

# Role of Complex Configurations in Nuclear Spectroscopy

N. Lo Iudice  
Università di Napoli Federico II

Dresden2010

# A QPM study of low-lying spectra in

- **Spherical heavy nuclei**

in collaboration with Ch. Stoyanov (Sofia)

-- **Deformed heavy nuclei**

in collaboration with A.V. Sushkov (Dubna)

# Multiphonon excitations: Exp. evidence

## \* High-energy

(N. Frascaria, NP A482, 245c(1988);  
T. Auman, P.F. Bortignon, H.  
Hemling, Ann. Rev. Nucl. Part.  
Sc. 48, 351 (1998))

Double

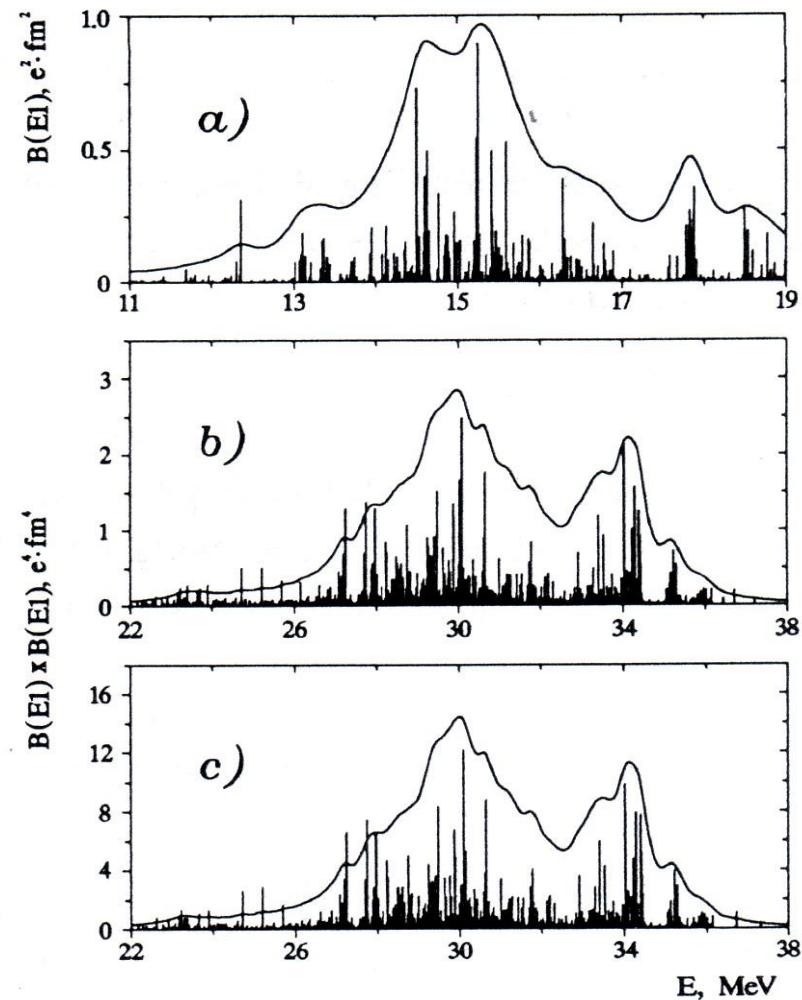
$$D \times D |0\rangle$$

and

triple

$$D \times D \times D |0\rangle$$

dipole giant resonances



# Multiphonon excitations: Exp. evidence

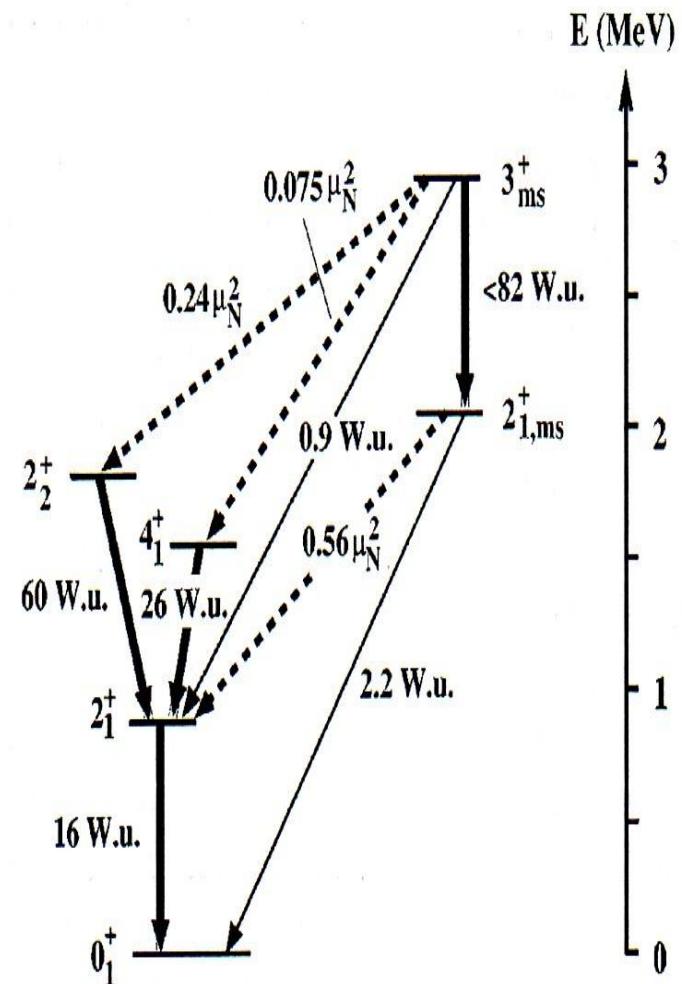
## \*\* Low-energy

M. Kneissl, H.H. Pitz, and A. Zilges, Prog. Part. Nucl. Phys. 37, 439 (1996); M. Kneissl, N. Pietralla, and A. Zilges, J.Phys. G, 32, R217 (2006) :

- Two- and three-phonon multiplets

$$Q_2 \times Q_3 |0\rangle, \quad Q_2 \times Q_2 \times Q_3 |0\rangle$$

- In particular:  
Proton-neutron (F-spin) mixed-symmetry states  
(N. Pietralla et al. PRL 83, 1303 (1999))



**QPM** (Soloviev, Theory of Atomic Nuclei: Quasiparticles and Phonons, Bristol, (1992)):  
**A brief outline**

$$H = H_{sp} + V_{pair} + V_{pp} + V_{ff}$$

$$V_{pp} = \sum_{\lambda} G_{\lambda} P_{\lambda}^{\dagger} P_{\lambda}$$

$$P_{\lambda}^{\dagger} = \sum_{ij} f_{ij}^{\lambda} (a_i^{\dagger} \times a_j^{\dagger})^{\lambda}$$

$$V_{ff} = \sum_{\lambda} \kappa_{\lambda} F_{\lambda}^{\dagger} F_{\lambda}$$

$$F_{\lambda}^{\dagger} = \sum_{ij} f_{ij}^{\lambda} (a_i^{\dagger} \times a_j)^{\lambda}$$

1° step: From particle to quasiparticle

$$\{a^{\dagger} a\} \Rightarrow \{a^{\dagger} a\}$$



$$\begin{aligned} H[(a^{\dagger} a), (a^{\dagger} a^{\dagger}), (aa)] &\Rightarrow H[(a^{\dagger} a), (a^{\dagger} a^{\dagger}), (a a)] \\ (\text{ph}) &(\text{qp}) \end{aligned}$$

# A brief outline of QPM (Soloviev, Theory of Atomic Nuclei: Quasiparticles and Phonons, Bristol, (1992))

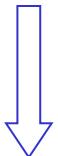
2<sup>nd</sup> step: From quasiparticles to RPA phonons  
of multipolarity  $\lambda$

$$\left\{ \begin{array}{c} \alpha^\dagger \alpha^\dagger \\ \alpha \alpha \end{array} \right\} \xrightarrow{\hspace{2cm}} \left\{ \begin{array}{c} O_\lambda^\dagger \\ O_\lambda \end{array} \right\}$$

$$O_\lambda^\dagger = \sum_{kl} [X_{kl}(\lambda) \alpha_k^\dagger \alpha_l^\dagger - Y_{kl}(\lambda) \alpha_k \alpha_l]$$

### 3° step: From particle to phonon Hamiltonian

$$H = H_{sp} + V_{pair} + V_{pp} + V_{ff}$$



$$H_{QPM} = \sum_{n\lambda} \omega_n(\lambda) Q_\lambda^\dagger Q_\lambda + H_{vq}$$



$$\begin{aligned} \Psi_v = & \sum_n c_n Q_v^\dagger(n) |0\rangle + \sum_{ij} C_{ij} Q_i^\dagger(i) Q_j^\dagger(j) |0\rangle \\ & + \sum_{ijk} C_{ijk} Q_i^\dagger(i) Q_j^\dagger(j) Q_k^\dagger(k) |0\rangle \end{aligned}$$

# Spherical Nuclei: $\pi$ - $v$ Symmetric and MS states

## Symmetric

$$|n, v\rangle_s = Q_S^n |0\rangle = (Q_p + Q_n)^n |0\rangle$$

## MS

$$|n, v\rangle_{MS} = (Q_p - Q_n) (Q_p + Q_n)^{(n-1)} |0\rangle$$

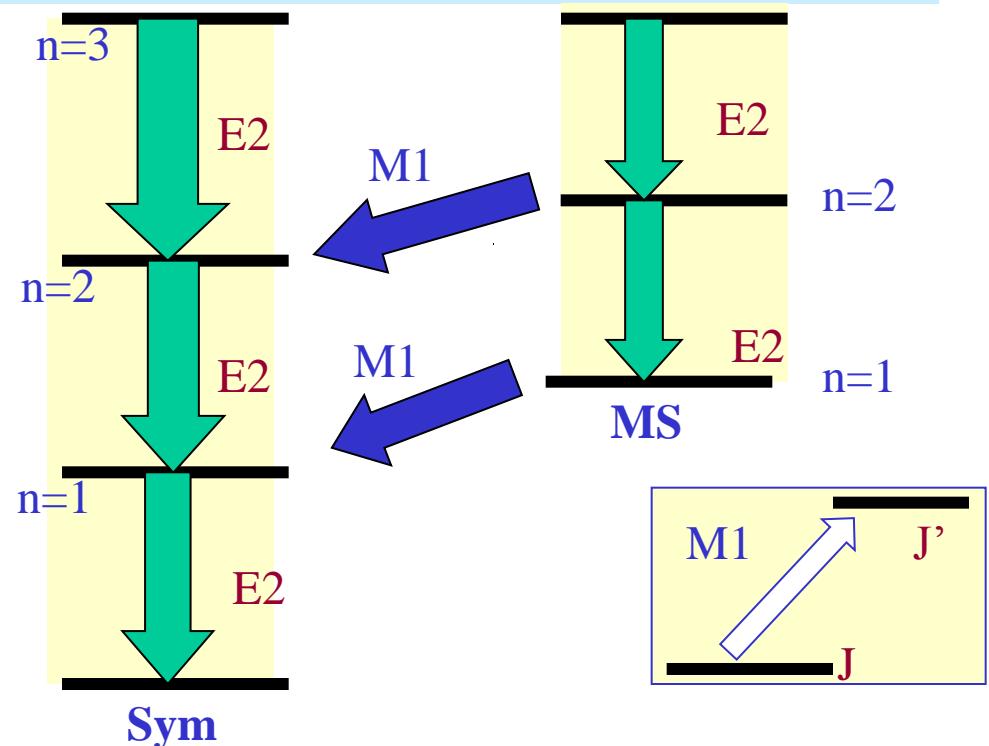
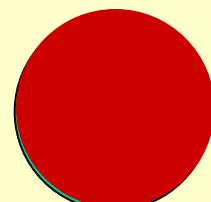
## Signature: Transitions

$$\mathcal{M}_{(E2)} \propto Q_S \quad n \rightarrow n-1 \quad (\Delta n=1)$$

symmetry preserving  $(\Delta F=0)$

$$\mathcal{M}_{(M1)} \propto J_n - J_p \quad n \rightarrow n \quad (\Delta n=0)$$

symmetry changing  $(\Delta F=1)$



## Scissors multiplet

$$S |n, v\rangle_s = (J_p - J_n) Q_S^n |0\rangle$$

$$\propto [(Q_p - Q_n) (Q_p + Q_n)^{(n-1)}] |0\rangle$$

$$\propto |n, v\rangle_{MS}$$

Preliminaries: **Testing the isospin nature of the QRPA  $2^+$  states through the ratio**

$$B(2^+)_{RPA} = \left| \frac{\langle 2^+ | (Q_p - Q_n) | 0 \rangle}{\langle 2^+ | (Q_p + Q_n) | 0 \rangle} \right|^2$$

