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1 Evaluation of the microlayer contribution to bubble growth in horizontal pool

- boiling with a mechanistic model that considers dynamic contact angle and base
 expansion
- 4

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Abstract

9 Recently a new mechanistic model for pool and nucleate flow boiling was developed in our 10 group. This model is based on the balance of forces acting on a bubble and considers the evaporation of the microlayer underneath the bubble, thermal diffusion around the cap of bubble 11 12 due to the super-heated liquid and condensation due to the sub-cooled liquid. Compared to other 13 models we particularly consider the temporal evolution of the microlayer underneath the bubble 14 during the bubble growth by consideration of the dynamic contact angle and the dynamic bubble 15 base expansion. This enhances, in our opinion, the model accuracy and generality. In this paper 16 we further evaluate this model with experiments and direct numerical simulation (DNS) in order 17 to prove the importance of dynamic contact angle and bubble base expansion.

18 Keywords: nucleate boiling; microlayer; force balance; dynamic contact angle; dynamic base
 19 expansion; bubble geometry

20 1. Introduction

21 Nucleate boiling is an efficient heat transfer process. Its physical modelling is still not fully 22 mature as it involves complex two-phase fluid dynamics with mass, momentum and energy transfer at 23 the liquid-vapor interface and further heat conduction through solid walls. The bubble dynamics of 24 nucleation boiling has been heavily investigated since the 1950s, first in pool boiling. In the 1950s 25 Forster and Zuber [1] as well as Plesset and Zwick [2] modelled the bubble growth in a uniformly 26 superheated liquid. Zuber [3] extended this model to non-uniform temperature fields. Then Mikic et al. 27 [4], Prosperetti and Plesset [5], and Laburtsov [6], derived dimensionless relations for inertia 28 controlled and heat (or thermal diffusion) controlled growth. Cooper and Loyd [7] identified a thin 29 liquid microlayer underneath the bubbles and modelled it on the basis of experimental findings. Then 30 Van Stralen et al. [8] proposed a model based on the evaporation of the microlayer underneath the 31 bubble and heat diffusion from a relaxation microlayer around the bubble. In 1993, Klausner et al. [9] 32 developed a model based on the balance of the forces acting on the bubble to predict its departure and 33 lift-off. The authors obtained satisfactory prediction accuracy against their own data of flow boiling 34 with refrigerant R113. They recommended a fixed bubble base diameter (contact diameter) of 0.09 35 mm, an advancing contact angle of $\pi/4$ and a receding contact angle of $\pi/5$. Later, modified versions of 36 the Klausner model have been brought up by others with other values of base diameter, advancing and 37 receding contact angle to predict their own experimental data. Examples are Yun et al. [10], Situ et al. 38 [11], Sugrue [12], Thorncroft et al. [13] and Chen [14]. Klausner applied the Mikic model to simulate 39 the bubble growth while Situ and most of the latter authors employed the Zuber [4] formulation. Zuber 40 included in his formulation a parameter b to account for bubble sphericity. This parameter has been used by the latter authors with different values between 0.24 and 24 to fit the models with their 41 experimental data [15]. Yun et al. [10] improved Klausner's model by incorporating a bubble 42 43 condensation model as well as evaluating the model for a wider range of pressure, temperature, and 44 flow rates for water. More recently, in 2015, Colombo and Fairweather [15] developed a mechanistic 45 model to simulate the bubble growth and departure. In the model, they considered the contribution of 46 the microlayer, the superheated thermal liquid layer and the condensation to bubble growth (Figure 1). 47 Based on the suggested contact angles from Klausner et al. [9] and other empirically measured contact angles, the model gave a good agreement with data from different experiments. Later in 2017, Raj et al. 48 49 [16] tried to formulate a similar model as an analytical solution with countable validations. In 2018, 50 Mozzocco et al. [17] developed a model for the mechanistic prediction of bubble departure and lift off. 51 Different to the models of Colombo and Fairweather [15] and Raj et al. [16], where the condensation is 52 being modelled with the correlation of Ranz and Marshall [22], the author applied a parametric 53 constant to capture the effect of convective heat transfer for saturated and subcooled flow conditions. 54 The model was also validated with different experimental data. It was found that the bubble dynamics 55 models still require some empirical constants under different conditions. For the force analysis in the 56 models, the bubble is always considered as a hemisphere or truncated sphere and the impact of bubble

57 deformation during the bubble growth is not considered.



58

59 Figure 1: Schematic sketch of the bubble during its growth: β_{ad} and β_{re} are the advancing and

60 receding side contact angles, d_w is the bubble base diameter and θ_w is wall orientation angle, (1)

61 *evaporation from superheated layer, (2) evaporation from microlayer, (3) condensation.*

62 Basing on previous studies, e.g. of Colombo and Fairweather [15], Raj et al. [16] and Mozzocco et 63 al. [17], our group recently developed a mechanistic model to simulate and predict the bubble departure 64 in pool boiling and flow boiling on a smooth wall. The model considers the heat transfer contributions 65 from the microlayer, the superheated layer surrounding the bubble and condensation at the bubble's top. Moreover, the formation, evaporation and depletion of the microlayer (dryout formation) as well as 66 the change of the bubble geometry during the bubble growth are considered in this model. In our 67 68 opinion, this enhances the model accuracy and generality. The calculation of the microlayer is 69 supported by the consideration of dynamic contact angle and bubble base expansion. The differences 70 between the present model and previous models are given in Table 1.

In this work, our model of horizontal pool boiling will be applied to evaluate the role of the microlayer beneath the bubble to the bubble growth. We compare results obtained with our new model with the experiments from Duan et al. [19] for pool boiling of water at 1 atm and corresponding Direct Numerical Simulations (DNS) from Sato and Niceno [20]. The comparisons help to verify the concept related to the consideration of dynamic contact angle, dynamic base expansion and geometry change with bottleneck.

