



# Workshop on Gamma Strength and Level Density in Nuclear Physics and Nuclear Technology

Dresden-Rossendorf, 30 August – 3 September, 2010

## *Pygmy Resonances in Skin Nuclei*

N. Tsoneva, H. Lenske

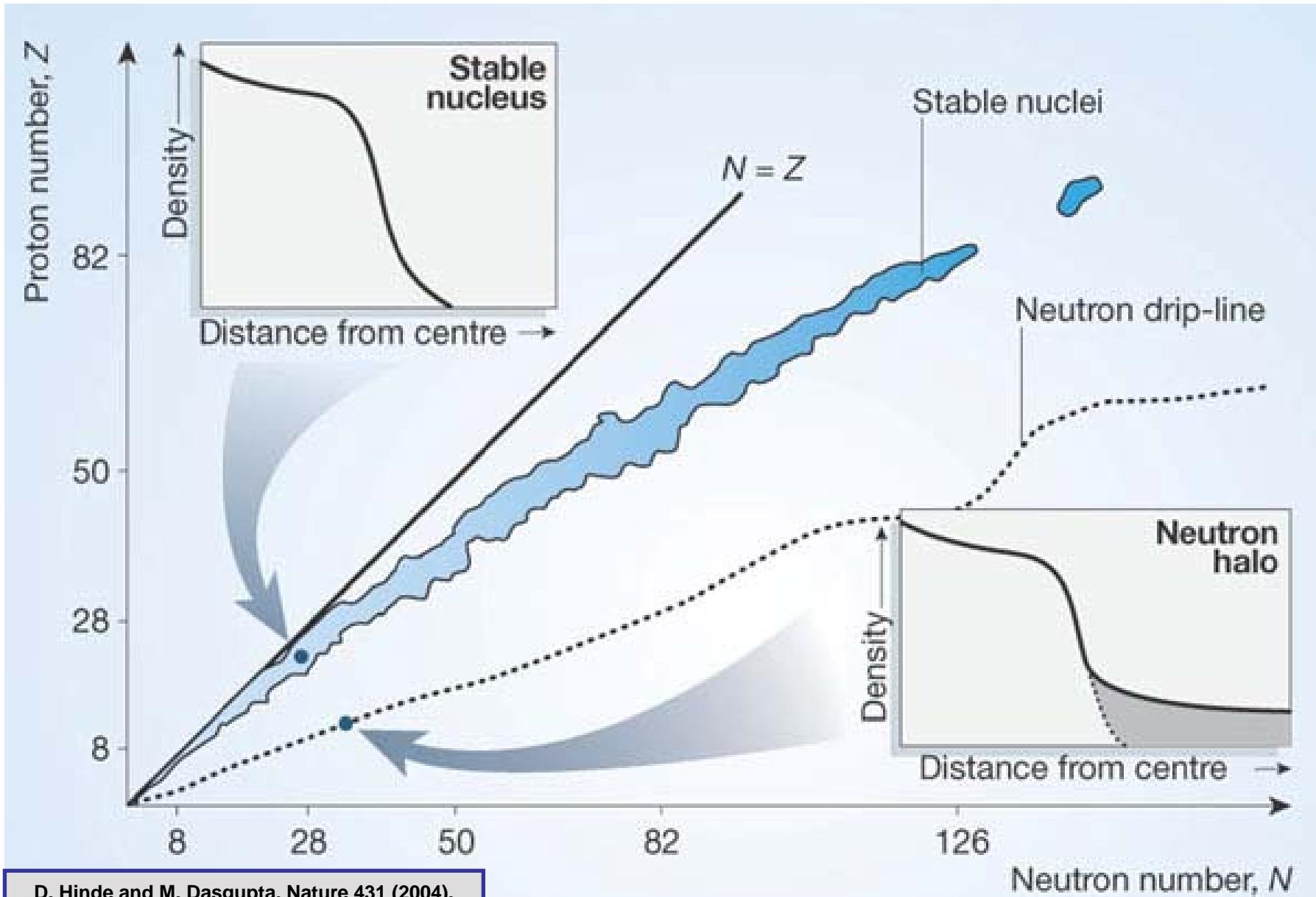
Institut für Theoretische Physik, Universität Giessen, Germany

# Collaborators

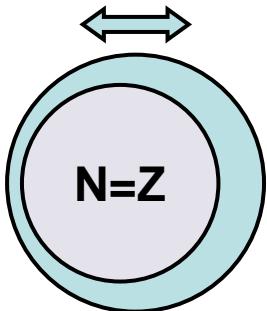
- R. Schwengner
- A. Tonchev, G. Rusev
- P. von Neumann-Cosel, B. Özel
- N. Pietralla
- A. Zilges, S. Volz
- U. Kneissl, M. Scheck
- Ch. Stoyanov, M. Grinberg, V. Ponomarev

# Nuclear Halos

Observation of halos in light nuclei : Tanihata et al., Phys. Rev. Lett., 2676 (1985).



# *Skin Excitations*



*Oscillations of extra neutrons from the periphery vs. the isospin symmetric core* Y. Suzuki et al., PTP 83 (1990) 180.  
P. Isacker et al., PRC 45 (1992) R13.

## *Pygmy Resonances*

*Experiment*

*Pygmy Dipole Resonance*

*Theory*

**Stable nuclei :** A. Zilges et al., PLB 542 (2002) 43.  
Govaert et al., PRC 57 (1998) 2229.  
N. Ryezayeva et al., PRL 89 (2002) 272502.

- Mostly of electric character  
A. Tonchev et al., PRL 104, 072501 (2010);
- Located below the particle emission threshold ;
- Up to 1% of EWSR

**Unstable nuclei:** A. Leistenschneider et al., PRL 86 (2001) 5442.  
E. Tryggestad et al., PLB 541 (2002) 52.  
P. Adrich et al., PRL 95 (2005) 132501.

- Located closely above the particle emission threshold ;
- About 5-7% of EWSR

DFT

J. Chambers et al., PRC 50 (1994) R2671.

QPM

V. Ponomarev in PRL 89 (2002) 272502.

N. Tsoneva et al., PLB 586 (2004) 213.

QRPA-PC

D. Sarchi et al., PLB 601 (2004) 27.

G. Tertychny et al., Phys. Lett. B 647, 104 (2007).

RRPA and RQRPA

N. Paar et al., Rep. Prog. Phys. 70, 691 (2007).

J. Piekarewicz, PRC 73 (2006) 044325.

RQTBA

E. Litvinova, PRL 105, 022502 (2010).

*Other Pygmy Resonances:* N. Tsoneva, H. Lenske, PLB sub.

# The Quasiparticle-Phonon Model

V. G. Soloviev: *Theory of Complex Nuclei* (Pergamon Press, Oxford, 1976)

$$H = H_{MF} + H_M^{ph} + H_{SM}^{ph} + H_M^{pp}$$

$$H_{MF} = H_{sp} + H_{pair}$$

$$H_{res} = H_M^{ph} + H_{SM}^{ph} + H_M^{pp}$$

$$R^\lambda(r_1, r_2) = \kappa^\lambda R_\lambda(r_1) R_\lambda(r_2)$$

$$\kappa^\lambda = (\kappa^\lambda_0, \kappa^\lambda_1)$$

N. Tsoneva, H. Lenske, Ch. Stoyanov, Phys. Lett. B 586 (2004) 213  
N. Tsoneva, H. Lenske, Phys. Rev. C 77 (2008) 024321

# Phenomenological Density Functional Approach for Nuclear Ground States

The total binding energy can be expressed as an integral over an energy-density functional

$$B(A) = \sum_{q=p,n} \int d^3r (\tau_q(\rho) + E_{\text{int}}) + E_q^{\text{pair}}(k, \rho)$$

P. Hohenberg, W. Kohn, Phys. Rev. 136 (1964) B864.  
W. Kohn, L. J. Sham, Phys. Rev. 140 (1965) A 1133.

$$E_{\text{int}} = \frac{1}{2} \sum_q \rho_q U_q(\rho)$$

In terms of single-particle wave functions and occupancies the kinetic energy density, number and pairing densities are:

$$\tau_q = \sum_j v_{jq}^2 \frac{\hbar^2}{2M_q} |\vec{\nabla} \varphi_{jq}(\vec{r})|^2 \quad \rho_q(\vec{r}) = \sum_j v_{jq}^2 |\varphi_{jq}(\vec{r})|^2 \quad \kappa_q(\vec{r}) = \frac{1}{2} \sum_j v_{jq} u_{jq} |\varphi_{jq}(\vec{r})|^2$$

$$\left( -\frac{\hbar^2}{2M_q} \vec{\nabla}^2 + \Sigma_q(\vec{r}) - \eta_{jq} \right) \varphi(\vec{r}) = 0$$

$$\Sigma_q(\rho) = \frac{1}{2} \frac{\partial}{\partial \rho_q} \sum_{q'} \rho_{q'} U_{q'}(\rho) \longrightarrow \Sigma_q(\rho) = U_q(\rho) + U_q^{(r)}(\rho)$$

For finite nucleus we can replace the integration over density by radial integrals

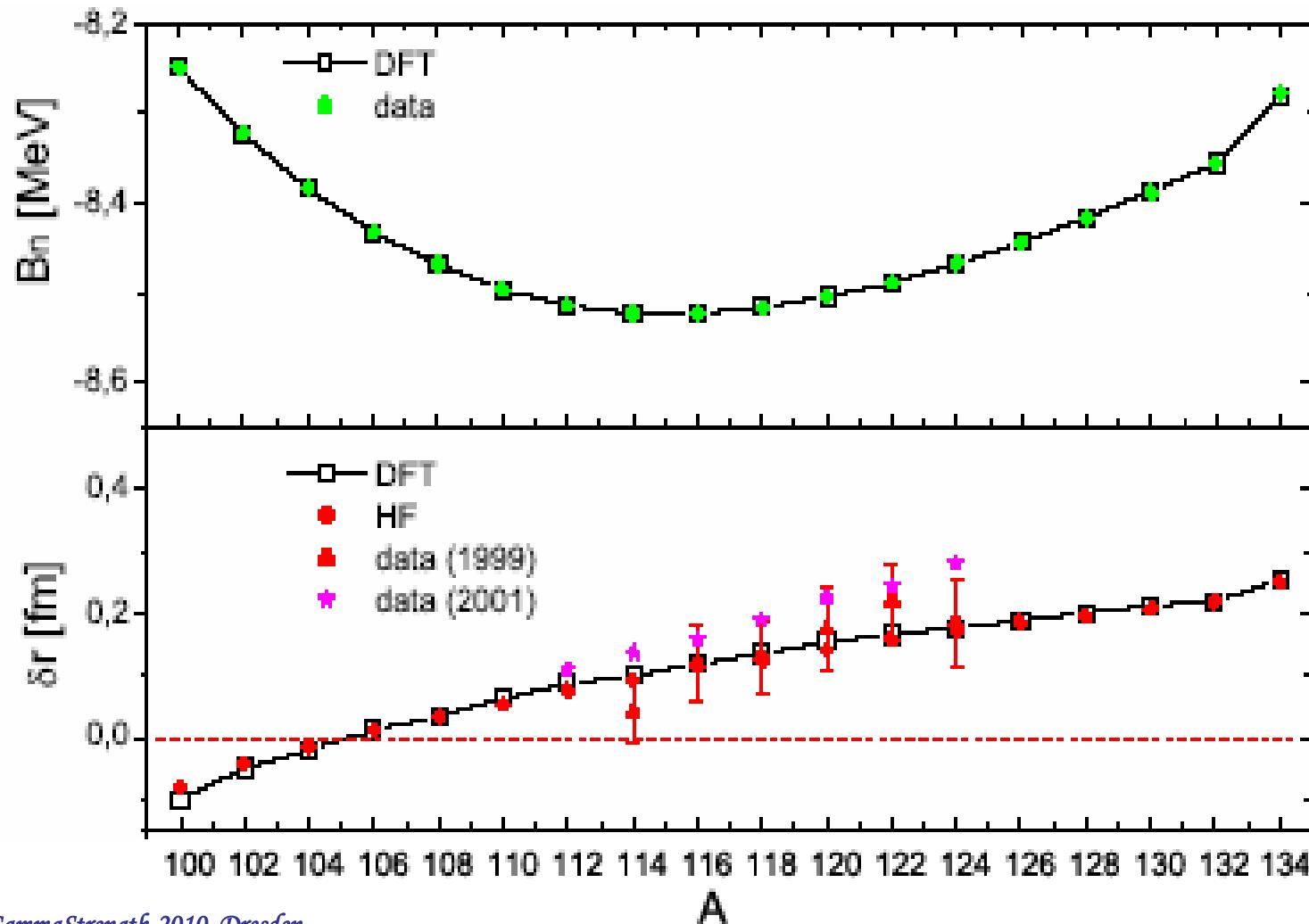
$$\rho(r) U_\alpha(r) = -2 \int_r^\infty ds \frac{\partial \rho(s)}{\partial s} \Sigma_\alpha(s) \quad U_{WS}(s)$$

where the density  $\rho(r)$  is calculated self-consistently with wave functions from the effective potential  $\Sigma_\alpha(r)$ .  
Hence, by means of these relations we are able to calculate  $B(A)$  for arbitrary phenomenological single-particle potential.