1.  $B(2^+) < 1 \rightarrow |2^+ \rangle$  **isoscalar** ( $\Delta T=0$ )
2.  $B(2^+) > 1 \rightarrow |2^+ \rangle$  **isovector** ( $\Delta T=1$ )

**B(2<sup>+</sup>)** is very sensitive to the ratio **G<sub>2</sub>/κ<sub>2</sub>**

In <sup>136</sup>Ba

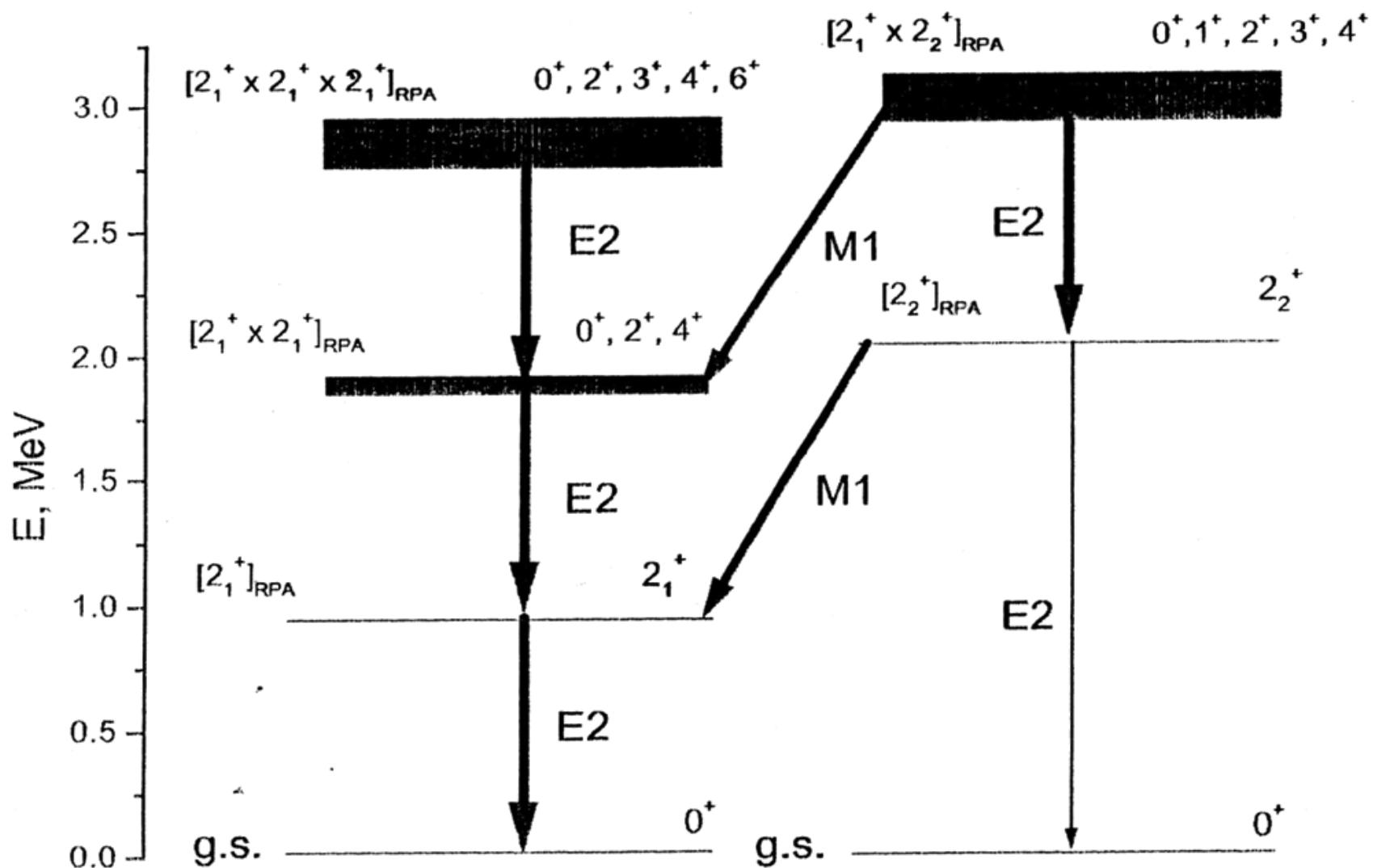
$B(E2)_{RPA}$	$B(M1)_{RPA}$	$B(2_{iv}^+)$
$\frac{G^{(2)}}{\kappa_0^2}$	$g.s. \rightarrow 2_{iv}^+$	$2_{iv}^+ \rightarrow 2_{is}^+$
	$\left[ e^2 b^2 \right]$	$\left[ \mu_N^2 \right]$
0	0.0032	0.042
0.85	0.011	0.24
		22.6

# Low-lying states in $^{94}\text{Mo}$ :

## Energies and phonon structure

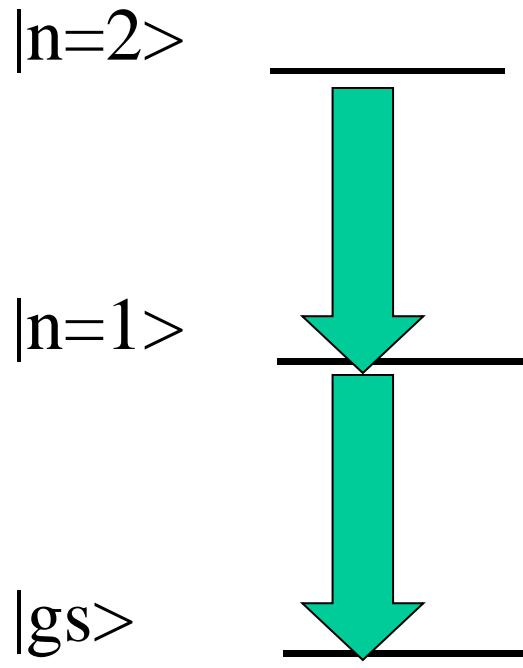
	State T J $\pi$	E (keV) EXP	E (keV) QPM	Structure, %
IS	$2_{1,\text{is}}^+$	871	860	93% [ $2_{\text{is}}^+$ ] <sub>RPA</sub>
	$2_{2,\text{is}}^+$	1864	1750	82% [ $2_{\text{is}}^+ \otimes 2_{\text{is}}^+$ ] <sub>RPA</sub>
IV	$4_{1,\text{is}}^+$	1573	1733	82% [ $2_{\text{is}}^+ \otimes 2_{\text{is}}^+$ ] <sub>RPA</sub>
	$1_{1,\text{iv}}^+$	3129	2880	90% [ $2_{\text{is}}^+ \otimes 2_{\text{iv}}^+$ ] <sub>RPA</sub>
	$2_{1,\text{iv}}^+$	2067	1940	95% [ $2_{\text{iv}}^+$ ] <sub>RPA</sub>
	$2_{2,\text{iv}}^+$	2393	2730	27% [ $2_{\text{is}}^+ \otimes 2_{\text{iv}}^+$ ] <sub>RPA</sub>
	$2_{3,\text{iv}}^+$	2740	3014	59% [ $2_{\text{is}}^+ \otimes 2_{\text{iv}}^+$ ] <sub>RPA</sub>
	$4_{1,\text{iv}}^+$		3120	64% [ $2_{\text{is}}^+ \otimes 2_{\text{iv}}^+$ ] <sub>RPA</sub>
	$3_{1,\text{iv}}^+$	2965	2940	87% [ $2_{\text{is}}^+ \otimes 2_{\text{iv}}^+$ ] <sub>RPA</sub>
	$1_2^+$		3550	40% [ $1_1^+$ ] <sub>RPA</sub>

# $^{94}\text{Mo}$ level scheme.



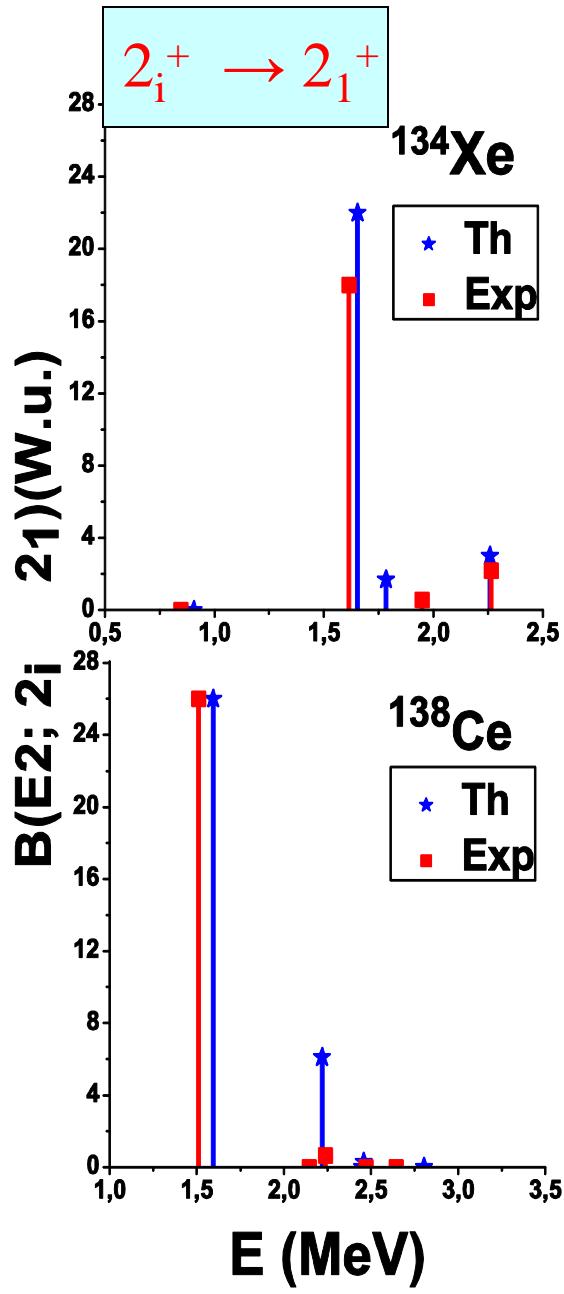
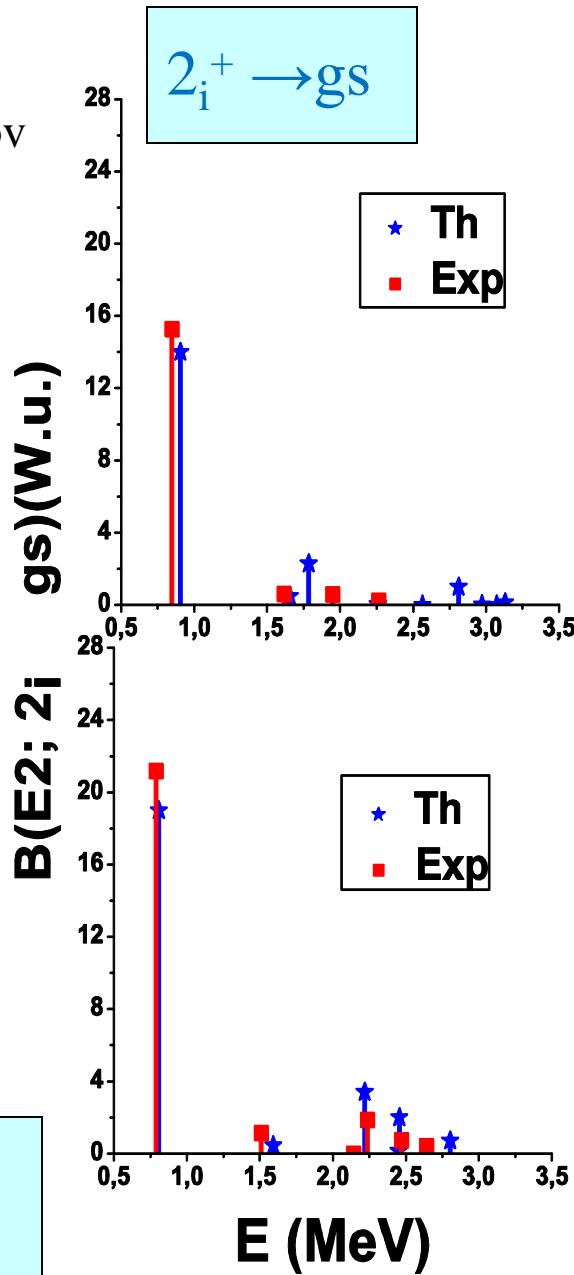
# N=80 isotones

