Do nuclei go pear-shaped?

Coulomb excitation of ²²⁰Rn and ²²⁴Ra at REX-ISOLDE(CERN)

> Marcus Scheck University of the West of Scotland Peter A. Butler, Liam P. Gaffney University of Liverpool for the IS475 collaboration

CGS XV - Dresden 2014



Nuclear shell structure





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 $E_{L} \leq \varepsilon_{F} \leq E_{L+3}$

Nuclear shell structure





 $E_{L} < \varepsilon_{F} < E_{L+3}$ $\Delta E = E_{L+3} - E_{L} \ll$



Nuclear

shell structure

⇒enhanced octupole collectivity



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Multipole expansion of the shape: 2^{L} -pole and L=3 \Rightarrow Octupole





Multipole expansion of the shape: 2^{L} -pole and L=3 \Rightarrow Octupole







Multipole expansion of the shape: 2^{L} -pole and L=3 \Rightarrow Octupole



Reflection Asymmetric





Experimental observables $E_{3^{-}}$ and B(E3, 0⁺ \mapsto 3⁻)



Excitation energy E₃₋



Neutron Number N

T.Kibédy & R.H.Spear, At. Data and Nucl. Data tables 80 (2002) 35



Experimental observables $E_{3^{-}}$ and B(E3, 0⁺ \mapsto 3⁻)



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Excitation energy E₃₋

B(E3, $0^+ \mapsto 3^-$)-strength



T.Kibédy & R.H.Spear, At. Data and Nucl. Data tables 80 (2002) 35

Experimental observables $E_{3^{-}}$ and B(E3, 0⁺ \mapsto 3⁻)



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Excitation energy E₃₋

Inverse sum rule



T.Kibédy & R.H.Spear, At. Data and Nucl. Data tables 80 (2002) 35



ISOL → **IS**otope **OnL**ine separation **DE**tector





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CERN accelerator complex



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Physical processes

²³⁸U binding energy: 1.8 GeV



Target nucleus





Physical processes

²³⁸U binding energy: 1.8 GeV







Physical processes

²³⁸U binding energy: 1.8 GeV



- **1.** Spallation \Rightarrow heavy nucleus
- **2.** Fission \Rightarrow medium mass nucleus
- 3. Fragmentation \Rightarrow light nucleus



Physical processes

²³⁸U binding energy: 1.8 GeV



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Target Outline

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ISOL → **IS**otope **OnL**ine separation **DE**tector





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Radioactive ion beam EXperiment - REX

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Coulomb excitation at Miniball



DSSD Particle detector



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Coulomb excitation at Miniball







Coulomb excitation at Miniball

Miniball Triple Cluster Projectile **REX:** E_{beam}~2.83 MeV/u A/q 4-4.5 (²²⁴Ra⁵²⁺) ~66% E_{safe} (⁶⁰Ni) ²²⁴Ra/ ²²⁰Rn Mary **Coulex Target** (⁶⁰Ni, ¹¹²Cd, ¹²⁰Sn) Target recoil **Miniball:** DSSD

DSSD: Angles 15°-53° Front 16 strips Back 24/2 strips

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Miniball: 8x Triple Cluster ⇒ 24 HPGe Detectors Solid Angle coverage: ~60% of 4π DSSD Particle detector



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De-excitation process





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De-excitation process



E1 10⁴-10⁶x more probable



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De-excitation process



E1 10⁴-10⁶x more probable



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Populate 3⁻ level with E3 in Coulex \Rightarrow observe E1(and E2) decay γ ray(s)



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Particle Detector: (inverse kinematic)



Polar angle θ [°]



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Particle Detector: (inverse kinematic)





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Particle Detector: (inverse kinematic)







Particle Detector: (inverse kinematic)

HPGe γ-ray Detector array







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Particle Detector: (inverse kinematic)

HPGe γ-ray Detector array



Different Targets (Z)



Disentangle one- and multi-step excitation paths



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CoulEx: Experimental Info

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Different Targets (Z)



Disentangle one- and multi-step excitation paths

Literature (²²⁴Ra)

- Lifetimes (2x)
- Branching ratios (4x)
- Multipole mixing ratios

CoulEx: Experimental Info



CoulEx: Experimental Info



Decay Transitions



B(E3, $3^- \mapsto 0^+$) strength



Inverse sum rule





Nuclear surface



$$R(\Theta) = c(\beta_{\lambda})R_0 \left[1 + \sum_{\lambda=2}^{\infty} \sqrt{\frac{2\lambda+1}{4\pi}} \beta_{\lambda} P_{\lambda 0}(\cos\Theta) \right]$$

Our experiments: β_2, β_3 & Theory*: β_4

*W.Nazarewicz, Nucl. Phys. A429 (1984) 269



Nuclear surface



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Nucleus	λ	β_{λ}
²²⁰ Rn	2	0.119
	3	0.095
	4	0.002*
²²⁴ Ra	2	0.154
	3	0.097
	4	0.080*

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Nuclear surface



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Nuclear Schiff Moment

$$S = \Sigma rac{\langle +_{gs} || \hat{S}_z || -
angle \langle - || \hat{V}_{PT} || +_{gs}
angle}{E_0 - E_i} + c. \ c.$$





Nuclear Schiff Moment

$$S = \sum rac{\langle +_{gs} || \hat{S}_{z} || - \rangle \langle - || \hat{V}_{PT} || +_{gs}
angle}{E_{0} - E_{i}} + c. \ c$$

 $\sim eta_{3} eta_{2}$
 $\hat{S}_{z} = rac{e}{10} \sum_{\pi} (r_{\pi}^{2} - rac{5}{3} ar{r}_{ch}^{2}) z_{\pi}$

Asymmetric proton distribution (Pear shape!)





