

# Atomistic simulations on the mobility of di- and tri-interstitials in Si

related publications (since 2001):

Posselt, M., Gao, F., Zwicker, D.,  
*Atomistic study of the migration of di- and tri-interstitials in silicon,*  
**Phys. Rev. B 71 (2005) 245202**

Posselt, M., Gao, F., Zwicker, D.,  
*Migration of di- and tri-interstitials in silicon,*  
**Nucl. Instr. Meth. B 228 (2005) 212**



# methods to determine diffusion coefficients

## self-diffusion coefficient per defect $D_s$

sum of the squared displacements of all atoms vs. time

$$ssd_a(t) = \sum_{i=1}^N (\mathbf{r}_i(t) - \mathbf{r}_i(0))^2 = \text{const.} + 6D_s t$$

$D_s$ : mobility of the lattice atoms due to the presence of the defect

## defect diffusivity $D_d$

is obtained by monitoring the trajectory of the center-of-mass of the defect using the Wigner-Seitz-cell analysis

trajectory is decomposed into  $n_s$  segments

for each segment m the squared displacement is calculated

$$sd_d(m) = (\mathbf{R}(t_m) - \mathbf{R}(t_{m-1}))^2,$$
$$t_m = t_{m-1} + \Delta t$$

## (tracer) correlation factor

$$f = \frac{D_s}{D_d}$$



# di-interstitial

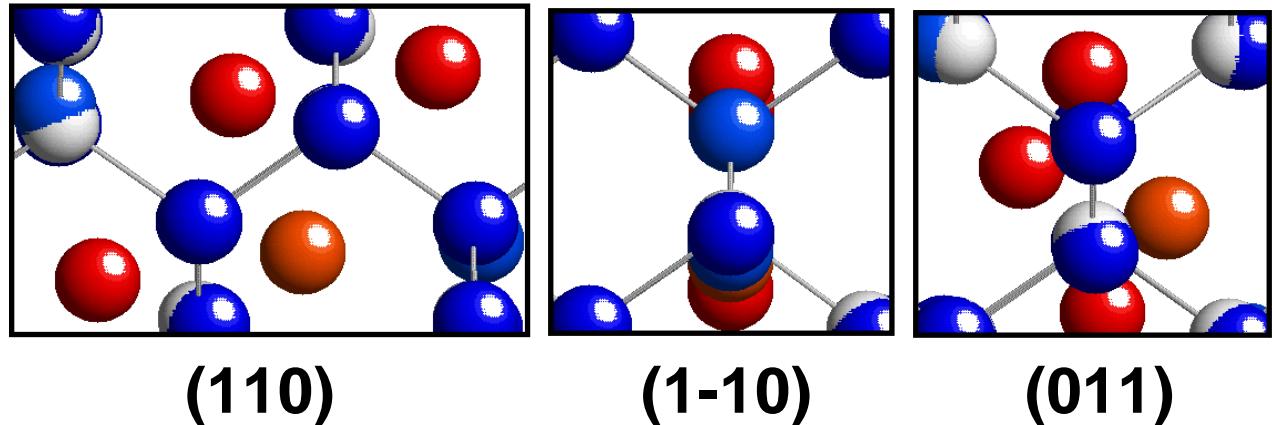
## structure and energetics

$I_2^A$

“Z structure” ( $C_{2h}$ )

$E_f = 6.10 \text{ eV}$

$E_b = 1.74 \text{ eV}$



**CP:** Gilmer 1995 (SW): 5.70 eV; Marques 2001 (T3): 6.32 eV

**TB:** Rasband 1996: 8.0 eV; Hane 2000: 5.85 eV

**DFT:** Richie 2004: 6.46 eV



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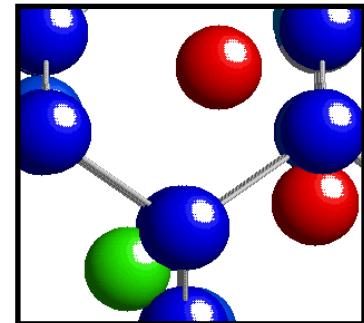
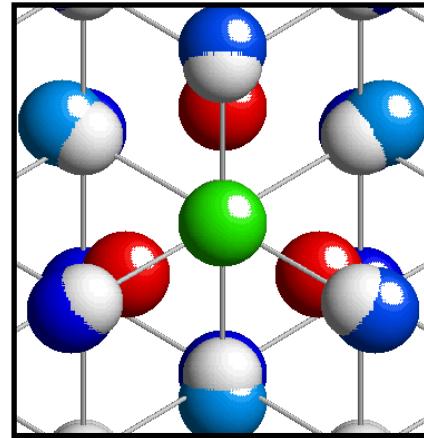
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$I_2^B$

"modified triangle in  $\{111\}$ " ( $C_{1h}$ )

$$E_f = 6.14 \text{ eV}$$
$$E_b = 1.70 \text{ eV}$$



(1-10)

**DFT:** Richie 2004: 6.46 eV

(111)

similar configuration (found by TB and DFT): "triangle in  $\{111\}$ " ( $C_{1h}$ )

**TB:** Rasband 1996: 7.3 eV; Hane 2000: 5.64 eV; Bongiorno 2000: 4.91 eV

**DFT:** Kim 1999: 4.9-6.0 eV; Jones 2002: 5.19 eV; Chichkine 2002: 4.84-4.96 eV;

Richie 2004: 5.66 eV; Lopez 2004: 5.76-5.84 eV



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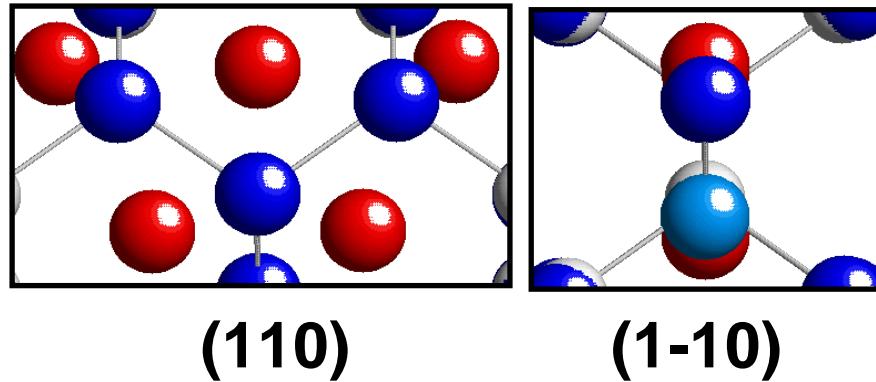
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$I_2^C$

“W structure” ( $C_{2v}$ )

$E_f = 6.37 \text{ eV}$

$E_b = 1.47 \text{ eV}$



**TB:** Rasband 1996: 7.7 eV; Hane 2000: 6.07 eV



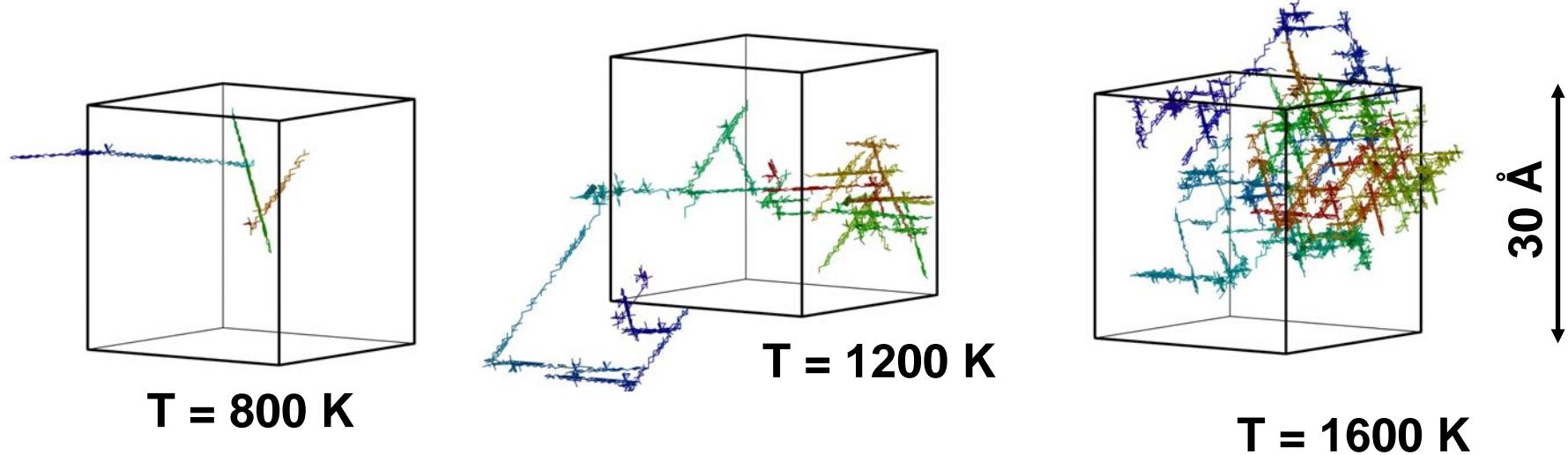
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## *migration*