N.L., Ch. Stoyanov, D.Tarpanov  
PRC 77 (08)



## E2 Transitions

$(\Delta F=0, \quad \Delta n = 1)$

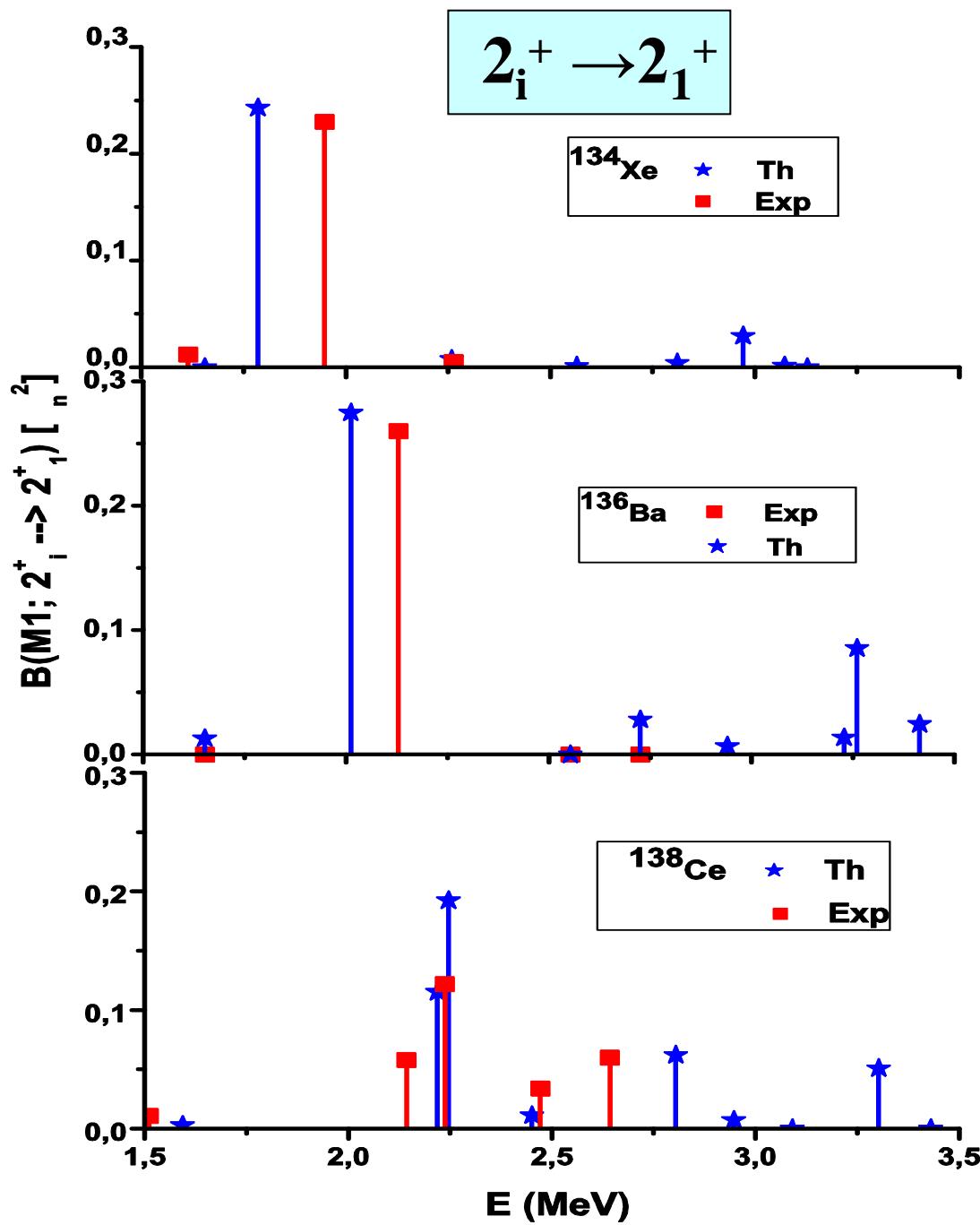
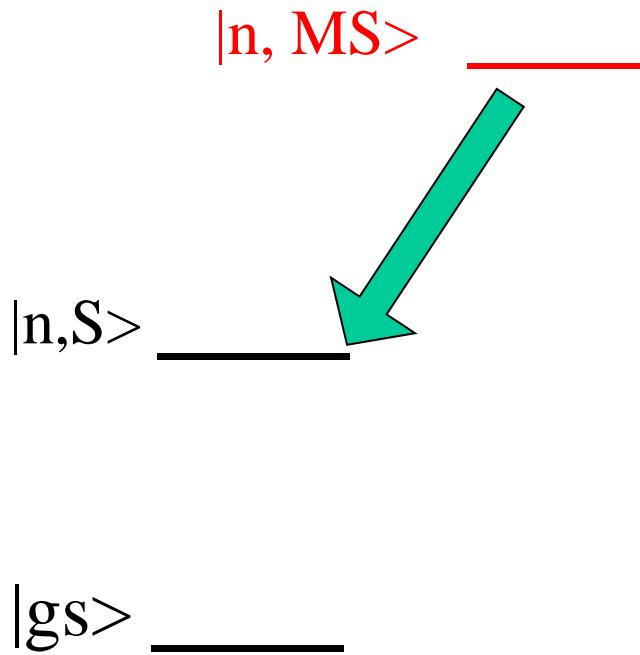


N=80

## M1 Transitions

( $\Delta n=0$ ,  $\Delta F=1$ )

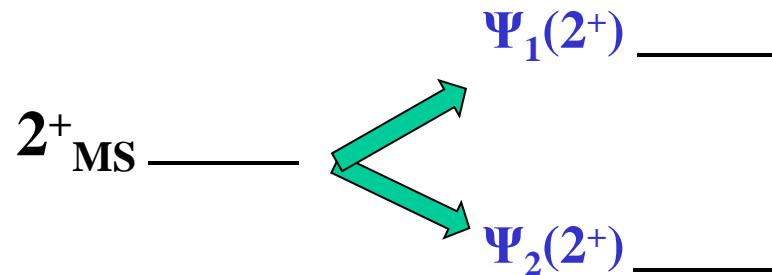
QPM versus EXP



# Splitting of B(M1)

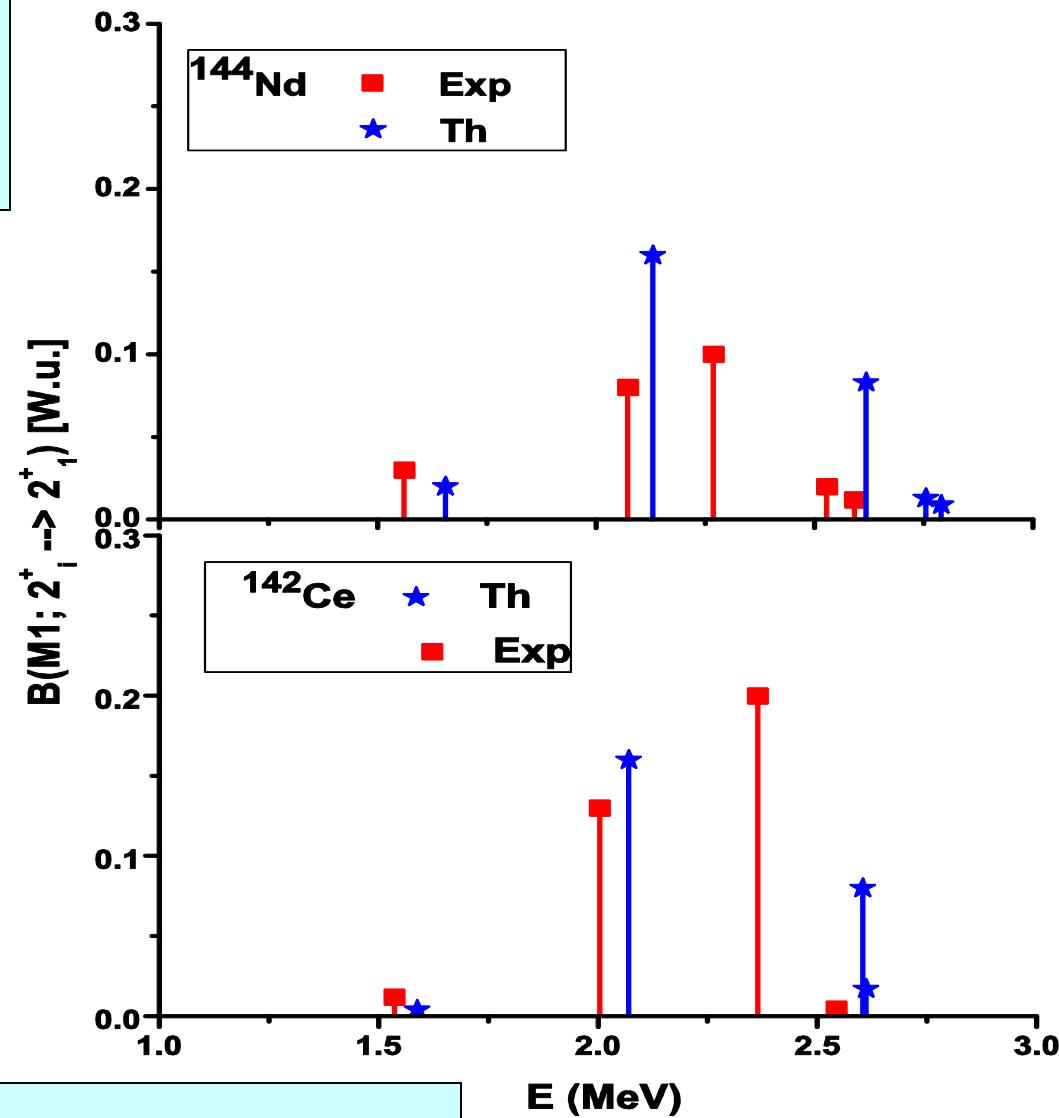
## in N=84 isotones

N. L. Ch. Stoyanov N. Pietralla PRC 80(2009)



Why the splitting?

