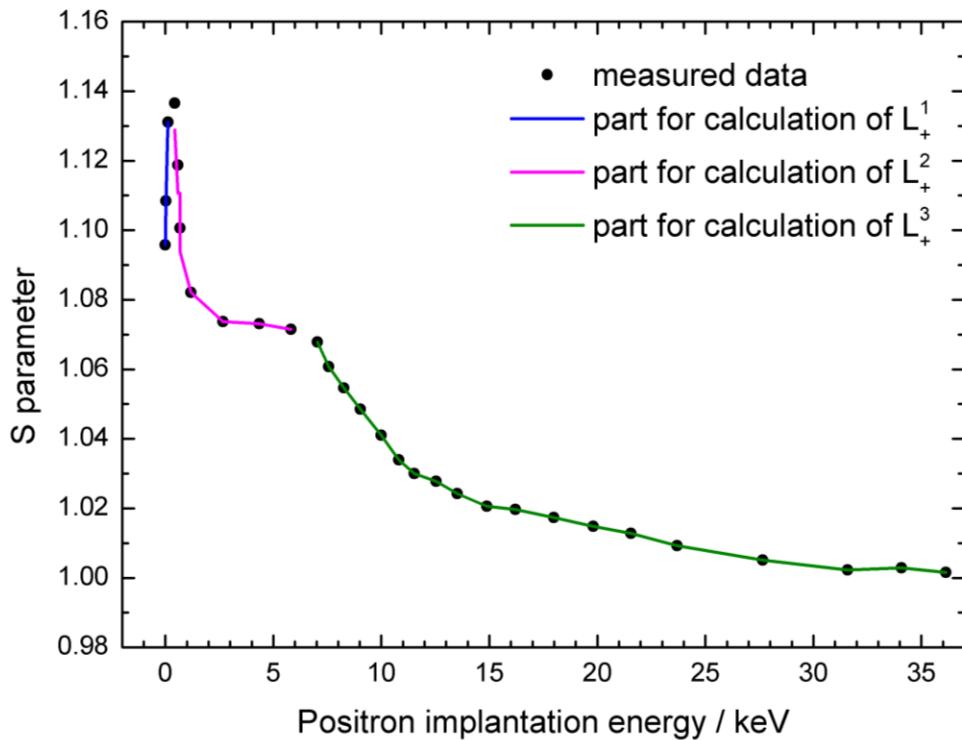


smearing due to  
implantation profile

$$S = m \cdot S_{\text{defect}} + (1 - m) \cdot S_{\text{bulk}}$$

# Depth-resolved defect profiling

## Calculation of the diffusion length $L_+$

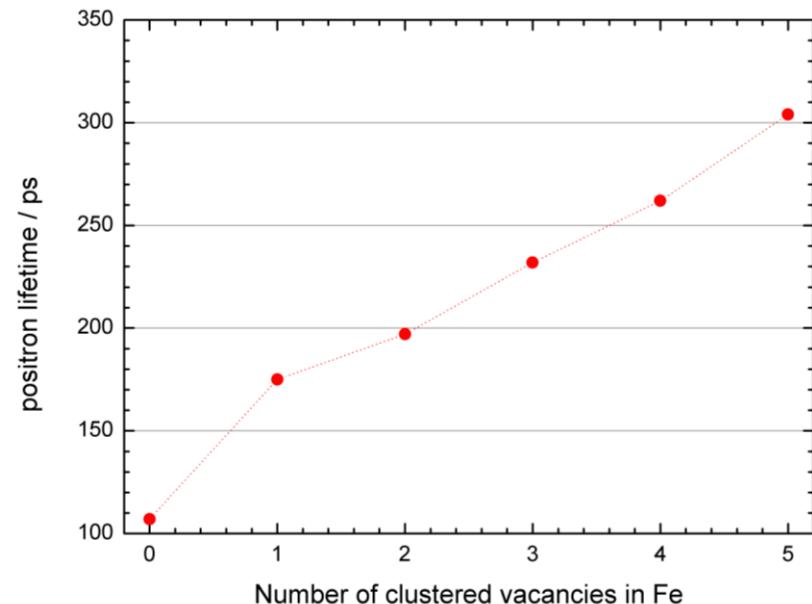
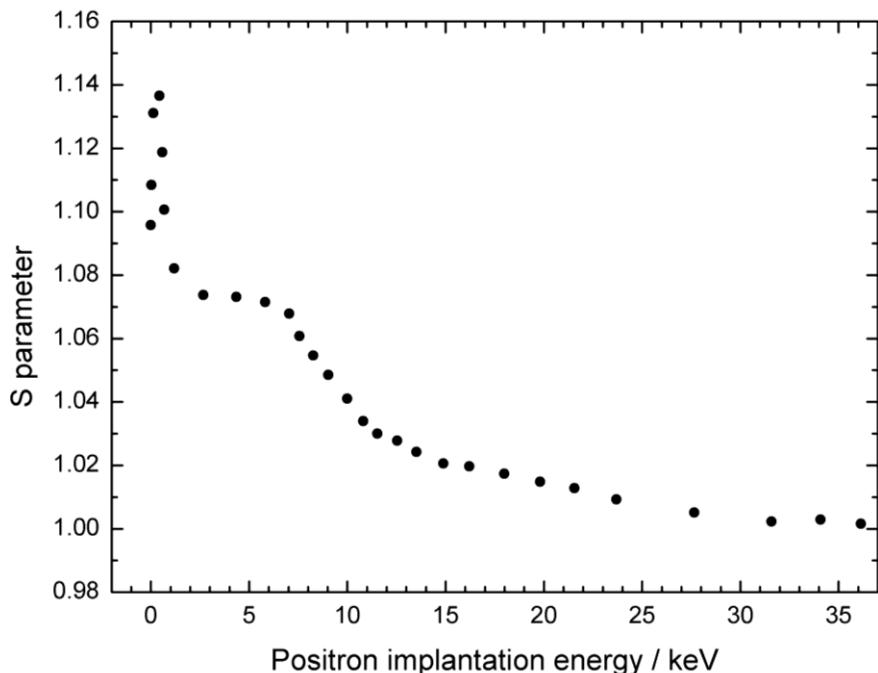


VEPFIT:

A. van Veen *et al.*, Analysis of positron profiling data by means of “VEPFIT”, Positron beams for solids and surfaces, P.J. Schultz *et al.*, Amer. Inst. Phys., NY (1990) 171-196.