# The Ground State

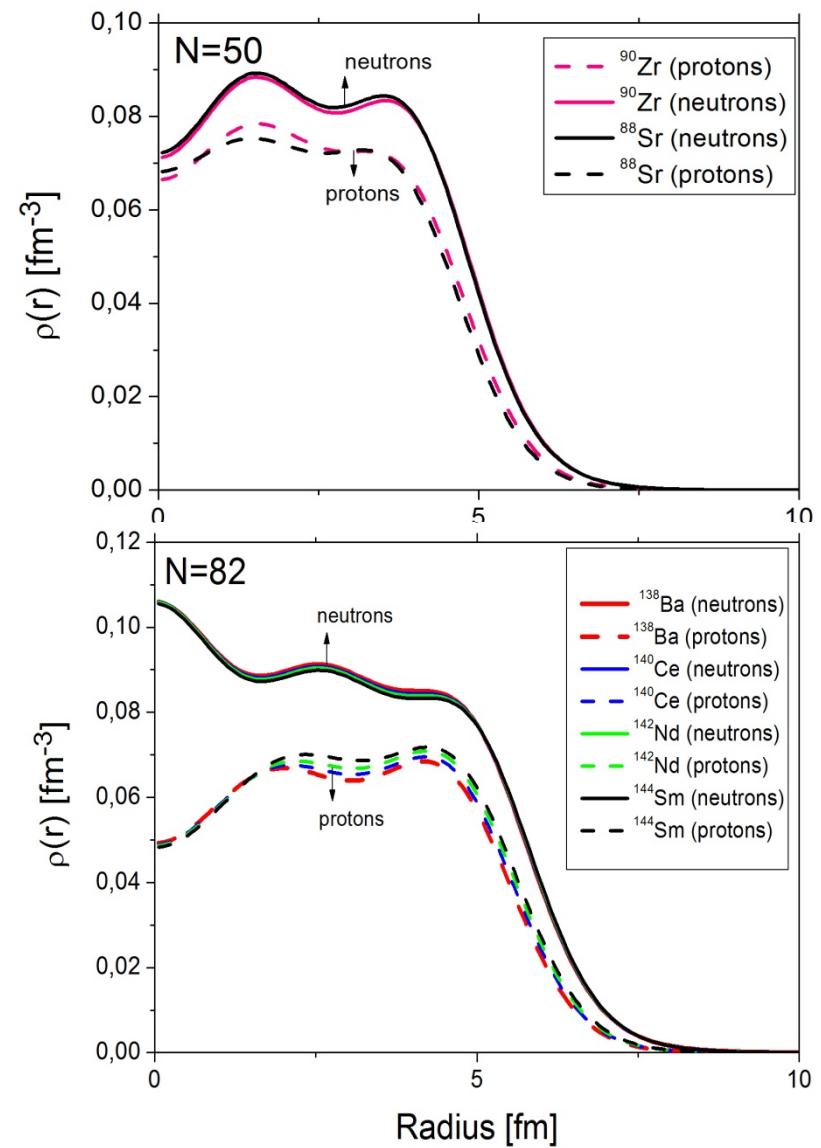
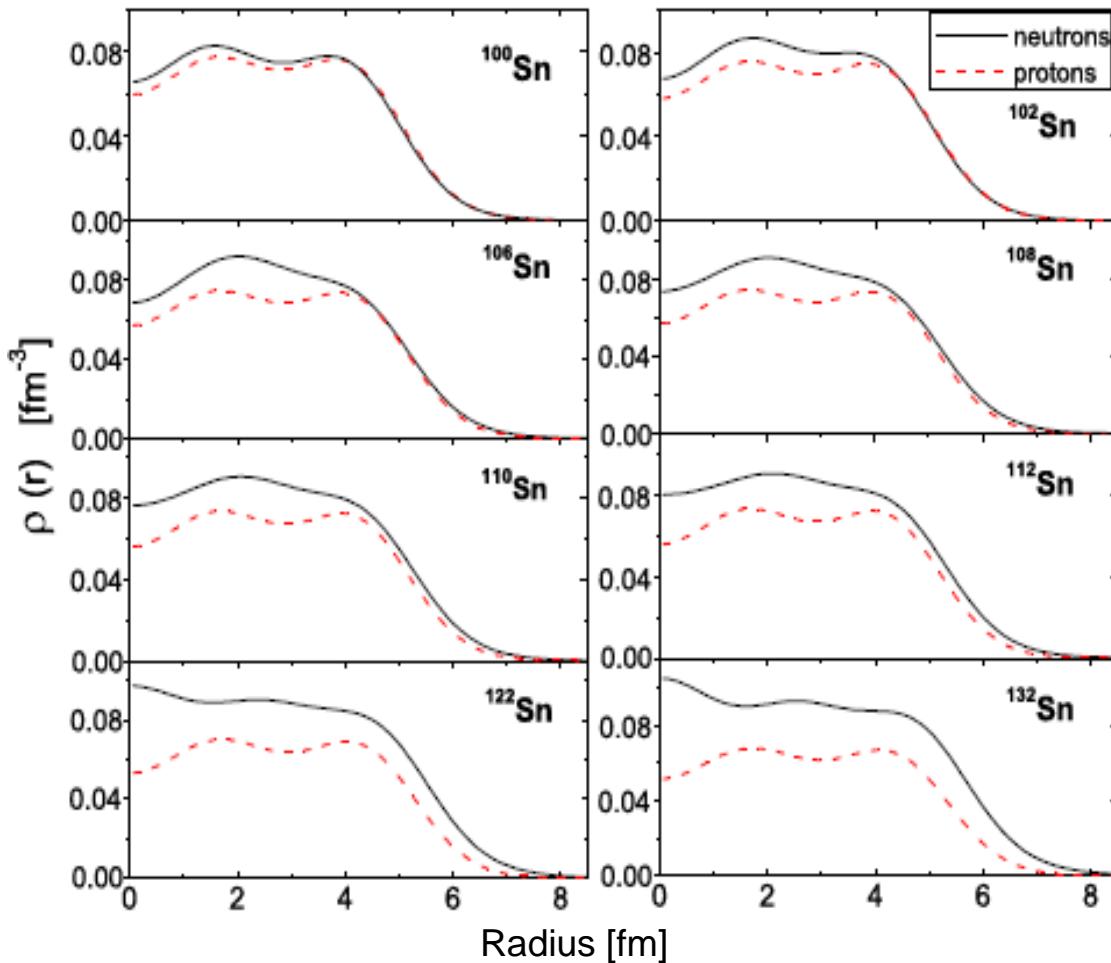
*Binding energy and skin thickness*

$$\delta r = \sqrt{\langle r^2 \rangle_n} - \sqrt{\langle r^2 \rangle_p}$$



# Calculations of Ground State Densities in $Z=50$ , $N=50$ and $N=82$ Nuclei

$$\delta r = \sqrt{< r^2 >_n} - \sqrt{< r^2 >_p}$$



# The Model Basis

V. G. Soloviev: Theory of Atomic Nuclei: *Quasiparticles and Phonons* (Inst. Of Phys. Publ., Bristol, 1992)

$$Q_{\lambda\mu i}^+ = \frac{1}{2} \sum_{\tau} \sum_{jj'}^{n,p} \left\{ \psi_{jj'}^{\lambda i} [\alpha_j^+ \alpha_{j'}^+]_{\lambda\mu} - (-1)^{\lambda-\mu} \varphi_{jj'}^{\lambda i} [\alpha_{j'} \alpha_j]_{\lambda-\mu} \right\} ,$$

$$a_{jm} = u_j \alpha_{jm} + (-)^{j-m} v_j \alpha_{j-m}^+$$

$$[Q_{\lambda\mu i}, Q_{\lambda'\mu' i'}^+] = \frac{\delta_{\lambda,\lambda'} \delta_{\mu,\mu'} \delta_{i,i'}}{2} \sum_{jj'} [\psi_{jj'}^{\lambda i} \psi_{jj'}^{\lambda i'} - \varphi_{jj'}^{\lambda i} \varphi_{jj'}^{\lambda i'}] - \sum_{\substack{jj' j_2 \\ mm' m_2}} \alpha_{jm}^+ \alpha_{j'm'}^-$$

$$\times \left\{ \psi_{j'j_2}^{\lambda i} \psi_{jj_2}^{\lambda' i'} C_{j'm'j_2m_2}^{\lambda\mu} C_{jmj_2m_2}^{\lambda'\mu'} - (-)^{\lambda+\lambda'+\mu+\mu'} \varphi_{jj_2}^{\lambda i} \varphi_{j'j_2}^{\lambda' i'} C_{jmj_2m_2}^{\lambda-\mu} C_{j'm'j_2m_2}^{\lambda'-\mu'} \right\}$$

$$[H, Q_{\alpha}^+] = E_{\alpha} Q_{\alpha}^+$$

# The Wave Function

$$\Psi_\nu(JM) = \left\{ \sum_i R_i(J\nu) Q_{JMi}^+ + \sum_{\substack{\lambda_1 i_1 \\ \lambda_2 i_2}} P_{\lambda_2 i_2}^{\lambda_1 i_1}(J\nu) [Q_{\lambda_1 \mu_1 i_1}^+ \times Q_{\lambda_2 \mu_2 i_2}^+]_{JM} \right. \\ \left. + \sum_{\substack{\lambda_1 i_1 \lambda_2 i_2 \\ \lambda_3 i_3 I}} T_{\lambda_3 i_3}^{\lambda_1 i_1 \lambda_2 i_2 I}(J\nu) [[Q_{\lambda_1 \mu_1 i_1}^+ \otimes Q_{\lambda_2 \mu_2 i_2}^+]_{IK} \otimes Q_{\lambda_3 \mu_3 i_3}^+]_{JM} \right\} \Psi_0$$

$$M(X\lambda\mu) = \sum_{\tau j j'} \frac{\langle j || X\lambda || j' \rangle}{\sqrt{2\lambda+1}} \left\{ \frac{u_{jj'}^{(\pm)}}{2} \sum_i (\psi_{jj'}^{\lambda i} + \varphi_{jj'}^{\lambda i}) (Q_{\lambda\mu i}^\dagger + (-)^{\lambda-\mu} Q_{\lambda-\mu i}) \right. \\ \left. + v_{jj'}^{(\mp)} \sum_{mm'} C_{jmj'm'}^{\lambda\mu} (-)^{j'+m'} \alpha_{j'm'}^\dagger \alpha_{j'-m'} \right\}$$

# The Charge Transition Density

$$\rho(\vec{r}) = \langle \Psi_f | \delta(\vec{r} - \vec{r}_k) | \Psi_i \rangle$$

$$\rho(\vec{r}) = e \sum_{\lambda\mu} (-)^{\lambda} C_{J_i M_i \lambda \mu}^{J_f M_f} \rho_{\lambda}(\vec{r}) Y_{\lambda \mu}^*(\theta, \varphi)$$

In terms of QRPA phonons:

$$\rho_{\lambda i}(\vec{r}) = \sum_{j \geq j'} \frac{1}{1 + \delta_{jj'}} \rho_{jj'}^{(\lambda)}(\vec{r}) g_{jj'}^{\lambda i} u_{jj'};$$

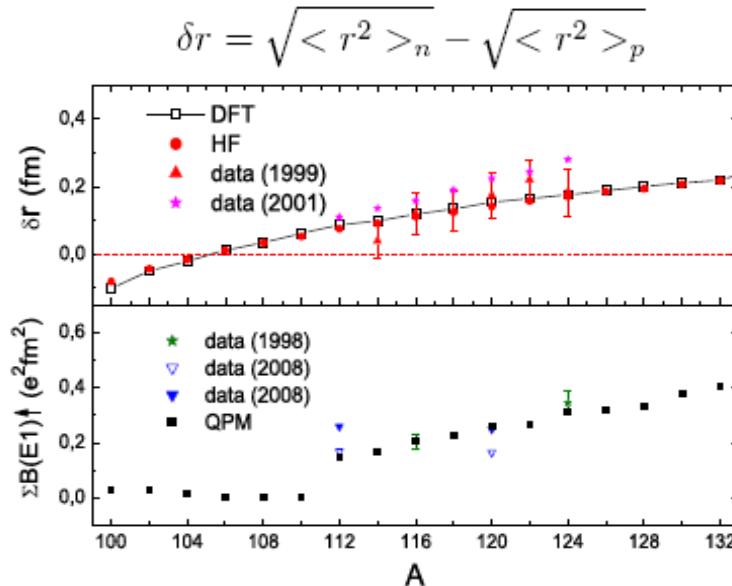
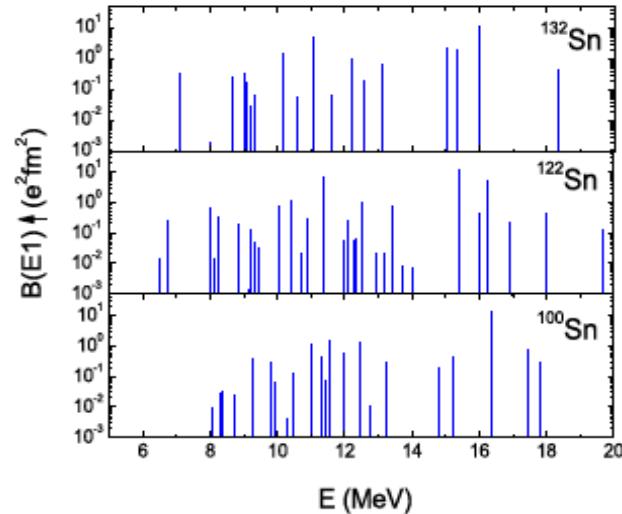
$$\rho_{jj'}^{(\lambda)}(\vec{r}) = - \left[ 1 + (-)^{l+l'+\lambda} \right] (-)^{j+\lambda+1/2} \frac{\hat{j} \hat{j}'}{\hat{\lambda} \sqrt{4\pi}} \times \\ C_{j \frac{1}{2} j' - \frac{1}{2}}^{\lambda 0} R_j^*(\vec{r}) R_{j'}(\vec{r}),$$

$$\hat{j} = \sqrt{2j+1}; \quad g_{jj'}^{\lambda i} = \psi_{jj'}^{\lambda i} + \varphi_{jj'}^{\lambda i} \text{ and } u_{jj'} = u_j v_{j'} + u_{j'} v_j$$