**center of mass trajectories over a period of 4.4 ns**



*temperature dependent migration mechanism*

**low T – high mobility along <110> axes, change between equivalent directions occurs seldom and requires a long time**

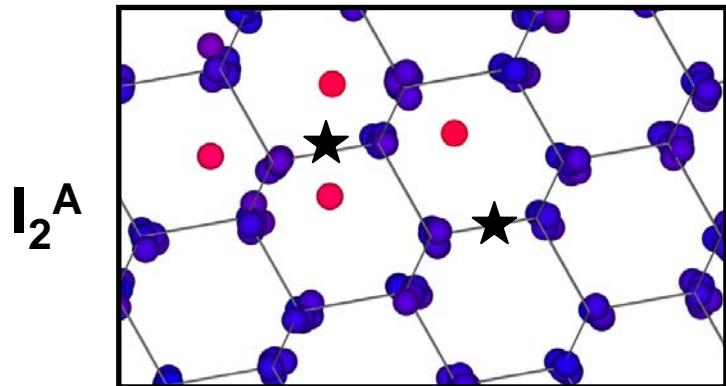
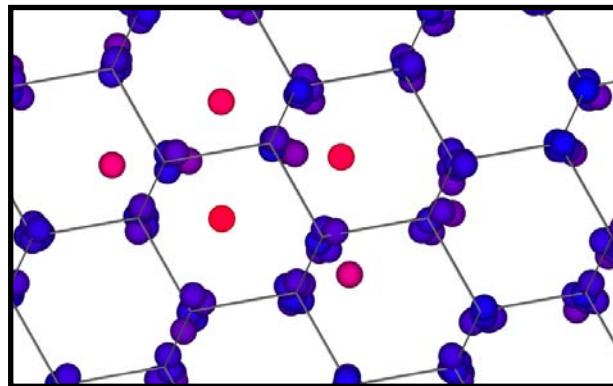
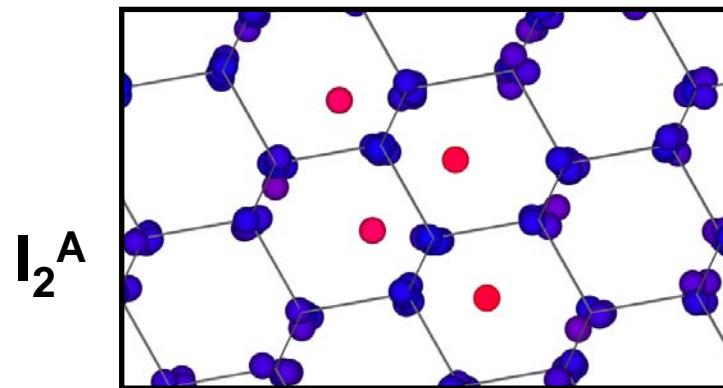
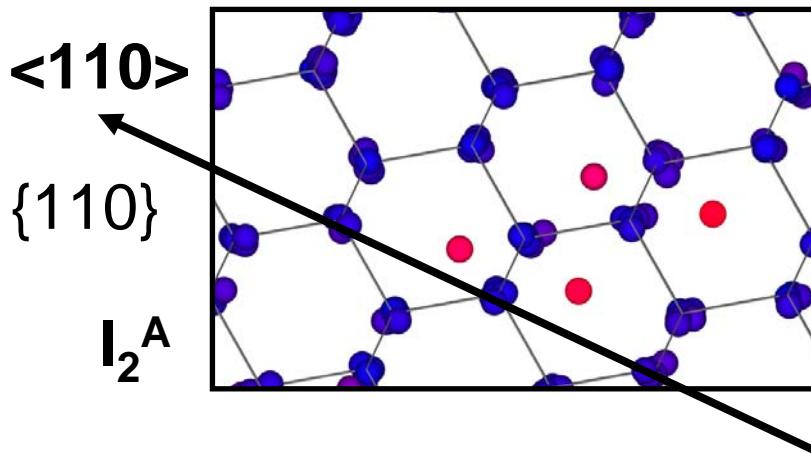
**high T – frequent change between equivalent <110> directions**



*migration along <110>: in a {110} plane, as  $I_2^A$  ...*

snapshots: migration distance: 2<sup>nd</sup> n.n. distance

2 ps



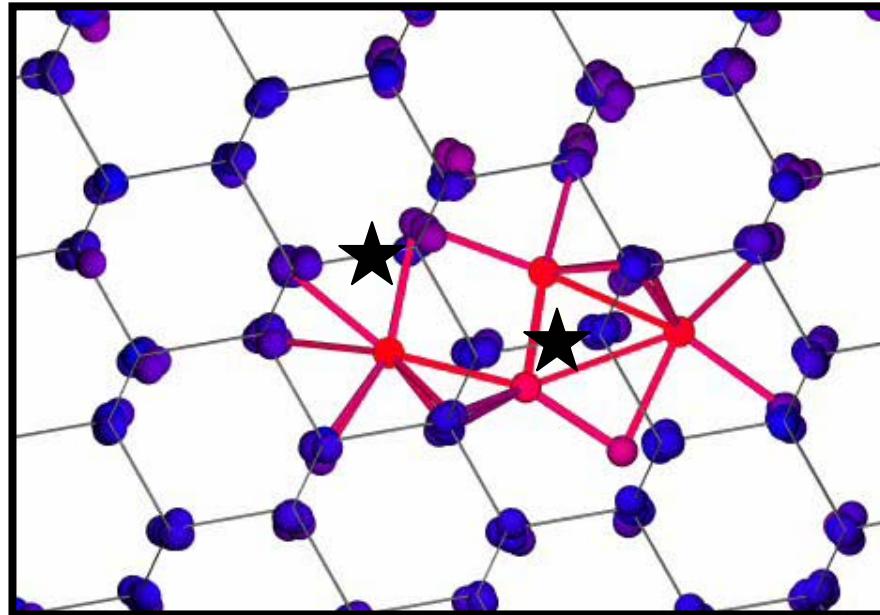
movie 1c  
(~3 ps)

