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Using Eu^{3+} as an atomic probe to investigate the local environment in $LaPO_4\text{-}GdPO_4$ monazite end-members

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Abbreviations used in the article:

Time-resolved laser fluorescence spectroscopy (TRLFS)

Abstract

In the present study, we have investigated the luminescent properties of Eu³⁺ as a dopant in a

series of synthetic lanthanide phosphates from the monazite group. Systematic trends in the

spectroscopic properties of Eu³⁺ depending on the size of the host cation and the dopant to

ligand distance have been observed. Our results show that the increasing match between host

and dopant radii when going from Eu³⁺-doped LaPO₄ toward the smaller GdPO₄ monazite

decreases both the full width at half maximum of the Eu³⁺ excitation peak, as well as the

⁷F₂/⁷F₁ emission band intensity ratio. The decreasing Ln···O bond distance within the LnPO₄

series causes a systematic bathochromic shift of the Eu³⁺ excitation peak, showing a linear

dependence of both the host cation size and the Ln···O distance. The linear relationship can

be used to predict the energy band gap for Eu³⁺-doped monazites for which no Eu³⁺

luminescent data is available. Finally, mechanisms for metal-metal energy transfer between

host and dopant lanthanides have been explored based on recorded luminescence lifetime

data. Luminescence lifetime data for Eu³⁺ incorporated in the various monazite hosts clearly

indicated that the energy band gap between the guest ion emission transition and the host ion

absorption transition can be correlated to the degree of quenching observed in these materials

with otherwise identical geometries and chemistries.

keywords: Eu³⁺, monazite, incorporation, TRLFS, luminescence, quenching

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1 Introduction

Crystalline lanthanide orthophosphates (LnPO₄) doped with other elements of the lanthanide group have recently gathered substantial attention due to the favorable electronic properties of the 4f elements that can be employed for applications ranging from light display systems and nanoelectronic devices², medical and biological labels for in vitro imaging³ to applications in targeted drug release⁴. Orthophosphates offer an easily synthesized and robust solid matrix for the dopants, and LnPO₄ nanoparticles can be tailored for a variety of purposes. The chemical durability and structural flexibility of LnPO₄ make lanthanide phosphates crystallizing in the monazite structure attractive as host phases for the conditioning of long-lived radionuclides produced during the nuclear fuel cycle or in the dismantling of nuclear weapons. 5-10 The monazites are known to incorporate large quantities of actinides (> 20%)^{6,11}, and several studies report on the structural incorporation of actinides such as U, Th, Pu, Am, and Cm, within the monazite structure either through direct substitution by a trivalent actinide on the host cation site^{12,13}, or through coupled substitution of an actinide of higher oxidation state with a mono- or divalent cation to preserve charge neutrality 14,15. Eu³⁺ is often chosen as dopant in the investigated phosphates mainly due to its luminescent properties. Eu³⁺ is a preferred choice as an activator ion in the development of red-emitting phosphors due to its strong, long-lived luminescence emission. 16,17 Furthermore, crystal-field perturbation results in a fine structure in the luminescence spectra that depends on the site symmetry of the Eu³⁺ ion which, thus, can be used as a local structure probe for the determination of site symmetries in a host lattice.¹⁸ In general, luminescent properties of lanthanide ions depend on the host composition and structure as well as the concentration (i.e. interatomic distance) of luminescent centers present in the materials. 19-22 Therefore, local changes in the host material and the concentration range of dopants used will alter the spectroscopic properties of the luminescent probe and, depending on the application, may affect the suitability of the material.

In the present work we have studied Eu^{3+} incorporation and the impact of systematic trends within the host crystal structure on the dopant luminescence in a series of $LnPO_4$ end-members ($LaPO_4$ -GdPO_4) crystallizing in the monazite structure. The ionic radius of the host cation in these monazite end-members decreases systematically from La^{3+} ($r_{ion}^{IX} = 1.216 \, \mathring{A}$)²³ toward Gd^{3+} ($r_{ion}^{IX} = 1.107 \, \mathring{A}$)²¹ by ~10 %. A preferential incorporation of Eu^{3+} in monazites with a host cation radius similar to Eu^*s ($r_{ion}^{IX} = 1.120 \, \mathring{A}$)²³, e.g. $SmPO_4$ or $GdPO_4$, could be expected. In addition, the systematic decrease of the $Ln\cdots O$ bond distance in the series of monazite hosts with otherwise identical symmetry and chemistry provides an opportunity to study the impact of bond distance on the ligand field effect and the luminescent properties of the Eu^{3+} ion. Finally, by comparing the Eu^{3+} doped monazites with isolated fluorescent centers ($c_{Eu} = 500$ ppm) with pure $EuPO_4$, the influence of the lanthanide concentration in terms of metal-metal concentration quenching effects can be evaluated.