# QRPA Calculations on the Dipole Response in Sn Isotopes

N. Tsoneva, H. Lenske, PRC 77 (2008) 024321

A connection between the total PDR strength and the neutron/proton skin thickness is observed



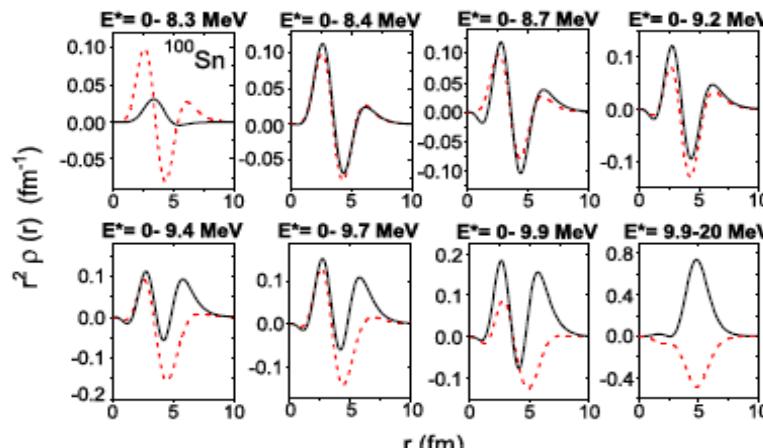
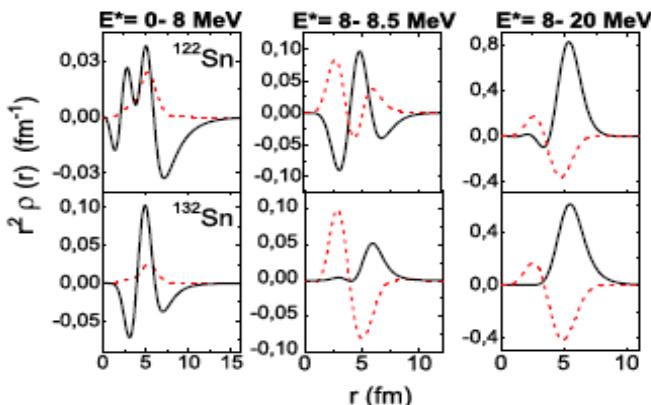
Neutron number increasing

Neutron skin increasing

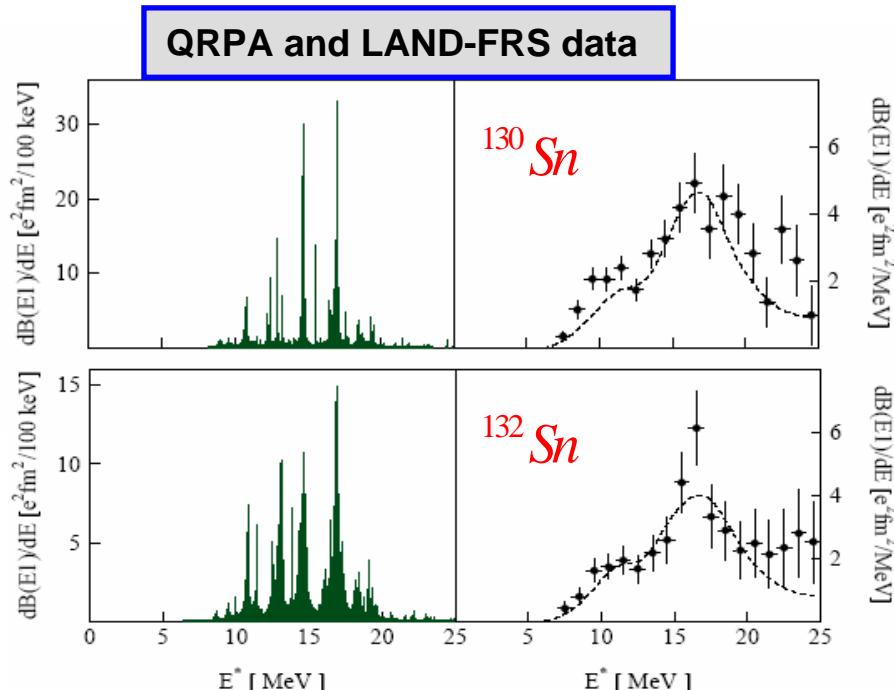
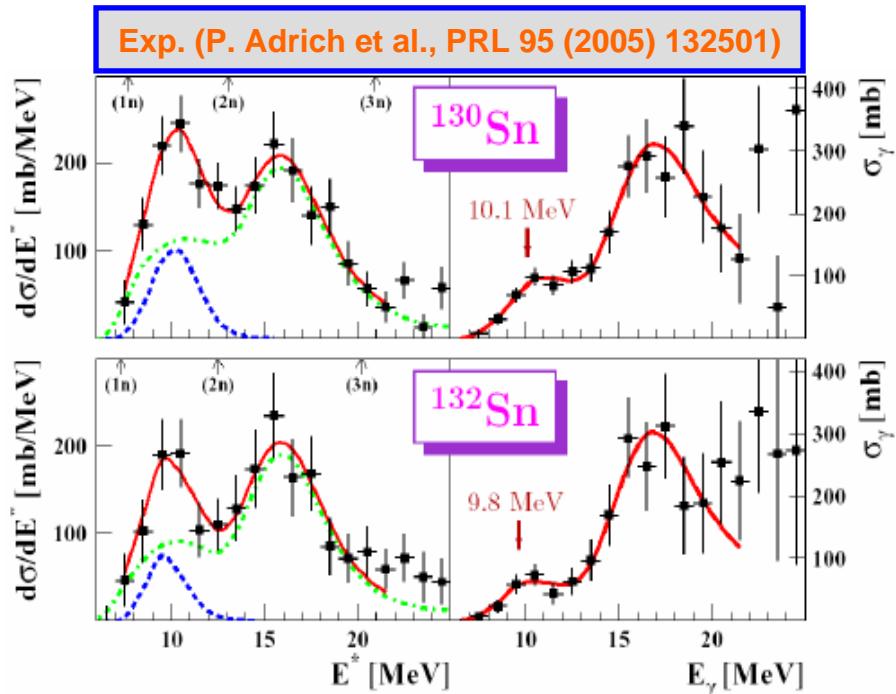
Exp. in Sn-116 and Sn-124:

K. Govaert et al,  
Phys. Rev. C 57 (1998) 2229.

Exp. in Sn-112,Sn-120:  
B. Ozel et al,  
Nucl. Phys. A 778 (2007) 385.



*QPM calculations of excitation energies and integrated cross sections in  $^{130,132}\text{Sn}$  in comparison with recent data\* / A. Klimkiewicz and the LAND-FRS collaboration, private communication/.*



N. Tsoneva, H. Lenske, PRC 77 (2008) 024321

Nucl.	PDR (Energy) region	$\langle E \rangle_{PDR}$ [MeV]	$\int \sigma^{PDR}$ [mb MeV]	$E_{max}^{PDR}$ [MeV]	$\int \sigma^{PDR}$ [mb MeV]	$E_{LET}^{GDR}$ [MeV]	$\int \sigma^{GDR}$ [mb MeV]	$E_{GDR}^{max}$ [MeV]	$E_{GDR}^{max}$ [MeV]	$\int \sigma^{GDR}$ [mb MeV]	$\int \sigma^{GDR}$ [mb MeV]
$^{130}\text{Sn}$	0-7.4	5.8	8.2	10.1(7)	130(55)	8-11	137.3	15.9(5)	16.	1930(300)*	1616
$^{132}\text{Sn}$	0-8	7.1	10.4	9.8(7)	75(57)	8-11	97.6	16.1(7)	16.1	1670(420)*	1518

\* The integration is taken up to 20 MeV.

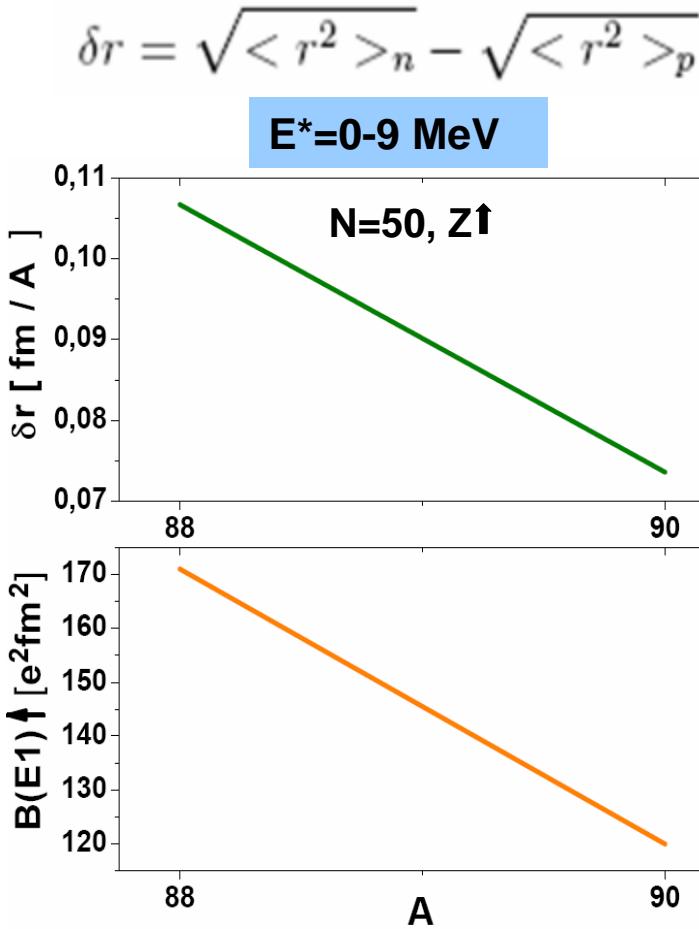
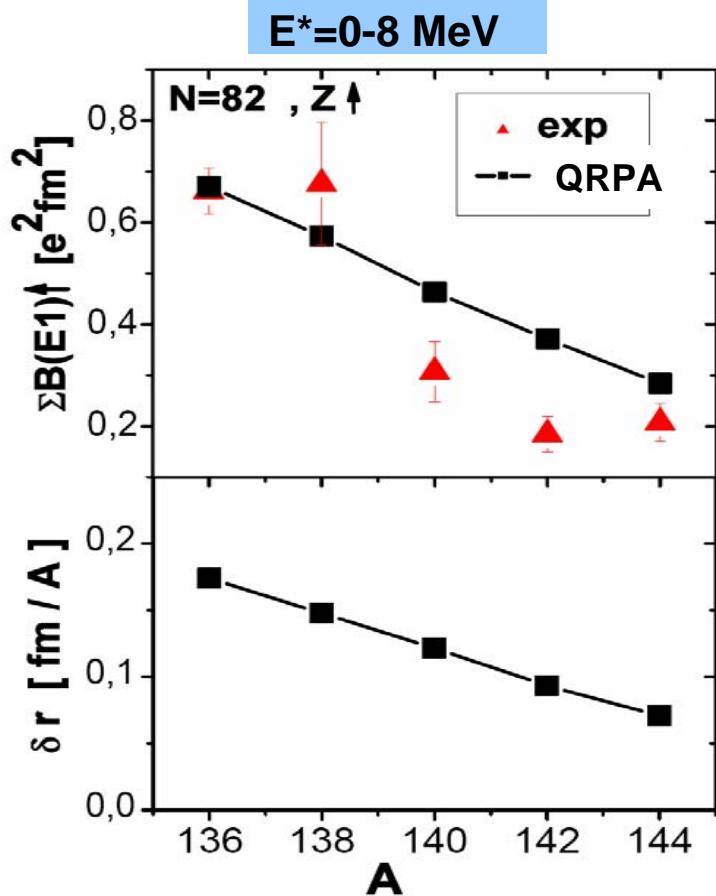
# QRPA Calculations of the Total PDR Strength in $N=82$ and $N=50$ Isotones

A connection between the total PDR strength and the neutron skin thickness is observed

Electron accelerator S-DALINAC, TU Darmstadt,  
Bremsstrahlung photons at 10 MeV.