migration distance:  
*2<sup>nd</sup> n.n. distance*

{110}

atoms belonging to  
the defect change  
continuously

bond switching



*place the cursor on the figure and  
double click to start the movie*

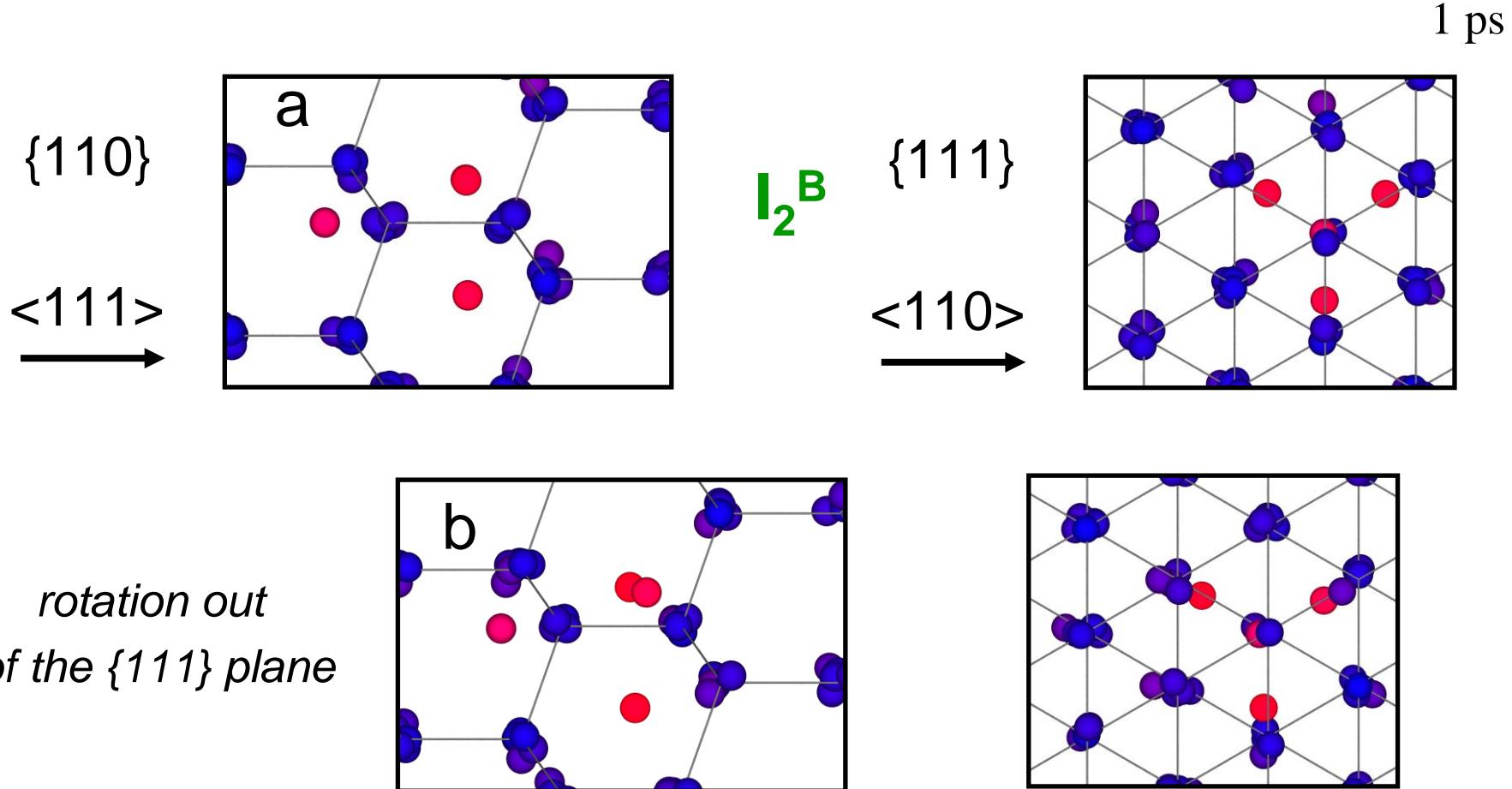


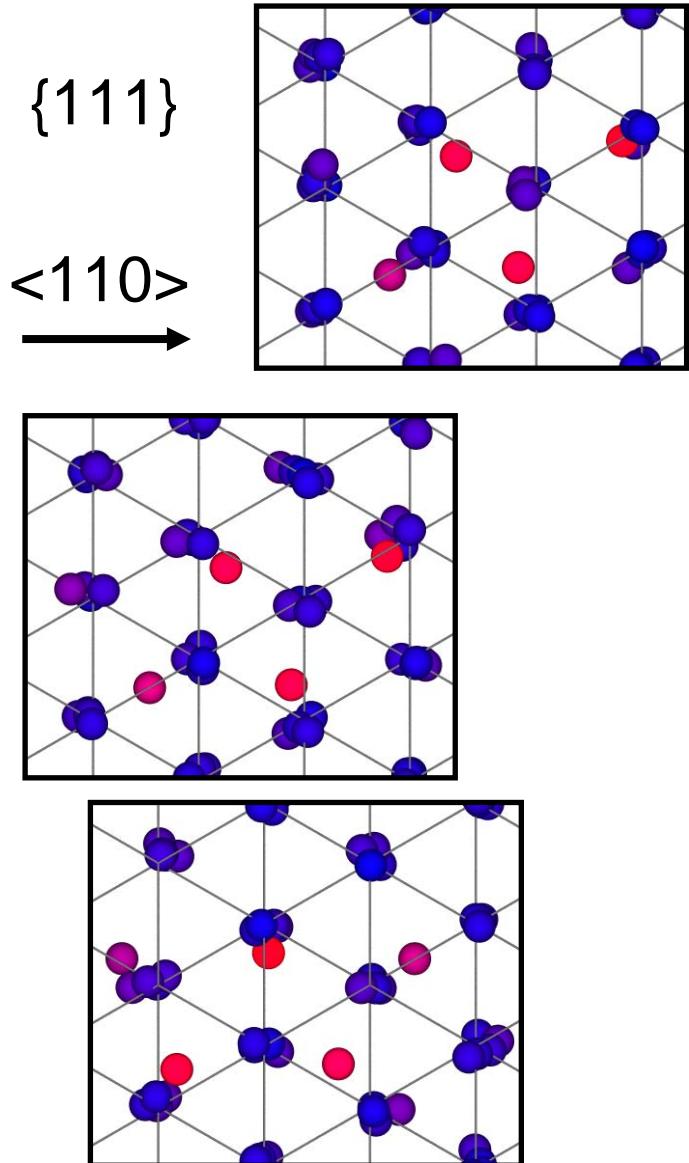
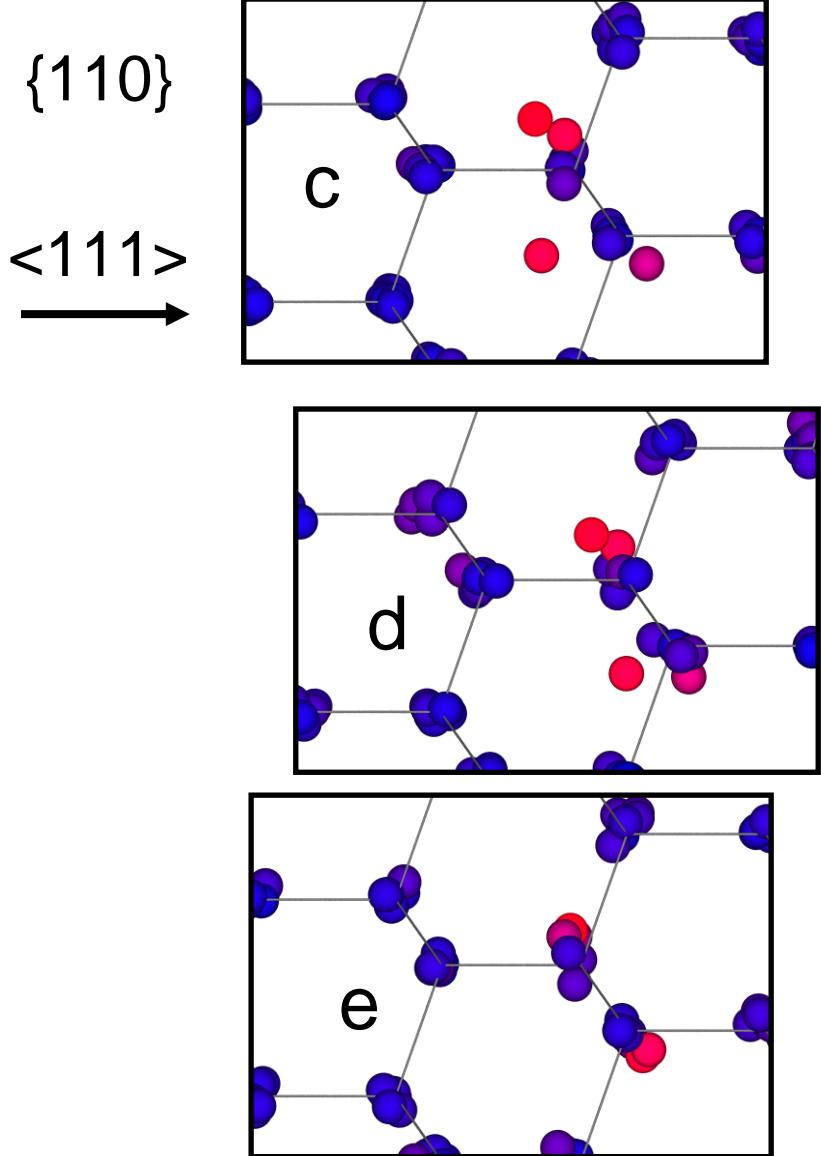
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change between different  $\langle 110 \rangle$  directions ( $\{110\}$  planes)  
via transformation:  $I_2^A \rightarrow I_2^B$  (immobile)  $\rightarrow I_2^A$