Phonon coupling  
induced by the neutron  
shell structure in  
N=84 nuclei



$$\Psi_1(2^+) = c_1 |n=1, 2^+_{\text{MS}}\rangle + c_2 |n=2\rangle + c_3 |n=3\rangle$$

$$\Psi_2(2^+) = b_1 |n=1, 2^+_{\text{MS}}\rangle + b_2 |n=2\rangle + b_3 |n=3\rangle$$

# Deformed Nuclei: From one to many $0^+$

The issue:

Large abundance of  $0^+$  levels populated in (p,t) experiments on

$^{158}\text{Gd}$   $n=13$   $0^+$  ( $E < 3.2$  MeV)

(Lesher *et al.* PRC 66, 051305(R) (2002))

$^{228}\text{Th}$ ,  $^{230}\text{Th}$  and  $^{232}\text{U}$

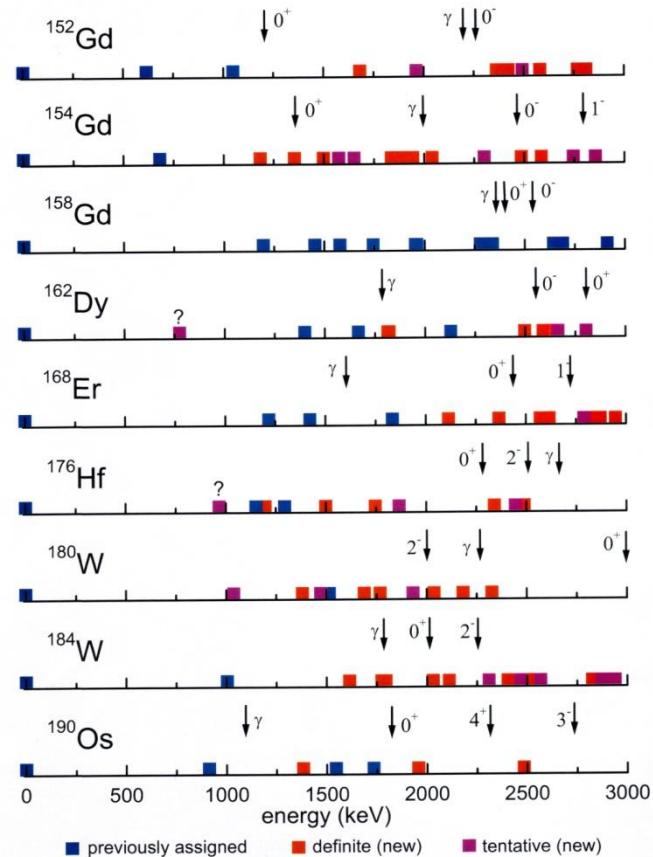
$n \sim 10$  ( $E < 3.0$  MeV)

(Wirth *et al.* PRC 69, 044310 (2004))

$^{168}\text{Er}$   $n \sim 25$  !! ( $E < 4$  MeV)

D. Bucurescu *et al.*, PRC 73, 064309 (2006)

This plot gives only the excitation energies of the states. The arrows are the double phonon estimations.

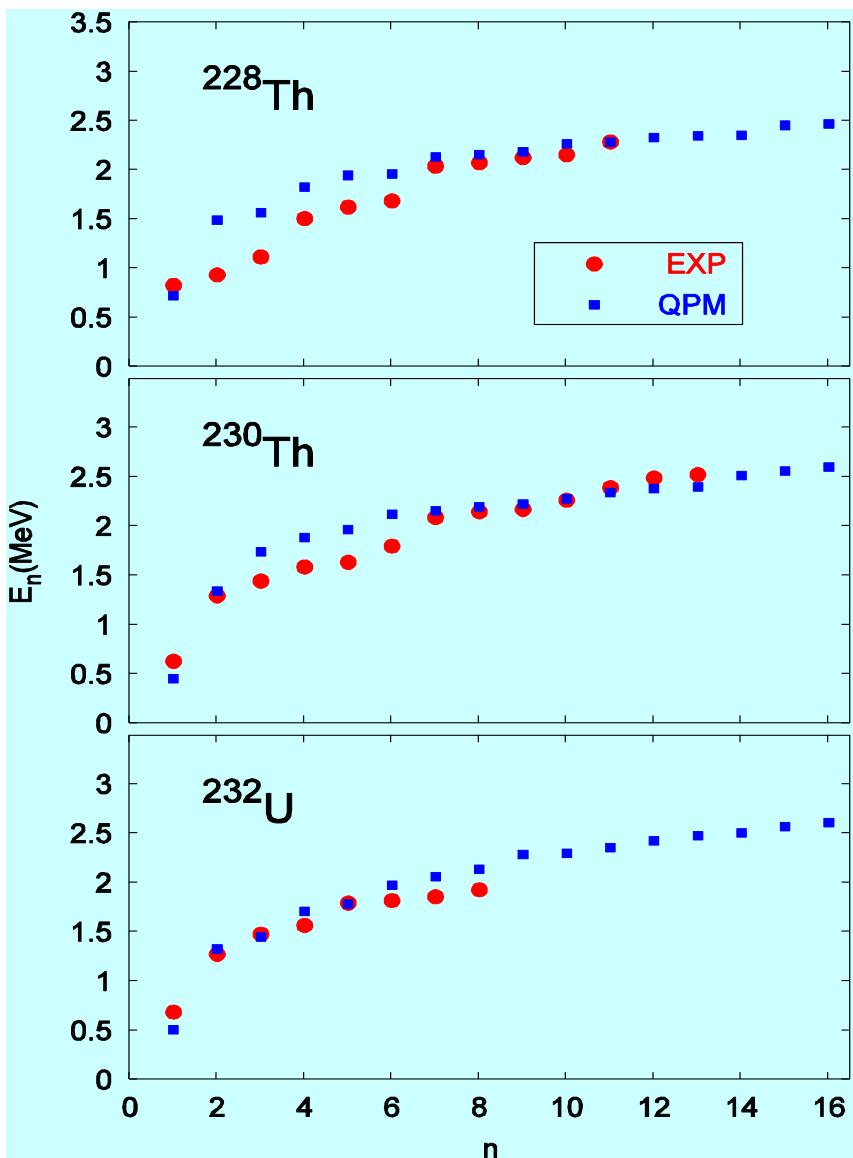
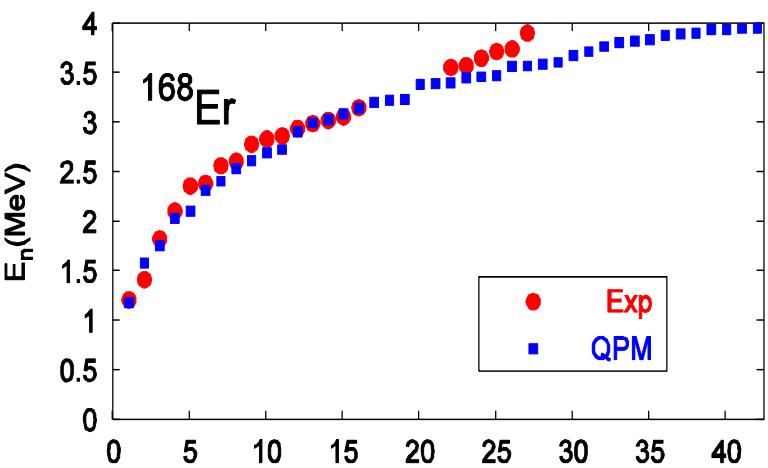
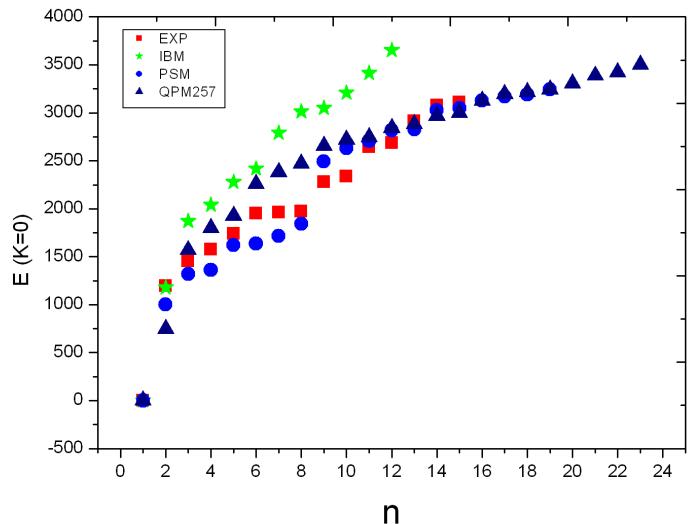


## Systematic

D. A. Meyer *et al.*, PRC 74, 044309 (2006)  
and references therein

# QPM accounts for all $0^+$ levels and even more!!

N.L. A.V. Sushkov, N. Yu. Shirikova PRC 70 (04); PRC 72 (05)



# Nature of the $0^+$ :Quadrupole collective ( $\beta$ -band)?

$|K^\pi=0^+> \sim Q_0 |0>$

No !!

$B(E2, 0^+ \rightarrow 2_g^+) \ll B_{vib}(E2)$

$\sim <0|Q_0^2|0> \sim 33$  w.u.