S. Volz et al., Nucl. Phys. A, 779 (2006) 1-20;  
D. Savran et al., PRL 100, (2008) 232501

- Proton number increasing
- Neutron skin decreasing



# Skin Thickness and Electric Dipole Response

The skin thickness is defined as:

N. Tsoneva, H. Lenske, PRC 77, 024321 (2008)

$$\delta r = \sqrt{\langle r_n^2 \rangle} - \sqrt{\langle r_p^2 \rangle}, \quad \text{where } \langle r_q^2 \rangle = \frac{1}{A_q} \int d^3r r^2 \rho_q(\vec{r})$$

$$\Delta_3 r^2 = \sum_i \langle 0 | \tau_{3i} r_i^2 | 0 \rangle \quad \tau_3 = \pm 1$$

The intrinsic nuclear dipole transition operator in laboratory coordinates:

$$\vec{D} = \sum_i \vec{r}_i \left( q_p \frac{1}{2} (1 - \tau_{3i}) + q_n \frac{1}{2} (1 + \tau_{3i}) \right); \quad q_T = \frac{1}{2} (q_n + (-)^T q_p) \text{ isoscalar (T=0) and isovector (T=1) charges}$$

$$\vec{x}_T = \sum_i \vec{r}_i (\tau_{3i})^T$$

$$\vec{D} = q_0 \vec{x}_0 + q_1 \vec{x}_1$$

The reduced isovector/isoscalar dipole transition moment and the dipole transition probability are :

$$\vec{M}_d^{(T)} = \langle 0 | (\tau_3)^T \vec{r} | d \rangle; \quad B_d(E1) = \left| q_0 \vec{M}_d^{(0)} + q_1 \vec{M}_d^{(1)} \right|^2$$

The isovector/isoscalar interference term :

$$\Re \sum_d \vec{M}_d^{(0)} \vec{M}_d^{(1)*} = \frac{1}{2q_0 q_1} \left( \sum_d B_d(E1) - q_0^2 \sum_d |\vec{M}_d^{(0)}|^2 - q_1^2 \sum_d |\vec{M}_d^{(1)}|^2 \right)$$

In QRPA basis  $|\alpha\rangle = |(ij)JM\rangle$

$$\frac{1}{2} \sum_d \vec{M}_d^{(0)} \cdot \vec{M}_d^{(1)*} = \boxed{\sum_{i,j} \vec{M}_{ij}^{(0)} \cdot \vec{M}_{ij}^{(1)*} v_i^2} - \sum_{i,j} \vec{M}_{ij}^{(0)} \cdot \vec{M}_{ij}^{(1)*} v_i^2 v_j^2 + \sum_{i,j} \vec{M}_{ij}^{(0)} \cdot \vec{M}_{ij}^{(1)*} u_i v_i u_j v_j$$

$$\Re \sum_{i,j} \vec{M}_{ij}^{(0)} \cdot \vec{M}_{ij}^{(1)*} v_i^2 = \sum_{i,j} \langle i | \vec{r} | j \rangle \cdot \langle j | \tau_3 \vec{r} | i \rangle v_i^2 = \boxed{\sum_i \langle i | \tau_3 r^2 | i \rangle v_i^2}$$

# *Skin Thickness and Electric Dipole Response*

N. Tsoneva, H. Lenske, PRC 77, 024321 (2008)

Relation between the non-energy weighted dipole sum rule and the skin measure:

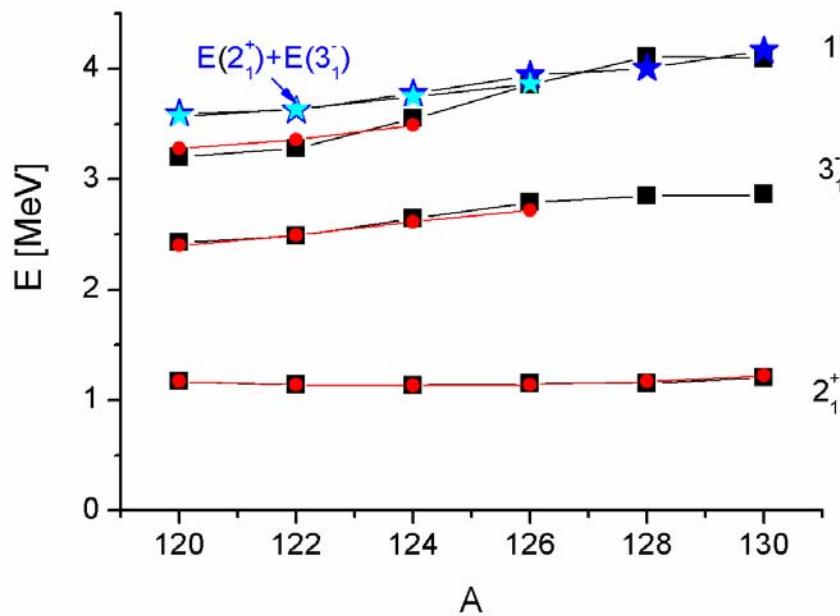
$$\Delta_3 r^2 = \frac{1}{4q_0 q_1} \left( \sum_d B_d(E1) - q_0^2 \sum_d |M_d^{(0)}|^2 - q_1^2 \sum_d |M_d^{(1)}|^2 \right)$$

+ ground state pairing correlations

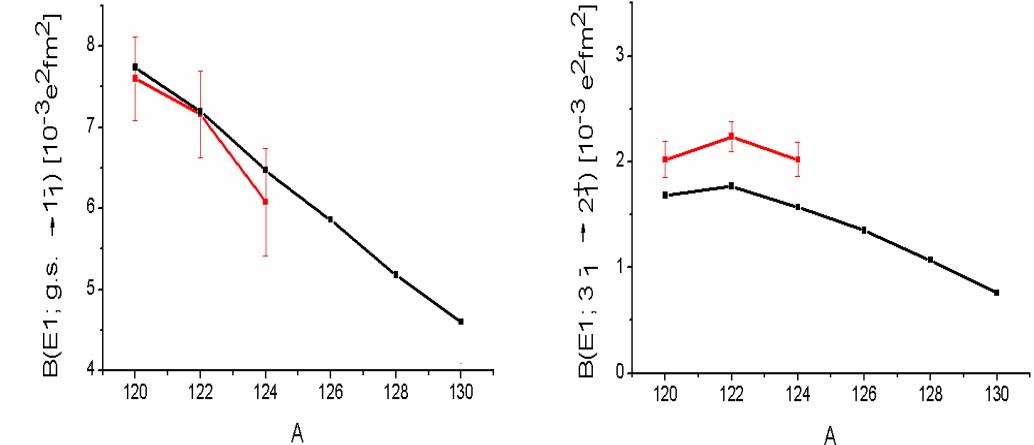
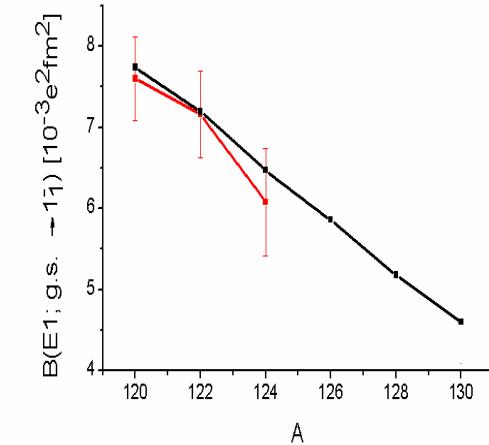
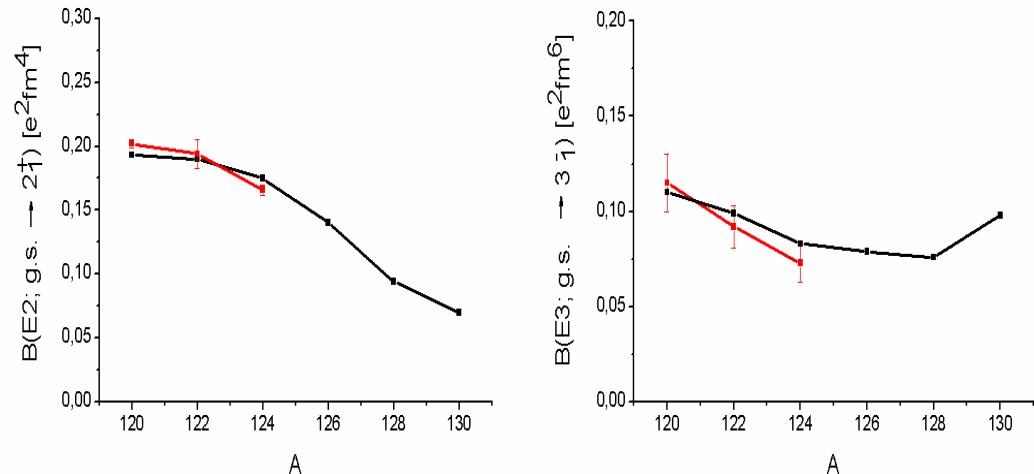
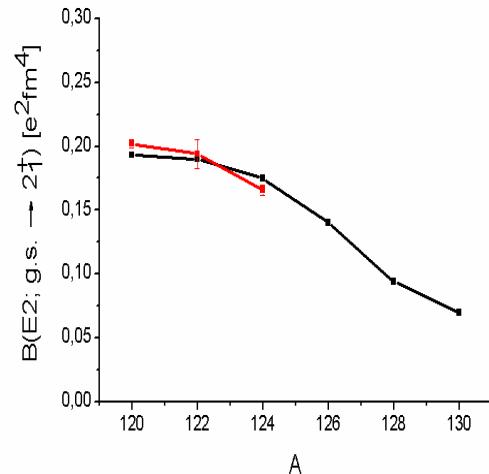
# Two-phonon 1- states

U. Kneissl, N. Pietralla, and A. Zilges, J. Phys. G: Nucl.Part.Phys. **32**, R217 (2006)

Sn isotopes



- energy of the  $1^-_1$ ,  $2^+_1$  and  $3^-_1$  states from QPM;
- ★— unperturbed energy  $E(2^+_1) + E(3^-_1)$  from QPM;
- experimental energy of the  $1^-_1$ ,  $2^+_1$  and  $3^-_1$  states;
- ★— unperturbed  $E(2^+_1) + E(3^-_1)$  energy from the data



The data are taken from J. Bryssinck et al., Phys. Rev. C59(1999)1930

N. Tsoneva, GammaStrength-2010, Dresden

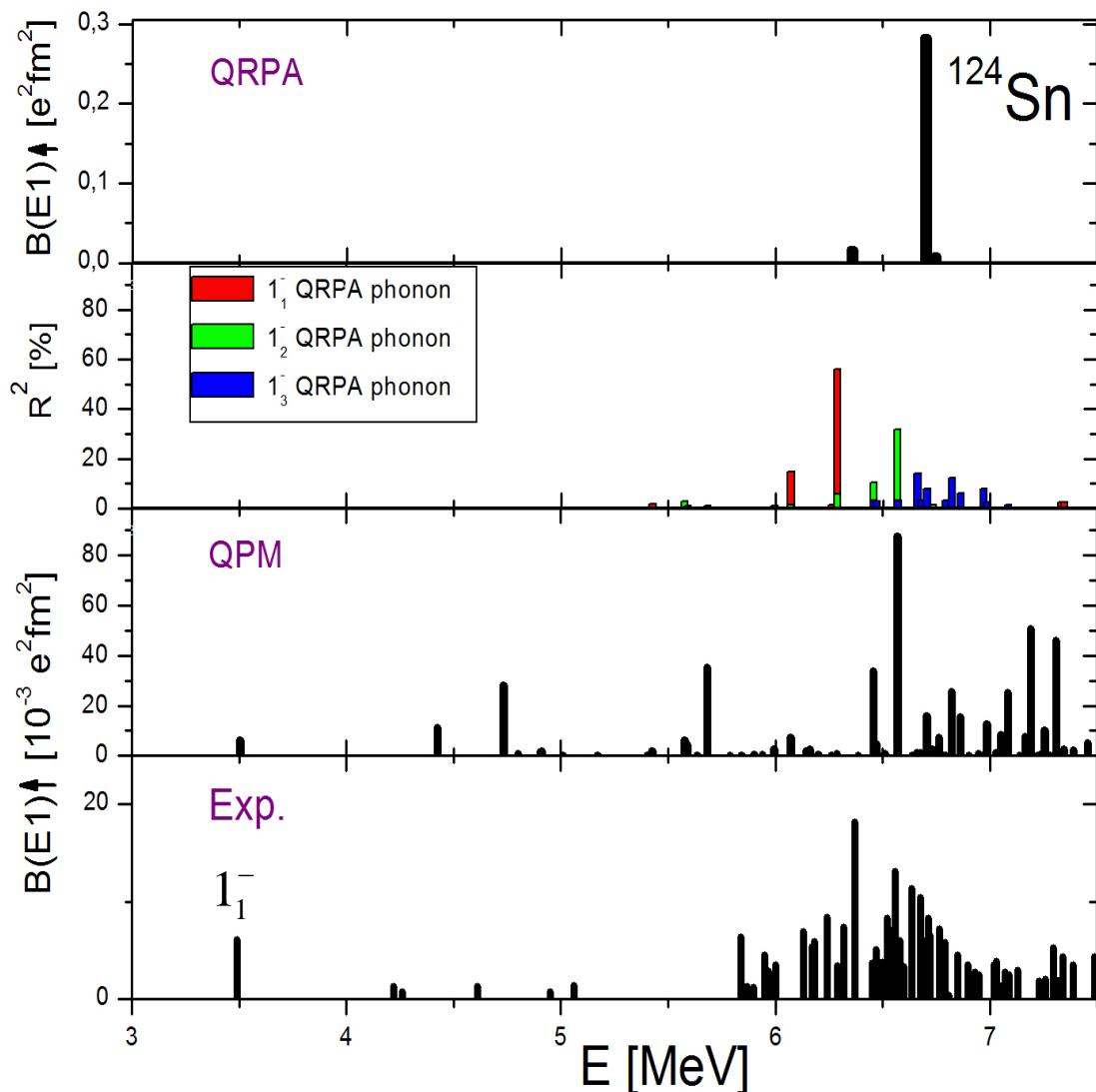
**QPM results for the energies and B(E1), B(E2) and B(E3) transition probabilities of the first 1<sup>-</sup>, 2<sup>+</sup> and 3<sup>-</sup> states in Sn isotopes in comparison with experimental data.**