# Depth-resolved defect profiling

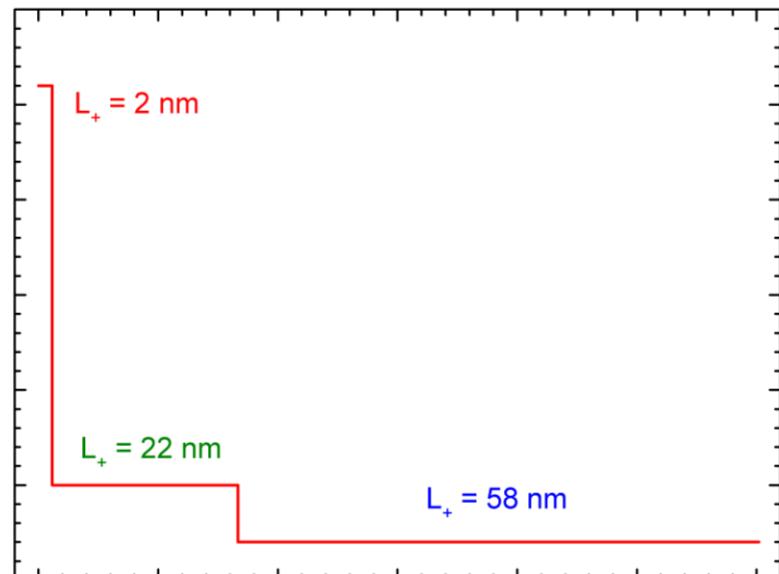
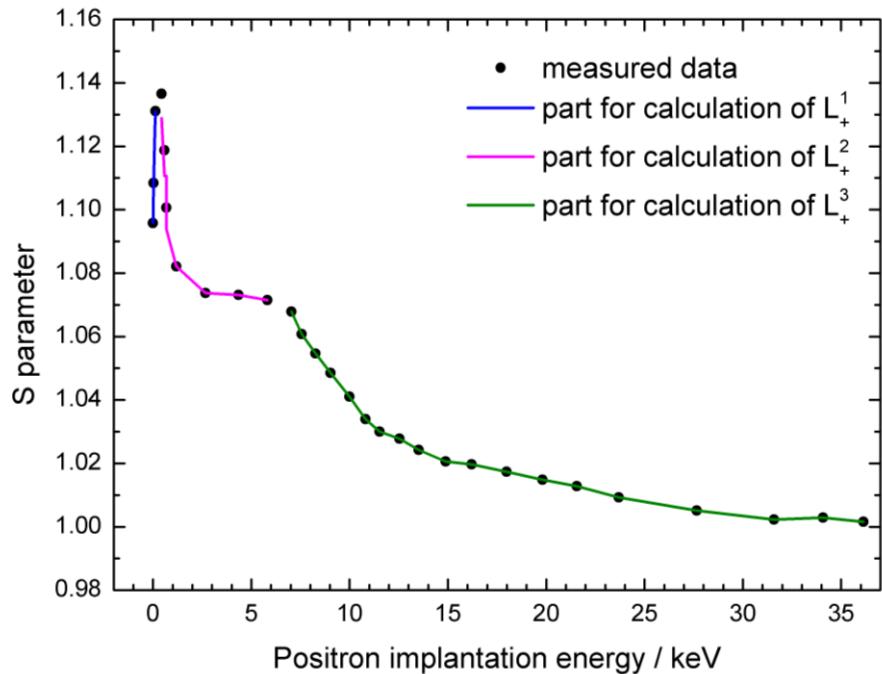
## Identification of defects – depth-resolved positron lifetime measurement



- identification of defect type via positron lifetime
- difficulty: availability of setups for depth-resolved positron lifetime