Table 1: Published models for calculating bubble growth and departure ("•" indicates that the respective physical mechanism is modelled)

Authors	rs Growth			Departure model (force balance model)		
	Microlayer	Superheated thermal layer	Condensation	Force balance	Contact angle/ base expansion	Geometry change
Zuber [3]		•				
Plesset and Zwick [2]		•				
Mikic et al. [4]		•				
Cooper and Lloyd [7]	•					
Van Stralen et al. [8]	٠	٠				
Klausner et al. [19]		•		•	• Constant/ Constant	
Yun et al. [10]		٠	•	•	• Constant/ $d_w = 2r_b/15$	
Colombo and Fairweather [15]	• (no dryout)	•	•	•	• Constant and case dependent/ constant	
Raj et al. [16]	• (no dryout)	•	•	•	• No statement	
Mazzoco et al. [17]	• (no dryout)	٠	•	٠	• No statement	
Present study	• (incl. formation, evaporation and depletion (dryout))	•	•	•	• Dynamic /Dynamic	•

80 2. Bubble Growth and Detachment Model

81 2.1 Bubble Growth Rate

82 The bubble growth process can be divided into two periods: the inertia controlled period and the thermal diffusion controlled period [4]. When the bubble is still small, its growth in diameter is quite 83 84 fast and determined by the inertia of the liquid being displaced. Hence this period is referred to as 85 inertia controlled growth. In this period a microlayer is formed underneath the bubble, which was 86 postulated and proven by Cooper in 1969 [7]. After a while the growth of the bubble diameter becomes 87 slower and it is no longer limited by liquid displacement but by evaporative heat flux at the gas-liquid 88 interface. This is hence referred to as thermal diffusion controlled growth. An essential evaporative 89 heat flux contribution in this period comes from the microlayer, which is well superheated. In this 90 period, the microlayer underneath the bubble extends with the growth of the bubble (Figure 2). When 91 the bubble grows into the sub-cooled liquid, where the temperature is lower than saturation 92 temperature, the condensation slows down the growth of bubble and sometimes even shrinks the 93 bubble.



Figure 2: Schematic sketch of the inertia and thermal diffusion controlled bubble growth on a
horizontal heating surface.

Mikic et al. [4] derived a model for the inertia controlled growth of a bubble on a heated surface. Theiranalysis, which bases on the Clausius-Clapeyron equation, relates the time dependent bubble radius

99

$$r_b(\mathbf{t}) = \left\{ \frac{\pi}{7} \left(\frac{T_w - T_{sat}}{T_{sat}} \right) \frac{h_{fg} \rho_g}{\rho_l} \right\}^{1/2} t,\tag{1}$$

100

101 to the wall temperature T_w and the saturation temperature of the liquid T_{sat} given the latent heat h_{fg} 102 and the densities of gas and liquid ρ_a , ρ_l . Mikic et al. further introduced the constants

103

$$A = \sqrt{\frac{\pi}{7} \left(\frac{T_{W} - T_{sat}}{T_{sat}}\right) \frac{h_{fg} \rho_g}{\rho_l}} \quad and \quad B = Ja \sqrt{\frac{12\alpha_l}{\pi}},$$
(2)

104

105

106 with the Jacob number $Ja = \frac{\rho_l c_{pl}(T_w - T_{sat})}{\rho_g h_{fg}}$, the thermal diffusivity α_l and the heat capacity c_{pl} of the 107 liquid and claimed that for $\frac{A^2 t}{B^2} \ll 1$ growth is inertia controlled while for $\frac{A^2 t}{B^2} \gg 1$ it is thermal 108 diffusion controlled. As in an applicable model we need to have a clear distinction, we will further 109 consider $\frac{A^2 t}{B^2} = 1$ as a demarcation value between the two states. With that, the maximal inertia 110 controlled bubble radius is given as

111

$$r_{m,g} = \frac{B^2}{A}.$$
(3)

112

In the inertia controlled growth period the shape of the bubble is hemispherical. The heat flux is given by heat conduction through the microlayer on the superheated surface

$$\dot{Q} = k_l \frac{(T_w - T_{sat})}{\delta_{mi}^0(x)} = k_l \frac{\Delta T_{sat}}{\delta_{mi}^0(x)},\tag{4}$$

117 where k_l is liquid thermal conductivity, $\delta_{mi}^0(x)$ the initial microlayer thickness at a distance x from 118 the nucleation site (Figure 2) and ΔT_{sat} the wall superheat. According to our assumption that $\frac{A^2t}{B^2} = 1$ 119 demarcates the transition, the thermal diffusion controlled growth period sets in when the bubble 120 reaches the maximal inertia controlled bubble radius $r_{m,g}$. Then bubble growth is mainly fed by the 121 evaporation of the microlayer and the superheated liquid surrounding the bubble cap. Considering the 122 heat balance between the latent heat of the liquid microlayer evaporation and the heat conducted 123 through the microlayer we find for the microlayer thickness $\delta_{mi}(t,x)$ that

124

$$-\rho_l h_{fg} \frac{d\delta_{mi}(t,r)}{dt} = \frac{k_l \Delta T_{sat}}{\delta_{mi}(t,x)}.$$
(5)

125

126 Considering further the mass balance the volumetric bubble growth rate $\dot{V}_{mi,g}$ can be calculated from

$$\dot{V}_{mi,g} = \dot{V}_{mi,l} \frac{\rho_l}{\rho_g} = \frac{\rho_l}{\rho_g} \pi \int_0^{r_w} \frac{d\delta_{mi}(t,x)}{dt} x dx,$$
(6)

128

where $\dot{V}_{mi,l}$ is the evaporated liquid volume rate from the microlayer and r_w is the bubble base radius. In the thermal diffusion controlled period the shape of the bubble changes from hemispherical to truncate regular spherical and a liquid layer is formed underneath the bubble outside of the microlayer which is termed macrolayer [21] (Figure 2).

133 The thermal diffusion controlled growth, sometimes referred to as macrolayer evaporation, can be 134 calculated by the Labuntsov solution [6]

135

$$\left(\frac{dr_b}{dt}\right)_{ma} = \frac{1}{2}B_1 t^{-\frac{1}{2}},\tag{7}$$

136

137 where $B_1 = c_1 J a \alpha_l^{1/2}$ and $c_1 = \left(\frac{12}{\pi}\right)^{1/2} \left[1 + \frac{1}{2} \left(\frac{\pi}{6Ja}\right)^{2/3} + \frac{\pi}{6Ja}\right]^{1/2}$.