Nucl.	Energy [MeV]	Trans. B(E1; $I_\nu^\pi \rightarrow J_{\nu'}^{\pi'}$ ) [ $10^{-3} e^2 \text{fm}^2$ ]			
		$J_{\nu'}^{\pi'}$	Exp.	QPM	
		Eλ	$I_\nu^\pi$	Exp.	QPM
<sup>120</sup> Sn	$2_1^+$	1.171	1.171	E2	$0_1^+$ 0.200(3)
				E1	$3_1^-$ 2.02(17)
	$3_1^-$	2.401	2.424	E3	$0_1^+$ 0.115(15)
	$1_1^-$	3.279	3.203	E1	$0_1^+$ 7.60(51)
	$2_1^+$	1.141	1.137	E2	$0_1^+$ 0.194(11)
				E1	$3_1^-$ 2.24(14)
<sup>122</sup> Sn	$3_1^-$	2.493	2.486	E3	$0_1^+$ 0.092(10)
	$1_1^-$	3.359	3.281	E1	$0_1^+$ 7.16(54)
	$2_1^+$	1.132	1.133	E2	$0_1^+$ 0.166(4)
				E1	$3_1^-$ 2.02(16)
<sup>124</sup> Sn	$3_1^-$	2.614	2.645	E3	$0_1^+$ 0.073(10)
	$1_1^-$	3.490	3.549	E1	$0_1^+$ 6.08(66)
	$2_1^+$	1.141	1.151	E2	$0_1^+$ -
				E1	$3_1^-$ -
<sup>126</sup> Sn	$3_1^-$	2.720	2.792	E3	$0_1^+$ -
	$1_1^-$	-	3.856	E1	$0_1^+$ -
	$2_1^+$	1.168	1.154	E2	$0_1^+$ -
				E1	$3_1^-$ -
<sup>128</sup> Sn	$3_1^-$	-	2.849	E3	$0_1^+$ -
	$1_1^-$	-	4.115	E1	$0_1^+$ -
	$2_1^+$	1.221	1.204	E2	$0_1^+$ -
				E1	$3_1^-$ -
<sup>130</sup> Sn	$3_1^-$	-	2.861	E3	$0_1^+$ -
	$1_1^-$	-	4.094	E1	$0_1^+$ -
	$2_1^+$	1.221	1.204	E2	$0_1^+$ -
				E1	$3_1^-$ -

N. Tsoneva, H. Lenske, Ch. Stoyanov,  
**Phys. Lett. B 586 (2004) 213**  
N. Tsoneva, H. Lenske, Phys. Rev. C  
**77 (2008) 024321**

# *QPM calculations in $^{124}\text{Sn}$ in Comparison with Experimental Data*

K. Govaert et al., Phys. Rev. C 57 2229 (1998)  
 N. Tsoneva, H. Lenske, PRC 77, 024321 (2008)



*Two-phonon  $1_1^-$  state*

$$B(E1; \text{g.s.} \Rightarrow 1_1^-)_{\text{QPM}} = 6.06 \times 10^{-3} e^2 \text{fm}^2$$

$$B(E1; \text{g.s.} \Rightarrow 1_1^-)_{\text{exp}} = 6.08 \times 10^{-3} e^2 \text{fm}^2$$

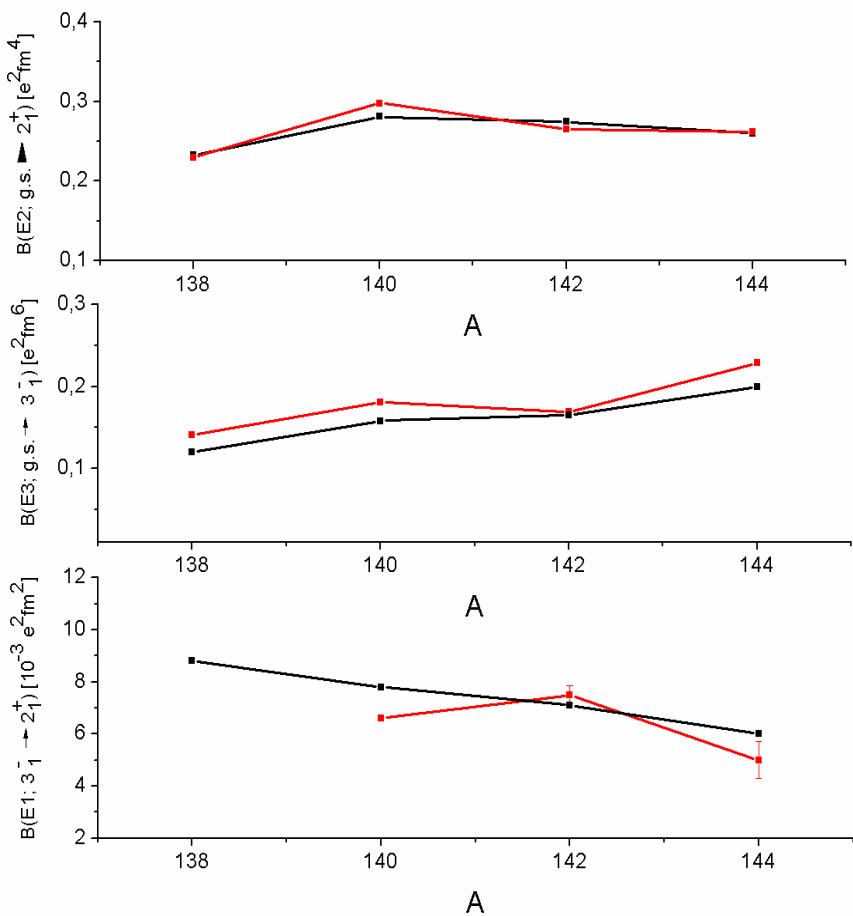
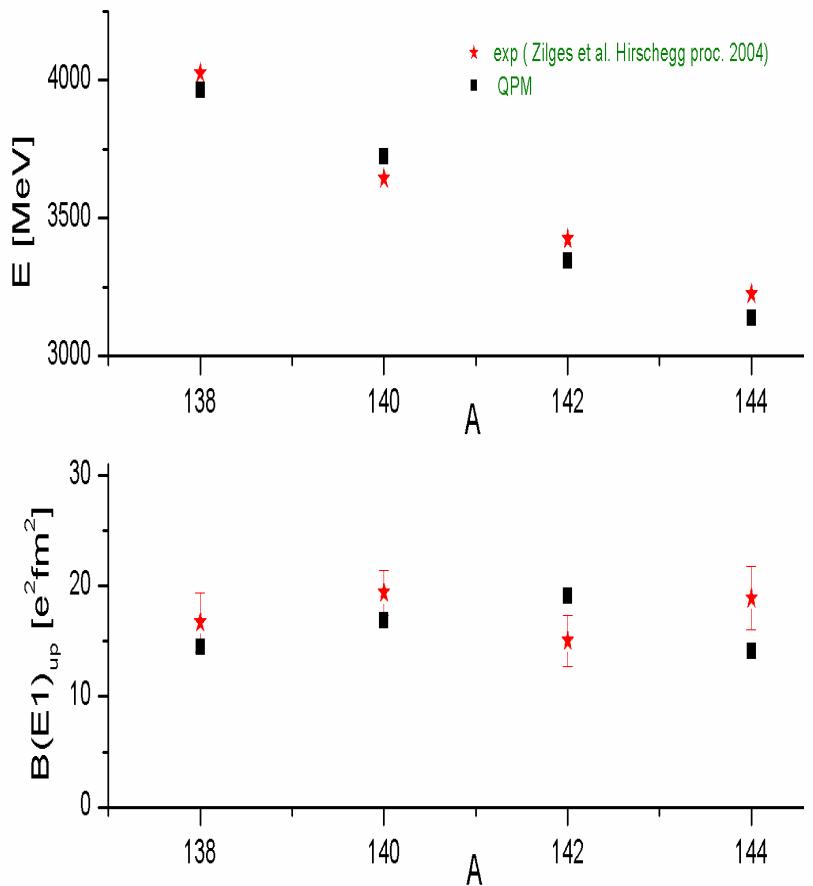
*PDR strength  $E^* = 5.7-7.5 \text{ MeV}$*

$$\sum_{\text{QPM}}^{PDR} B(E1) \uparrow = 0.324 e^2 \text{fm}^2$$

$$\sum_{\text{QPM}}^{PDR} B(E1) \uparrow = 0.345(43) e^2 \text{fm}^2$$

# QPM Calculations on Energies and Transition Probabilities of the Two-Phonon 1- states Compared to Experimental data in $N=82$ isotones

S. Volz et al., Nucl. Phys. A, 779 (2006) 1-20.  
 D. Savran et al., PRL 100, (2008) 232501.

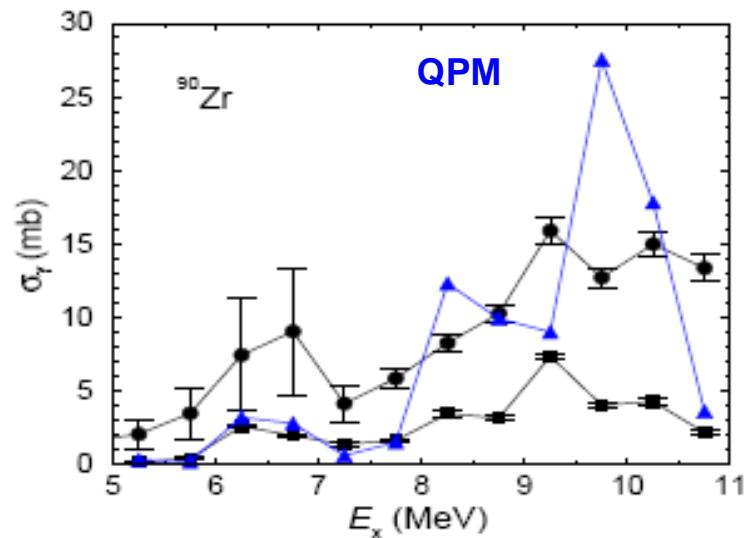
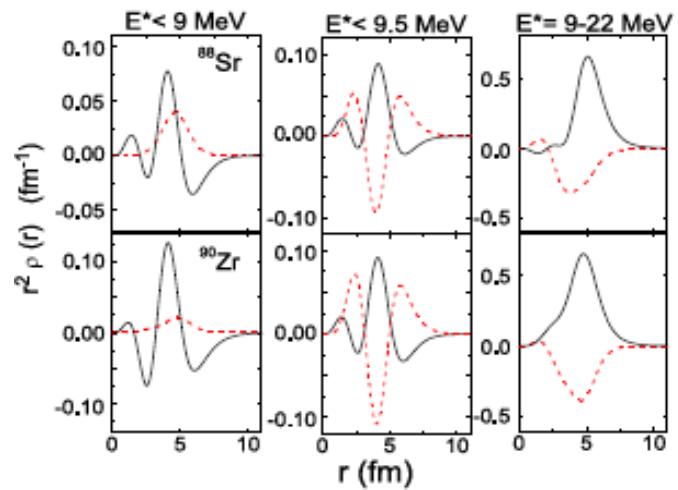
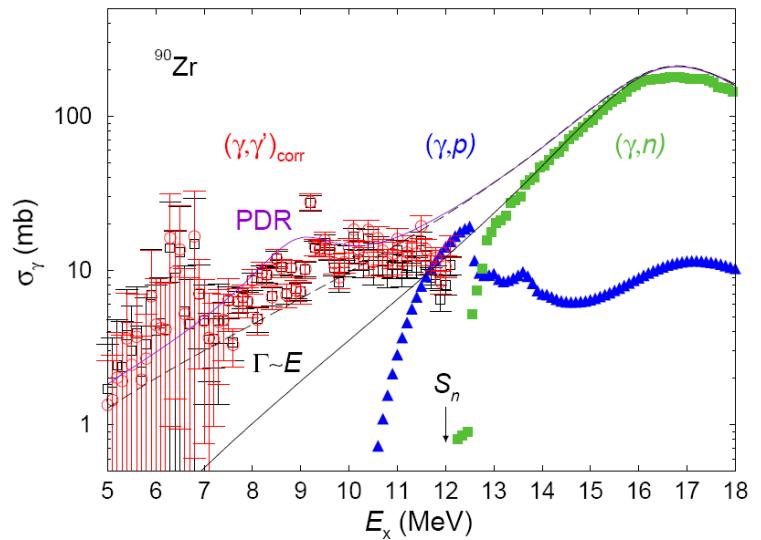
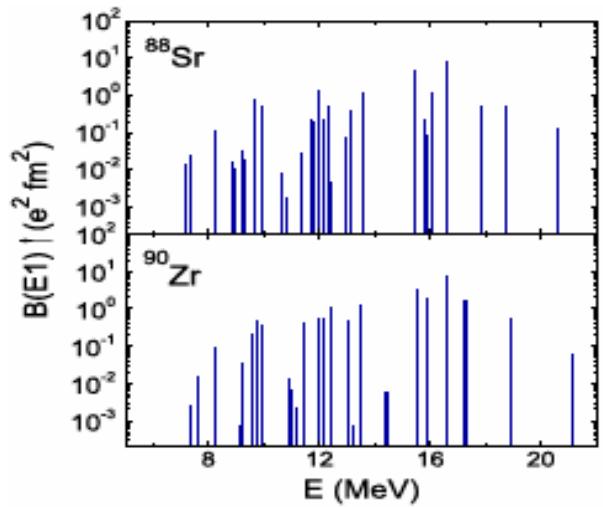