$I_2^A$



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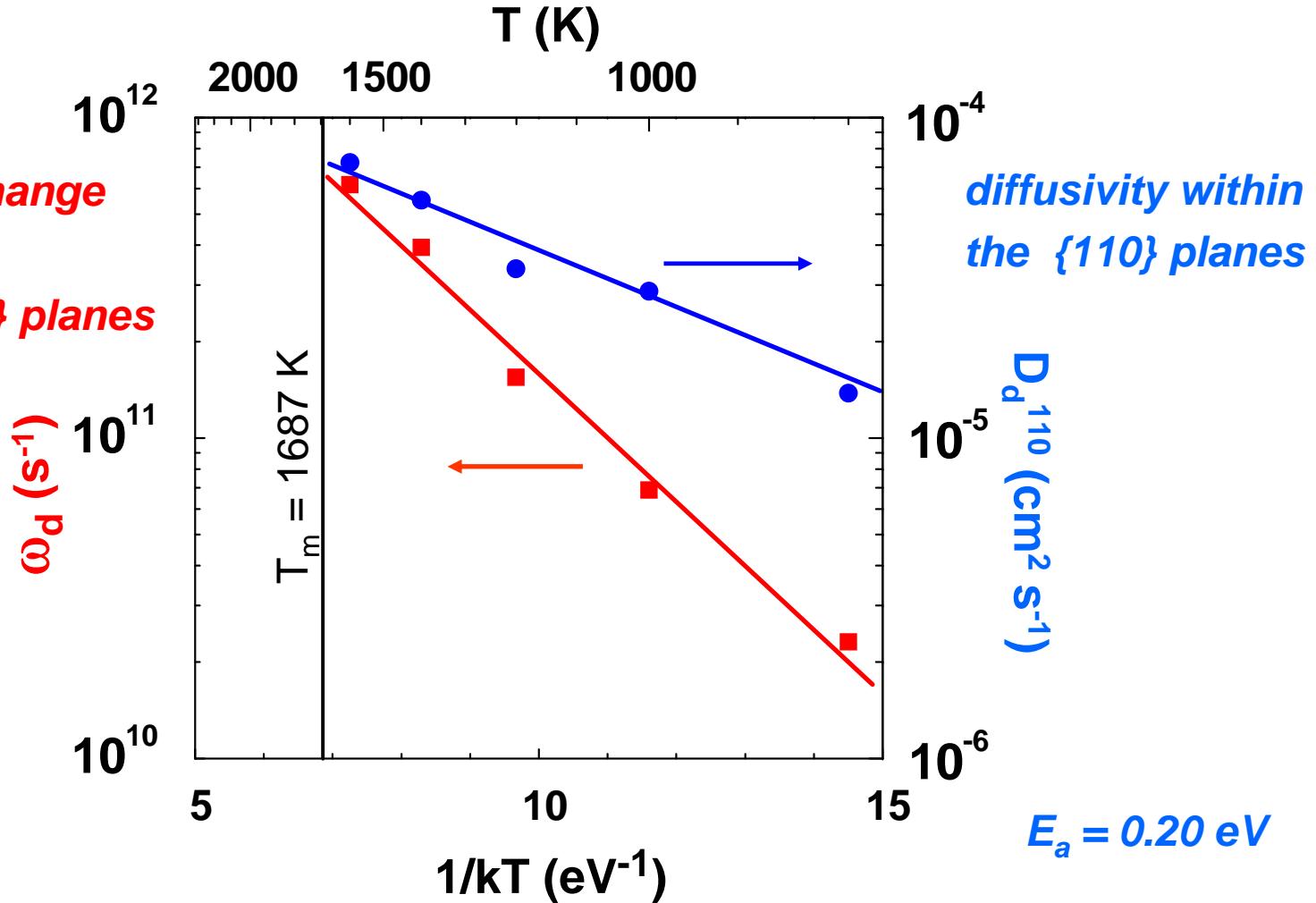
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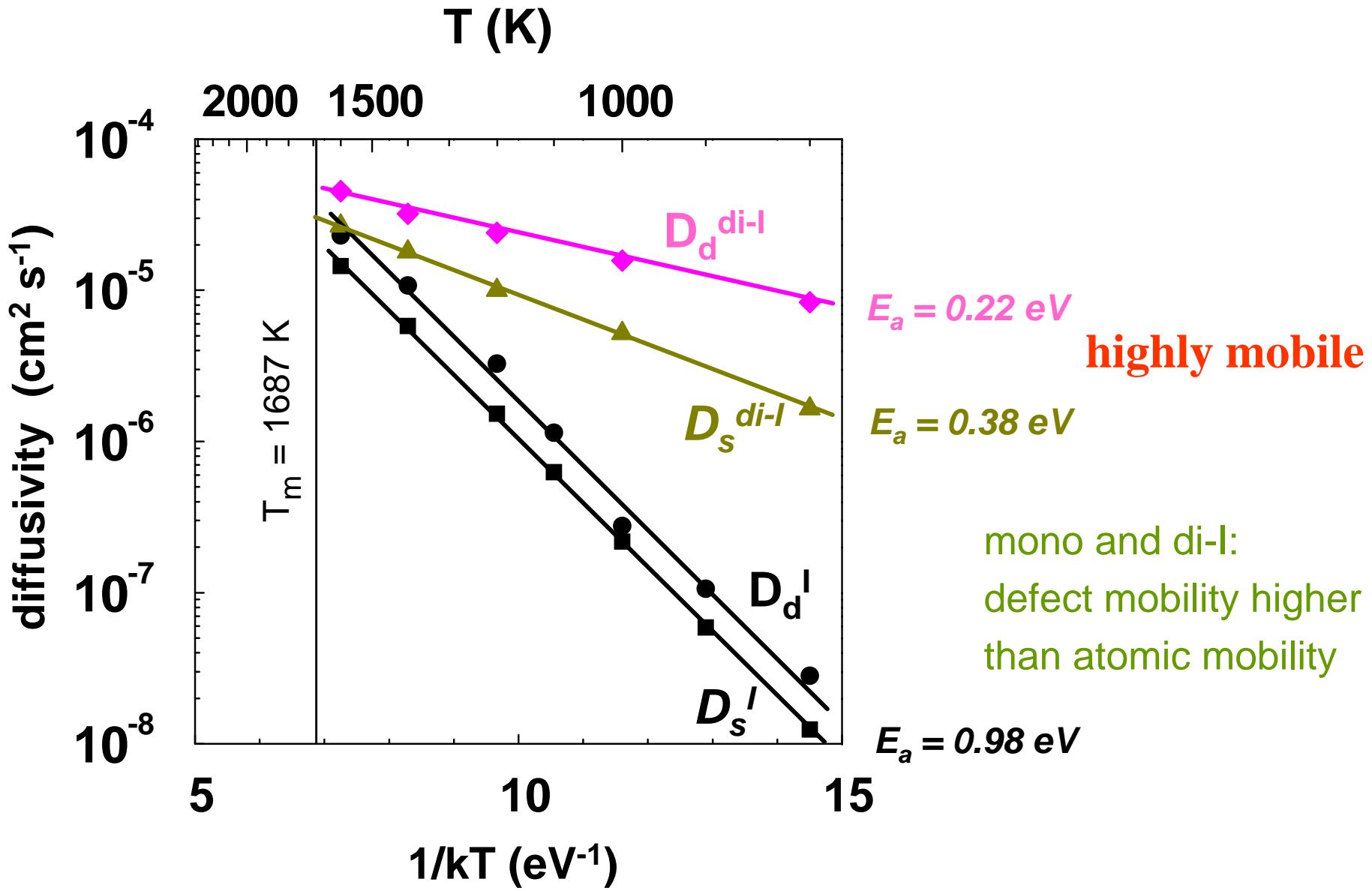
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# detailed analysis of migration of the di-I

*rate for the change  
between  
different {110} planes*

$E_a = 0.46 \text{ eV}$





# tri-interstitial

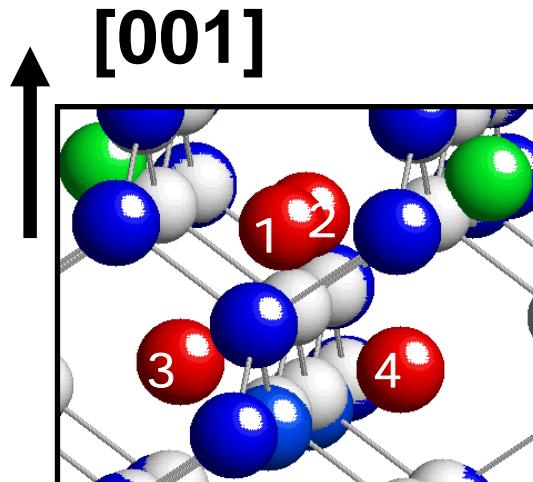
## structure and energetics

$I_3^A$

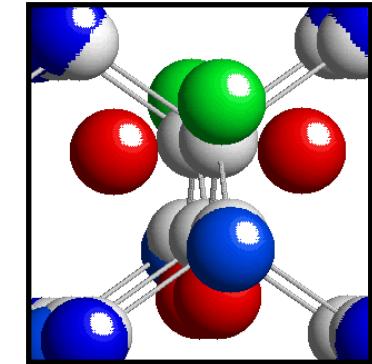
"mod. tetrahedron" ( $C_{2v}$ )

$$E_f = 7.54 \text{ eV}$$

$$E_b = 4.22 \text{ eV}$$



near (110)



near (1-10)