138 The bubble radius growth rate in the thermal diffusion controlled growth period is calculated as

139

$$\frac{dr_b}{dt} = \frac{V_{mi,g}}{A_b} + \left(\frac{dr_b}{dt}\right)_{ma} \left(1 - f_{sub}\right),\tag{8}$$

140

141 where A_b is the bubble surface area and f_{sub} is the portion of the bubble surface in contact with the 142 sub-cooled liquid. Eventually, condensation, that occurs when the bubble comes in contact with the 143 sub-cooled liquid, is also accounted for in this model. The bubble shrinkage rate is determined by the 144 heat balance between the latent heat of condensed steam and the condensation heat flux based on the

145 Ranz and Marshall correlation [15, 16, 22]. With Eq. (8) the bubble growth rate can be written as

146

$$\frac{dr_b}{dt} = \frac{\dot{V}_{mi,g}}{A_b} + \left(\frac{dr_b}{dt}\right)_{ma} \left(1 - f_{sub}\right) - \frac{k_l \left((2 + 0.6Re^{0.5} Pr^{0.3})(T_{sat} - T_{sub})\right)}{2r_b \rho_g h_{fg}} f_{sub}.$$
(9)

147

Superheat is required to activate the bubble on the wall. A liquid layer with the temperature between the superheated wall temperature T_{wall} and saturation temperature T_{sat} is considered as a superheated thermal layer with a thickness of $\delta_{th,sat}$. The condensation starts when the height of the bubble is larger than $\delta_{th,sat}$. In pool boiling, the temperature distribution in the thermal layer is simplified to a linear one, that is

$$\delta_{th,sat} = \frac{T_{wall} - T_{sat}}{T_{wall} - T_{sub}} \cdot \delta_{th}.$$
(10)

154

In pool boiling, the total thermal layer thickness is considered to be at equilibrium conditions giving $\delta_{th} = (T_{wall} - T_{bulk})/(k_l \dot{q}_{wall})$ [21].

157 During the thermal diffusion controlled growth period the microlayer extends with the expansion of the 158 bubble base and further supports the bubble growth. The newly formed part of the microlayer will be 159 distributed based on the thickness at the outer border of the original microlayer.

160 **2.2 Forces Acting on a Growing Bubble**

For a bubble growing on a superheated surface a force balance analysis has been elaborated based on the work of Klausner et al. [9], Thorncroft et al. [13] and Chen et al. [14]. Considering the conservation of momentum in the direction tangential (subscript x) and the perpendicular (subscript y) to the heating surface, the forces acting on the bubble are given as

165

$$F_{total,y} = F_{growth,y} + F_{drag,y} + F_{cp,y} + F_{sl,y} + F_{b,y} + F_{surf,y},$$
(11)

$$F_{total,x} = F_{growth,x} + F_{growth,b} + F_{drag,x} + F_{b,x} + F_{surf,x}.$$
(12)

166

 F_{growth} is the bubble growth force, $F_{growth,b}$ is the added mass force due to the bubble growth in the 167 bulk liquid field, F_{drag} is the quasi-steady drag force due to the viscous fluid flowing around the 168 bubble, F_{cp} is the contact pressure due to the effect of the wall, F_b is the buoyancy force, F_{sl} is the 169 lift force resulting from the asymmetrical flow distribution in the tangential direction of the wall, F_{surf} 170 is the surface tension force due to the interfacial contact with the wall. In the conventional force 171 balance model [9, 13, 14] for horizontal pool boiling the bubble departs or lifts off when the force 172 becomes balanced in the perpendicular direction of the wall. In horizontal pool boiling, only the forces 173 174 in the direction perpendicular to the wall will be considered.

176 2.2.1 Growth Force F_{growth}

In the study of Klausner et al. [9] a hemispherical bubble growing on a heating surface was considered.
According to the Rayleigh equation, the pressure on a growing bubble in pool boiling is given as

179

$$\rho_l \left(r_b \ddot{r_b} + \frac{3\dot{r_b}^2}{2} \right) = p_l(r_b) \,. \tag{13}$$

180

By integrating the pressure difference distribution around the bubble $p_l(r_b)$ the force due to the expansion of bubble can be calculated. Due to the symmetric growth in the tangential direction in horizontal pool boiling the growth force in the tangential direction is 0 and the one in perpendicular direction can be expressed as

185

$$F_{growth,y} = -\rho_l \pi r_w^2 (r_b \ddot{r_b} + \frac{3\dot{r_b}^2}{2}).$$
(14)

186

187 Here, r_w is the bubble base radius which equals the bubble radius r_b when the bubble is 188 hemispherical. Later, Chen et al. [14] extended this model to truncated spherical bubbles.

189 2.2.2 Drag Force F_{drag}

190 Due to the relative motion between bubble and liquid phase the quasi-steady drag force on the bubble 191 in the perpendicular direction can be derived as

192

$$F_{drag,y} = 1/2\rho_l v_b^2 \pi r_b^2 C_D,$$
(15)

193

194 where

195

$$v_b = \frac{dh_c}{dt},\tag{16}$$

196

197 is the velocity of the bubble in the wall perpendicular direction and

198

$$h_c = \sqrt{r_b^2 - r_w^2} + r_b \tag{17}$$

199

is the height of bubble without bottleneck. C_D is the drag force coefficient, which depends on turbulence intensity, bubble Reynolds number and bubble shape. Due to the pre-assumption of a spherical bubble shape, C_D is simplified with the correlation proposed by Moore [23] and Clift et al. [24] as

$$C_D = \frac{16}{Re_b} (1 + 0.15Re_b^{0.5}).$$
(18)

206 Chen [14] considered this formula as not only valid for small Re_b , but also for $Re_b > 50$.

207 2.2.3 Contact Force F_{cp} and Buoyancy F_b

As a part of the bubble contacts the liquid and another part the heating surface, the effect of the total pressure acting on the outward surface of the bubble F_{tp} [14] can be expressed as

$$F_{tp} = F_b + F_{cp} + F_h, (19)$$

211

where F_b , F_{cp} , F_h are the buoyancy force, contact pressure force and hydrodynamic force respectively.

For horizontal pool boiling the buoyancy is given as

215

$$F_{b,y} = (\rho_l - \rho_v) V_b g. \tag{20}$$

216

The contact pressure force, F_{cp} , is evaluated by the model of Thorncroft et al. [13], which only exists in the perpendicular direction of the heating surface and is given as

219

$$F_{cp} = \frac{1}{2} \pi d_w^2 \frac{\sigma}{r_c}.$$
 (21)

220

Here, r_c is the radius of curvature at the points on the out border of bubble base (defined as $r_c = 5 \times r_b$ by Klausner et al. [9]) and σ is the surface tension. According to the study of Thorncroft et al. [13], the hydraulic dynamic force F_h includes the quasi-steady drag force, the shear lift force F_{sl} and the added mass force. In horizontal pool boiling, only the quasi-steady drag force is involved.