Nuclear Schiff Moment







Nuclear Schiff Moment



(Pear shape!)

Lab.

frame

N.Auerbach, V.V.Flambaum, & V. Spevak PRL 76 (1996) 4316 J.Dobaczewski & J.Engel, PRL **94** (2005) 232502



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Nuclear Schiff Moment



Asymmetric proton distribution , (Pear shape!)



N.Auerbach, V.V.Flambaum, & V. Spevak PRL 76 (1996) 4316 J.Dobaczewski & J.Engel, PRL **94** (2005) 232502





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Nuclear Schiff Moment



Asymmetric proton distribution , (Pear shape!)



On 223Ra E1 E2 M1+E2 z=0.14ns $11/2^{+}$ 174.7 z=0.3ns $9/2^{+}$ 130.3 z=0.4ns $7/2^{+}$ 61.5 z=0.6 ns $7/2^{+}$ 61.5 z=0.4ns $7/2^{+}$ 61.5 z=0.4ns $7/2^{+}$ 29.9 z=0.2 ns z=0.6 ns

> J=3/2-Parity doublet π no longer a good QN \Rightarrow states mix

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Nuclear Schiff Moment



Asymmetric proton distribution , (Pear shape!)



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Nuclear Schiff Moment



Asymmetric proton distribution (Pear shape!)



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J.Dobaczewski & J.Engel, PRL 94 (2005) 232502

Mid-term future?



IS552: Coul-Ex ^{222,226,228}Ra & ^{221,222}Rn



Mid-term future?



IS552: Coul-Ex 222,226,228 Ra & 221,222 Rn



Beam development β-decay 221,223 At $\rightarrow ^{221,223}$ Rn

Mid-term future?



IS552: Coul-Ex ^{222,226,228}Ra & ^{221,222}Rn



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...the ISOLDE beam operator crew



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...the ISOLDE beam operator crew

...the funding organizations! Especially:







Why odd-mass?







²²⁴Ra: Comparison to Theory





BCP: Barcelona-Catania Paris Energy Density Functional D1S: HFB Mean-Field (D1S Gogny Force)



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L.M.Robledo et al., PRC 81 (2010) 034315

²²⁴Ra: Comparison to Theory





L.M.Robledo et al., Phys.Rev.C 81 (2010) 034315

GOC/D1S: Hartree-Fock Bogoliubov

(Gogny D1S Force)

BCP:

Barcelona Catania Paris Energy Density Functional

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²²⁴Ra: Comparison to Theory



GOC/D1S:

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Hartree-Fock Bogoliubov (Gogny D1S Force)

BCP:

Barcelona Catania Paris Energy Density Functional



L.M.Robledo et al., Phys.Rev.C 81 (2010) 034315

E1 moments in nuclei



Electric dipole



Not possible!!! Only protons are charged

Mechanism

Divide center of charge and center of mass

E1 strength in spherical nuclei?



Coupling quadrupole and octupole degrees-of-freedom

3500

3000

2500

2000

1500

1000

500

0

Excitation Energy [keV]

3-

 2^+

Example: Nd-isotopic chain

Spherical nucleus

iE1

E₄



 E_{2^+}

 E_1

92

Question: Are there nuclei that have a static octupole deformation? Nuclear Schiff moment?

82

84

86

Neutron Number N

88

90



Odd-even parity levels: energy differences

E [MeV E2 E2 E1 13 2.0 11 10^{+} 9 8⁺-1.0 5 220Rn

J.F.Cocks, P.A.Butler et al., PRL 78, 2920 (1997)





Odd-even parity levels: energy differences

E [MeV E2 E2 **E1** 13 12+ 2.0 11 10^{+} 9 8⁺-1.0 5 4^+ 220Rn

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Odd-even parity levels: energy differences

E E2 [MeV E2 **E1** 13 12^{+,} 2.0 11 10⁺-9 8^{+.} 1.0 6 5 3 4^+ 220Rn 0

J.F.Cocks, P.A.Butler et al., PRL 78, 2920 (1997)



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Production of ISOL-Radioactive Ion Beams

Physical processes

²³⁸U binding energy: 1.8 GeV



- **1.** Spallation \Rightarrow heavy nucleus
- **2.** Fission \Rightarrow medium mass nucleus
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Target Outline



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ISOLDE @ CERN





ISOLDE @ CERN




ISOLDE @ CERN

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