(P. E. Garrett J. P. G 27 (2001) R1)

$B(E0) \ll B_{vib}(E0) \sim$

$<0|(r^2)^2|0>/<0|r^2|0>^2$

$\sim 85 \div 230 (10^{-3})$

J. L. Wood et al. NPA651 (1999) 323

But we need more experimental information

# Nature of the $0^+$ : Pairing vibration?

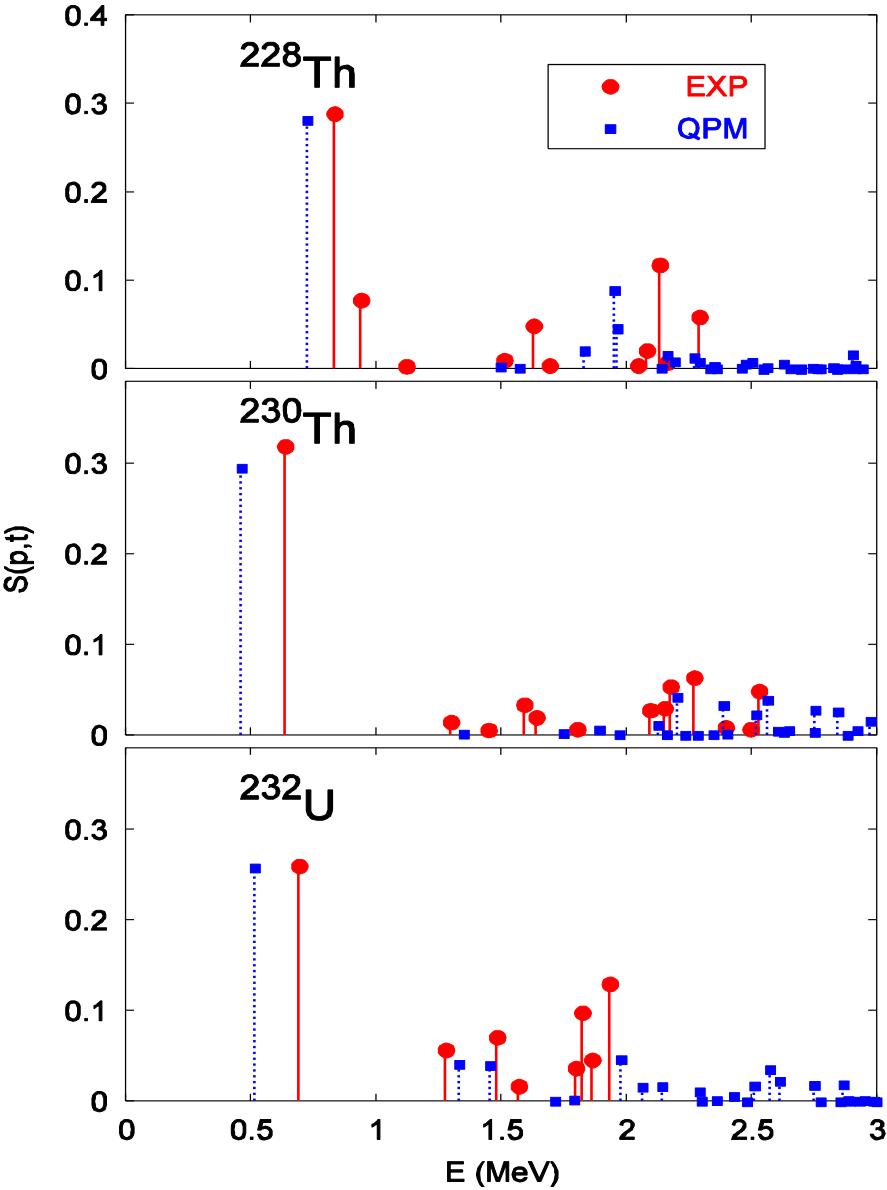
$$\langle \mathbf{0} | \mathbf{P}_0^2 | \mathbf{0} \rangle \sim |\langle \mathbf{n} | \mathbf{P}_0 | \mathbf{0} \rangle|^2$$

$$\mathbf{P}_0 = \sum_{\mathbf{q}} \mathbf{a}_{\mathbf{q}} \mathbf{a}_{-\mathbf{q}}$$

Normalized (p,t) spectroscopic factors

$$S_n(p,t) = [\langle n | P_0 | 0 \rangle / \langle 0 | P_0 | 0 \rangle]^2$$

# $S(p,t)$ and pairing collectivity



RPA w.f.

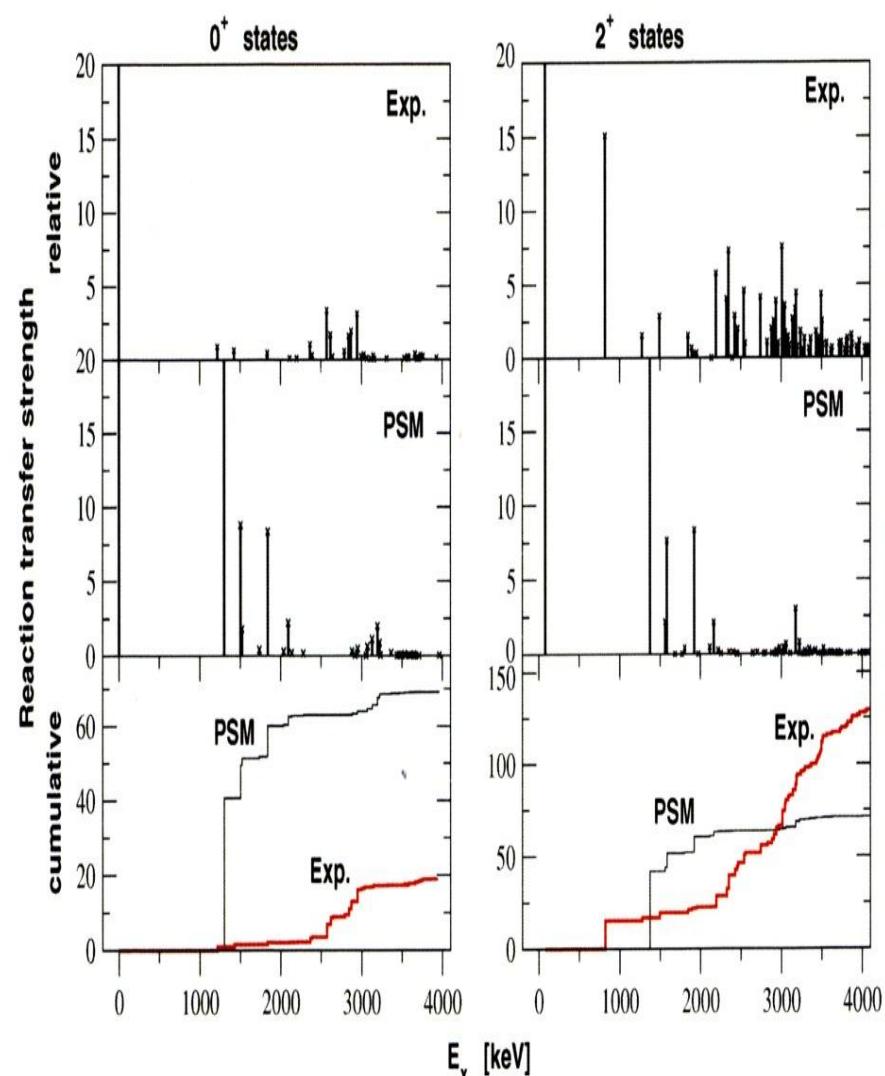
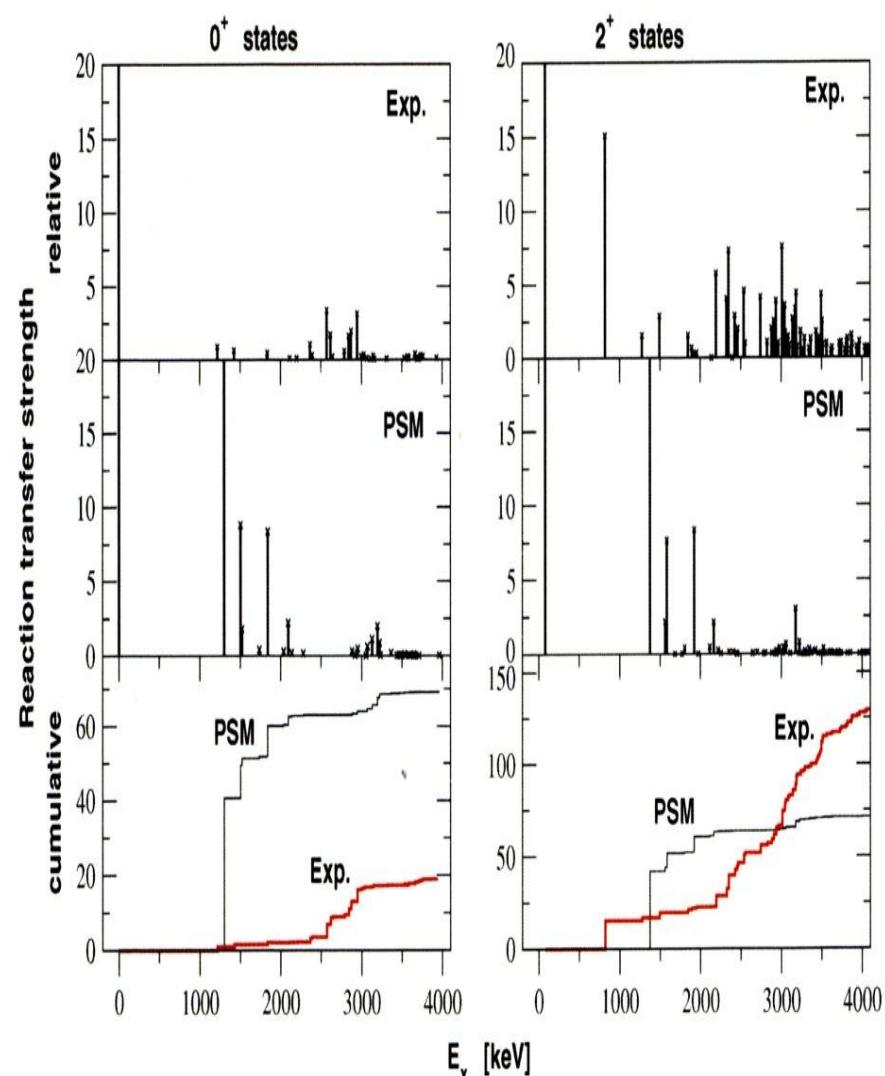
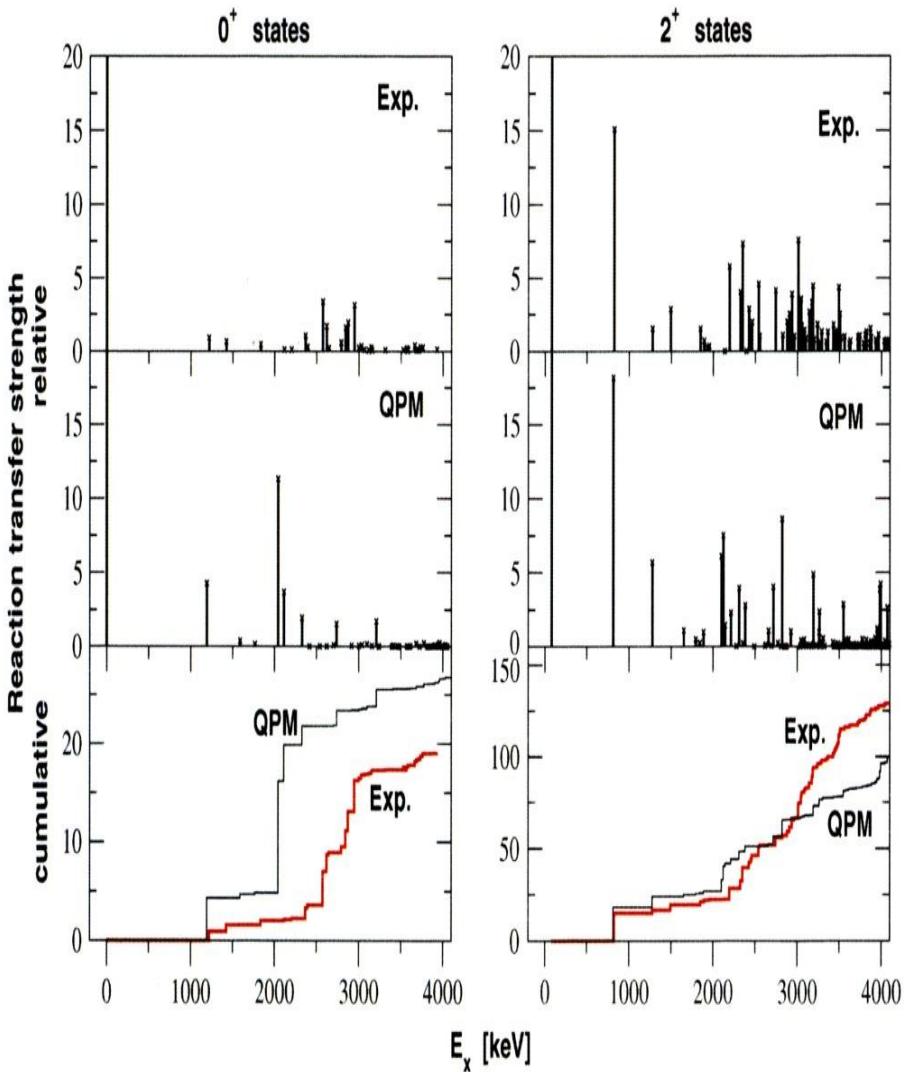
$$|0^+ \rangle_{\text{RPA}} \sim 0.46 [(521\uparrow)(521\uparrow)] + 0.44 [(505\uparrow)(505\uparrow)] + 0.39 [(523\downarrow)(523\downarrow)] + 0.37 [(411\uparrow)(411\uparrow)] + ..$$

Pairing acts **coherently** only  
in the **lowest RPA  $0^+$**  !!!