2 Experimental section

2.1 Lanthanide phosphate synthesis and characterization

The lanthanide phosphates LaPO₄ to GdPO₄ crystallizing in the monazite structure were synthesized by precipitation (excluding the redox sensitive CePO₄ and radioactive PmPO₄) similar to the procedure described in Roncal-Herrero et al.²⁴

Lanthanide nitrate salts were dissolved in deionized water (MilliQ) in concentrations of 0.3-0.5 M. A 14.8 M aqueous solution of H₃PO₄ was slowly added to the solution, causing precipitation of LnPO₄:Eu³⁺ according to Reaction 1. Details on the reagents used in the synthesis can be found in the supporting information (S.I.).

$$\text{Ln}(\text{NO}_3)_3 + \text{H}_3\text{PO}_4 \xrightarrow{500 \text{ ppm Eu}^{3+}} \text{LnPO}_4:\text{Eu}^{3+} + 3\text{HNO}_3$$
 (Reaction 1)

The suspension was heated in an oven at 90°C for 1 week to complete the precipitation. The solid was recovered by centrifugation (10,000 rpm, 10 min) and washed with MilliQ water. The washing step was repeated several times until the supernatant was free of nitrate ions (NO_3^- test strips). Subsequently the powders were dried in an oven at 90 °C for 12 h. The dry powders were milled in an agate mortar and calcined for 2h at 600°C in order to remove any nitrate residues. As a final step, sintering of LnPO₄ was carried out at 1450°C for 5h to obtain the crystalline monazite solids. Characterization of the synthetic monazites was done with X-ray powder diffraction (XRD), using a D4 Endeavor diffractometer with a θ –2 θ geometry (Bruker AXS GmbH) operating at 50 kV and 30 mA with a CuK α radiation (λ = 1.5418 Å) in the range 2θ = 10–100°. The XRD patterns of all synthesized monazites are in a perfect agreement with the corresponding data from the ICDD database, confirming the sole presence of highly crystalline, monoclinic monazite. XRD patterns for pure EuPO₄ and Eu³⁺-doped GdPO₄ are shown in Figure 1. For the XRD patterns of all synthetic monazites the reader is referred to the S.I., Figure S1.

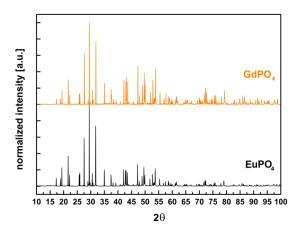


Figure 1: XRD patterns of synthetic EuPO₄ monazite and Eu³⁺-doped GdPO₄ monazite

2.2 Time-resolved laser fluorescence spectroscopy TRLFS

The Eu³⁺ ion exhibits many favorable luminescence properties, such as a non-degenerate ground state (${}^{7}F_{0}$) as well as emitting state (${}^{5}D_{0}$) and an even number of *f*-electrons (4 f^{6}) for which the number of crystal field levels is dependent on the site symmetry of the ion.²⁵ Therefore, Eu³⁺ is ideally suited for systematic studies of the structural incorporation of Eu³⁺ in crystalline solid phases, such as this series of synthetic monazites.

Detailed information on the Eu^{3+} environment in crystalline solids can be obtained by combining the luminescence data obtained from recorded excitation spectra, emission spectra, and luminescence lifetimes, as discussed below. Selective excitation of the Eu^{3+} ion from the 7F_0 ground state to the 5D_0 excited state, which both are non-degenerate due to their J=0 nature, allows for the determination of the number of non-equivalent species present in the solid matrix. In an excitation spectrum (integrated luminescence intensity as a function of excitation energy) of the $^7F_0 \rightarrow ^5D_0$ transition, one singlet signal is obtained for every Eu^{3+} species present in the system. The signal position, gives a first indication of the local environment of the respective Eu^{3+} species, where a stronger ligand field generally results in a lower energy transition and consequently in a stronger bathochromic shift of the signal. 26,27

For Eu³⁺ incorporation in the synthetic monazites only one singlet species corresponding to the structural incorporation of the dopant on the host lanthanide site is expected.

Selective excitation of the Eu^{3+} species in the solid matrix yields emission spectra and luminescence lifetimes of the single species. The emission spectrum allows for identification of the site symmetry in the host by making use of the splitting pattern of especially the ${}^5D_0 \rightarrow {}^7F_1$ and ${}^5D_0 \rightarrow {}^7F_2$ transitions. The crystal-field perturbation splits up the 7F_J terms in a number of crystal field levels that depends on the symmetry class. For crystal fields of orthorhombic or lower symmetries, the 2J+1 degeneracy is completely lifted. Thus, the monazite cation lattice site with a monoclinic (C_1) symmetry would result in a full 3-fold and 5-fold splitting of the 7F_1 and 7F_2 bands, respectively, for Eu^{3+} incorporation.

The Eu^{3+} luminescence lifetime, τ , has been correlated with the number of coordinating water molecules around the ion in solution through a linear empirical relationship, the so-called Horrocks equation 28,29 , Equation 1.

$$n(H_2O)$$
 [water molecules] = 1.07 [water molecules · ms]× τ^{-1} [ms⁻¹] – 0.62 (1)

For an incorporated ion without hydration water molecules in the first coordination sphere and in the absence of other quench processes (e.g. metal-to-metal energy transfer) the expected luminescence lifetime according to Eq. 1 is ~1.7 ms. However, significantly longer lifetimes (> 3 ms) have been reported for incorporated Eu³⁺ species.³⁰⁻³²

In the present work time-resolved laser fluorescence spectroscopy (TRLFS) for the collection of Eu³⁺ excitation and emission spectra was performed with a pulsed Nd:YAG (Spectra Physics) pumped dye laser set-up (Radiant Dyes Narrow Scan K) by directly exciting the Eu³⁺ ion from the ground ⁷F₀ state to the emitting ⁵D₀ state. The emitted luminescence emission light was directed into a monochromator (Acton SpectraPro 300i) with a 300- or 1200 lines/mm grating and the emission was monitored with an intensified CCD camera (Princeton Instruments) 10 µs after the exciting laser pulse in a time window of 10 ms. The laser pulse

energy and the exact excitation wavelength were monitored in every measurement with optical power meter (Newport 1918-R) and wavelength meter (High Finesse WS-5), respectively. To achieve the desired spectral resolution the solid samples were cooled to approximately 10 K in a helium refrigerated cryostat. Luminescence lifetime measurements were performed at two temperatures (10 K and at room temperature, RT) by monitoring the luminescence emission as a function of delay time (up to 12 ms) between the laser pulse and the camera gating. Lifetime measurements at 10 K were conducted with the laser set-up described above. The room temperature TRLFS measurements were performed with a Nd:YAG pumped OPO laser system (Powerlite Precision II 9020 - PANTHER EX OPO, Continuum). Eu³⁺ was excited at 394 nm and the time-resolved emission signal was directed into a monochromator (Oriel MS 257) with a 300 lines/mm grating followed by detection with an intensified CCD camera (Andor iStar).