The data are taken from: S. Raman et al, At. Data Nucl. Data Tabl. 78 (2001) ;

N. Pietralla, Phys. Rev. C59 (1999) 2941.

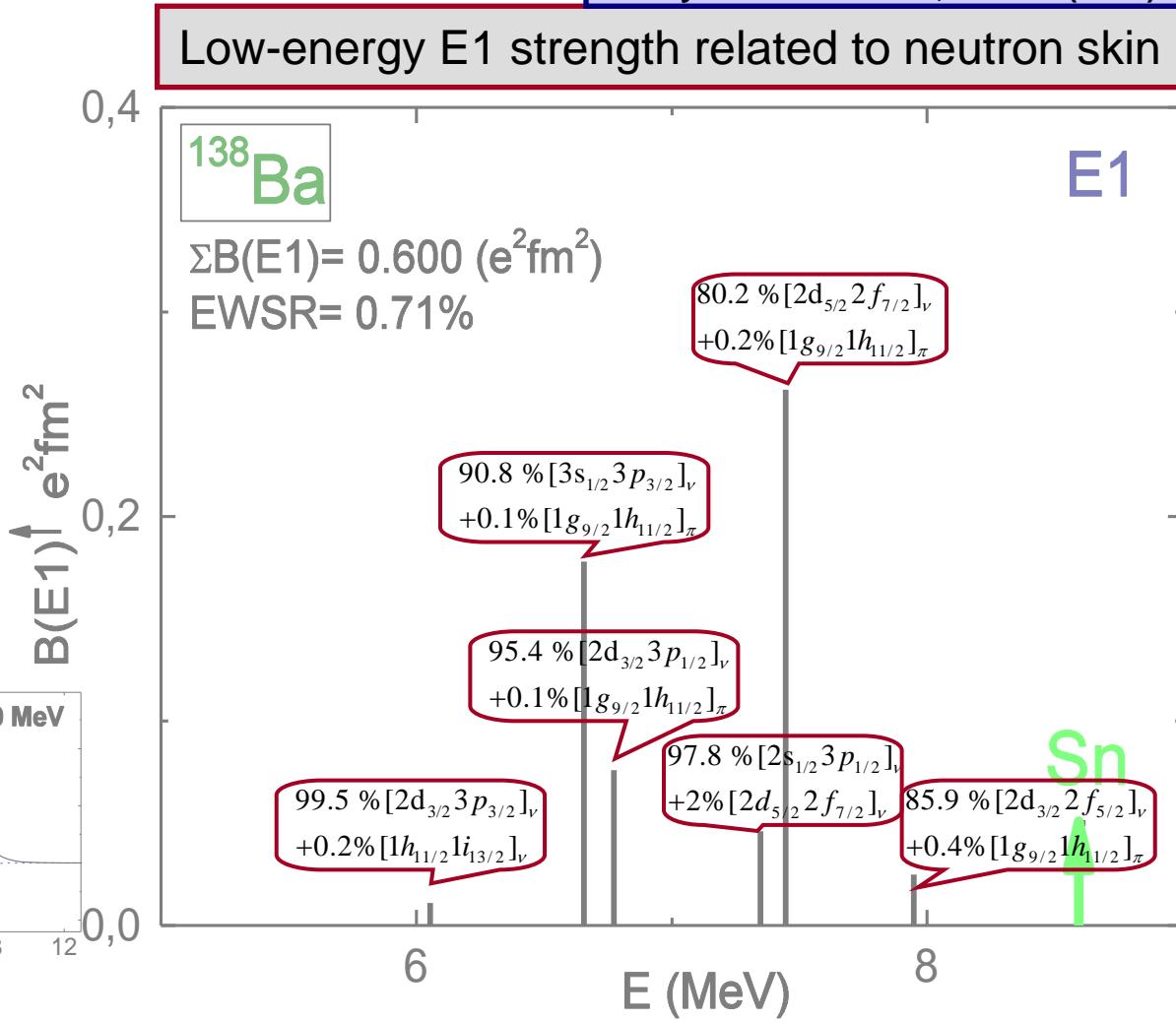
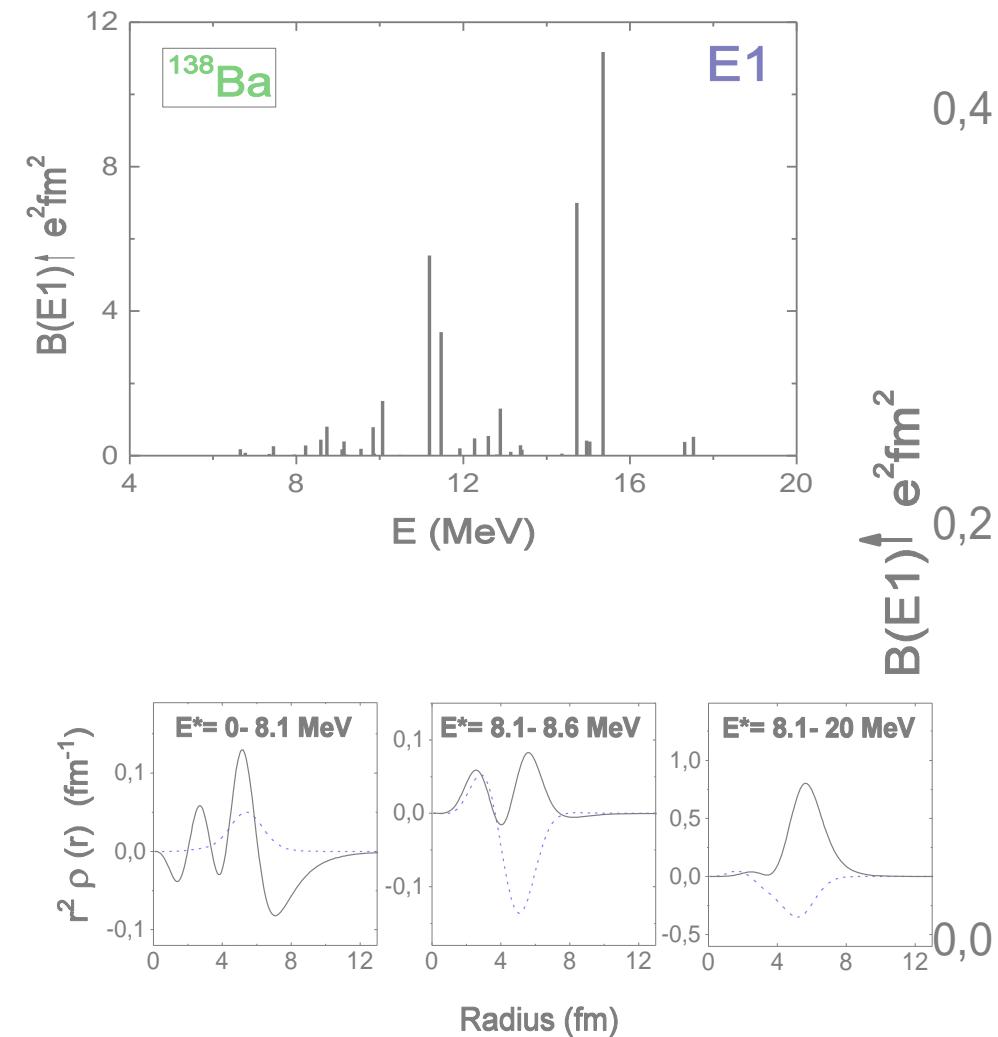
# QPM Calculations of Dipole Photoabsorption Cross Section in $^{90}\text{Zr}$ in comparison with Experimental Data Obtained from Inelastic Photon Scattering (ELBE-Rossendorf)

R. Schwengner et al, Phys. Rev. C 78 (2008) 064314

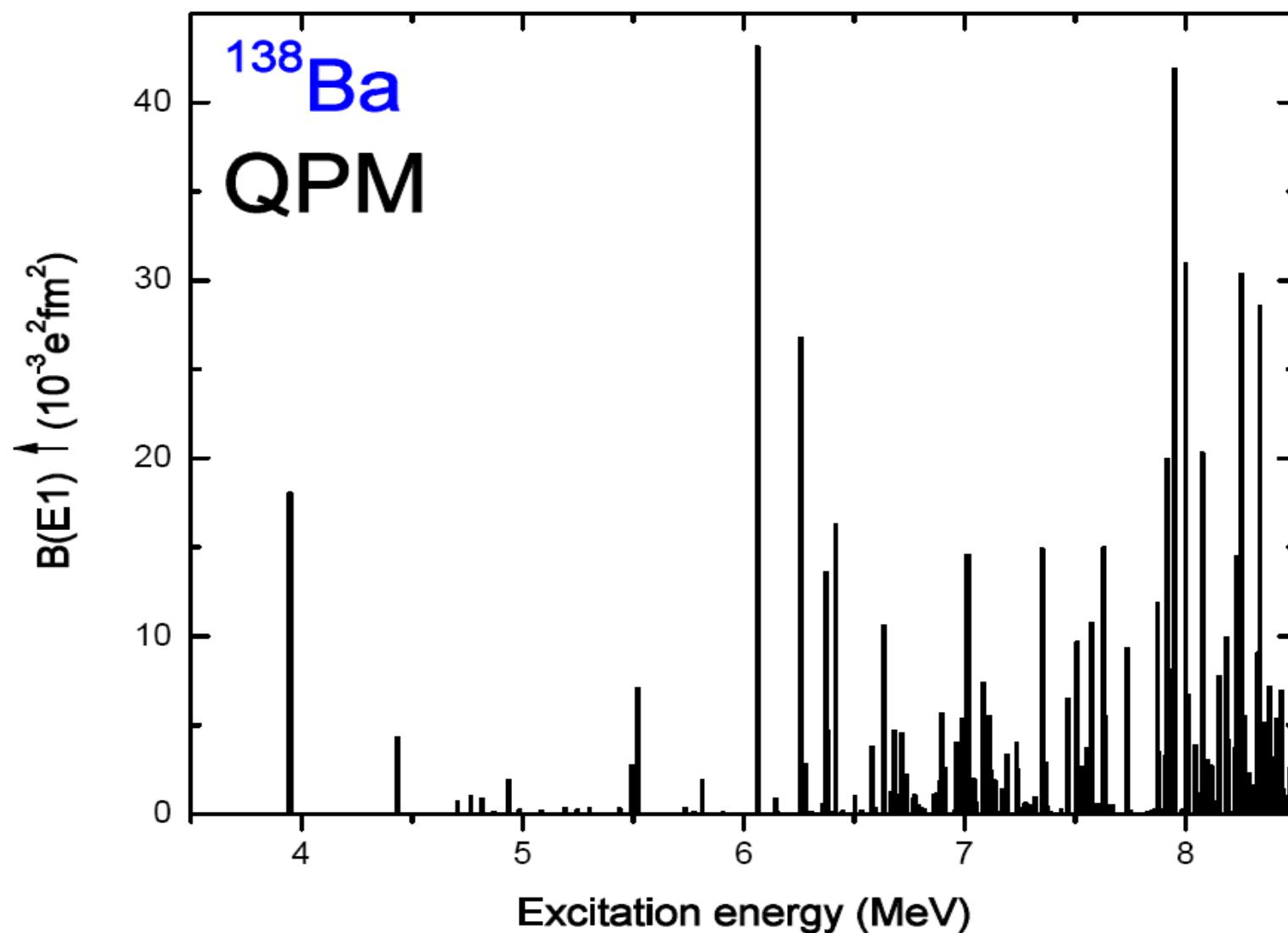


# QRPA Calculations of $1^-$ States in $^{138}\text{Ba}$

Phys. Rev. Lett. 104, 072501 (2010)