225

226 2.2.4 Surface Tension Force F_{surf}

At the interface between two materials, physical properties change rapidly over distances comparable to the molecular separation scale. Formally, surface tension is defined as the force per unit of length that acts orthogonally to an imaginary line drawn on the interface. For asymmetric bubbles contacting the heating wall the surface tension force in the tangential direction of the heating surface has been derived by Klausner et al. [9] as

232

$$F_{surf,y} = -2 * r_w * \sigma \frac{\pi}{\beta_{ad} - \beta_{re}} (\cos(\beta_{ad}) - \cos(\beta_{re})), \qquad (22)$$

- where r_w is the contact radius and β_{ad} and β_{re} are the advancing and receding angle of macrolayer. In the model the surface tension is dependent on the base diameter.
- 236 Zhao [21] investigated symmetric bubble growth in horizontal pool boiling where the advancing and 237 receding angles are equal. They considered the formation of dryout during the bubble growth. In their
- model the surface tension only exists in the perpendicular direction and is dependent on dryout radius, which is given as

$$F_{surf,y} = 2 * \pi r_d \sigma \sin(\theta). \tag{23}$$

Here, θ is the contact angle of the microlayer to the wall. Because the microlayer evaporation depletion and dryout formation is also considered in the present model, the surface tension will depend on the dryout radius as well.

243 2.3 Contact Angle β and Bottleneck h_{bt}

244 2.3.1 Contact Angle

The contact angle plays an important role in the calculation of the forces on the bubble. However measurements and reliable models for the contact angle are rather scarce in previous studies. Klausner et al. [9] recommended $\beta_{ad} = \pi/4$ and $\beta_{re} = \pi/5$ from their measurements in R113 for flow boiling. As described and found by Mukherjee [25], the contact angle does vary during the ebullition cycle, as it is only dependent on the liquid and vapor properties and the material of the solid surface.

250 In this paper, we introduce a scheme to calculate the dynamic contact angle based on the analysis of 251 forces. In horizontal pool boiling, when the bubble is in the inertia controlled period, the bubble is considered hemispherical when the contact angle is $\frac{\pi}{2}$. The surface tension, which keeps the bubble on 252 the wall, is equal to 0 in this period because the dryout radius r_d is 0. However the fast expansion of 253 254 the bubble prevents the bubble from departure. Further the dryout radius r_d increases when the sum of 255 the negative forces which point toward the wall (mainly surface tension force) is much higher than the 256 one of the positive forces (Figure 3). This negative total force will lead to a deformation of the bubble to reach the force balance in short time. In other words, the negative total force will drive the bubble to 257 258 form a curvature and a contact angle to reduce the surface tension force in the negative direction until 259 the forces on the bubble are balanced. The contact angle at which the force is again balanced is referred 260 to as expected contact angle (β_s). From the force calculation this expected contact angle can be derived 261 as

262

$$\beta_s = 2 * \operatorname{asin}(\frac{F_{growth,y} + F_{drag,y} + F_{cp,y} + F_{sl,y} + F_{b,y}}{F_{surf}}).$$
(24)



265 Figure 3: Bubble with dynamic contact angle β and expected contact angle β_s in pool boiling.

266 The constant 2 in Eq. (24) means that the contact angle β is two times of the microlayer contact angle 267 θ , which is used to calculate the surface tension force in this work. β_s is continuously changing due to 268 the change of forces during the bubble growth.

269 Further, β can be calculated with the base radius and the bubble radius as

270

$$\beta(t) = \arcsin(\frac{r_w(t)}{r_b(t)}).$$
(25)

271

It decreases from an initial value $\beta(0) = \frac{\pi}{2}$ towards the expected value β_s in some finite time interval. Due to the force balance and the increase of the positive forces in the wall perpendicular direction (i.e. buoyancy in horizontal pool boiling), β_s keeps increasing during bubble growth and consequently β will following this increase. If the force becomes positive during this time period, the bubble will start to depart and form a bottleneck.

277 2.3.2 Bottleneck

As stated by many researchers [4, 10-14] sphericity is considered as an important case dependent parameter, which needs recalibration to improve the accuracy of the model. In order to reduce the case dependency, the consideration of the bubble deformation during the bubble growth is required. In our model, the shape of bubble is first hemispherical in the inertia controlled growth period. Then it gradually changes from hemispherical to spherical during the thermal diffusion controlled period. Later it becomes a sphere plus a bottleneck according to the force balance. Finally it turns into a perfect sphere after lift-off.

In the bottleneck phase the bubble's main body starts departing but as the evaporation of microlayer still produces enough vapor the main body remains connected to the wall. The base diameter of the bubble starts to shrink when the evaporation of microlayer is less than required to form a new bottleneck. Unlike in the conventional force analysis model the bubble departure or lift-off criterion is that the bottleneck breaks up or the base diameter shrinks to 0. The bottleneck formation process is shown in the Figure 4.



Figure 4: Formation of a bottleneck after the moment when force balance is reached and before bubble
 departure.

The contact angle of the bottleneck should depend on the wettability of the heater surface. Usually the contact angle of the bottleneck is considered as 90° which is larger than that during bubble growth. Therefore the total force becomes negative again during the bottleneck formation.

297 The base radius r_w will shrink when the $\dot{V}_{mig} < v_b \pi r_w^2$ due to volume conservation, that is

$$\frac{d(\pi r_w^2 h_{bt})}{dt} = \dot{V}_{mig} - v_b \pi r_w^2,$$
(26)

where h_{bt} is the height of bottleneck. The bottleneck height h_{bt} can be calculated from the bubble velocity and the time difference from the moment when the force becomes positive (t_{fp}) to the time and point t according to

$$h_{bt} = v_b (t - t_{fp}).$$
 (27)

When the microlayer is completely consumed or the pressure difference along the bottleneck reaches a limit, the bottleneck will break. From the Young-Laplace equation the pressure inside the bubble is given as

$$p = p_0 - \sigma \left(\frac{1}{R_1} + \frac{1}{R_2}\right).$$
(28)

Considering the bubble geometry in reality, the pressure at the bubble center point A and base point B (Figure 4) can be approximated as

306

291

$$p_A = p_0 - \sigma(\frac{1}{r_b} + \frac{1}{r_b}) \text{ and } p_B = p_0 - \sigma(\frac{1}{r_w} + \frac{1}{r_\infty}).$$
 (29)

307

308 Further it can be considered that the pressure at point B must be balanced with that at point A 309 following

$$p_B' = p_A + \frac{1}{2}\rho_g v_p^2 + \rho_g gh.$$
(30)

However due to the force acting on the bubble, p_B' differs from p_B when p_B is strongly dependent on the base radius r_w . With the shrinking of r_w , p_B decreases. The difference $\Delta p_{B'B} = p_B' - p_B$ increases according to

$$\Delta p_{B'B} = \frac{1}{2} \rho_g v_p^2 + \rho_g g h + \sigma \left(\frac{1}{r_w} + \frac{1}{r_\infty} - \frac{2}{r_b} \right). \tag{31}$$

313 When $\Delta p_{B'B}$ is larger than the total force in perpendicular direction acting on the base radius, that is,

$$\Delta p_{B'B} \ge \frac{\left|F_{total,n}\right|}{A_{base}},\tag{32}$$

- the bottleneck will break up and the bubble will depart from the wall. Of course, if the base radius
- shrinks to 0 earlier, the bubble will also depart. The complete bubble growth and departure model for
- 316 horizontal pool boiling is described in following scheme (Figure 4).