3 Results and discussion

3.1 Eu³⁺ incorporation in LnPO₄ monazites

Excitation spectra of LaPO₄, SmPO₄, and GdPO₄ monazites doped with 500 ppm Eu³⁺ are presented in Figure 2 together with the excitation spectrum of pure EuPO₄. PrPO₄ and NdPO₄ doped with Eu³⁺ did not yield any detectable europium luminescence signal due to strong metal-metal quenching induced by the host lanthanides. The Eu³⁺ luminescence quenching phenomenon observed in some of the investigated solids will be discussed separately in the following section.

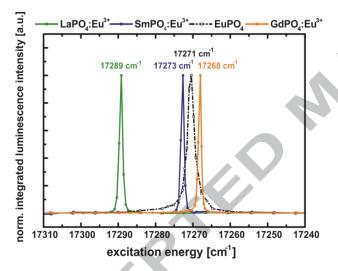


Figure 2: Eu^{3+} excitation spectra of the ${}^7F_0 \rightarrow {}^5D_0$ transition in LaPO₄, SmPO₄, and GdPO₄ monazites doped with 500 ppm Eu^{3+} (colored lines) and pure $EuPO_4$ (black line).

The Eu³⁺-doped monazites show one narrow excitation peak with a half width of around 1 cm⁻¹, corresponding to Eu³⁺ incorporation on the host lattice sites in the crystalline monazite structure. The size of the host cation can be seen to influence the recorded Eu³⁺ luminescence signal in two ways: A slight excitation line narrowing can be seen across the monazite series (excluding EuPO₄) with a FWHM of 1.03 cm⁻¹, 0.95 cm⁻¹, 0.92 cm⁻¹ for Eu³⁺-doped LaPO₄, SmPO₄, and GdPO₄, respectively. This can be explained by slight local distortions of the monazite crystal lattice around the incorporated Eu³⁺ ion, which is more pronounced for larger differences between the host and dopant cation radii, see Table 1.

Table 1: Host lanthanide radii and average Ln···O bond distances in monazites.

Monazite	Ln ³⁺ radius	Average Ln···O	
	r _{Ln(III)} IX [Å]*	distance [Å]**	
LaPO ₄	1.216	2.5787	
CePO ₄	1.196	2.5554	
PrPO ₄	1.179	2.5396	5
$NdPO_4$	1.163	2.5242	
PmPO ₄	1.144	2.5106 [†]	
SmPO ₄	1.132	2.4988	-
EuPO ₄	1.120	2.4878	-
GdPO ₄	1.107	2.4760	-

^{*}from Shannon²³

Furthermore, as the Ln···O bond length decreases from LaPO₄ toward GdPO₄ (Table 1) the ligand field effect that the oxygen atoms exert on the incorporated Eu³⁺ ion increases, leading to a visible bathochromic shift of the excitation signal. This shift follows a linear trend as a function of both ionic radius of the host cation and Ln···O bond distance (Figure 3), with excellent accuracy ($R^2 = 0.99999$ and $R^2 = 0.99984$, respectively). The average bond distances are calculated from the nine Ln·· O distances in the LnO₉ polyhedron obtained from the refined monazite structures in Ni et al.³³.

^{**}calculated from the refined monazite structures in Ni et al. 33

[†]predicted value from spectroscopic data, this study.

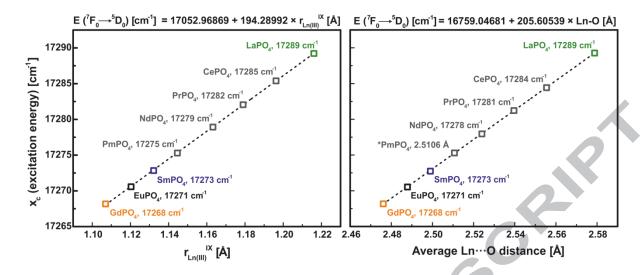


Figure 3: The Eu^{3+} excitation energy plotted as a function of the host cation radius (left) and average $Ln\cdots O$ distance in the monazite structure (right). Colored and black squares represent experimental data. Gray squares represent predicted values for the Eu^{3+} excitation energy or average $Pm\cdots O$ distance (*).