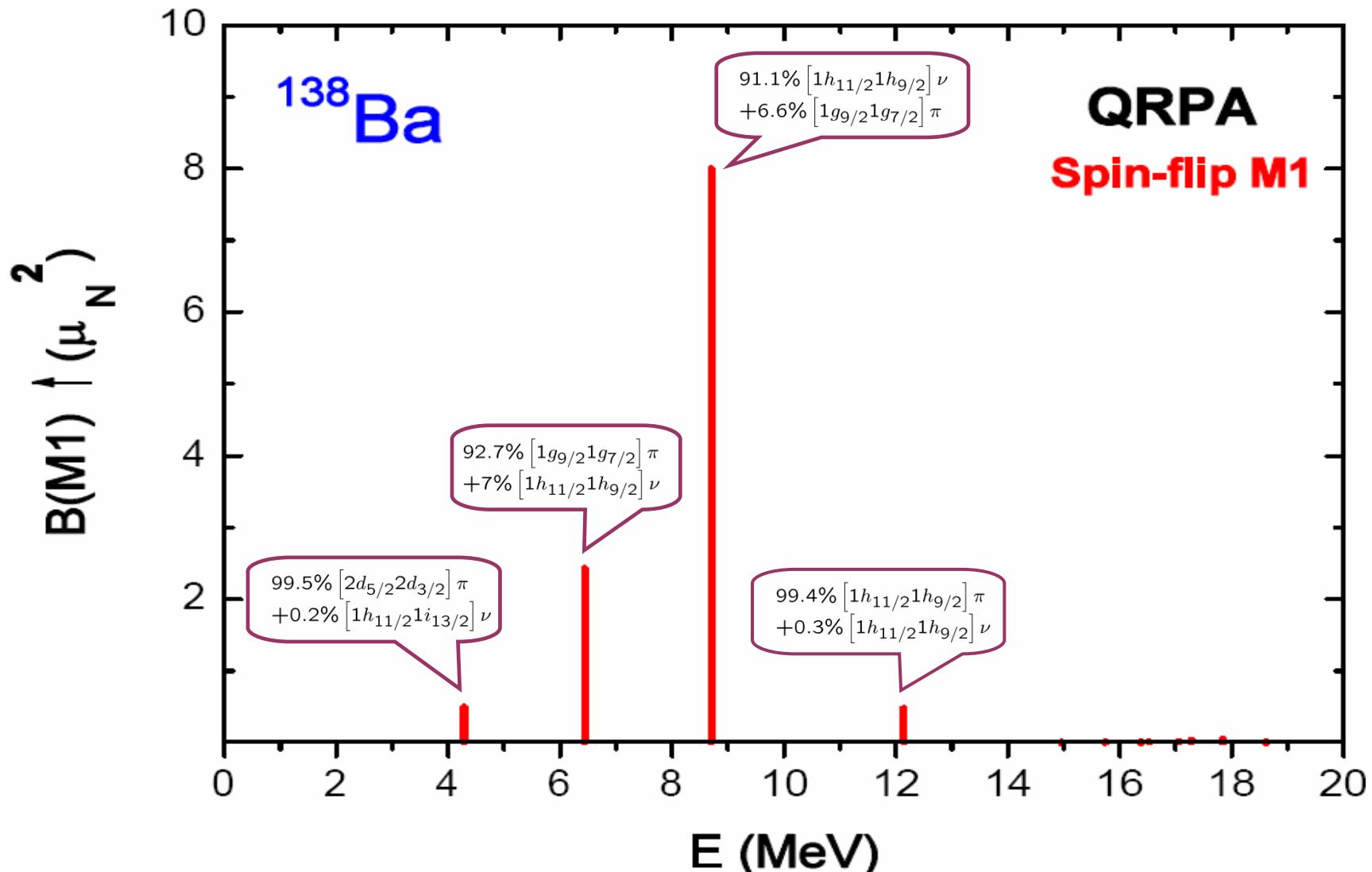


# QPM Calculations of E1 Strength in $^{138}\text{Ba}$



# Are There Other than E1 Dipole Excitations in the PDR Region?

## QRPA Calculations of $1^+$ States in $^{138}\text{Ba}$



*Parity Measurements with Polarized Photon Beams of Low-energy Dipole Excitations in  $^{138}\text{Ba}(\vec{\gamma}, \gamma')$  at HIGS, Duke, USA*

Phys. Rev. Lett. 104, 072501 (2010)

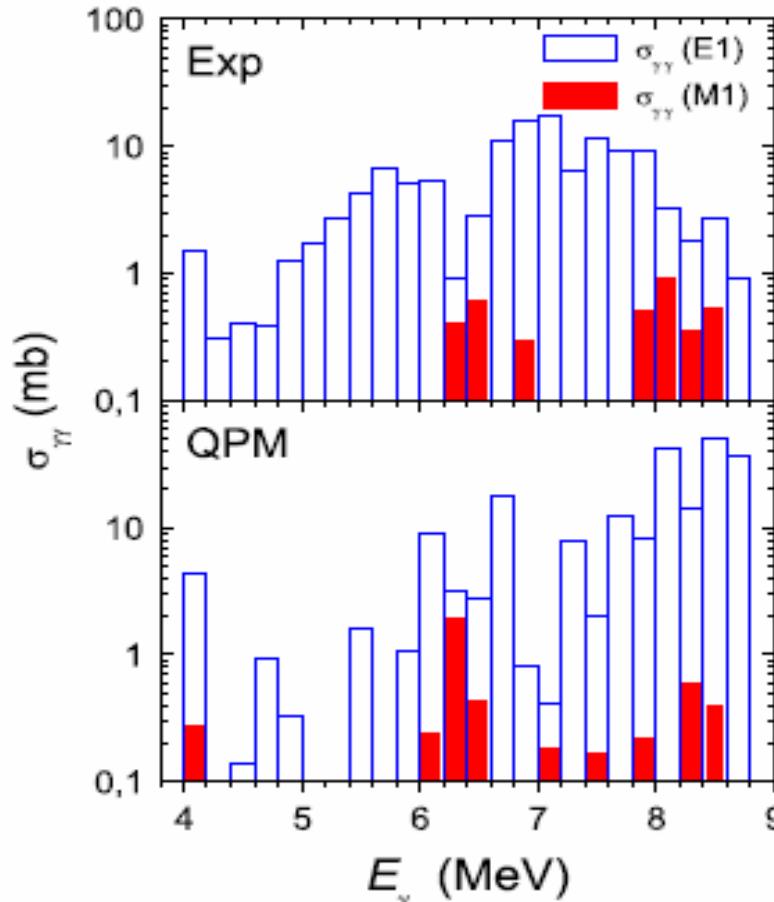
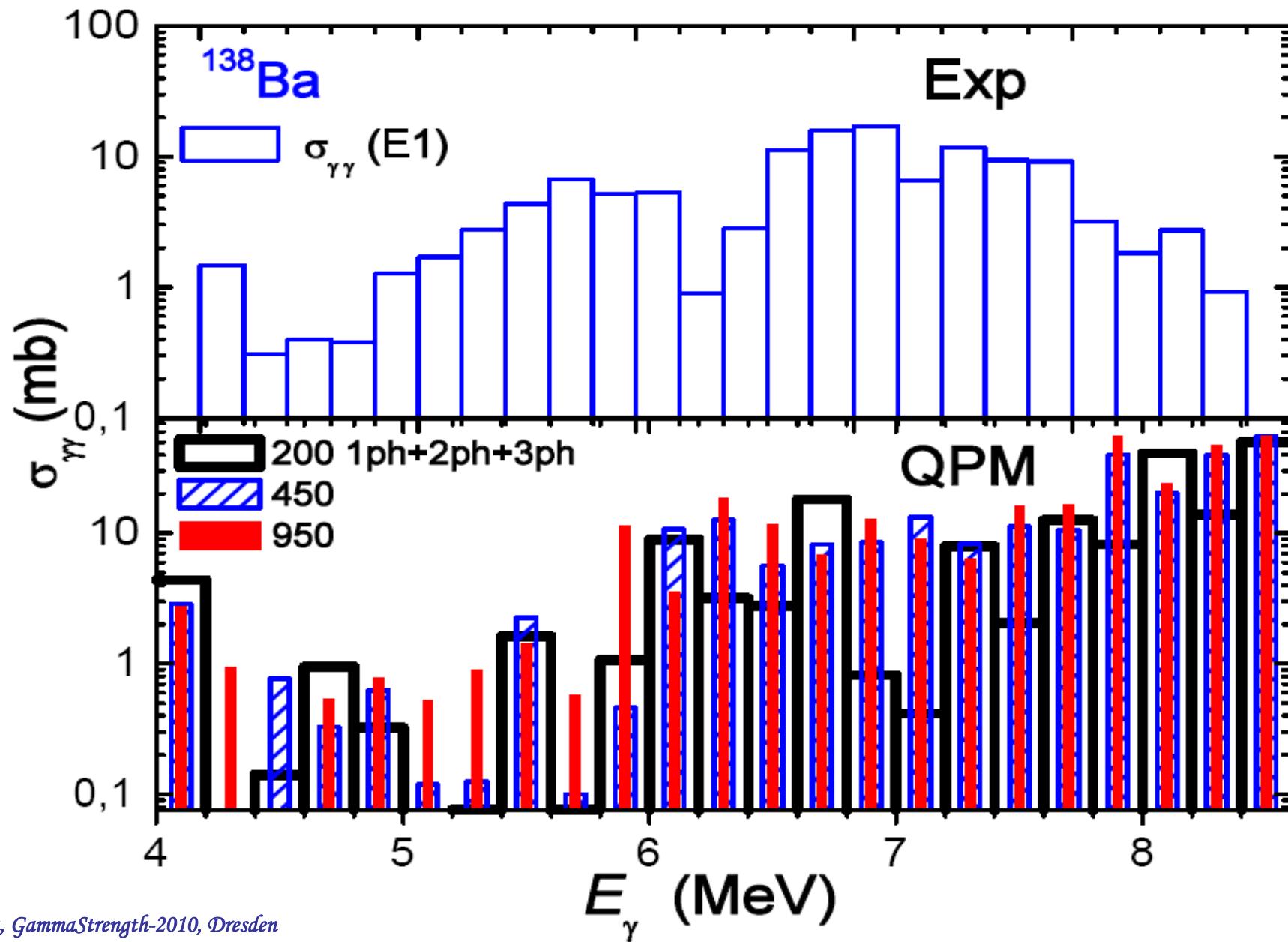


TABLE I.  $E1$  and  $M1$  parameters deduced in  $^{138}\text{Ba}$  below the neutron-separation energy in comparison with the QPM calculations.

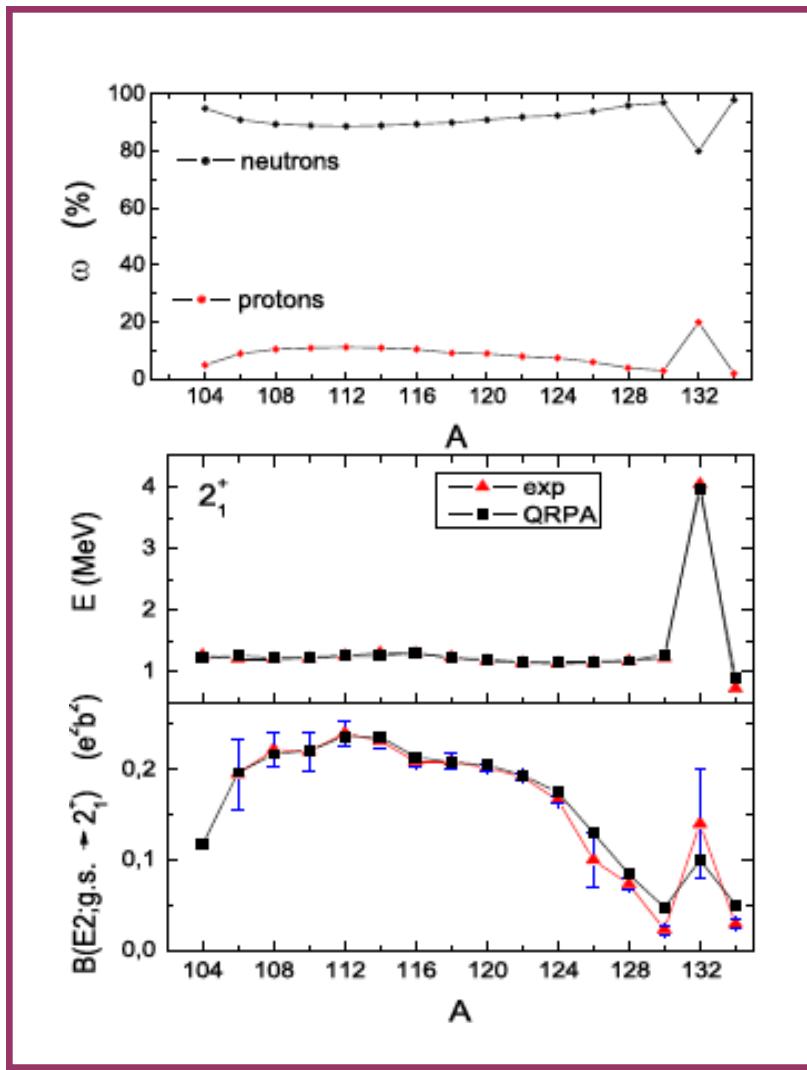
	$\langle E_{E1} \rangle$ [MeV]	$\Sigma B(E1) \uparrow [e^2 \text{ fm}^2]$	$\langle E_{M1} \rangle$ [MeV]	$\Sigma B(M1) \uparrow [\mu_N^2]$	EWSR $_{E1}$ [%]
Experimental	6.7	0.96(18)	6.9	2.5(6)	1.3
QPM	7.3	1.22	6.9 <sup>a</sup>	2.9 <sup>a</sup>	1.8

<sup>a</sup>4.1 MeV  $< E^* <$  8.5 MeV.