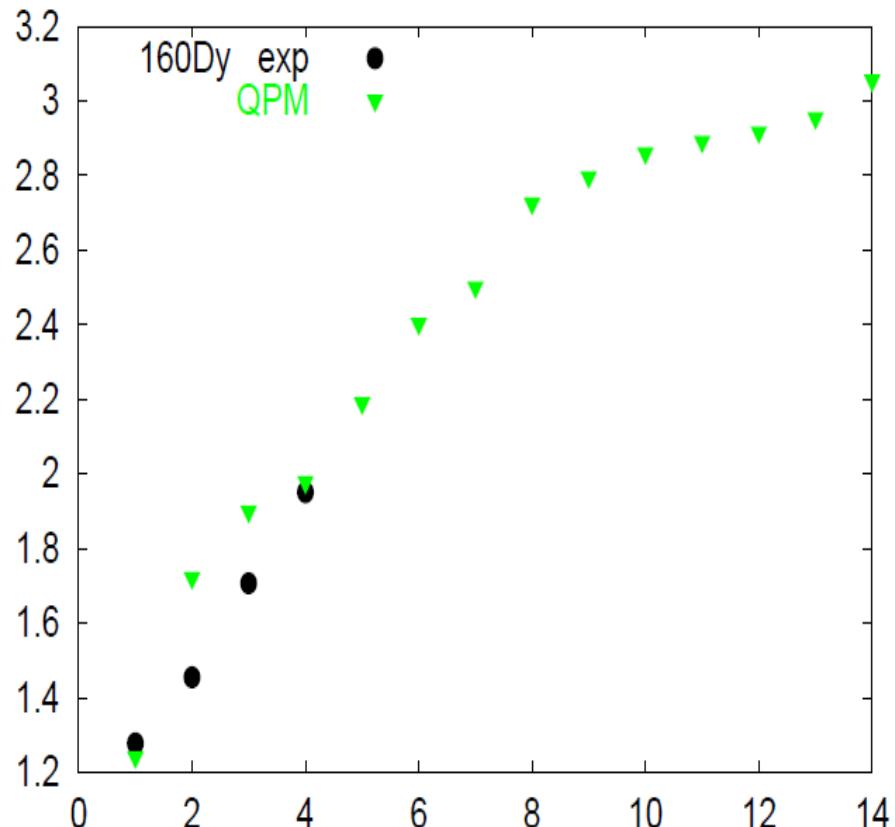
Fragmentation due to

- i) s.p. decay (Landau damping)
- ii) phonon coupling (collisional damping)  
(spoils partly pairing coherence,  
especially in  $^{168}\text{Er}$ )

# $^{168}\text{Er}$ as a special case (Bucurescu et al., PRC 73, 064309 (2006))



# $0^+$ in transitional nuclei: $^{160}\text{Dy}$

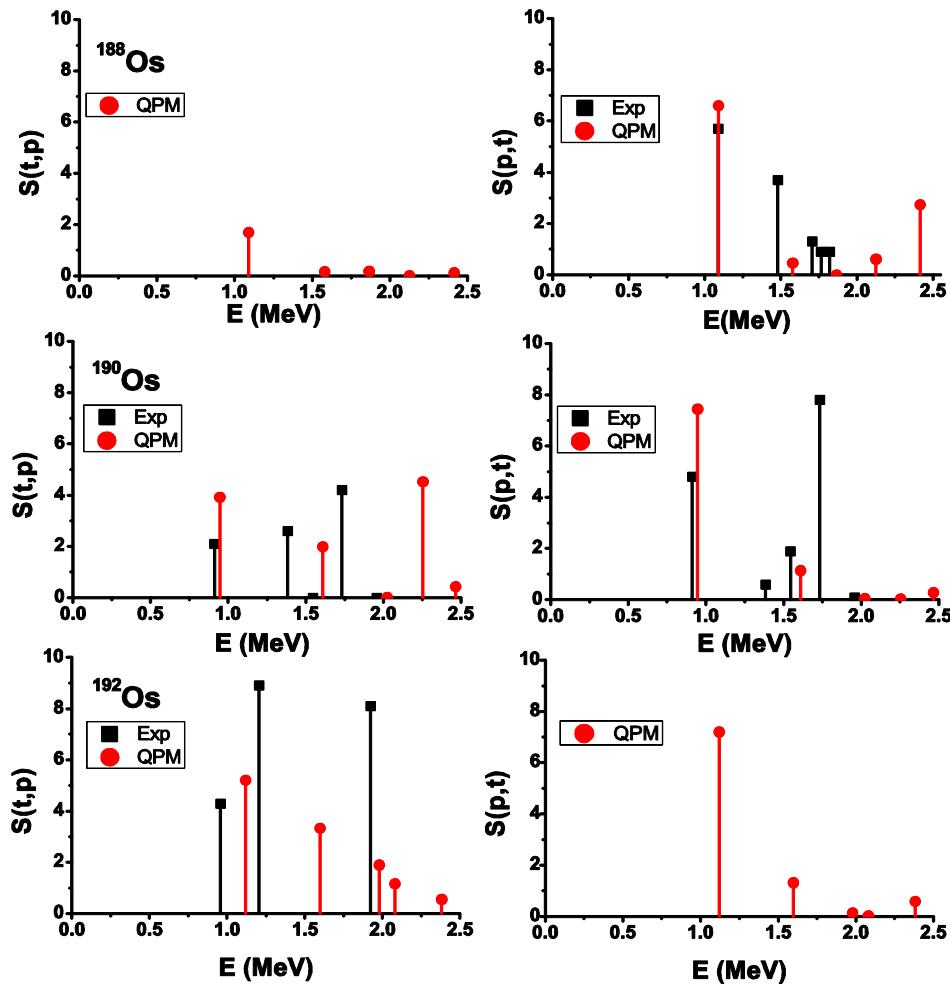


$S(pt)$  for  $1279.95 \text{ keV}$  state

Exp	Calc
0.15	0.18

# $0^+$ in $\gamma$ -soft nuclei: Os isotopes

N. Lo Iudice and A. V. Sushkov, PRC 78, 054304 (2008).



**Evolution toward  $\gamma$  softness  
(from  $A=188$  to  $A=192$ )**

-Increasing strengths  
 $S(t,p)$  and  $S(p,t)$

-Increasing complexity of  $|\Psi_0\rangle$

\*Fragmentation of  $|\Psi_0\rangle$

$|\Psi_0\rangle \sim c_1 |(20)_1\rangle + c_2 |(20)_2\rangle + \dots + \dots c_{22} |(22)_1, (22)_1\rangle$

\*\* dominance of  $\pi$ -pairing in  $|(20)_1\rangle$  and of  $\nu$ -pairing in others

# Dominant two-phonon configurations

$^{158}\text{Gd}$	MeV
$31 \otimes 31$	1.96
$44 \otimes 44$	2.9

$^{168}\text{Er}$	MeV
$22 \otimes 22$	2.8
$4^- \otimes 4^-$	2.6

$^{160}\text{Dy}$	MeV
$22 \otimes 22$	1.7
$32 \otimes 32$	2.5
$4^- \otimes 4^-$	3.3
$44 \otimes 44$	3.6

$^{190}\text{Os}$	MeV
$22 \otimes 22$	0.94
$33 \otimes 33$	2.5
$32 \otimes 32$	2.8
$44 \otimes 44$	3.6

# Nature of $0^+$ states

multiphonon excitations ?      NO (in general)

$$|0^+ \rangle \sim |(\lambda x \lambda)^0 \rangle$$

Elementary one-phonon excitations ?   Yes

Collective  $\beta$ -vibrations?                  No!

$$|K^{\pi=0^+} \rangle \sim Q_0 |0 \rangle$$

Pairing vibrations?                  Yes

$$|K^{\pi=0^+} \rangle \sim P_0 |0 \rangle = G \sum a_a^\dagger a_{-a}^\dagger |0 \rangle$$

More specifically

Damped Pairing vibrations

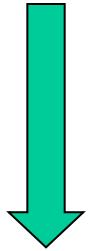
Due to phonon coupling

# $4^+$ state in Os isotopes

Double- $\gamma$ ? (C.Y. Wu et al. PRC 64 (01))