317

318 *Figure 5: Scheme of the model including the sub-models for bubble growth and forces.*

319 2.4 Base Diameter and Initial Microlayer Thickness

320 Also the base diameter is a key parameter which plays an important role in the force balance analysis. 321 The deformation of the bubble causes the expansion of the base radius r_w with another rate than the growth of the bubble radius r_b . In Klausner's work, the authors considered $d_w = 2 * r_w$ as a constant 322 of 0.09 mm. Later Thorncroft [13] adopted $d_w = 2r_b \sin(\beta)$ in order to improve the modelling 323 accuracy. A constant ratio with bubble diameter $d_w = \frac{2r_b}{15}$ was used by Yun et al. [10]. In this work 324 we prefer to consider the relationship between the expansion rate of base radius $\vec{r_w}$ and that of the 325 bubble $\dot{r_b}$ instead of absolute values r_w and r_b (as in Thorncroft et al. [13]) in order to account for a 326 smooth growth of bubble. Our approach is based on Thorncroft's work and so we express the 327 328 expansion rate of r_w as

329

$$\dot{r_w} = \dot{r_b}\sin(\frac{\pi}{2} - \beta). \tag{33}$$

330

331 The initial microlayer thickness is defined as

$$\delta_{mi}^{0}(\mathbf{x}) = C_{mi}\sqrt{\nu_{l}\cdot t} = \sqrt{C\alpha_{l}\cdot \tau_{g}}, \qquad 0 \le t \le t_{g}$$
(34)

333

where the constants $C_{mi} = 0.8$ and $C = C_{mi}^2 Pr = 0.64 \cdot Pr$ were defined in Cooper's original paper [7], Pr is Prandtl number v_l the kinematic viscosity of liquid, τ_g the microlayer formed time at position r in the bubble base and t_g the maximal inertia controlled growth time. Cooper et al. also pointed out that C has a range between $(0.09 \sim 1.0) \cdot Pr$ according to different experiments [7]. The microlayer thickness as a function of distance to the nucleation site is given as [21]

339

$$\delta_{mi}^0(x) = \frac{C\alpha_l \rho_g h_{fg} x}{2k_l \Delta T_{sat}}.$$
(35)

340

In earlier investigations [18] we found that C is a function of surface roughness and surface profile. Another more recent experimental correlation from Utaka et al. [26] for water boiling from a quartz glass surface (smooth) at atmospheric pressure is also considered, giving

344

$$\delta_{mi}^0(x) = 4.46e^{-3} * x. \tag{36}$$

345

However this correlation is valid only for water. From DNS calculations of Sato et al. [27] it was that *C*, as derived from Utaka's case, matches Duan's data for $\Delta T_{sat} = 9 K$. In this work, we adapted Utaka's experimental data to Cooper's correlation resulting in $C = 0.0755 \cdot Pr$.

349 2.5 Heat Flux

350 2.5.1 Heat Flux Transfer from Wall to Liquid

The heat flux from the wall to liquid phase in the nucleate boiling process is divided into several terms: evaporation of microlayer $\dot{Q}_{e,mi}$, evaporation of macrolayer $\dot{Q}_{e,ma}$, heat transfer from wall to gas in the dryout \dot{Q}_{dryout} , quenching \dot{Q}_q and single phase convection (wall to liquid) $\dot{Q}_{n,c}$, which are given as

$$\dot{Q}_{out} = \begin{cases} \dot{Q}_{e,mi} = \dot{m}_{mi}h_{fg} = \frac{k_l\Delta T_{sat}}{\delta_{mi}} & r_w > x > r_d \\ \dot{Q}_{e,ma} = \dot{m}_{ma}h_{fg} = \frac{k_l\Delta T_{sat}}{\delta_{ma}} & r_b > x > r_w \\ \dot{Q}_{dryout} = \frac{k_g\Delta T_{sat}}{\sqrt{\pi\alpha_g\tau_d}} & r_d > x \\ \dot{Q}_q = \frac{k_l\Delta T_{sat}}{\sqrt{\pi\alpha_l\tau_q}} & t > t_d (unif.T_{wall}) \text{ or} \\ \dot{Q}_q = \frac{k_l\Delta T_{sat}\sqrt{\pi}}{2\sqrt{\alpha_l\tau_q}} & t > t_d (unif.\dot{Q}_{in}) \\ \dot{Q}_{n,c} = h_c(T_w - T_b) & flow boiling & x > r_b . \end{cases}$$

$$(37)$$

 δ_{ma} is the distance between the interface to the wall in the wall perpendicular direction.

Quenching means the rewetting of the bulk liquid on the wall between the bubble departure and nextactivation. The formula is from Zhao's work [21].

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359 2.5.2 Heat Transfer in the Wall

In the previous analyses the impact of wall thickness or wall material on the boiling heat transfer was usually not considered. However, as the wall can be a thermal buffer system with a high thermal conductivity it can impact the hot spot (dryout) underneath the bubble. In our model, the heat flux transferred in the wall tangential direction is considered and calculated. The heat flux in the wall tangential direction is given as

$$\dot{Q}_{t,w} = k_w \Delta T_{w,t} / \Delta L_w \,, \tag{38}$$

365 while the total heat flux through the wall is given as

$$\dot{Q}_{total} = \dot{Q}_{t,w} + \dot{Q}_{out} + \dot{Q}_{in}.$$
(39)