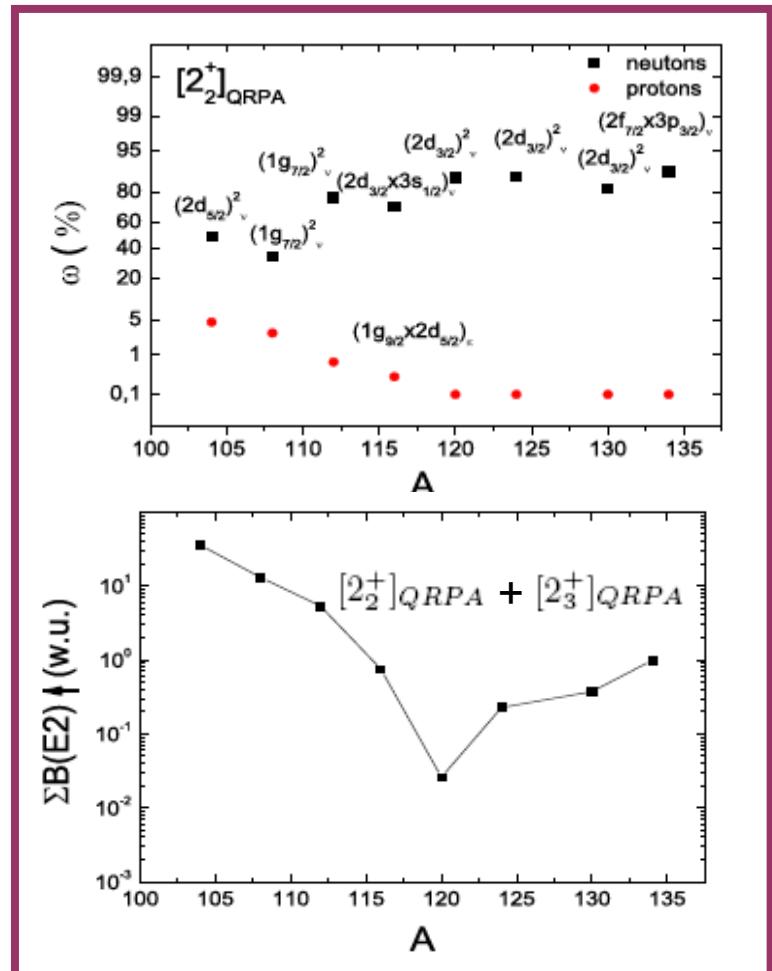
# QPM Calculations of 1<sup>-</sup> States within Different Phonon Spaces



# Low-Energy Quadrupole Excitations in Sn Nuclei

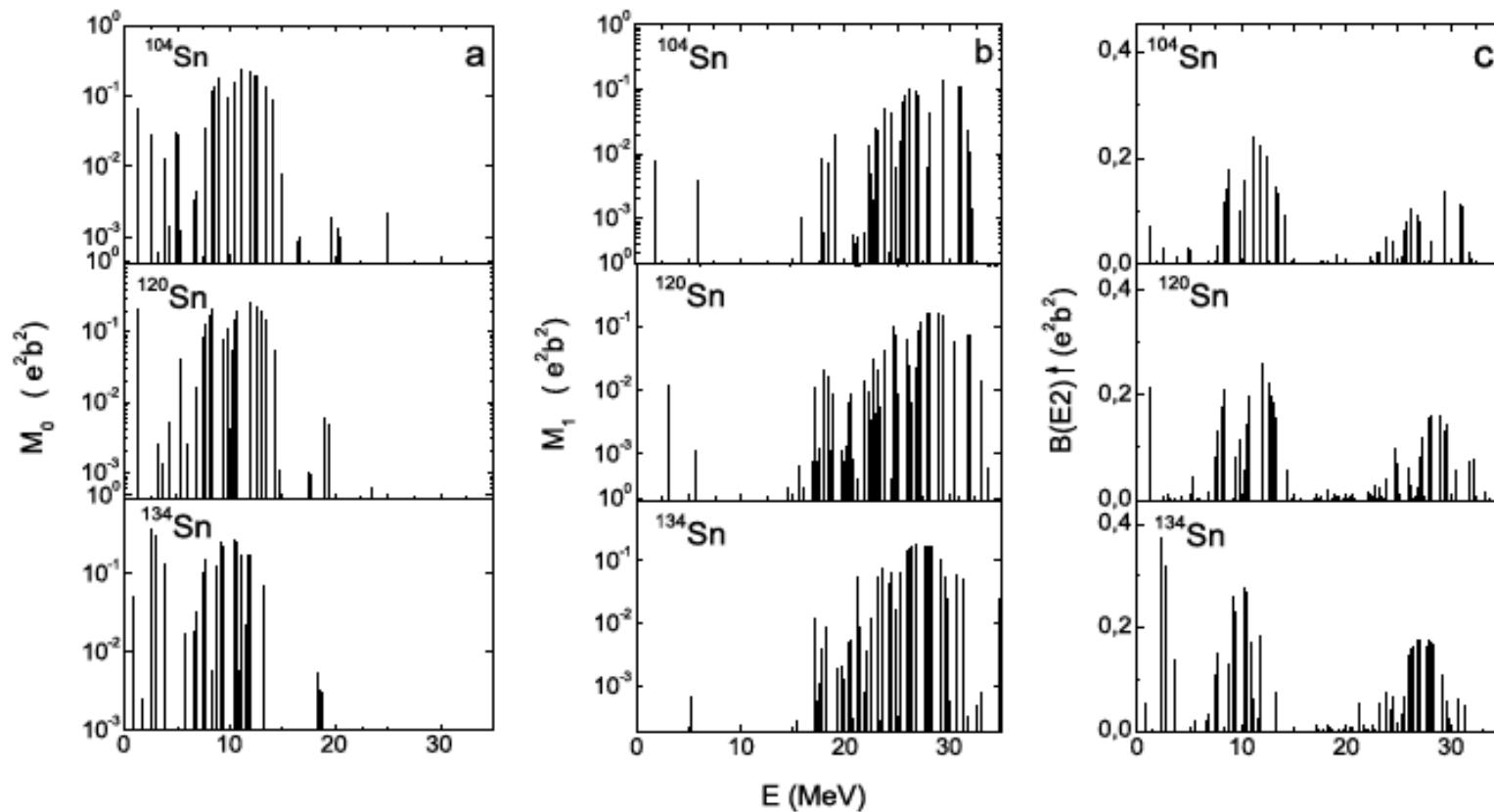


$$\omega_{j_1 j_2}(\lambda \mu i) = \sum (|\psi_{j_1 j_2}^{\lambda \mu i}|^2 - |\varphi_{j_1 j_2}^{\lambda \mu i}|^2) * 100(%)$$



# *Isoscalar and isovector quadrupole states in Sn nuclei*

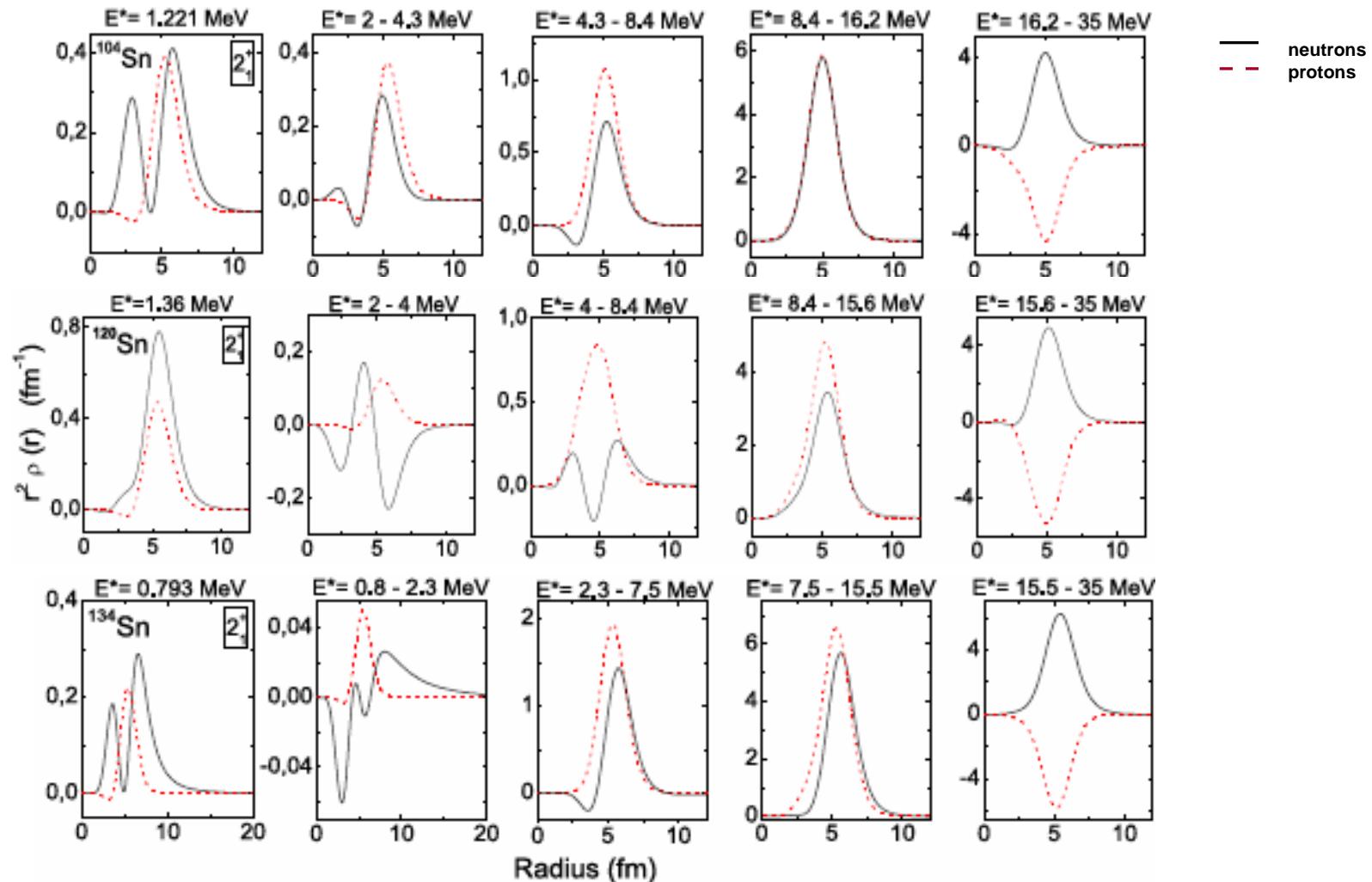
$$M_{0(1)}(2^+) \approx \left| \left\langle 2^+ \left\| \sum_k^p r_k^2 Y_{2\mu}(\Omega_k)_-^+ \sum_k^n r_k^2 Y_{2\mu}(\Omega_k) \right\| g.s. \right\rangle \right|^2$$



# QRPA Calculations of Isoscalar and Isovector Quadrupole States in Sn Isotopes

## A Possible Signature of a Pygmy Quadrupole Resonance

N. Tsoneva, H. Lenske, PLB submitted, arXiv:0910.3487 [nucl-th]



# Conclusions

- A correlation between the total PQR strength and the neutron-to-proton ratio  $N=Z$  defining the size of the neutron or proton skin.
- The PQR is independent of the type of nucleon excess.
- Investigations the assumption that the low-energy dipole strength in  $N=82$  should be related mostly to E1 strength. Even though, in order to determine the pure dipole strength associated with PQR and neutron skin phenomenon , the magnetic contribution must be identified and subtracted.
- $B(E2)$  transitions of low-energy mixed-symmetry  $2^+$  states in Sn isotopes are found correlated with the number of the excess nucleons. These states are clustered in a confined energy region and may be considered forming a Pygmy Quadrupole Resonance.
- Furthermore, the correlation of the Pygmy Quadrupole Resonance strength with the neutron (proton) skin thickness manifests itself via a transition from a neutron PQR to a proton PQR in  $^{104}\text{Sn}$ , the mass region where the neutron skin reverses into a proton skin.