–  $E_4 \sim 2 E_\gamma$

$R_4(E2) = B(E2, 4^+ \rightarrow 2^+)/B(E2, 2^+ \rightarrow 0^+) \sim 2$

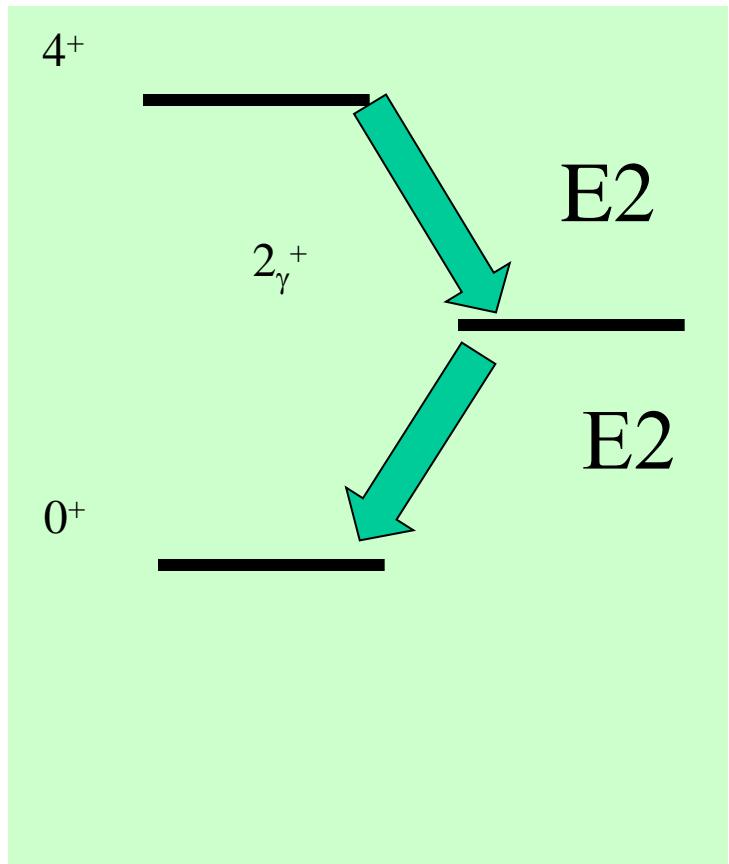


$|\Psi_4\rangle \sim |\gamma\gamma\rangle$

with

$$|c(n=1)|^2 < 25 \%$$

one-phonon hexadecapole admixture

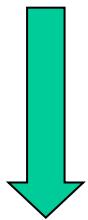


# $4^+$ state in Os isotopes

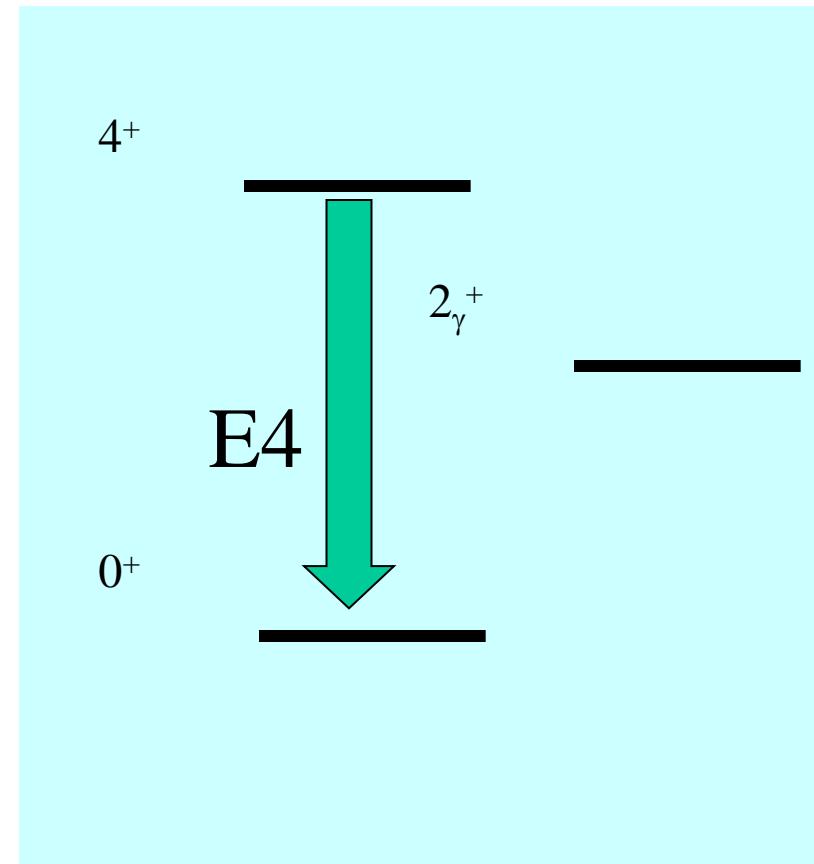
Hexadecapole one-phonon? (D. G. Burke PRC 66 (02))

-B(E4, K=4 → 0) large

- From (t, α) (d,  ${}^3\text{He}$ )  
large admixtures of  
 $5/2^+[402]_\pi + 3/2^+ [402]_\pi$



$|\Psi_4\rangle \sim |n=1,4+\rangle$



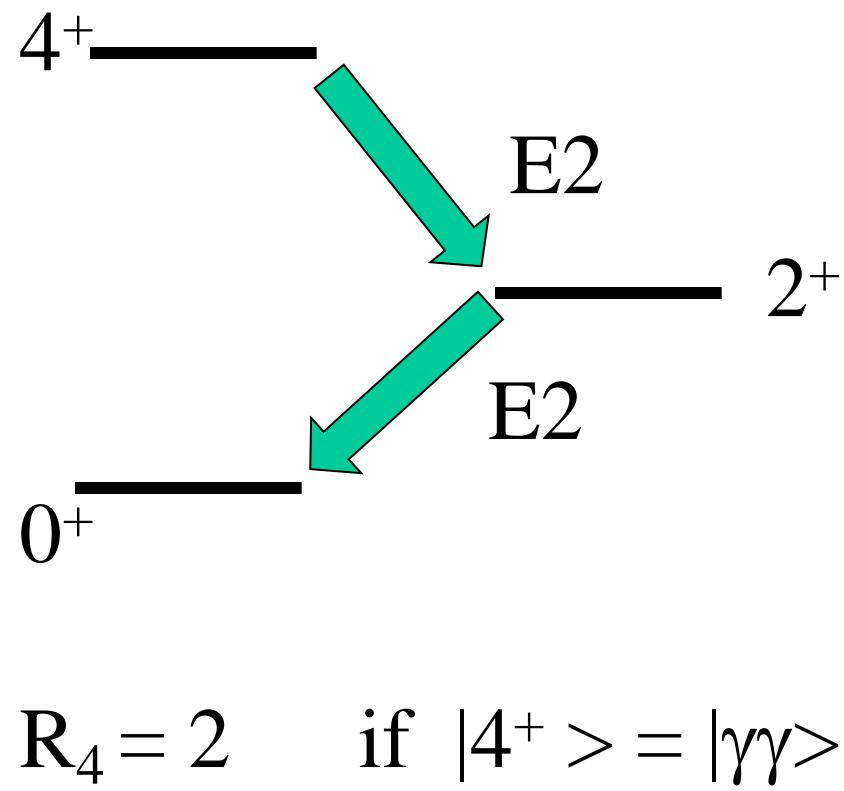
# **4<sup>+</sup> state in Os isotopes**

N. Lo Iudice and A. V. Sushkov, PRC 78, 054304 (2008).

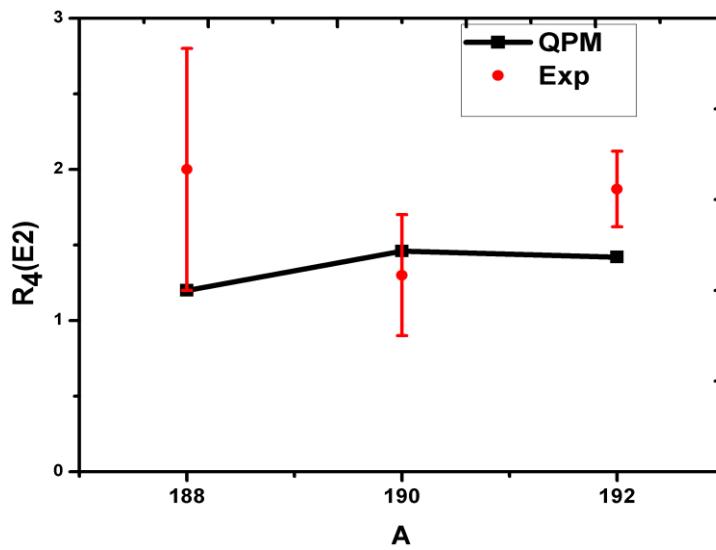
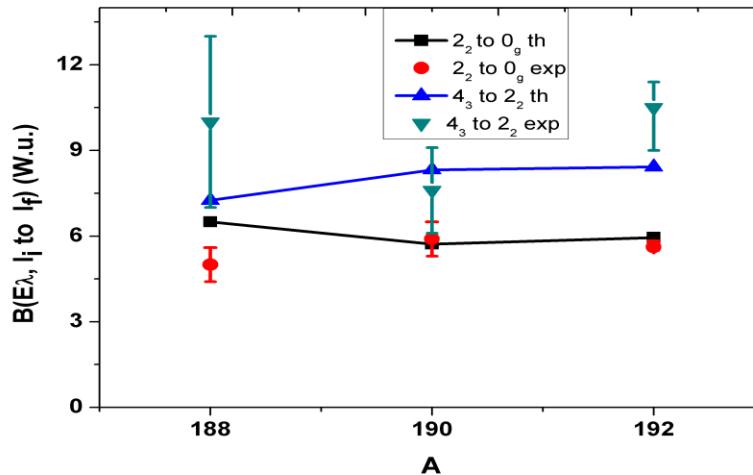
QPM

$$\begin{aligned} |\Psi_4\rangle \sim & 0.60 |n=1, 4^+\rangle \\ & + 0.35 |n=2, \gamma\gamma\rangle \end{aligned}$$

$$R_4(E2) = B(E2; 4^+ \rightarrow 2^+)/B(E2; 2^+ \rightarrow 0_g)$$

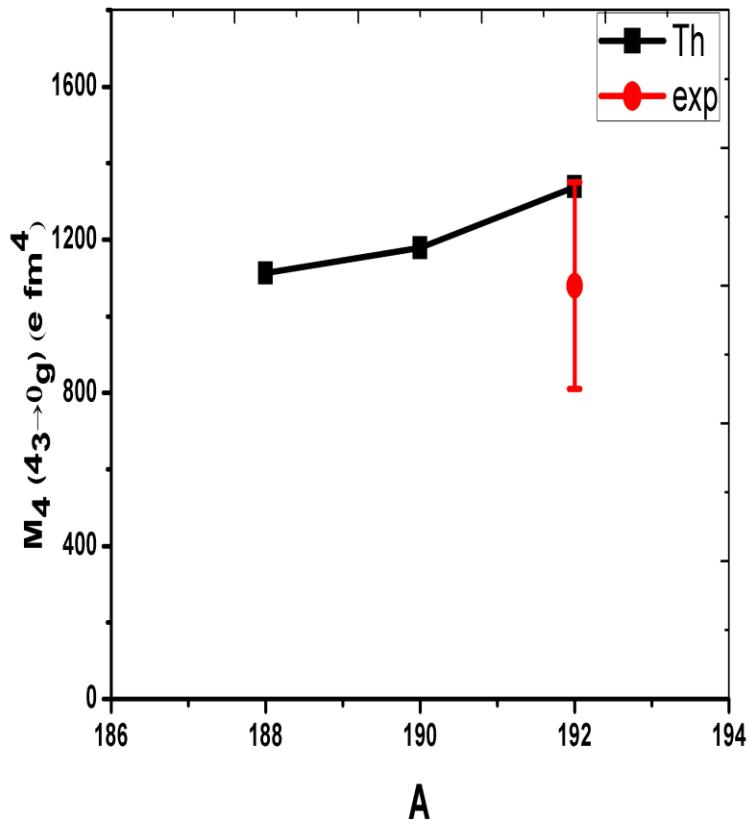
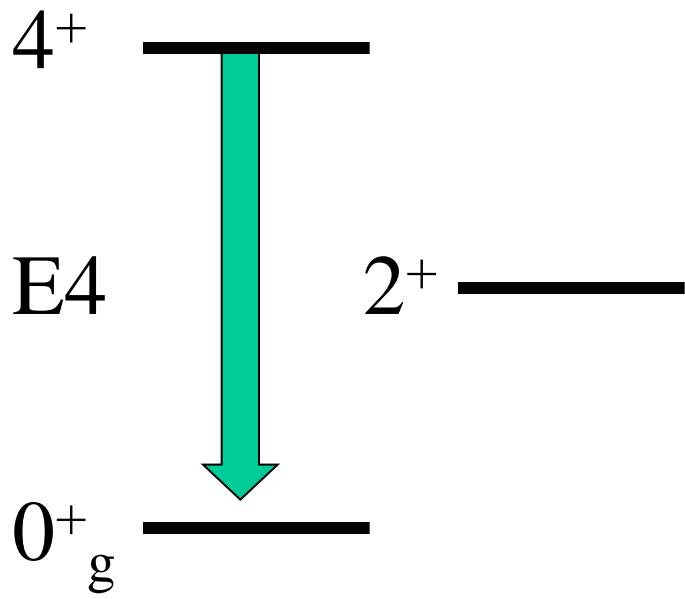