The linear fit of the experimental data (colored squares for Eu^{3+} -doped monazites, black square for pure $EuPO_4$ monazite) yield an expression for the excitation energy which can be calculated when either the lanthanide cation radius (Equation 2) or the average $Ln \cdot \cdot \cdot$ O distance in the monazite (Equation 3) is known.

$$E(^{7}F_{0} \to {}^{5}D_{0})[cm^{-1}] = 17052.96869 + 194.28992 \cdot r_{Ln(III)^{1X}}[\mathring{A}]$$
 (2)

$$E(^{7}F_{0} \to {}^{5}D_{0})[cm^{-1}] = 16759.04681 + 205.60539 \cdot Ln \cdots 0 \text{ [Å]}$$
(3)

Provided that the linear trend is valid throughout the monazite series these equations can be used to predict the excitation energies for Eu³⁺ incorporation in monazites for which no experimental data is available (CePO₄, PrPO₄, NdPO₄, PmPO₄). In addition, we can apply the results to predict the Pm·· O distance for PmPO₄, for which no crystallographic structure has been reported. The predicted excitation energy for Eu³⁺- doped PmPO₄ can be calculated with the known ionic radius of Pm³⁺ using Equation 2. Subsequently, a Pm·· O bond distance of

2.5106 Å can be calculated using that excitation energy and Equation 3. The predicted values are indicated in Figure 3 in gray. For a summary of all determined and predicted excitation energies the reader is referred to the S.I. (Table S1).

When exciting europium at the excitation peak maximum in Figure 2, the emission spectra and luminescence lifetimes of the incorporated Eu³⁺ ion can be recorded, Figure 4.

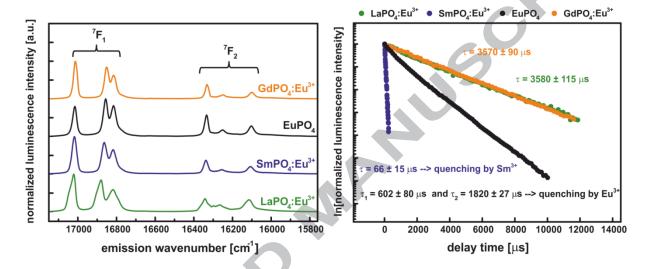


Figure 4: Eu³⁺ emission spectra (left) and luminescence lifetimes (right) in LnPO₄ monazites.

The emission spectra show a full 3-fold and 5-fold splitting of the 7F_1 and 7F_2 bands, respectively, corresponding to Eu $^{3+}$ incorporation on a low symmetry site, in accordance with the monoclinic (C_1) lattice site in the monazites. The relative intensities of these bands reflect the coordination symmetry around the Eu $^{3+}$ ion. 34,35 The $^5D_0 \rightarrow {}^7F_2$ transition has a predominant electric dipole character that is sensitive to changes in the ligand environment. In contrast, the $^5D_0 \rightarrow {}^7F_1$ transition retains its magnetic dipole character even in low symmetry systems and its intensity is not significantly influenced by the ligand environment. 36 Thus, when the site symmetry decreases, the relative intensity of the hypersensitive transition ($^5D_0 \rightarrow {}^7F_2$) increases, resulting in a larger $^7F_2/^7F_1$ ratio. For the Eu $^{3+}$ doped monazites a decrease in the $^7F_2/^7F_1$ ratio can be seen when going from LaPO₄ toward GdPO₄ with a ratio of 0.50 for LaPO₄, 0.41 for SmPO₄, and 0.37 for GdPO₄. This behavior can be explained by

the slight distortion of the crystal lattice accommodating a dopant with a dissimilar cation radius and the subsequent lowering of the site symmetry, as already explained above in connection to the observed excitation line narrowing. The largest difference of approximately 8%, between the size of the host and dopant cation radii, is observed for Eu³⁺ incorporation in LaPO₄, while a difference of just above 1 % applies for Eu³⁺ incorporation in SmPO₄ and GdPO₄.

The luminescence lifetimes recorded at 10 K of Eu $^{3+}$ incorporated in LaPO₄ and GdPO₄ decay monoexponentially with lifetimes of 3580 \pm 115 μs and 3570 \pm 90 μs , respectively. The long lifetimes speak for a full loss of the Eu $^{3+}$ hydration sphere upon incorporation in the monazite lattice, as can be expected after sintering of the samples at 1450°C. The lifetime recorded for Eu $^{3+}$ incorporation in SmPO₄ (66 \pm 15 μs) and the lifetimes obtained for pure EuPO₄ (602 \pm 80 μs and 1820 \pm 27 μs) are significantly shorter than 3600 μs , pointing toward quenching of the luminescence signal by e.g. the lanthanide neighbor atoms. As we can exclude quenching by water molecules due to the thermal treatment of the lanthanide phosphates, Eu $^{3+}$ luminescence must be quenched through a different mechanism. This quenching behavior will be discussed in detail in the following section.

3.2 Eu³⁺ luminescence quenching in LnPO₄ monazites

As discussed in the previous chapter, no Eu³⁺ luminescence could be detected in Eu³⁺-doped NdPO₄ and PrPO₄ monazites, while significantly shortened lifetimes in SmPO₄ and EuPO₄ were recorded in comparison to the non-quenched Eu³⁺-doped LaPO₄ and GdPO₄ hosts (Figure 4, right).