# Depth-resolved defect profiling

**S → L<sub>+</sub> → lifetime → defect profile**



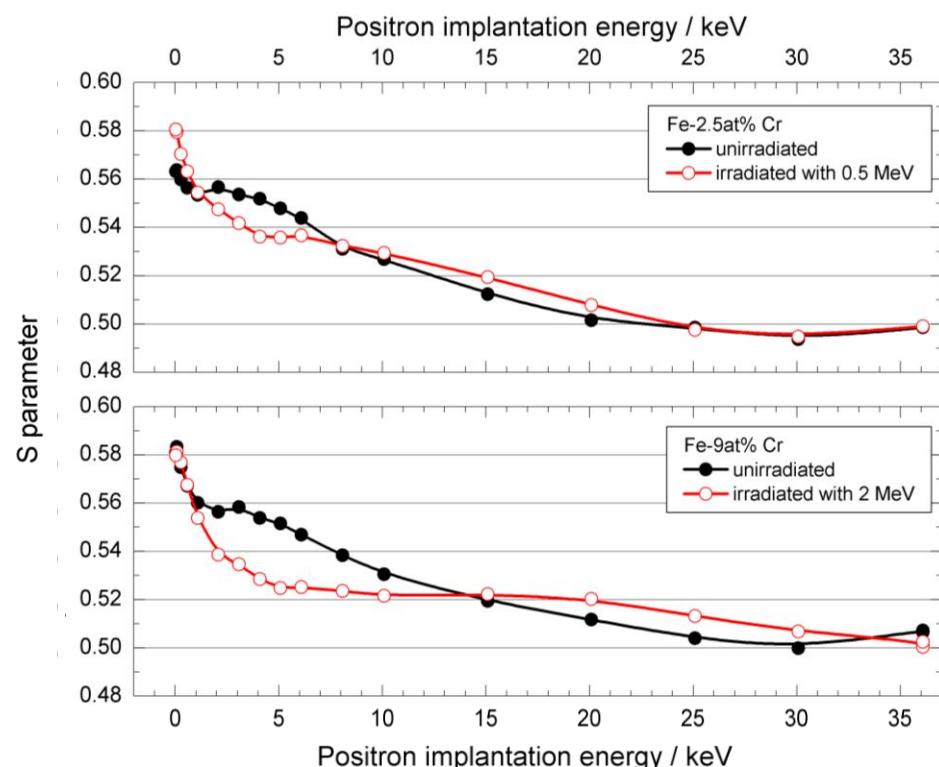
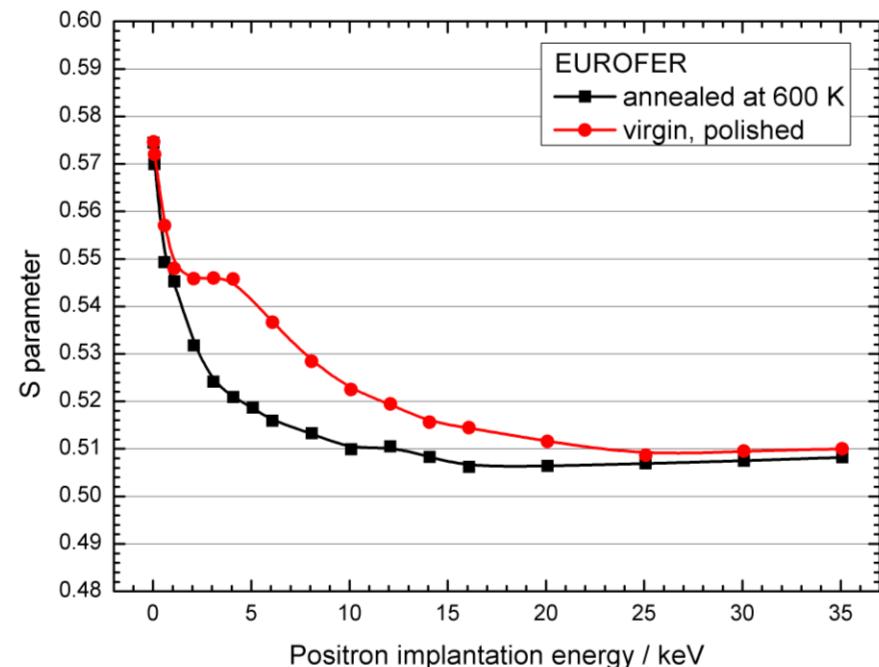
after Grynszpan *et al.*, Ann.  
Chim. Sc. Mat 32(4) (2007)

$$\bar{Z} = \frac{A \cdot E^r}{\rho}$$



# Depth-resolved defect profiling

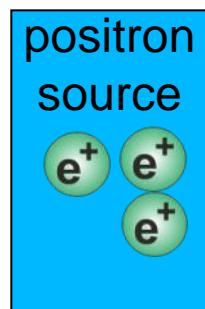
## Sensitivity of positrons



- positrons are sensitive to surface treatment (defects induced by polishing)
- temperature during ion implantation leads to annealing of defects

# Technical hints of PAS

## Source activity and positron lifetime measurements



**correlation between  
not related events**

usage of <sup>22</sup>Na for metals:

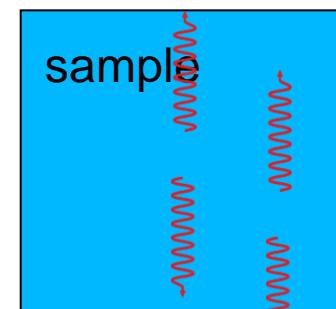
$$A_{\max} \sim \frac{1}{8 \cdot \tau_{\max}^{\text{estimated}}} [\text{Bq}]$$

start



$$\tau \sim 5 \text{ ns} \rightarrow A_{\max} \sim 25 \text{ MBq} \sim 0.67 \text{ mCi}$$

**Valid event for  
positron lifetime**



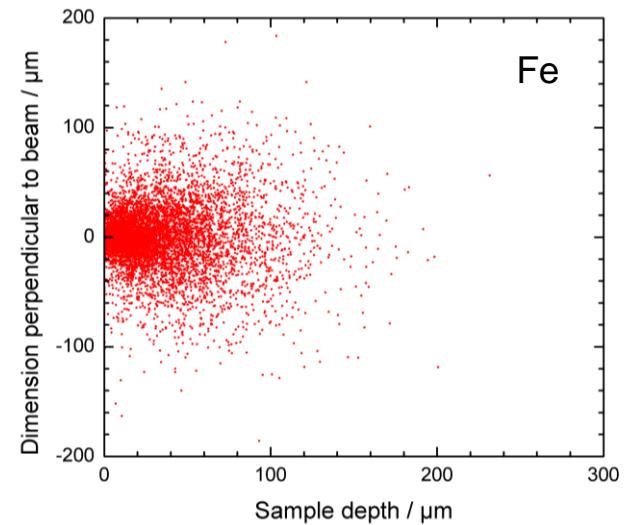
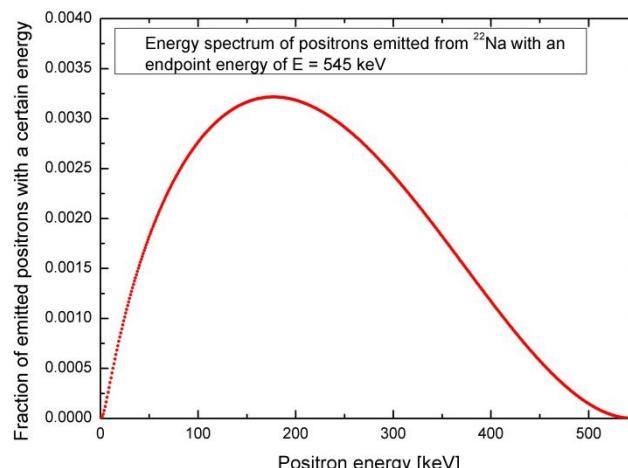
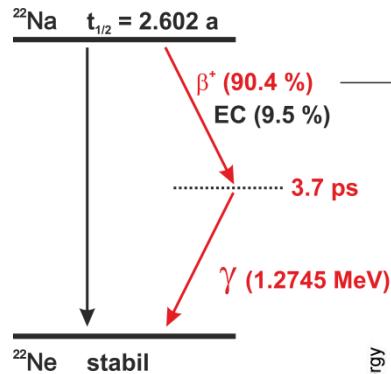
sample