366 Considering energy conservation it follows, that

$$\frac{dT_w}{dt} = \dot{Q}_{total} / (c_{pw} \rho_w \delta_w). \tag{40}$$



368 Figure 6 Scheme of the heat transfer along the wall underneath the bubble.

369 3. Results and Discussion

370 3.1 Experimental Database

371 In 2013, Duan et al. [19] used infrared thermometry and high speed video camera observation to 372 investigate the bubble nucleation and heat transfer during pool boiling of water. Using a transparent 373 indium-tin-oxid (ITO) heater (0.7 μ m thick) on a Sapphire substrate (250 μ m thick), it allowed the 374 author to measure the temperature distribution, bubble contact diameter and other parameters from the bottom of the heater. Two cases were studied in Duan's experiment: case 1 is $T_{sup} = 9 \pm 2^{\circ}C$, 375 $\dot{Q} = 28.7 \pm 0.6 \ kw/m^2$ under 1 bar and case 2 is $T_{sup} = 7.5 \pm 2^{\circ}C$, $\dot{Q} = 36 \pm 0.7 \ kw/m^2$ under 1 376 bar. Each experiment was repeated several times. The contact angle of water with the ITO wall surface 377 (wettability) is $\frac{\pi}{2}$ and was obtained in experiments with the same facility performed by Gerardi et al. 378 in 2009 [28]. 379

Recently, Sato and Niceno [20] developed a new direct numerical simulation model based on Color Functions. In their model they simulated the dry spot underneath the bubble and determined the bubble growth rate, shape change and the temperature distribution on the heater surface, which were in good agreement with experimental data. The disadvantage of a DNS simulation is that the simulation domain is strictly limited to the millimeter to centimeter range for reasons of limited computational power. Hence for large scale simulations (~ dm or m) simplified sub-models, as the one presented here are still required.

The simulation results from our sublayer model were compared with Duan's experiments and further with Sato's DNS. Moreover, the temperature distribution around the cavity and frequency have been analysed to compare modelling and experiments for Duan's case too. In the calculation, the bubble growth model is considered as a one dimension model which requires a time discretization. The microlayer and heat transfer on the wall is considered as a two dimension model which requires a tangential direction spatial discretization. The size of the wall in the model taken from Duan's case is 0.25 mm x 5 mm.

394 3.2 Discretization Dependency Study

The sub-model requires a time discretization for bubble dynamics and space discretization for the microlayer and the heat transfer inside the wall tangential direction. Both time and space are all discretized using a central differences scheme. The CFL number is controlled to be less than 1. Nine cases with temporal step length from 1 μ s to 30 μ s and spatial step length from 10 μ m to 50 μ m were tested. The simulation case is pool boiling at 1 bar with water. The results for bubble lift-off diameter for different discretization sizes are shown in the following.



402 Figure 7: Calculated bubble lift-off diameter for different space and time discretization

403 The deviation from the average value for all 9 cases is less than +1.47% and -1.60%. When the spatial 404 step length is less than 50 µm and temporal step length is less than 30 µs the model converges well.

405 **3.3** Comparison of the Model with Experiment, DNS in Pool Boiling Case

406 As mentioned, the geometry change is tracked in our model. Figure 8 shows the geometry of the 407 bubble from activation to lift-off (departure) from the wall. The first row of the images is taken from 408 Duan et al. [19] (experiment). The second row is the DNS calculation at the same conditions (Sato et 409 al. [27]). The third row is from our model. With our model, the bubble shape is hemispherical at activation t = 0 ms, then changes from hemispherical to spherical during growth until t = 6.9 ms, and 410 further changes to a truncated sphere plus bottleneck as a balloon at t = 12 ms (experiment at t \approx 13.2 411 412 ms). Of course the experiment and DNS calculation do not result in perfect hemispheres or spheres, but 413 qualitatively the bubble shape agrees still well among the three cases. Overall, our model reproduces 414 the bubble dynamic geometry during the bubble growth. As a qualitative comparison is not enough for 415 the validation, a further quantitative comparison is given in Figure 9.

	Time [ms]	0 (Bubble nucleation)	0.7	2.8	6.9	13.2
Experiment (Duan 2013)	HSV images					
DNS calculation (Sato 2015)		0.000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.0000 0.00000 0.0000 0.0000 0.0000 0.0000 0.00000 0.0000 0.0000				
Present model					0	~ 12 ms

417 Figure 8: Geometry of the bubble at different growth period from experiments of Duan et al. [19], DNS

418 calculations from Sato [27] and calculation with our model under the same conditions.



422 Figure 9: Bubble dynamics from a) three bubbles under same condition in Duan et al.'s experiments 423 [19], b) Sato et al.'s DNS calculations [27] and c) our model under the same conditions. d_w is the 424 base diameter, d_1 is the lateral diameter, h_b is the bubble height and d_d is the dryout diameter.

425 The bubble departure time in the experiment and DNS calculation is around 15 ms, while that in the

426 present calculation is around 13.3 ms. The maximal lateral bubble diameter in the experiment is around

427 3.9 mm and for DNS around 3.5 mm. The lateral diameter at the departure moment is around 3.6 mm

428 and 3.4 mm in experiment and DNS respectively. The none-perfectly spherical geometry of the bubble

429 in the experiment and DNS causes the obtained lateral diameter of bubble to differ from the equivalent

430 one. The equivalent bubble departure diameter is 3.8 ± 0.08 mm in the experiment. Due to the perfect

431 hemispherical, spherical and sphere plus bottleneck setup in our model, the maximal lateral diameter

and the diameter at departure are 3.2 mm in all cases. The difference between the departure diameterpredicted by our model, the one of the experiment and the one of the DNS is only 16% and 6%.

434 As mentioned above, our model considers the microlayer which contributes to bubble growth and the

formation of dryout area underneath the bubble. The dryout area can be measured or observed from the

436 temperature distribution on the wall. Duan et al. measured the temperature distribution under the

437 bubble on the wall with an IR camera through the ITO heater and Sapphire substrate (Figure 10).



438

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Figure 10: Temperature distribution underneath bubble on the wall measured with IR camera by Duan
et al. [19].