**CP:** Gilmer 1995 (SW): 7.08 eV; Lenosky 2000 (EDIP): 8.85 eV; Lenosky 2000 (L): 6.03 eV

*similar configuration (found by TB and DFT): "tetrahedron" ( $C_{2v}$ )*

**TB:** Bongiorno 2000: 6.69 eV; Lenosky 2000: 7.83

**DFT:** Kim 2000: ~6 eV; Chichkine 2002: 6.05 eV;

*Richie 2004: 6.96-7.11 eV; Lopez 2004: 7.27 eV*



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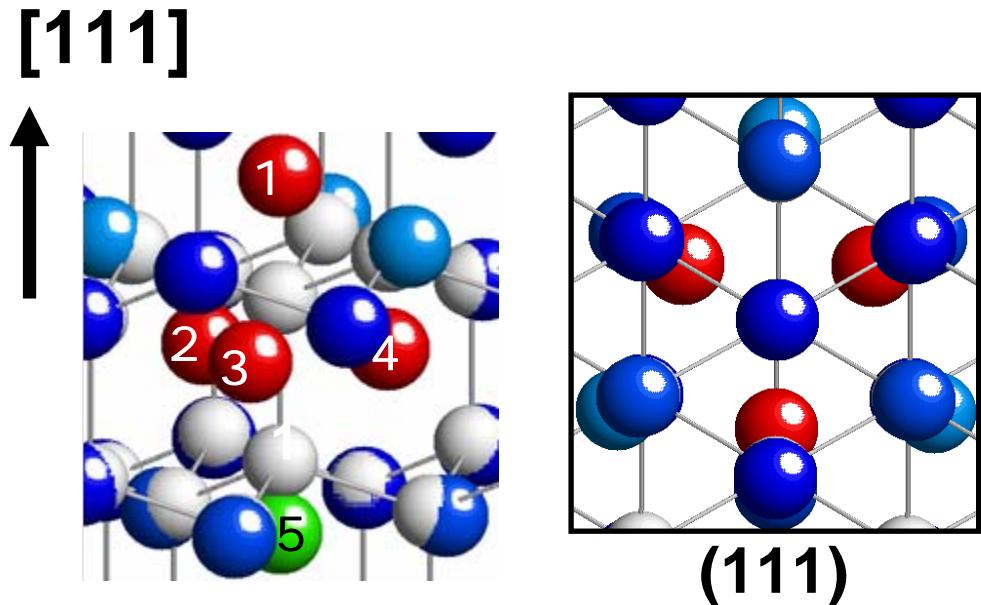
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$I_3^B$

“mod. bond-centered triple I” ( $C_{3v}$ )

$$E_f = 7.59 \text{ eV}$$
$$E_b = 4.17 \text{ eV}$$



similar configuration (found by DFT): “bond-centered triple” ( $C_{3v}$ )

**DFT:** Chichkine 2002: 6.09 eV; Lopez 2004: 7.32 eV



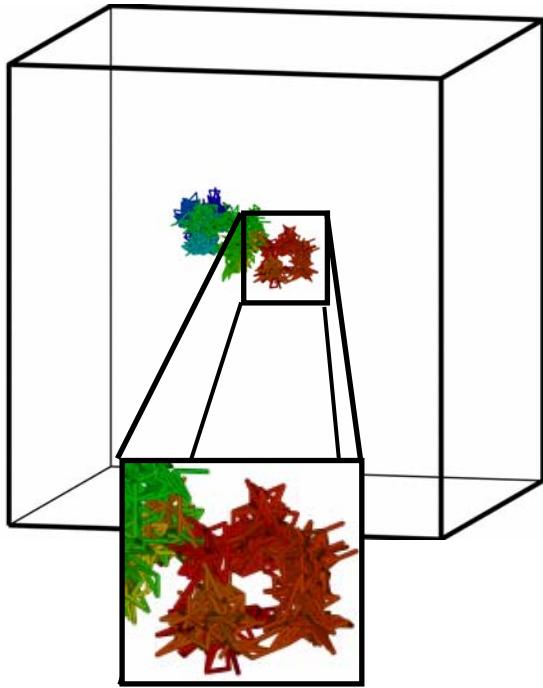
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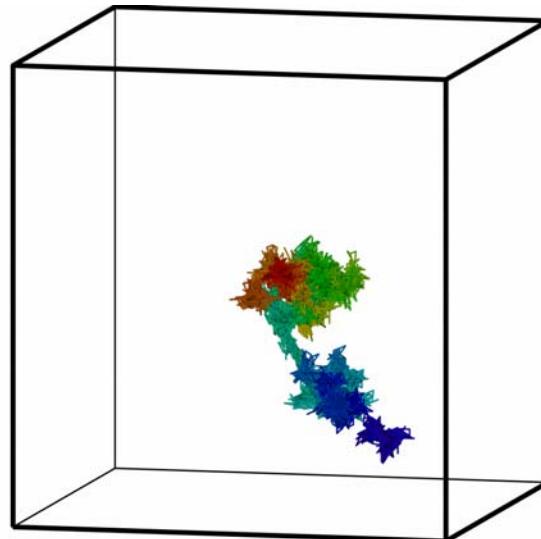
# *migration*

trajectories over a period of 14.4 ns

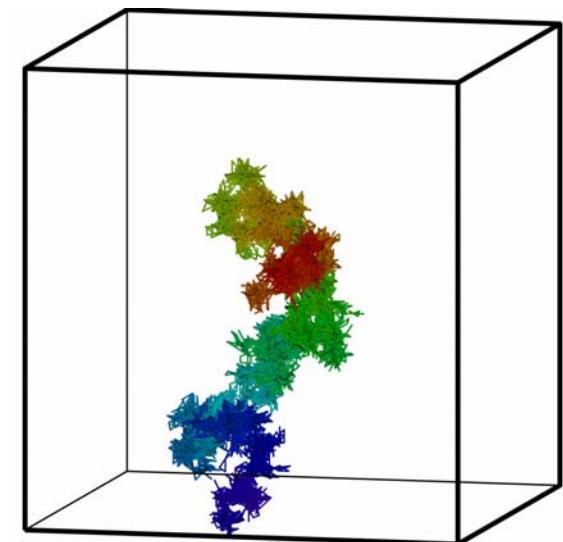


$T = 1400 \text{ K}$

complex trajectories, e.g. around a six member ring



$T = 1500 \text{ K}$



$T = 1600 \text{ K}$



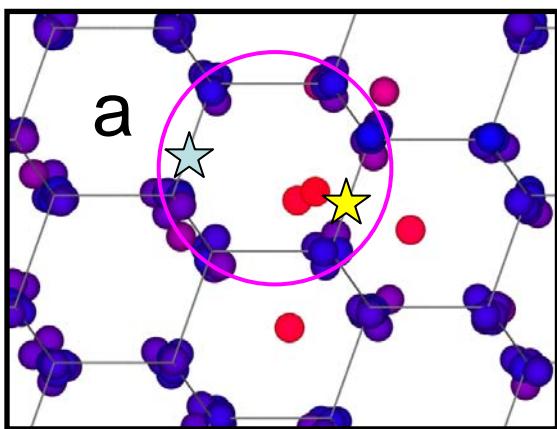
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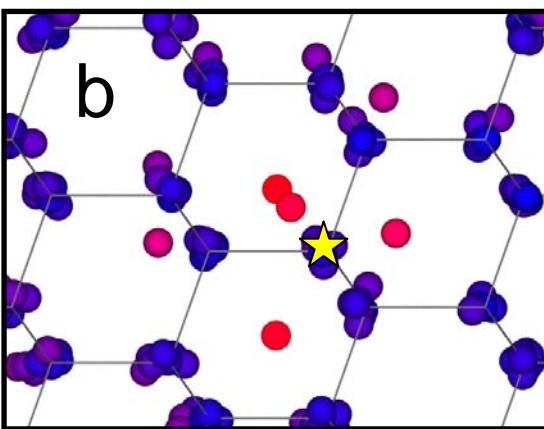
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35 ps