stop



# Technical hints of PAS

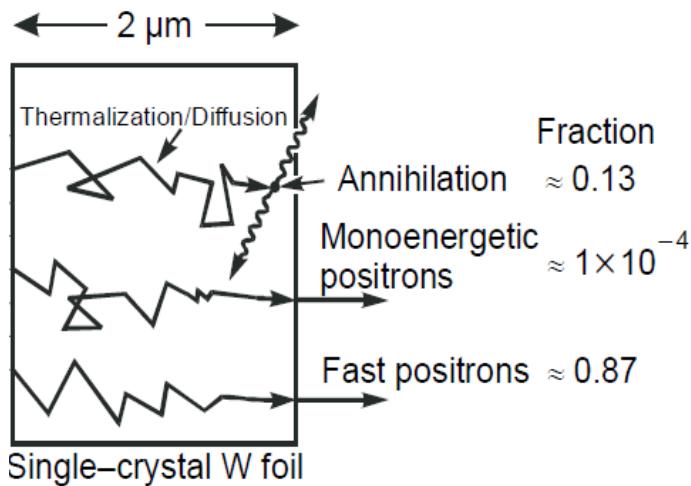
## Usage of non-monoenergetic positrons



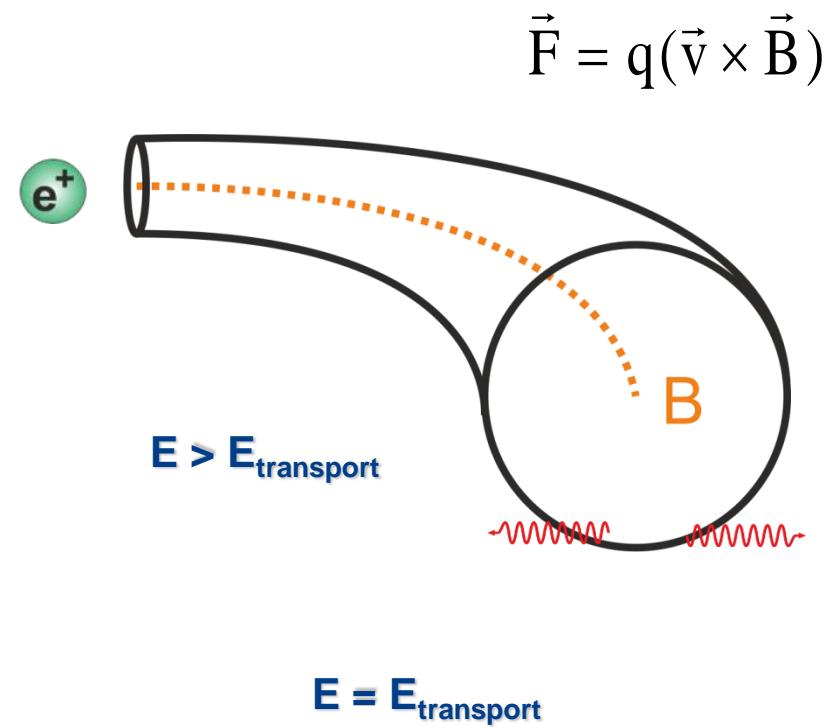
depth profiling becomes  
impossible without  
modification of energy !

# Technical hints of PAS

## Moderation of positrons and selection of correct energies

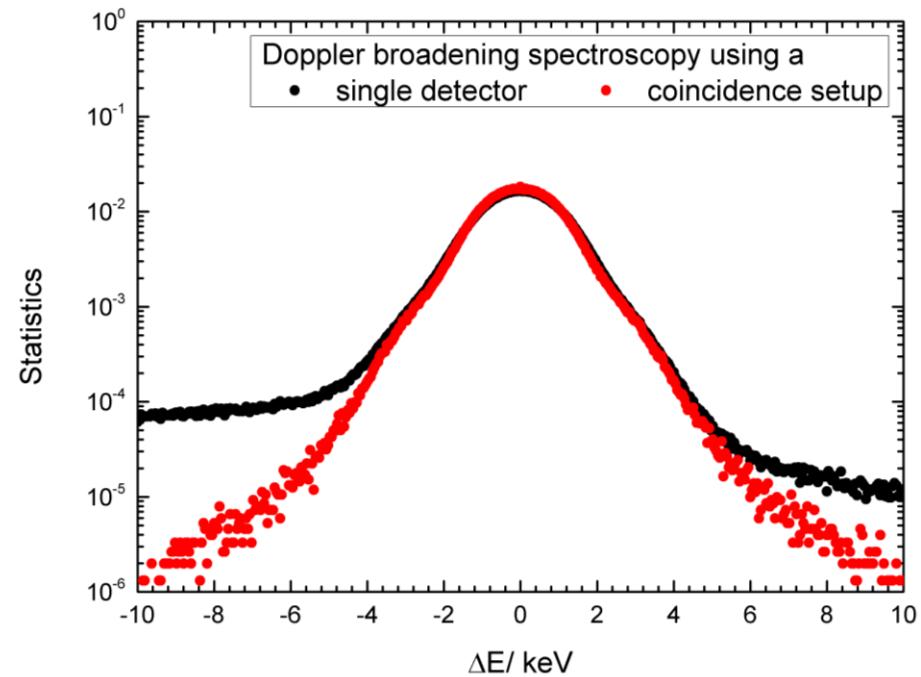
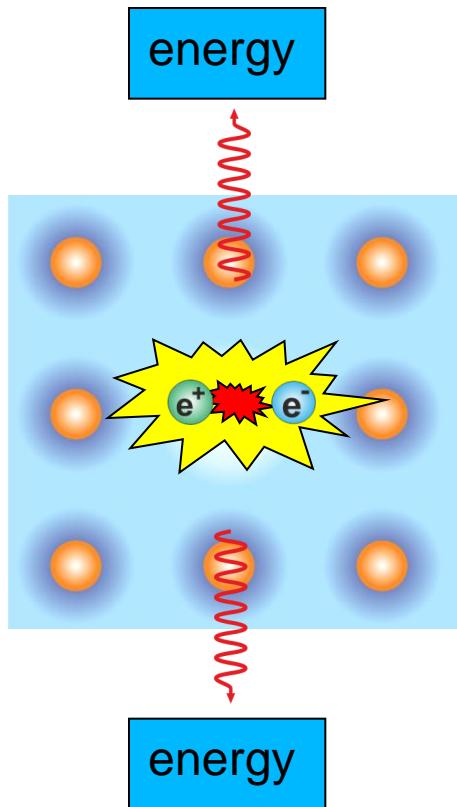