441 Duan et al. measured the temperature distribution in a radius of 2.5 mm from bubble activation (t = 0) 442 to complete bubble departure from the wall (t = 15 ms) until the bubble was far away from the wall (t = 15 ms) until the bubble was far away from the wall (t = 15 ms) until the bubble was far away from the wall (t = 15 ms) until the bubble was far away from the wall (t = 15 ms) until the bubble was far away from the wall (t = 15 ms) until the bubble was far away from the wall (t = 15 ms) until the bubble was far away from the wall (t = 15 ms) where the the bubble was far away from the wall (t = 15 ms) where the the bubble was far away from the wall (t = 15 ms) where the the bubble was far away from the wall (t = 15 ms) where the the bubble was far away from the wall (t = 15 ms) where the the bubble was far away from the wall (t = 15 ms) where the bubble was far away from the wal 117.44 ms) (Figure 11a). When the microlayer underneath the bubble is completely evaporated, the 443 dryout area will form, which has very low heat transfer coefficient because the gas directly contacts the 444 wall and there is no evaporative heat transfer any more. The temperature in the dryout area then 445 accordingly increases. This high temperature was observed by Duan from t = 2.5 ms until t = 8.75 ms. 446 447 The dryout area is rewetted again after bubble departure at t = 15 ms. Then the wall is also again reheated until the nucleate site gets back to activation temperature, which is 109°C in this case. The 448 449 position (r) of the lowest temperature values along the surface indicates the radius of base underneath the bubble from t = 2.5 ms to t = 8.75 ms. 450





453 *Figure 11: Temperature distribution on the wall at different times during the bubble growth: a)* 454 *experiment from Duan et al. [19], b) DNS from Sato et al. [27] c) our model.*

As shown in Figure 11 b), Sato et al. also analyzed the temperature distribution around the cavity. However, he found the dryout arises after a very short time (t = 0.4 ms) following activation. The temperature distribution between t = 0.4 and t = 8.8 ms has a much sharper turning point at the edge of the bubble base than that in the experiment. The reason may be that the sapphire substrate blurs the resolution of temperature profile, while the DNS calculation and our model calculation give the temperature on the wall surface directly. Nonetheless, our model still has a good agreement with experimental results and DNS in the temperature distribution profile.

	Exp (case 1)	Model	Error (Abs(Model-Exp)/Exp)
Bubble growth time	15 ms	13 ms	13%
Waiting time	200 ms	221 ms	10%
	Exp (case 2)	Model	
Bubble growth time	16 ms	16 ms	0
Waiting time	52 ms	83 ms	59%

462 Table 2: Comparison between model prediction and experimental data of Duan [19]

The comparison between the experimentally measured bubble growth time and waiting time and modelled value is shown in Table 2. From the experiment it is found that for case 1 there is a bubble growth time of 15 ms and a waiting time of 200 ms. While it is 16 ms and 52 ms in case 2. The calculated bubble growth time is 13 ms and waiting time is 221 ms in case 1. The growth time is 16 ms and waiting time is 83 ms in case 2.



Figure 12: Temperature history of the nucleation site a) Duan's experiment case 1; b) Model
calculation under conditions of case 1; c) Duan's experiment in case 2; d) Model calculation under
conditions of case 2.

The fast and abrupt decrease and increase of the temperature at the nucleation site (insert in Figure 12 b) is related to the temperature change at x = 0 in Figure 11. The difference between our model calculation and experiment is in the range of ~ 13% ((Model-Exp)/Exp*100%) for growth time, ~10% for waiting time in case 1; and ~ 0% for growth time, ~59% for waiting time in case 2.

477 3.4 Comparison of Different Approaches for Contact Angle and Base Diameter

In order to analyse the efficacy of the consideration of dynamic contact angle and base expansion inour model, we analysed five different modelling scenarios:

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- 484 3. A constant contact angle and a base diameter expansion following Thorncroft et al. [13];
- 485 4. A dynamic contact angle and a base diameter expansion following Yun's work [10] and
- 486 5. A dynamic contact angle and a base diameter expansion following our model.
- 487

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The five scenarios and their main parameters are further summarized in the Table 3. In the constant base diameter cases, the maximal inertia controlled bubble radius $(r_{m,g})$ is set to 0.09 mm. Having reached this value the bubble geometry changes from hemispherical to truncated spherical. Table 3: Overview of the model variations used to clarify the different approaches for base diameter
 expansion and contact angle



494 Figure 13: Base (d_w) and lateral diameter (d_l) calculated with different bubble base expansion rules 495 and constant or dynamic contact angle

From the comparison of the conventional setups from the former investigations, it can be found that our model (case 5) has a better agreement to the Duan's experiment (Figure 13) among the investigated mechanistic models. However, the present model still underestimated the base diameter and bubble growth speed. This deviation may be caused by the regular spherical setup of bubble's main body in the model while the bubble is not a perfect spherical in the experiment and DNS.

501 In case 1 and case 2 the microlayer contributes much less to the bubble growth than other three cases, 502 because the base diameter is only 0.09 mm, which is much lower than that of Thorncroft et al. [13] and 503 our model. Even the departure time is longer but the bubble size is much smaller than for cases 3 and 5. 504 Compared to cases 1 and 2, the base diameter of case 4 is even smaller which leads to the shorter 505 departure time and smaller bubble departure diameter.

506 From the departure criterion in Klausner's work [9], the bubble will depart when the forces are 507 balanced in the wall perpendicular direction for horizontal pool boiling, as shown in case 3. Due to the 508 negligence of the geometry change the bubble departs much earlier than in case 5. The bubble lateral 509 diameter in case 3 is only 75% of the one in case 5 (Figure 13).

510 **3.5** Contribution of Microlayer, Macrolayer and Condensation to the Bubble Growth

511 The contribution of the microlayer to the bubble growth will be discussed here.



513 Figure 14: Contribution of the microlayer, macrolayer and condensation to the bubble growth (bubble 514 diameter) during the bubble growing transient in saturate pool boiling under conditions of Duan's 515 case 1.

516 When the pool boiling is saturated there is no condensation anymore. In the inertia controlled period, 517 the microlayer evaporation is then the only contribution to the bubble growth. Later, during the thermal 518 controlled growth period, the macrolayer contributes more and more from 0 to 56% to the bubble 519 diameter at t = 5.4 ms and gets the dominant share to growth contribution especially after t = 5.4 ms 520 when the microlayer is completely dried out (Figure 14a). When the bubble departs at t = 13.3 ms, the 521 macrolayer contributes to 68% of the total bubble diameter. This contribution of the microlayer is 522 around 32%, which is similar to the value of 30% from experimental results of Chu [29] but smaller 523 than the 55% calculated by DNS in Sato's work [27]. As the initial microlayer thickness (Eq. (35)) is inversely proportional to the wall superheat, the total contribution from the microlayer becomes less 524 525 when the wall superheat is higher. This agrees qualitatively with the experimental data of Jung et al. [30], where contribution is 17% for 20 K superheat. 526

527 With a multitude of calculations for different experiments from Duan et al. [19], Klausner et al. [9], 528 Situ et al. [11] and Sugure et al. [12], in the proposed model, the microlayer contact angle θ in Eq. 529 (23) is suggested as half of contact angle of the macrolayer β (Figure 2) when the dryout radius r_d is 530 smaller than the contact based radius r_w . When r_d increases to r_w , θ will be equal to β . The r_{∞} 531 applied in Eq. (31) is suggested to be equal to r_w .