Various phenomena causing luminescence quenching of Eu³⁺ in a solid matrix have been reported, ranging from e.g. lattice defects in the solid structure³⁷ to excitation energy transfer to impurity ions present in the solid phase or metal-metal energy transfer between the dopant

and host cations³⁸. In the present study, the monazite synthesis was carried out under controlled conditions where the chemicals, synthesis steps, sintering conditions and sample handling have been kept constant. Thus, lattice defects and the presence of impurity ions should be very comparable within the monazite end-member series, which would imply that other quench mechanisms such as metal-metal energy transfer between Eu³⁺ and the lanthanide host cations are responsible for the observed differences in the luminescence properties of Eu³⁺. Metal-metal energy transfer can take place either via radiative energy transfer or through interionic processes involving direct excitation energy transfer between the two lanthanide ions without absorption or emission of photons.³⁹ Radiative energy transfer is only possible when one of the europium emission transitions $^5D_0 \rightarrow ^7F_J$ overlap with the absorption transition of another lanthanide, and in this case it is only the emission of the overlapping transition that is affected. The non-radiative relaxation process can be divided into resonant and non-resonant excitation energy transfer induced by either multipolar or exchange interactions between the interacting ions.³⁹ Resonant multipolar energy transfer occurs when the amount of energy delivered by the Eu³⁺ dopant is reasonably close to the amount of energy accepted by the host lanthanide. In the non-resonant case a fraction of excitation energy is either exchanged with the phonon field of the host lattice or transferred to a third ion. The extent of quenching through multipolar energy transfer has been shown to decrease exponentially with increasing energy mismatch, i.e. a larger band gap between donor and acceptor states. 40,41 The band gap in the present case is defined as the energy difference between the Eu $^{3+}$ $^5D_0 \rightarrow \,^7F_J$ emission transitions and the closest matching absorption transition of the accepting lanthanide. An exponential correlation cannot be deduced from our luminescence data but it is evident that the quenching of the Eu³⁺ luminescence is dependent on the size of the band gap ΔE , according to:

$$\Delta E(Eu^{3+} \rightarrow Nd^{3+}) \sim \Delta E(Eu^{3+} \rightarrow Pr^{3+}) < \Delta E(Eu^{3+} \rightarrow Sm^{3+}) < \Delta E(Eu^{3+} \rightarrow Eu^{3+})$$

The corresponding transitions are indicated in Figure 5, using identically colored arrows to indicate the 5D_0 to 7F_6 (purple), 7F_5 (orange), and 7F_0 (green) emission transitions and the closest matching absorption transitions. The arrow length is adapted to the individual band gaps, i.e. the length of the arrow indicating an emission transition does not necessarily match the arrow length of the closest matching absorption transition. For the corresponding transition energies the reader is referred to the S.I., Table S2. For Eu³⁺, the absorption transition is assumed to be $^7F_0 \rightarrow ^7F_6$, which plays an important role in e.g. the quenching of Tm³⁺ luminescence^{42,43}. It is however, clear that for every europium $^5D_0 \rightarrow ^7F_J$ emission transition a perfectly matched $^7F_J \rightarrow ^5D_0$ absorption transition is available and the energy band gap is, thus, zero. Energy transfer between matching transitions, however, does not lead to the observed quenching of the Eu³⁺ luminescence.

 La^{3+} is omitted from the figure due to the absence of f electrons and consequently f-f transitions. In addition, electronic transitions in La^{3+} from 5p to 4f or 5d states require substantially higher energies to occur and they will, thus, not interfere with the electronic transitions under consideration in the present study.

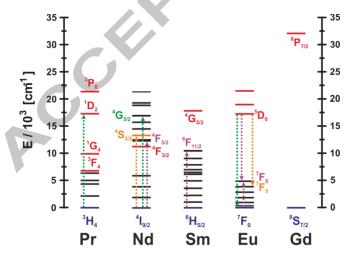


Figure 5: Partial energy level diagram of the lanthanides investigated in the present study. Emitting states are denoted in red. The colored arrows denote potential non-radiative transitions between donor and acceptor atoms, respectively. The figure is adapted from Bünzli and Piguet⁴⁴.

In both NdPO₄ (transitions indicated with purple and orange arrows) and PrPO₄ (green arrow) the energy gap difference is small, i.e. approximately 10 cm⁻¹ in NdPO₄ and 60 cm⁻¹ in PrPO₄. In neither of these solids any detectable luminescence from Eu³⁺ was observed. In SmPO₄ the band gap is approximately 1900 cm⁻¹ and in EuPO₄ 7400 cm⁻¹. In these solids Eu³⁺ luminescence was visible but luminescence lifetimes were reduced. The effect is significantly stronger in SmPO₄ ($\tau = 66 \pm 15 \,\mu s$) than in EuPO₄ ($\tau_1 = 602 \pm 80 \,\mu s$, $\tau_2 = 1820 \pm 27 \,\mu s$). In LaPO₄ and GdPO₄ non-radiative quenching is unlikely due to the absence of accepting energy levels below and close to the emitting ⁵D₀ term and the decay constants determined in these systems can be treated as entirely radiative deexcitation. In NdPO₄ and PrPO₄ where the energy band gap is very small, it is reasonable to assume that Eu³⁺ luminescence could be completely quenched by resonant multipolar energy transfer. In SmPO₄ and EuPO₄ nonresonant excitation energy transfer induced by either multipolar or exchange interactions should be considered due to the larger differences between the emission and absorption transitions. For the Sm³⁺ - Eu³⁺ couple, several studies reporting phonon assisted multipolar energy transfer between the lanthanide cations can be found 45-47. Thus, it is reasonable to assume that the same energy transfer mechanism applies to Eu³⁺-doped SmPO₄ monazite.