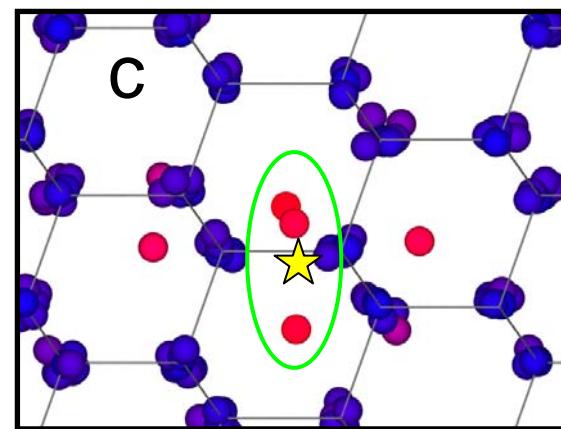
$I_3^B$



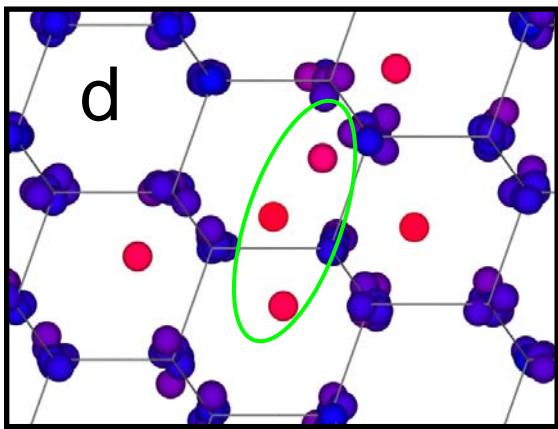
$I_3^A$



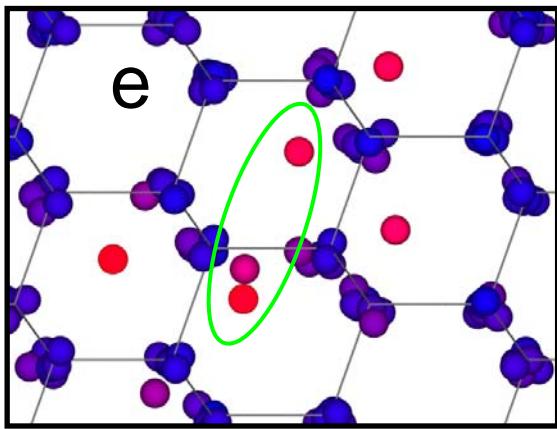
$I_3^B$



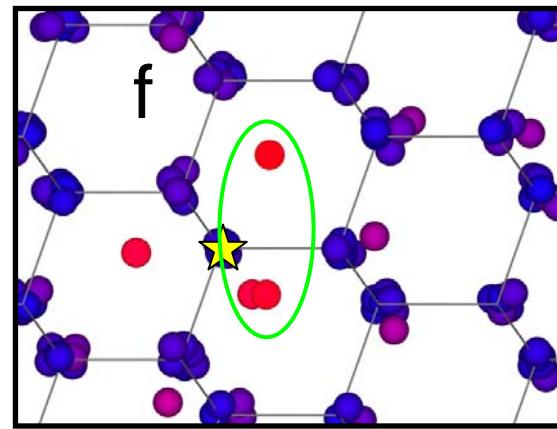
d



e



f



$I_3^A$

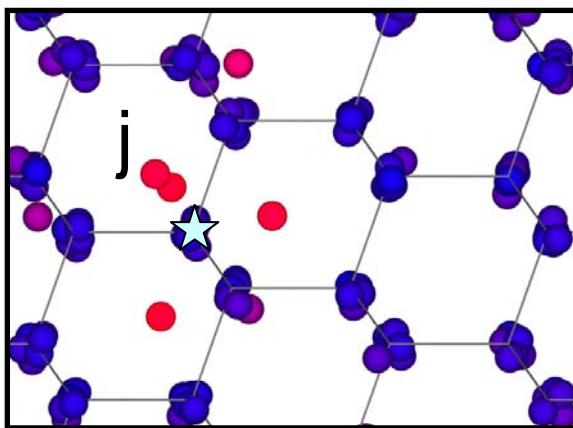
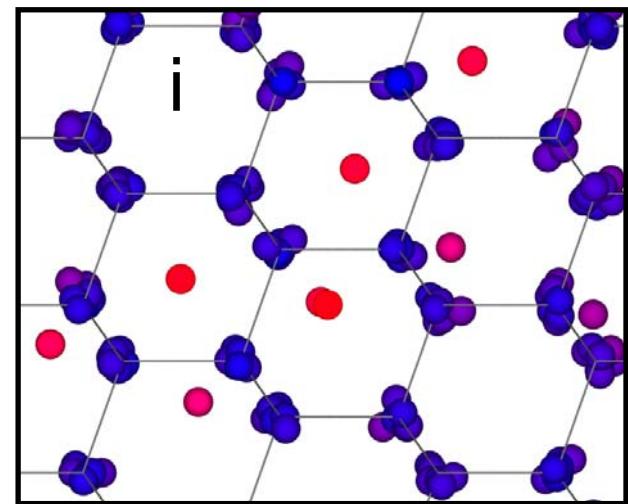
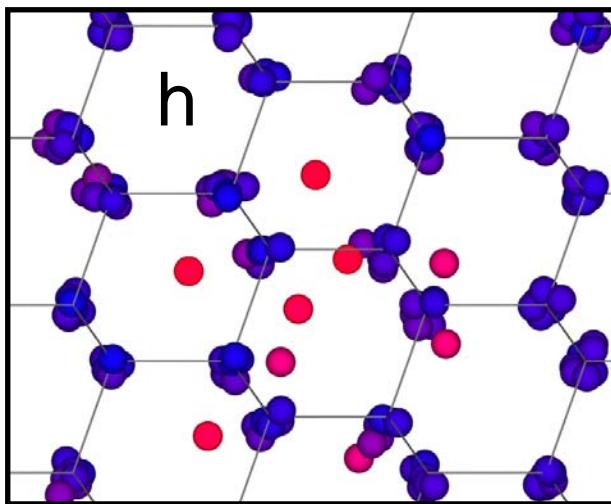
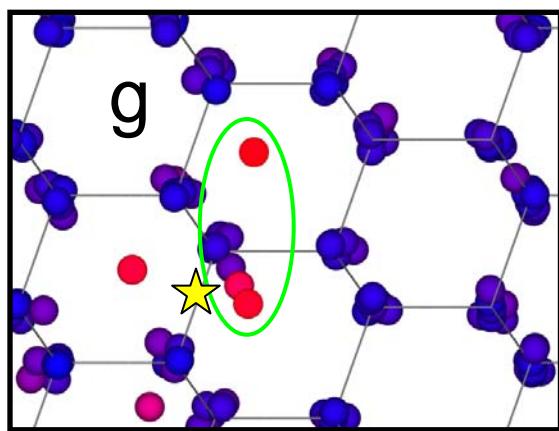


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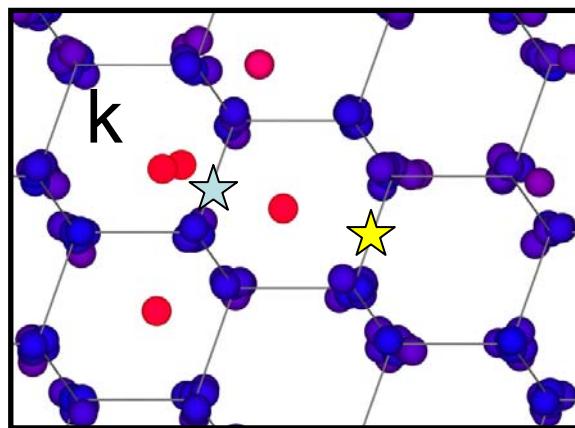
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$I_3$  B



$I_3$  A



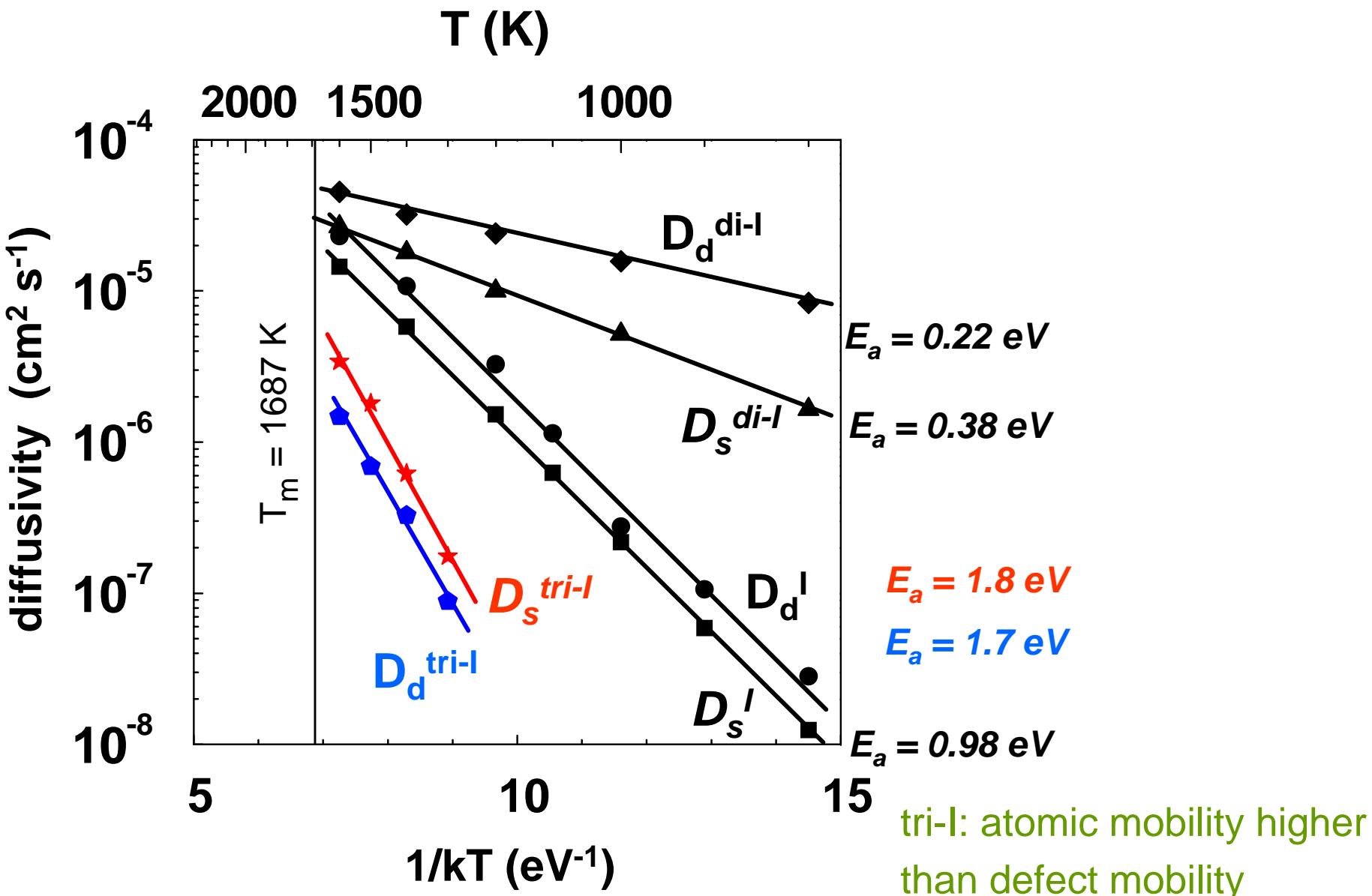
$I_3$  B



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# comparison with experimental data (di- and tri-I)