- energy of moderated positrons = 3 eV
- still a huge number of fast positrons
- bent tube to select positrons



# Technical hints of PAS

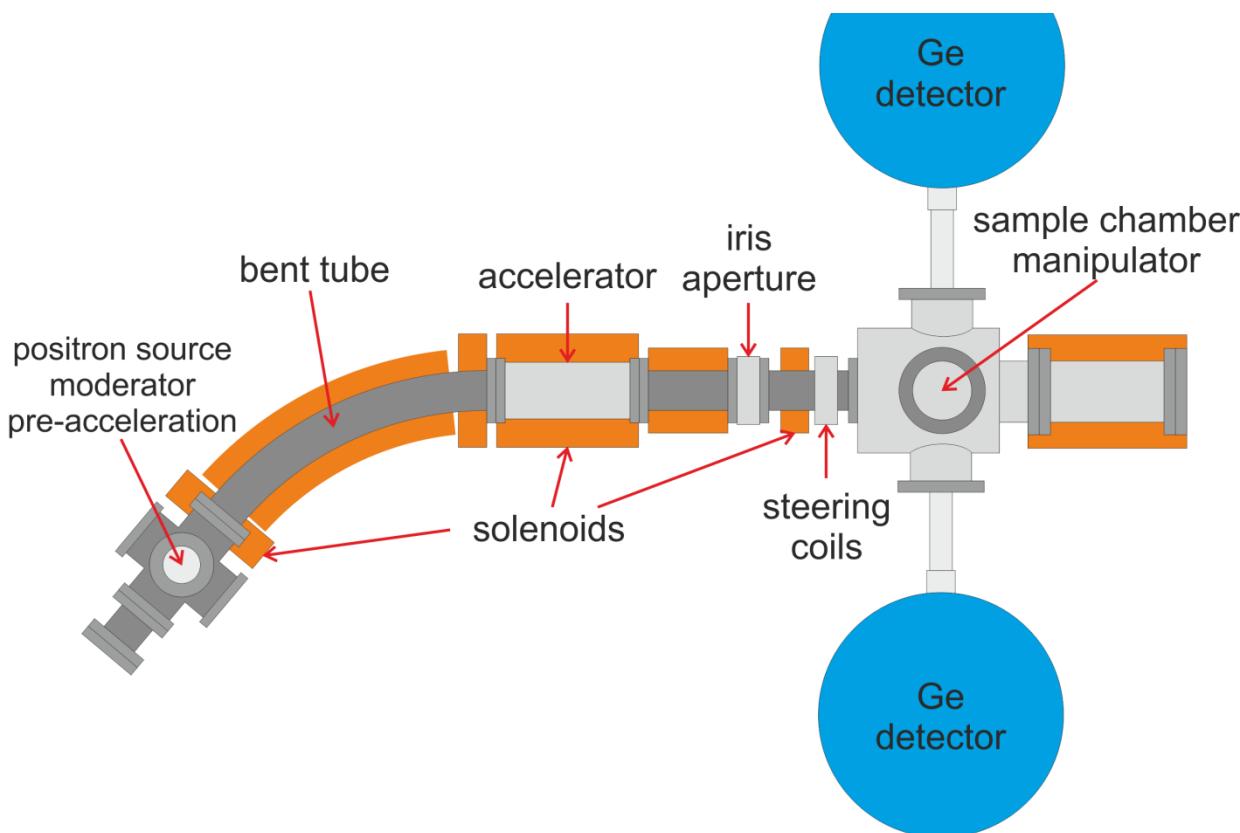
## Coincidence Doppler broadening



- better peak to background ratio
- important for chemical sensitivity