For multipole interactions the rate of energy transfer, k_{ET} , between a donor and acceptor atom can be correlated with their interatomic distance R_{DA} , according to equation 4:⁴⁸

$$k_{ET} = k_D \left[\frac{R_0}{R_{DA}} \right]^S = \frac{1}{\tau_D} \left[\frac{R_0}{R_{DA}} \right]^S$$
 (4)

Here, s = 6, 8, and 10, respectively, for dd, dq, and qq interactions. R_0 is the critical distance (also known as the Förster radius for dd-interactions in (bio)organic systems)⁴⁹, i.e. the distance at which the rate of energy transfer equals the reciprocal value of the lifetime of the donor level in the absence of acceptor ions, τ_D . In case of dipole-dipole interactions that usually feature large interaction lengths of several tens of angstroms^{50,51}, a critical distance R_0 can be calculated when both the quenched (τ_{DA}) and unquenched lifetimes are known:

$$R_0^6 = R_{DA}^6 \left(\frac{\tau_D}{\tau_{DA}} - 1\right) \tag{5}$$

Using the unquenched lifetime of 3570 μ s found for Eu³⁺ incorporation in GdPO₄, the average interatomic distance of 4.13 Å between two adjacent samarium atoms (connected to one another through an oxygen atom of a phosphate anion), and the quenched lifetime of 66 μ s for Eu³⁺-doped SmPO₄ the critical distance R₀ is found to be 8.02 Å. This distance is similar to reported critical distances for Eu³⁺ incorporation in solid matrices such as KGdTiO₄ (R₀ = 8.46 Å)⁵² or Y₂O₃ (R₀=8.4 Å)⁵³.

In order to assess the self-quenching mechanism in EuPO₄, a critical distance should be calculated. Equation $6^{54,55}$ provides a simple way of obtaining an estimate for the critical distance R₀ below which no concentration quenching of Eu³⁺ occurs.

$$R_0 \approx 2 \times \left(\frac{3V}{4\pi x_c N}\right)^{1/3} \tag{6}$$

Here N is the number of Eu^{3+} cations in the $EuPO_4$ unit cell (N = 4), V is the volume of the unit cell (2.902×10^{-28} m³ derived from the $EuPO_4$ unit cell parameters reported in Ni et al.³³), and x_c is the critical concentration ($Ln_{1-x}Eu_xPO_4$) beyond which concentration quenching is observed. As the focus of this paper has not been on resolving the quench mechanisms occurring in the Eu^{3+} doped monazites, we have not conducted a Eu^{3+} concentration dependent series for one of the monazites where a critical concentration could have been extracted. However, preliminary luminescence data on a $La_{1-x}Eu_xPO_4$ solid solution series indicates a slight deviation from the unquenched lifetime obtained for Eu^{3+} doped $LaPO_4$ for an x value of 0.1^{56} . Thus, by assuming a x_c value of 0.1 (also often encountered for Eu^{3+} in various solid matrices $La_{1-x}^{53,57-58}$) a critical distance of La_{1-x}^{59} , indicating that electric multipolar interactions would be responsible for the observed self-quenching in La_{1-x}^{59} . For a definite

assessment of the quench mechanism, however, a series of $Ln_{1-x}Eu_xPO_4$ solids should be synthesized for the extraction of a more accurate critical concentration.

Finally, in EuPO₄ the non-resonant energy transfer must be accompanied by a significant involvement of the phonon field or third party (impurity) ions to account for the excess excitation energy that is not dissipated through the acceptor absorption transition (${}^{7}F_{0} \rightarrow {}^{7}F_{6}$). To get an idea of the significance of lattice vibrations in the monazite solids and their impact on the luminescence lifetimes, room temperature lifetime measurements were conducted and compared to the lifetimes obtained at 10 K, Figure 6. In SmPO₄ no Eu³⁺ signal was obtained at RT, thus, a comparison cannot be made.

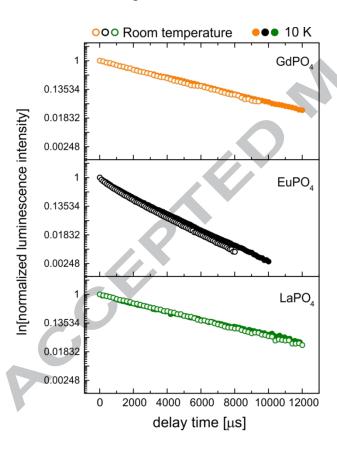


Figure 6: Comparison of lifetimes collected at room temperature (open symbols) and at 10 K (solid symbols) for LaPO₄, EuPO₄, and GdPO₄.

The difference between RT and 10 K lifetimes is in general very small. The absolute reduction of the lifetime in these solids lies between 130 μ s and 285 μ s, leading to a relative difference of 5-8 % in LaPO₄, GdPO₄, and for the longer component in EuPO₄. The largest

relative difference is observed for the shorter lifetime in EuPO₄ which is reduced from 602±80µs at 10 K to 465±60 µs at RT, i.e. a decrease of around 20%. Due to the overall low influence of temperature on the lifetimes, however, phonon assisted energy transfer dissipating an excess energy equivalent to 7400 cm⁻¹ is not very likely. Thus, for EuPO₄ impurities are expected to play a role in the deexcitation process. For Eu³⁺-doped SmPO₄ with a lifetime of 66µs at 10 K a similar absolute decrease of the lifetime as observed for the other monazite solids would be enough to completely quench the Eu³⁺ luminescence signal. It is not likely that the phonon field in SmPO₄ would behave very differently to the other monazites, however, for a definite assessment of the phonon contribution to the quenching of the Eu³⁺ luminescence signal and the subsequent contribution of third party ions, Eu³⁺ luminescence lifetimes in the SmPO₄ solid should be recorded at additional temperatures between RT and 10 K.