## a) “*direct*” observation of di- and tri-I (?)

EPR P6 center related to di-I? pro: Lee 1976, 1998  
contra: Jones 2002

PL W center related to tri-I? pro: Jones 2002  
contra: Lopez 2004



## **b) “*indirect*” proofs for the existence of di- and tri-I**

state-of-the-art description of defect evolution and TED of dopants (B) during post-implantation annealing:

Cowern et al. 1999..., Pelaz et al. 1997 ...

***formation of interstitial clusters must be assumed***

During ion implantation **only mono-interstitials and mono-vacancies** are formed. Their concentration is much higher than in the thermodynamic equilibrium.

***but - atomistic simulations of defect formation reveal:  
large variety of as-implanted defects is formed (also di- and tri-I)***



The **mono-interstitial** and the **mono-vacancy** are the only mobile intrinsic defects. They **recombine or form immobile clusters**. In particular self interstitial clusters - amongst them the **di-interstitial** - are introduced to obtain a transient storage of self-interstitials and to explain quantitatively the formation of {311} defects and dislocation loops as well as the TED

*but - present investigations: mobile di- and tri-I*



## Cowern 1998...: OR model for defect evolution

start: only  $I + 1$

40 keV Si

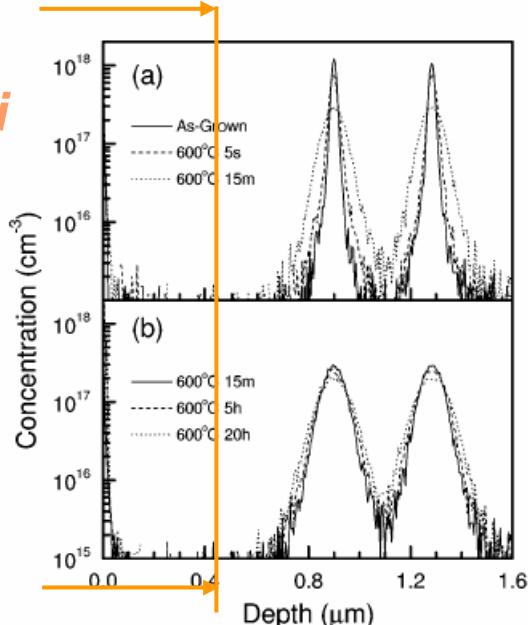


FIG. 1. B concentration profiles before and after annealing for a range of times at 600 °C.

$$E_b^c = Q^I - E_m^I - E_{fc}$$

$$\begin{array}{ll} Q^I \sim 4.5 \text{ eV} & E_b^{\text{di-l}} \sim 2.2 \text{ eV} \quad 1.7 \text{ eV} \\ E_m^I \sim 1 \text{ eV} & E_b^{\text{tri-l}} \sim 2.3 \text{ eV} \quad 2.5 \text{ eV} \end{array}$$

$E_b^c(n)$  non-monotonic

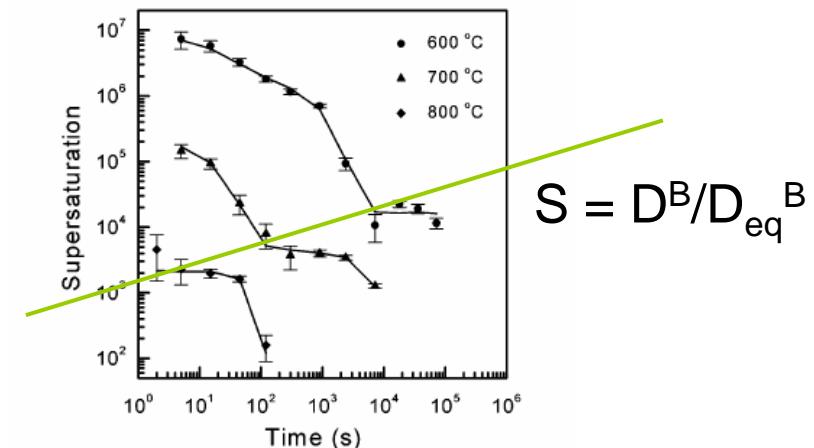
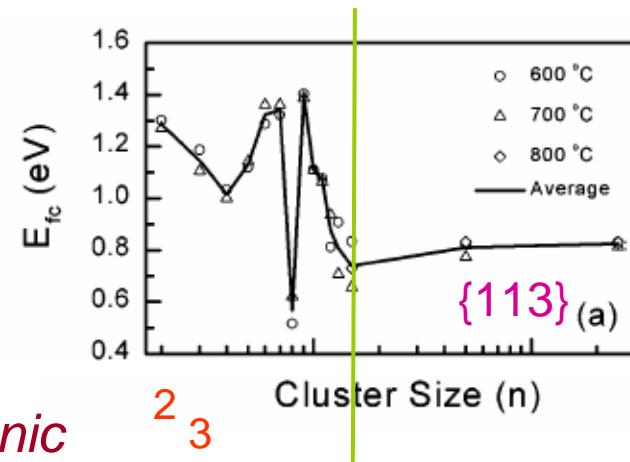


FIG. 2. Interstitial supersaturation,  $S$ , as a function of annealing temperature and time. Symbols with error bars represent experimental values with  $2\sigma$  uncertainties. Curves represent fits using an Ostwald ripening model (see text).



## Pelaz 1997...: KMC simulation of defect evolution and TED

40 keV Si

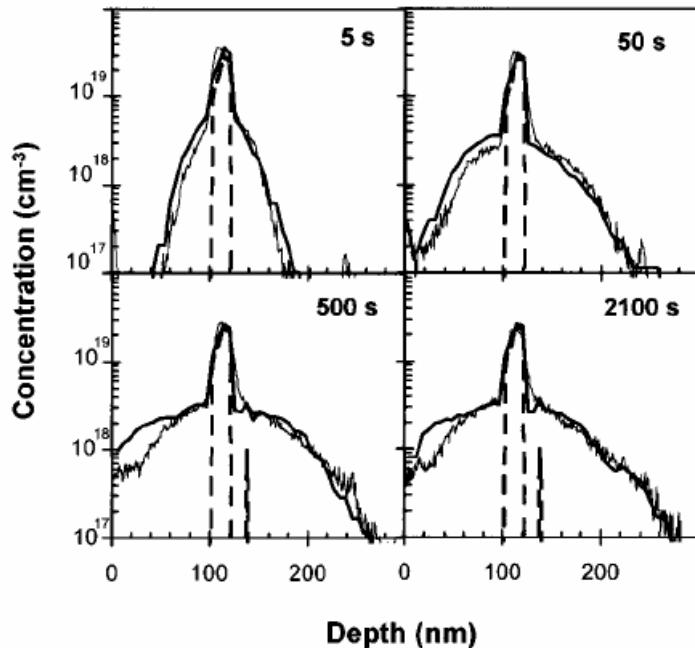


FIG. 2. Simulated and experimental profiles of a  $4.5 \times 10^{19} \text{ cm}^{-3}$  B spike after 40 keV  $9 \times 10^{13} \text{ cm}^{-2}$  Si implant and 5, 50, 500, and 2100 s anneal at 800 °C. Thin lines represent experimental data, thick solid lines the simu-

start: V,I from BCA

$$\begin{aligned} E_b^{\text{di-l}} &\sim 1.6 \text{ eV} & 1.7 \text{ eV} \\ E_b^{\text{tri-l}} &\sim 1.8 \text{ eV} & 2.5 \text{ eV} \end{aligned}$$

$E_b^c(n)$  monotonic

Aboy 2003:  $E_b^c(n)$  of Cowern  
 $E_m^l$  of Bracht



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**c) explanation of the long-range, trap-limited migration  
of implantation-induced I-like defects observed at  
room temperature by the high mobility of the di-I**



Kyllesbech Larsen et al. 1996:  
*implantation and ex-situ SRP measurements of deactivation*