# Realization of depth-resolved defect profiling

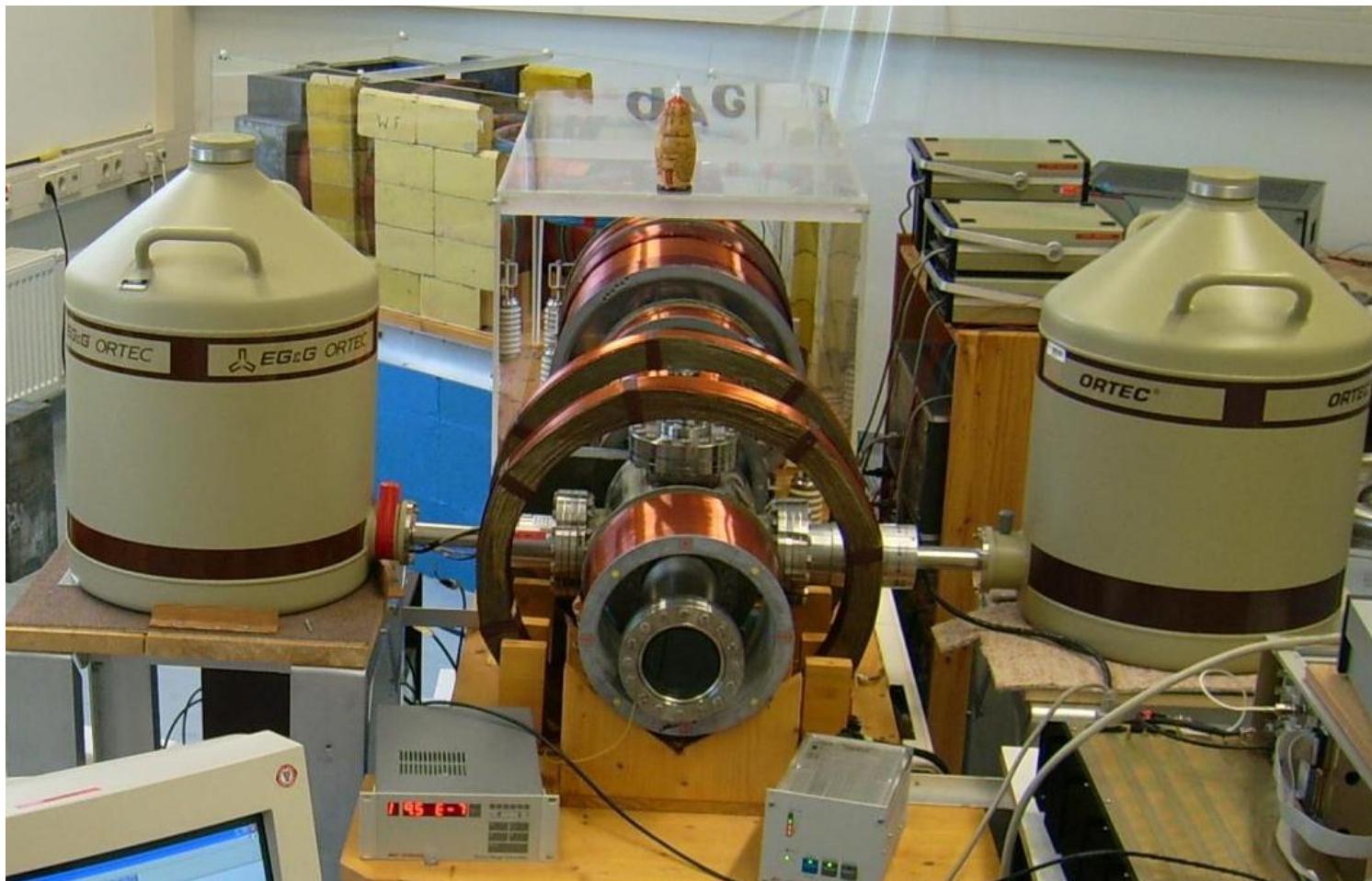
## Slow P<sup>O</sup>sitroN System Of Rossendorf - SPONSOR



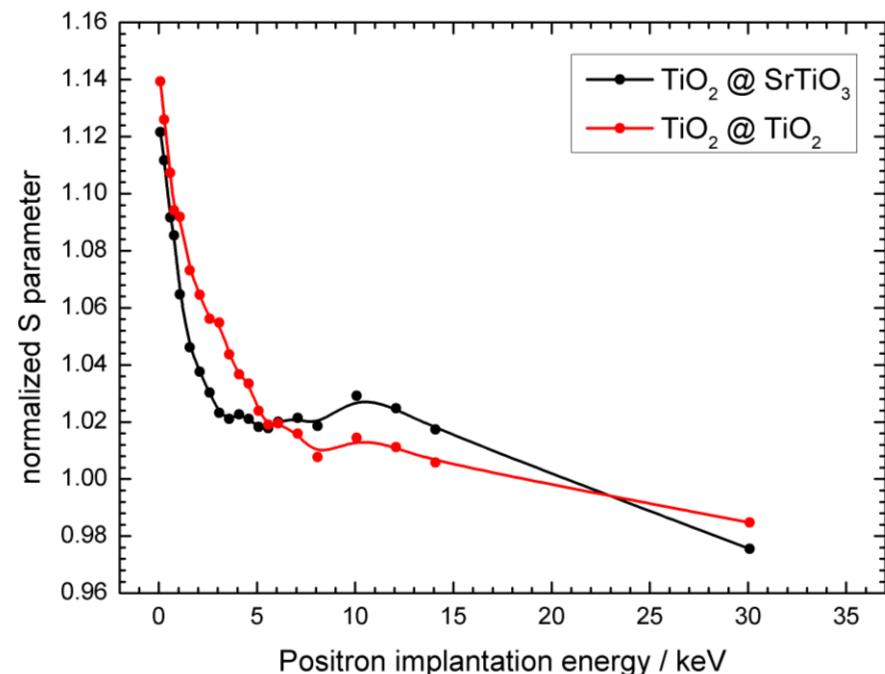
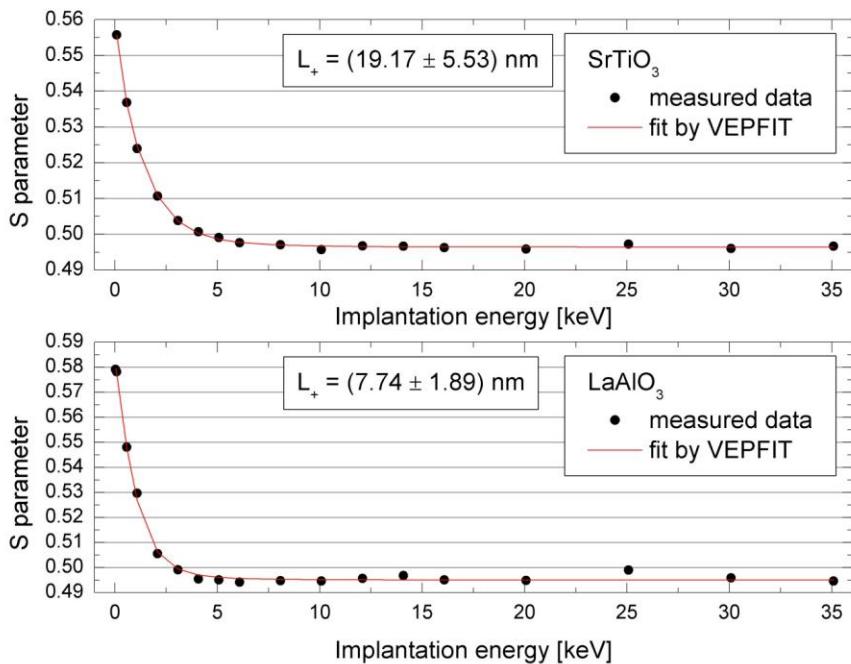
### Doppler broadening spectroscopy