4 Conclusions

The systematic decrease of the Ln³⁺ host cation radius and Ln···O bond distance in the series of synthesized Eu³⁺-doped monazites (LaPO₄-GdPO₄) has enabled the study of Eu³⁺ luminescence properties related to size differences between host and dopant cation radii and the ligand field effect, in this case exerted by the oxygen ligands, in the monazite solids. We have shown that the slight distortion of the monazite crystal lattice around the Eu³⁺ dopant, when going from very similar host- and dopant cation radii (such as Eu³⁺ doped in GdPO₄) towards larger differences (Eu³⁺ doped in LaPO₄) causes a slight broadening of the Eu³⁺ excitation peak and an increase of the ${}^{7}F_{2}/{}^{7}F_{1}$ emission peak ratio. Furthermore, the increasing influence of the oxygen ligand field on the Eu³⁺ dopant as the Ln···O bond distance decreases across the monazite series, results in a systematic shift of the Eu³⁺ excitation peak position. This trend shows a linear dependence of both the Ln³⁺ host cation radius and the Ln···O bond distance. This dependence was used to predict the energy band gap of the $^7F_0 \rightarrow ^5D_0$ transition for those Eu³⁺-doped monazites that were not synthesized in the present study (CePO₄ and PmPO₄) or the monazites that did not show any Eu³⁺ luminescence due to strong metal to metal induced quenching (NdPO₄ and PrPO₄). In addition, we could apply the predicted excitation peak position for Eu³⁺-doped PmPO₄ to further predict the average Pm·· O distance in PmPO₄, for which no crystallographic structure has been reported. To our knowledge, a perfect linear relationship between the dopant to ligand distance and the energy band gap has not been observed previously for Eu³⁺ incorporation in solid materials with different host cations. If a linear trend can be found to apply for other solid materials, the possibility for energy band gap predictions based on the known host to oxygen ligand distance could open new possibilities in the construction and tailoring of luminescent materials for various applications. For such predictions, however, the presence and proximity of other luminescent centers around the dopant ion must be accounted for as shown in the present study. Due to the absence of structural or chemical differences in the series of investigated monazites, we can

attribute the degree of Eu³⁺ luminescence quenching by neighboring lanthanide cations to the size of the energy band gap between the donor atom emission transition and the acceptor atom absorption transition alone. However, it has to be noted that the quenching behavior in the present study applies to a doping of 500 ppm (0.05%) Eu³⁺ in the synthetic monazite solids. A different degree of quenching is likely to be obtained when increasing the dopant concentration in the monazites. Finally, the observed phenomena and the lack of Eu³⁺ luminescence in certain monazites do not influence the performance of the solid phases as suitable hosts for the trivalent dopant. A perfect substitution of the Eu³⁺ dopant for the host cation sites in all investigated monazites was obtained, independent of the size of the host cation, promoting the use of these ceramic phases as hosts phases, for example for the immobilization of trivalent dopants, such as the minor actinides Am³⁺ and Cm³⁺.

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Supporting Information: Details on the reagents used for the monazite synthesis are given. XRD spectra of all synthesized monazite end-members are presented in Figure S1. The experimental and predicted excitation energies as well as the predicted $Pm\cdots O$ distance are compiled in Table S1. Table S2 summarizes the transition energies of the $Eu^{3+} {}^5D_0 \rightarrow {}^7F_J$ emission transitions and various absorption transitions of the host lanthanides.

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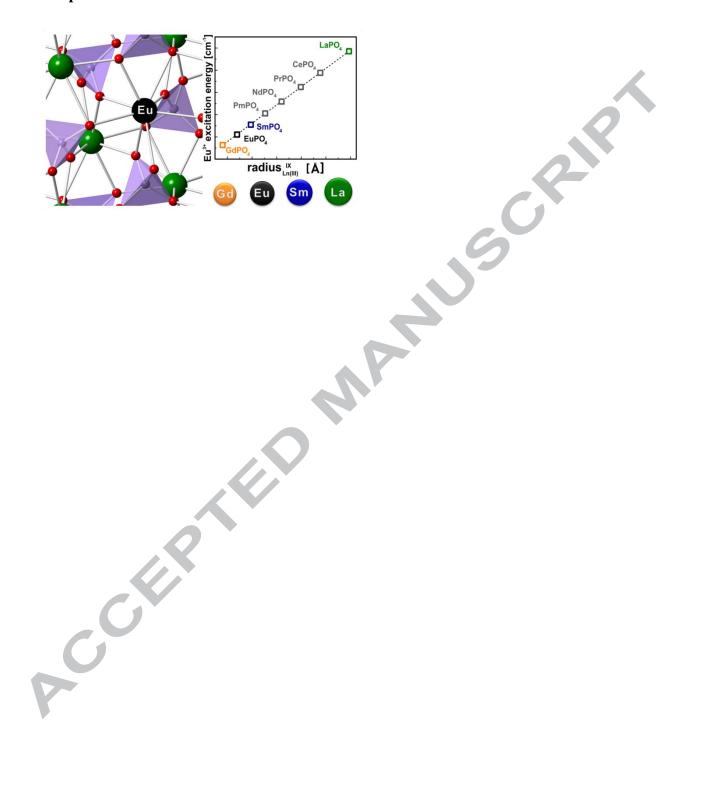
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- †data provided to reviewers

Graphical abstract



Supporting Information

Using Eu^{3+} as an atomic probe to investigate the local environment in $LaPO_4$ -GdPO $_4$ monazite end-members

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As starting materials for the monazite synthesis the following reagents were used: $La(NO_3)_3 \cdot 6H_2O$ (Alfa Aesar), $Pr(NO_3)_3 \cdot 6H_2O$ (Aldrich), $Nd(NO_3)_3 \cdot 6H_2O$ (Aldrich), $Sm(NO_3)_3 \cdot 6H_2O$ (Alfa Aesar), $Eu(NO_3)_3 \cdot 6H_2O$ (Alfa Aesar), $Gd(NO_3)_3 \cdot 6H_2O$ (Aldrich) and analytical grade 85% H_3PO_4 (Merck).