532 **4.** Conclusions

533 A mechanistic model of bubble behavior during boiling has been developed for both pool boiling 534 and flow boiling. The application of the model for the horizontal pool boiling case was introduced in 535 this work. The model includes several well developed conventional theories and sub-models with or 536 without modification and some new concepts. It covers the whole bubble life cycle including inertia controlled, thermal diffusion controlled and departure periods. The microlayer, which forms during the 537 538 inertia controlled growth period and the bubble base expansion, contributes to the bubble growth in this 539 model. The force balance equations based on Klausner et al., Throncroft et al. and Chen et al. were 540 applied to determine the departure of the bubble. The consideration of dynamic contact angle and dynamic bubble base expansion further allows the model to track microlayer formation, evaporation 541

and depletion process during bubble growth. It also allows tracking the bubble geometry change fromhemisphere to truncated sphere and further to sphere plus bottleneck continuously.

544 The calculated bubble dynamics such as growth dimensions at different time, departure diameter, 545 base diameter, dryout diameter, growth and waiting time are in good agreement with the available 546 experimental data. It shows the high accuracy of the integral model of bubble growth in our approach. 547 Moreover, the good agreement of the calculated temperature distribution along the heating wall with 548 the experimentally measured data shows the correctness of our microlayer model. The microlayer 549 model is strongly impacted by the dynamic contact angle and base expansion. The good agreement also 550 verifies these two ideas. Later, these ideas described in this work will be applied to calculate the bubble 551 dynamics in the flow boiling covering different conditions.

From our model it is found that only the force balance is not enough to predict the bubble departure in the horizontal pool boiling. The delay of the bubble departure due to the bubble deformation during the bubble growth (bottleneck) after force balance should be taken into account as well.

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559 Nomenclature

561	A_b	bubble surface area
562	A _{ma}	area of macrolayer
563	С	constant from Cooper
564	c _D	friction drag coefficient
565	c_{pl}	specific heat capacity of liquid
566	c_{pw}	specific heat capacity of wall
567	dl	bubble lateral diameter
568	d_w	bubble base diameter
569	$F_{b,v,y}$	buoyancy in wall perpendicular direction
570	$F_{cp,y}$	contact pressure force in wall perpendicular direction
571	F _{drag,y}	drag force in wall perpendicular direction
572	F _{growth,b}	growth force in bulk
573	F _{growth,y}	growth force in wall perpendicular direction
574	F _{sl,y}	sliding lift force in wall perpendicular direction (flow boiling)
575	F _{surf,y}	surface tension in wall perpendicular direction
576	F _{total,x}	total force in wall tangential direction
577	$F_{b,x}$	buoyancy in wall tangential direction

578	$F_{drag,x}$	drag force in wall tangential direction
579	$F_{growth,x}$	growth force in wall tangential direction
580	$F_{surf,x}$	surface tension in wall tangential direction
581	F _{sl,x}	sliding lift force in wall tangential direction
582	f _{sub}	the portion of the bubble surface in contact with sub cooled liquid
583	h_b	height of bubble top to the wall
584	h _{bt}	height of bottleneck
585	h_c	height of bubble center to the wall
586	h_{fg}	latent heat
587	k _l	thermal conductivity of fluid in liquid phase
588	k_g	thermal conductivity of fluid in gas phase
589	k_w	thermal conductivity of wall
590	\dot{m}_{ma}	mass flow of evaporated liquid in macrolayer
591	\dot{m}_{mi}	mass flow of evaporated liquid in microlayer
592	P_l	pressure difference on the bubble interface
593	P_r	Prandtl number
594	\dot{Q}_{in}	heat flux entering into wall
595	\dot{Q}_{out}	total heat flux from wall to fluid
596	$\dot{Q}_{e,mi}$	heat flux due to evaporation of microlayer
597	$\dot{Q}_{e,ma}$	heat flux due to evaporation of macrolayer
598	\dot{Q}_{dryout}	heat flux due to dryout
599	\dot{Q}_q	heat flux due to quenching
600	\dot{Q}_g	heat flux due to gas film (hotspot)
601	$\dot{Q}_{n,c}$	heat flux due to natural convection
602	$\dot{Q}_{total,w}$	total heat flux of a wall segment
603	$\dot{Q}_{n,w}$	conduction heat flux between neighboring wall segments
604	r	r coordinate/position
605	r_b	bubble radius
606	r_d	bubble dryout radius
607	$r_{m,g}$	maximum radius in initial growth regime
608	r_w	bubble contact radius (base radius)
609	Re_b	Reynold's number of bubble

610	T_b	bulk temperature
611	T_w	wall temperature
612	T_{∞}	temperature in the bubble in the inertia controlled growth regime
613	T _{sat}	saturation temperature
614	T _{sub}	subcooling temperature
615	t	time
616	t_d	time of departure
617	t_g	maximal inertia controlled growth time
618	$ au_g$	maximal inertia controlled growth time at different r position
619	$ au_d$	time counted from dryout starting
620	$ au_q$	time counted from quenching starting
621	v_b	bubble velocity in wall perpendicular direction
622	V_b	volume of bubble
623	$\dot{V}_{mi,g}$	total volume of formed gas
624	$\dot{V}_{mi,l}$	total volume of evaporated liquid
625	ΔL_w	distance between two neighboring wall segments
626	ΔT_w	temperature difference between two neighboring wall segments
627	ΔT_{sat}	super heating
628	ΔT_{sub}	subcooling
629	α_l	thermal diffusivity of fluid in liquid phase
630	$lpha_g$	thermal diffusivity of gas in liquid phase
631	β	contact angle of macrolayer in horizontal pool boiling
632	β_{ad}	advancing contact angle of macrolayer in flow boiling
633	β_{re}	receding contact angle of macrolayer in flow boiling
634	β _s	expected contact angle
635	θ	contact angle of microlayer
636	$ heta_w$	wall orientation angle
637	σ	surface tension
638	$ ho_g$	density of vapor
639	$ ho_l$	density of vapor
640	$ ho_w$	density of wall
641	δ^0_{mi}	initial microlayer thickness at time t_g
642	δ_{mi}	microlayer thickness

643	δ_w	wall thickness			
644	δ_{th}	thickness of thermal layer			
645	Subscript:				
646	dryout	at dryout area			
647	e	evaporation			
648	g	gas phase			
649	1	liquid phase			
650	mi	microlayer			
651	ma	macrolayer			
652	n,c	natural convection			
653	W	wall			
654	У	wall perpendicular direction			
655	Х	wall tangential direction			
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