- positron energy: 27 eV ... 36 keV
- energy resolution:  $(1.09 \pm 0.01)$  keV at 511 keV

# Realization of depth-resolved defect profiling



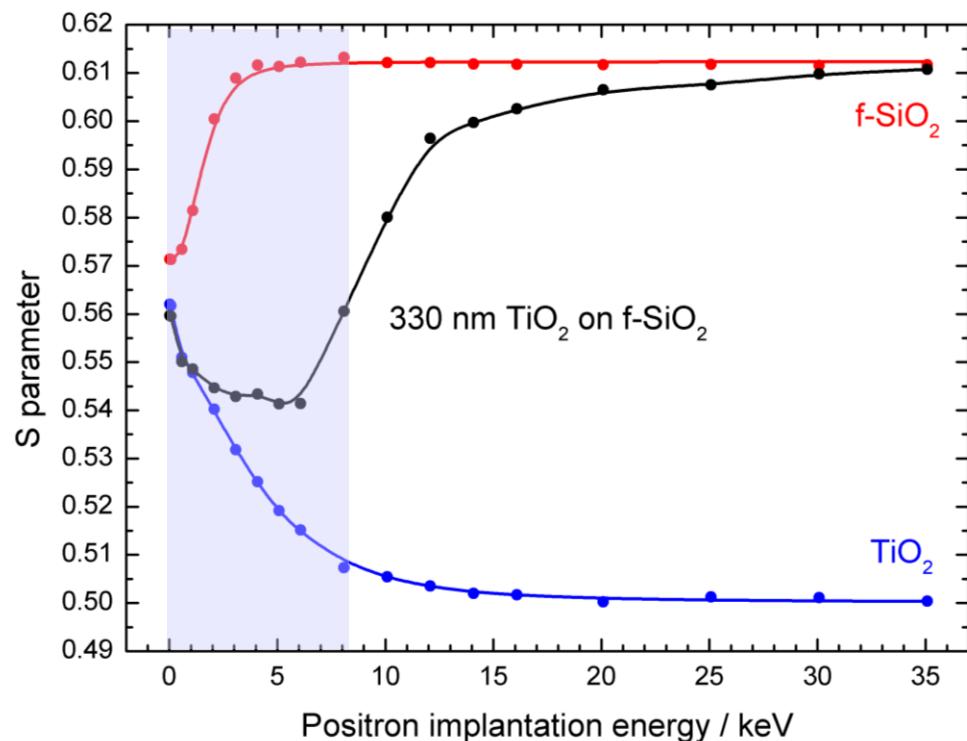
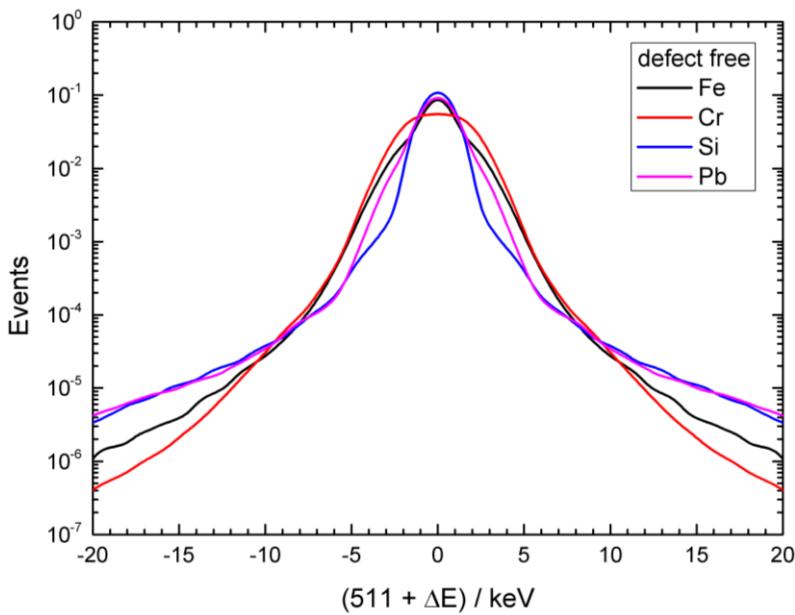
# DETI.2 – Quality of substrate materials



- Shorter diffusion length due to higher defect density/ larger defects
- $\text{SrTiO}_3$  is of better quality