The crystallinity and phase purity of the synthesized products were characterized by XRD. All measured XRD spectra are compiled in Figure S1.

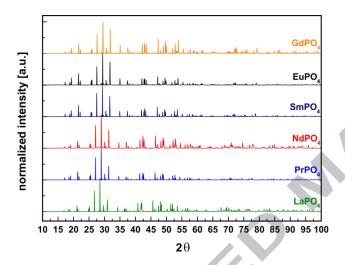


Figure S1: XRD spectra of all synthesized monazite end-members

From the linear equations obtained by plotting the Eu³⁺ excitation peak position as a function of host cation radius or average Ln·· O distance, the excitation energies for Eu³⁺ incorporation in monazites for which no experimental data could be obtained (CePO₄, PrPO₄, NdPO₄, PmPO₄) have been calculated. In addition, the excitation peak position for Eu³⁺-doped PmPO₄ could be further used to predict the average Pm·· O distance in PmPO₄, for which no crystallographic structure has been reported. The experimentally derived and predicted values for the excitation energies and the Pm·· O distance are tabulated in Table S1 below.

Table S1: Experimentally derived and predicted values for the Eu^{3+} excitation energies and the $Pm \cdot \cdot \cdot O$ distance in the synthetic monazite end-members.

Monazite	Experimental data	Predicted data*
	Eu ³⁺ excitation energy [cm ⁻¹]	Equation 2 / Equation 3
LaPO ₄	17289	-
CePO ₄	-	17285 / 17284
PrPO ₄	-	17282 / 17281
NdPO ₄	-	17279 / 17278
PmPO ₄	-	E = 17275 / R = 2.5106
SmPO ₄	17273	-
EuPO ₄	17271	-
GdPO ₄	17268	-

^{*}Eu³+ excitation energies are given in cm⁻¹ and Pm···O distance in Å.

The band gap, i.e. the energy difference between the $Eu^{3+} {}^5D_0 \rightarrow {}^7F_J$ emission transitions and the closest matching absorption transition of the accepting lanthanide has been calculated from available data in Martin et al. 1978. For the sake of consistency, the calculations have been done with the published emission transition energy of 17270 cm⁻¹ for the ${}^5D_0 \rightarrow {}^7F_0$ transition of the Eu^{3+} ion despite the experimentally derived values for this transition ranging from 17268 to 17289 cm⁻¹ in the various Eu^{3+} -doped monazites in the present study. The transition energies and energy gap differences are compiled in Table S2.

Table S2: Transition energies for the Eu³⁺ $^5D_0 \rightarrow ^7F_J$ emission transitions, chosen monazite host lanthanide absorption transitions and the energy difference (ΔE) of the emission- and absorption transitions.

Emission transition Eu ³⁺	Transition energy [cm ⁻¹]*	
$^{5}D_{0}\rightarrow$ $^{7}F_{6}$	12330	
$^{5}\mathrm{D}_{0} \!\! o^{7} \! \mathrm{F}_{5}$	13360	
$^{5}\mathrm{D}_{0}\!\!\rightarrow^{7}\!F_{0}$	17270	
Absorption transition Pr ³⁺	Transition energy [cm ⁻¹]*	ΔE (emission–absorption) [cm ⁻¹]
$^{3}\text{H}_{4} \rightarrow ^{1}\text{D}_{2}$	17334	$^{5}D_{0} \rightarrow ^{7}F_{0} (17270) - 17334 = -64$
Absorption transition Nd ³⁺	Transition energy [cm ⁻¹]*	ΔE (emission–absorption) [cm ⁻¹]
$^{4}I_{9/2} \rightarrow ^{4}F_{5/2}$	12320	$^{5}D_{0} \rightarrow ^{7}F_{6} (12330) - 12320 = 10$
$^{4}I_{9/2} \rightarrow ^{4}S_{3/2}$	13370	$^{5}D_{0} \rightarrow ^{7}F_{5} (13360) - 13370 = -10$
$^{4}I_{9/2} \rightarrow ^{4}G_{5/2}$	16980	$^{5}D_{0} \rightarrow ^{7}F_{0} (17270) - 16980 = 290$

Absorption transition Sm ³⁺	Transition energy [cm ⁻¹]*	ΔE (emission–absorption) [cm ⁻¹]
$^{6}\text{H}_{5/2} \rightarrow ^{6}\text{F}_{11/2}$	10470	$^{5}D_{0} \rightarrow ^{7}F_{6} (12330) - 10470 = 1860$
Absorption transition Eu ³⁺	Transition energy [cm ⁻¹]*	ΔE (emission–absorption) [cm ⁻¹]
$^{7}F_{0} \rightarrow ^{7}F_{6}$	4940	$^{5}D_{0} \rightarrow ^{7}F_{6} (12330) - 4940 = 7390$

*The transition energies are taken from Martin, W. C., Zalubas, R., and Hagan, L. 1978

Atomic Energy Levels – The Rare-Earth Elements: The Spectra of Lanthanum, Cerium,

Praseodymium, Neodymium, Promethium, Samarium, Europium, Gadolinium, Terbium,

Dysprosium, Holmium, Erbium, Thulium, Ytterbium, and Lutetium. Institute for Basic

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