40 keV Si  
 $5 \times 10^{13} \text{ cm}^{-2}$

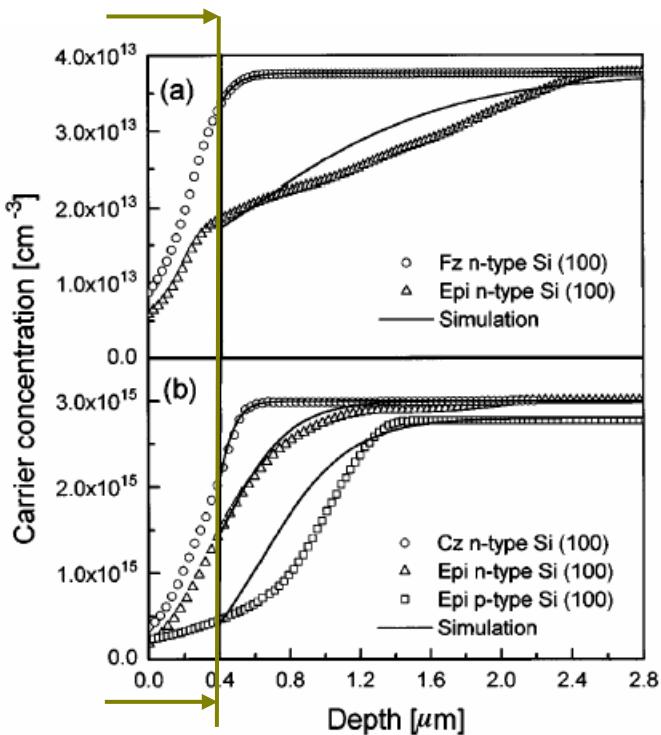


FIG. 1. SRP profiles of different homogeneously doped Si(100) substrates implanted with 40 keV  $^{28}\text{Si}$   $5 \times 10^{13} \text{ cm}^{-2}$ : (a) epitaxial ( $\Delta$ ) and Fz ( $\circ$ ) silicon P doped at a level of  $3.7 \times 10^{13} \text{ cm}^{-3}$ ; and (b) epitaxial ( $\Delta$ ), Cz ( $\circ$ ) silicon P doped at  $3.0 \times 10^{15} \text{ cm}^{-3}$ , and B-doped epitaxial Si ( $\square$ ) with a doping level of  $2.8 \times 10^{15} \text{ cm}^{-3}$ . The solid lines are obtained

injection and trapping of I-like defects

traps:

epi:  $[\text{O}] < 10^{15} \text{ cm}^{-3}$ ;  $[\text{C}] < 10^{15} \text{ cm}^{-3}$

FZ:  $[\text{O}] \sim 10^{16} \text{ cm}^{-3}$ ;  $[\text{C}] \sim 10^{17} \text{ cm}^{-3}$

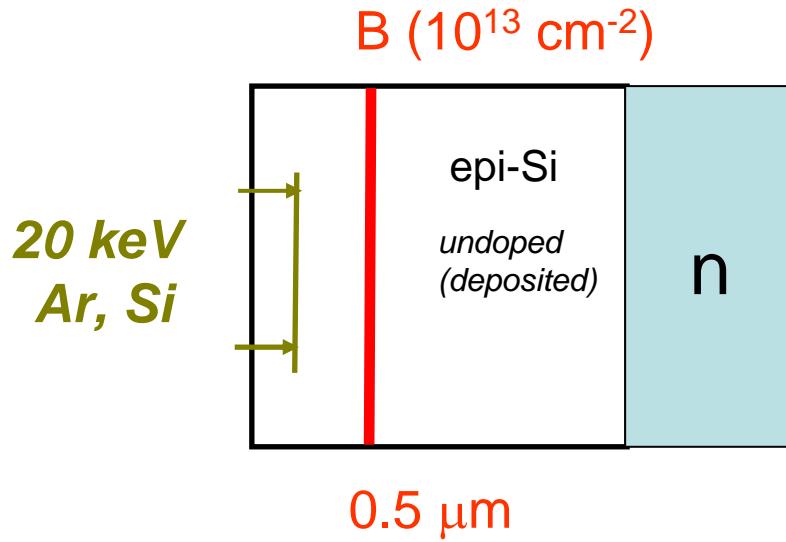
Cz:  $[\text{O}] \sim 10^{18} \text{ cm}^{-3}$ ;  $[\text{C}] \sim 10^{17} \text{ cm}^{-3}$

dopants  $\rightarrow$  deactivation

a very low fraction ( $\sim 10^{-5}$ ) of the ballistically formed defects is mobile and responsible for the deactivation



## Collart 1998: *implantation and in-situ resistivity measurement*



*sheet resistance*

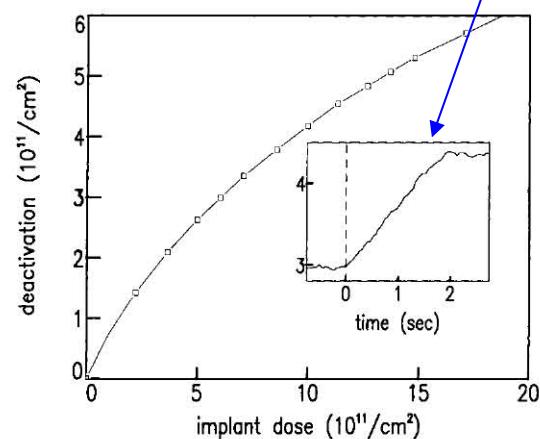


Fig. 5. Deactivation of a buried B layer as a function of Ar implant dose. The inset shows the deactivation in real time, during a two-second exposure of a previously unirradiated sample.

mobile I-like defects are formed  
during implantation



## Privitera 1996: *implantation and ex-situ SRP measurements*

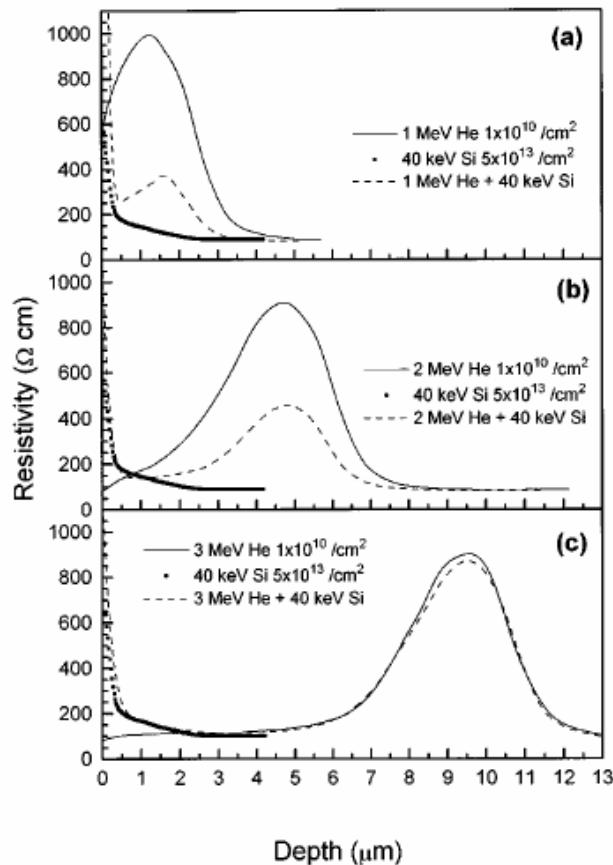


FIG. 1. Resistivity profiles for samples implanted with  $1 \times 10^{10}/\text{cm}^2$  He (solid line),  $5 \times 10^{13}/\text{cm}^2$  40 keV Si (dotted line) and with both He and Si (dashed line). The energy of the He implant was 1 MeV (a), 2 MeV (b), or 3 MeV (c).

epi:  $[\text{O}] < 10^{16} \text{ cm}^{-3}$ ;  $[\text{C}] < 10^{16} \text{ cm}^{-3}$   
n (phosphorus) doped  $\sim 10^{14} \text{ cm}^{-3}$

Si implants: deactivation by I-like defects

He implants: deactivation by V-like defects

**Si after He:**  
**reduction of deactivation by V-like defects**  
**due to injection and trapping of I-like defects**



lower bounds of the diffusivity of the I-like defects:

$10^{-11} \text{ cm}^2 \text{ s}^{-1}$  (Kyllesbech Larsen, Privitera),

$10^{-7} \text{ cm}^2 \text{ s}^{-1}$  (Collart)

if this were the value for the mono-I diffusivity at RT:

- about twenty orders of magnitude larger than  $D^I(\text{RT})$  obtained by diffusion experiments near the thermodynamic equilibrium (Bracht 1998...).
- much (5-10 orders of magnitude) larger than the mono-interstitial diffusivity often used in the interpretation of defect evolution and transition-enhanced diffusion of boron during post-implantation annealing (Pelaz 1997...)
- larger than many theoretical results (Colombo 2002)

***it could be the value for the di-I diffusivity ( $10^{-8} \text{ cm}^2 \text{ s}^{-1}$ )!***