# DETI.2 – Components of the depth profile

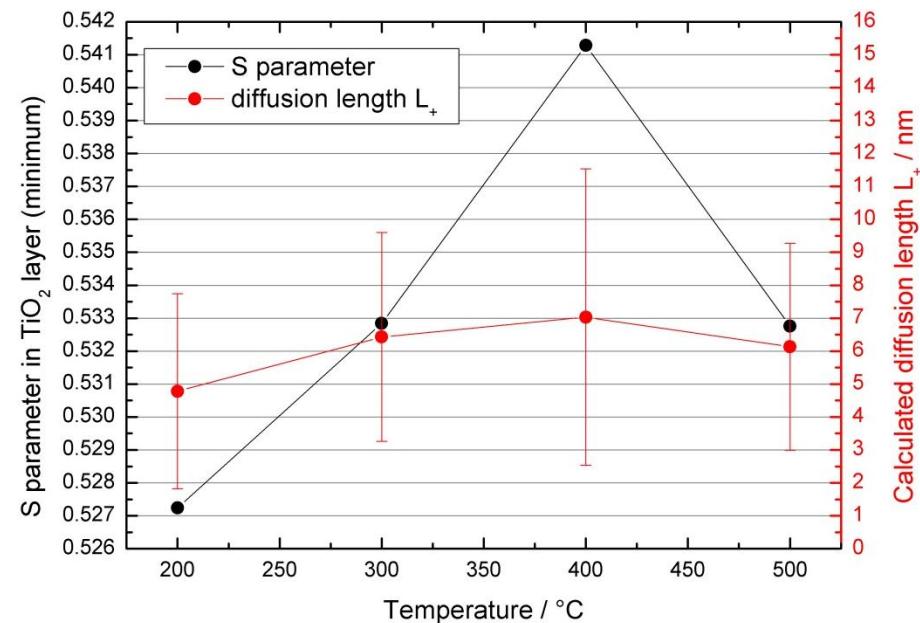
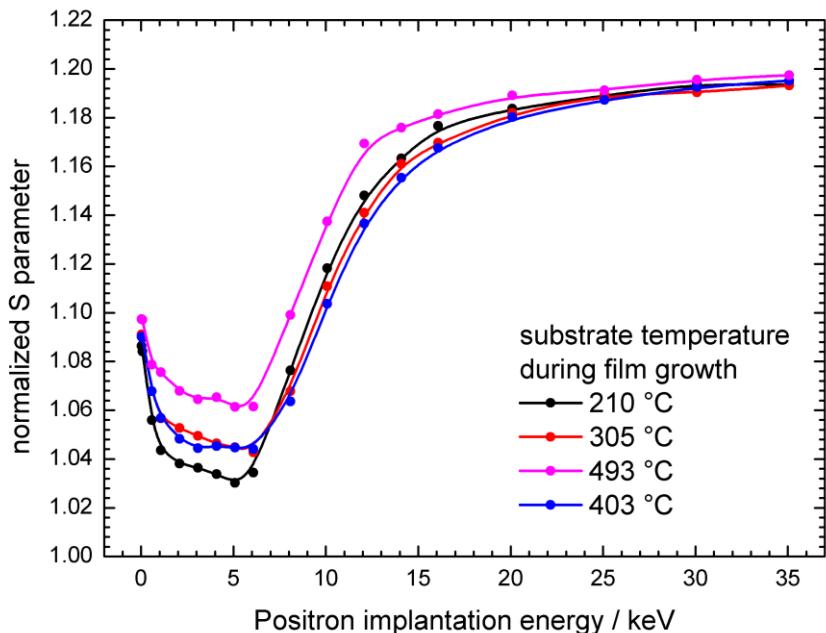
## Differences in S parameter – a question of reference



- S not only changes for different defect types/ concentrations
- also differences for different materials

# DETI.2 – Influence of growth conditions

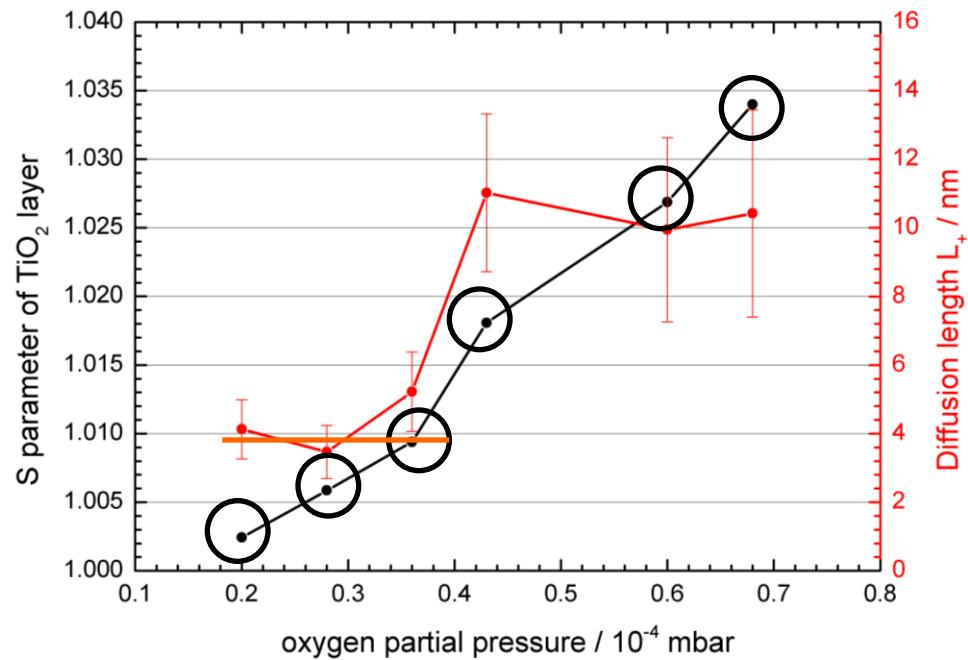
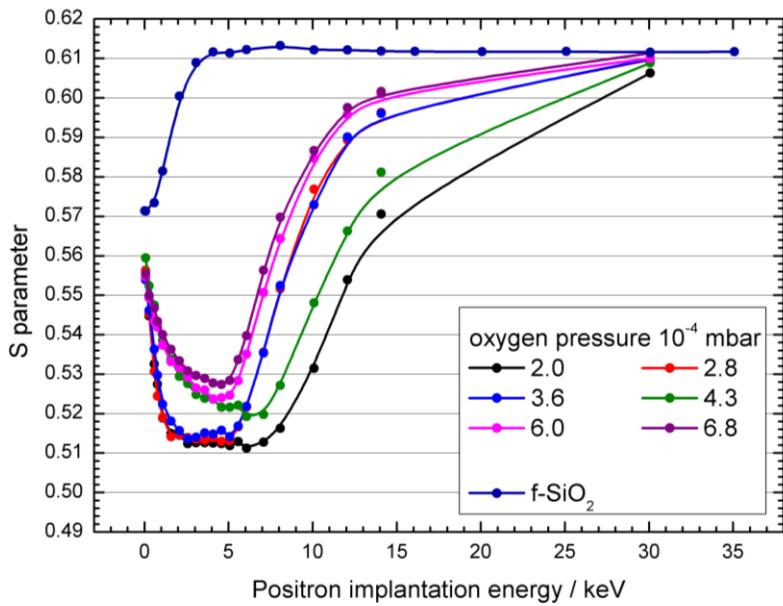
## film growth temperature



- Differences due to temperature
- unexpected jump in the S parameter

# DETI.2 – Influence of growth conditions

## oxygen partial pressure



- behaviour of L<sub>+</sub> and S:  
possible defect agglomeration



Many thanks for your attention !