$$R_4 = 2 \quad \text{if} \quad |4^+ \rangle = |\gamma\gamma\rangle$$



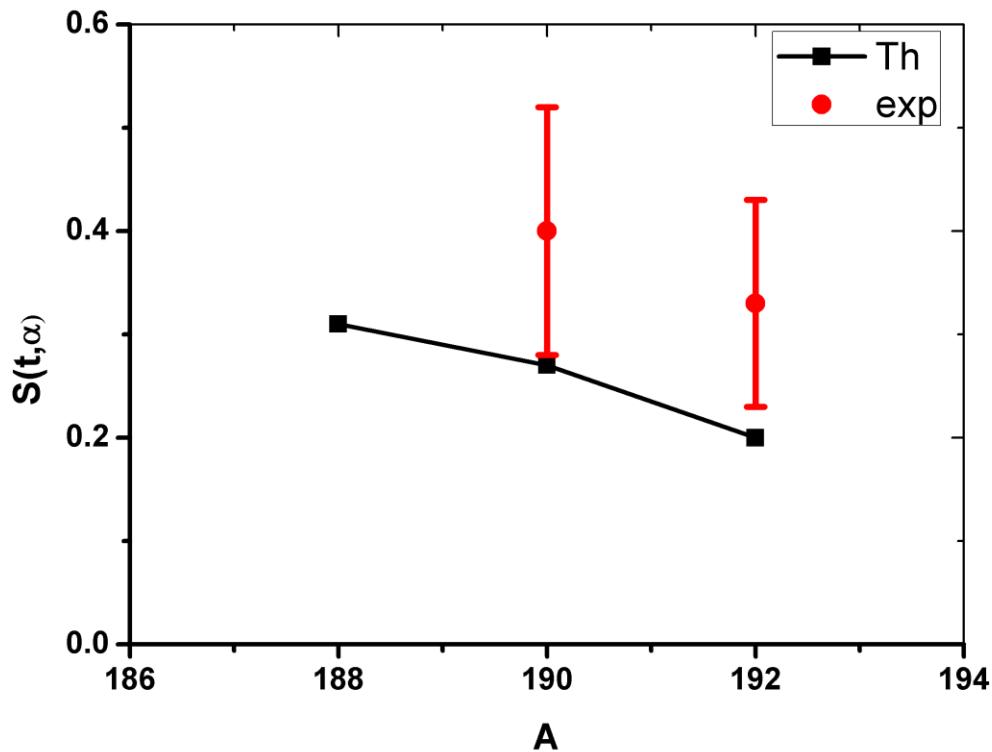
$\Psi(\text{QPM}) \sim 0.60 |n=1, 4^+\rangle + 0.35 |\gamma\gamma\rangle$

$$\mathcal{M}_4 (4^+ \rightarrow 0^+_g) = \langle 4^+ || M(\lambda=4) || 0^+_g \rangle$$



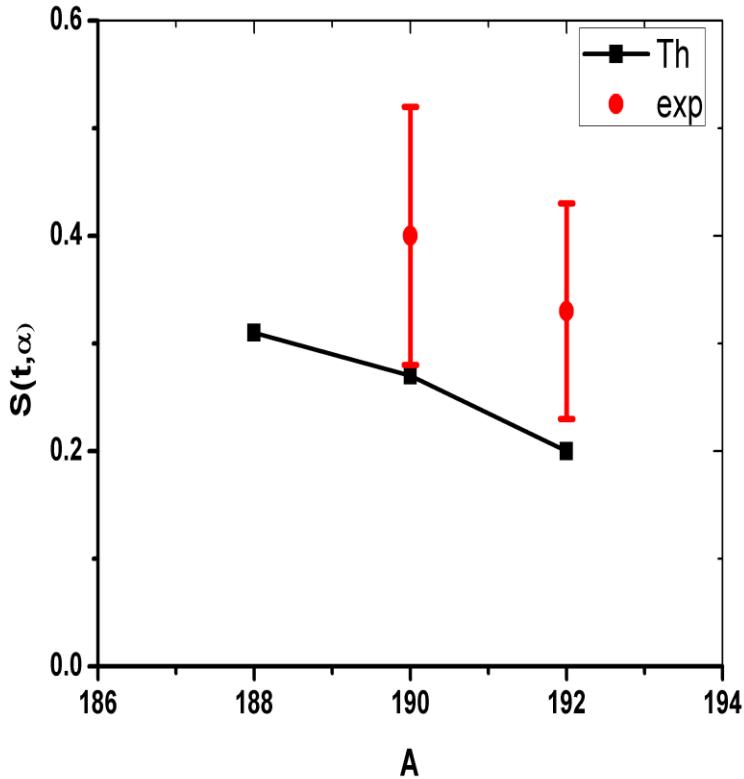
$\Psi(\text{QPM}) \sim 0.60 |n=1, 4^+\rangle + 0.35 |\gamma\gamma\rangle$

# (t, $\alpha$ ) reaction: Spectroscopic factor



$$\Psi(\text{QPM}) \sim 0.60 |n=1, 4^+\rangle + 0.35 |\gamma\gamma\rangle$$

# $(t,\alpha)$ and $(^3\text{He},d)$ reaction: Spectroscopic factor



Dominant configuration

$5/2^+[402]_\pi + 3/2^+ [402]_\pi$

$^{188}\text{Os}$ : 32%

$^{190}\text{Os}$ : 30%

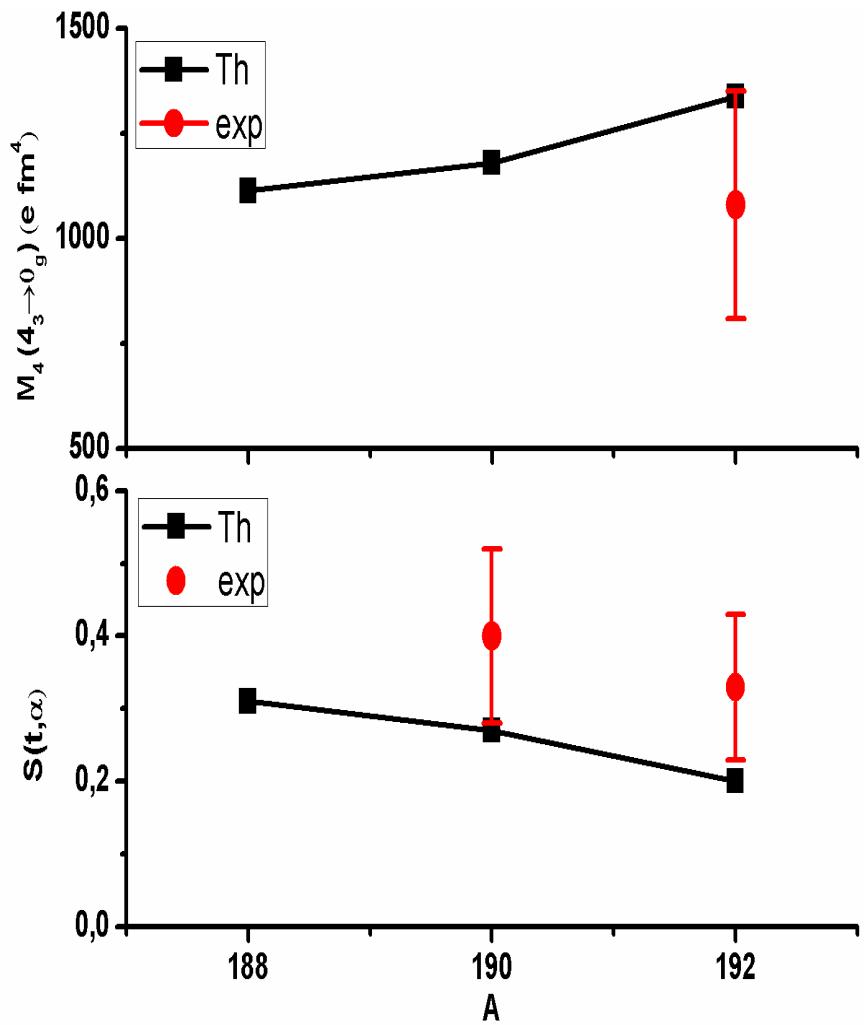
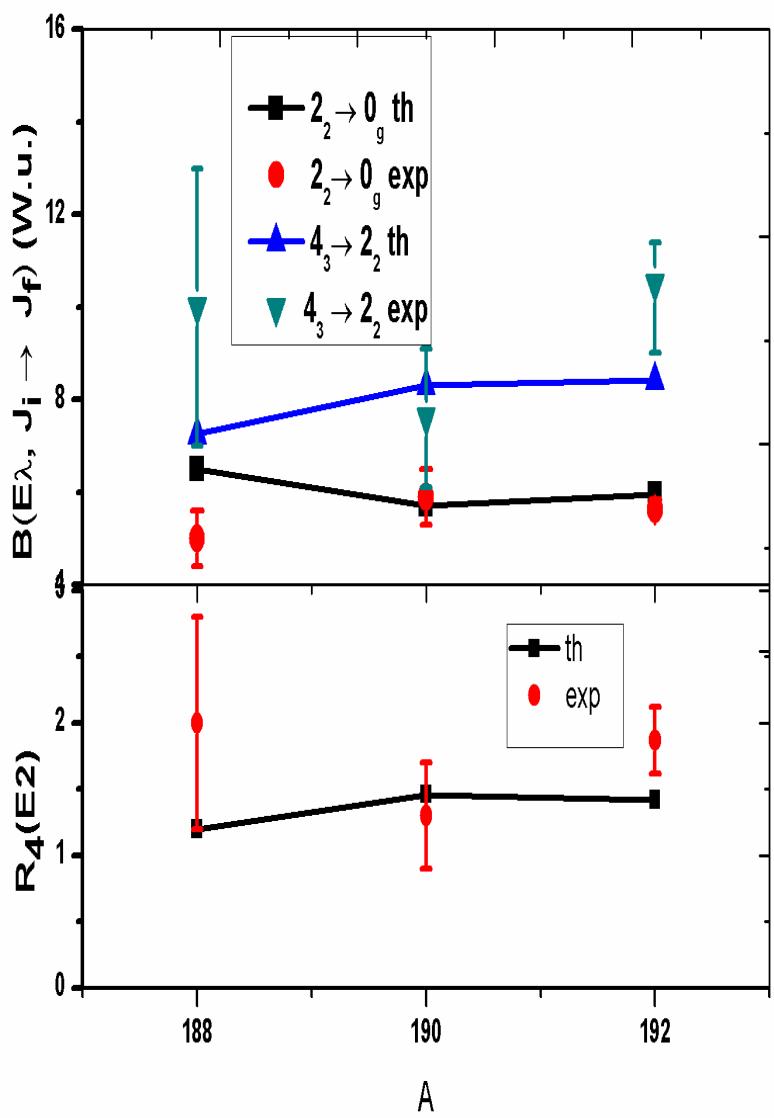
$^{192}\text{Os}$ : 35%

In agreement with recent experiments

(P. Garrett et al. Finustar 2 (08)  
and private communication)

$$\Psi(\text{QPM}) \sim 0.60 |n=1, 4^+\rangle + 0.35 |\gamma\gamma\rangle$$

# $4^+$ : QPM versus EXP



# THANK YOU