

QCD Equation of State

and compact stellar objects from Hard Thermal Loops

Quasiparticle Model

- elementary excitations of the QGP can be interpreted as quasiparticles with medium-modified properties

- derivation of the QCD thermodynamic potential via **Cornwall-Jackiw-Tomboulis formalism**

$$\Gamma[D, S] = I - \frac{1}{2} \{ \text{Tr} [\ln D^{-1}] + \text{Tr} [D_0^{-1} D - 1] \} + \{ \text{Tr} [\ln S^{-1}] + \text{Tr} [S_0^{-1} S - 1] \} + \Gamma_2[D, S]$$

from a 2-loop QCD functional

$$\Gamma_2 = \frac{1}{12} \text{loop} + \frac{1}{8} \text{loop} - \frac{1}{2} \text{loop}$$

- gauge invariance ensured by using hard-thermal loop (HTL) self-energies in dispersion relations $\omega(k)$

- contributions from quaquarks and -gluons, plasmons and plasminos, also Landau damping, to entropy density give

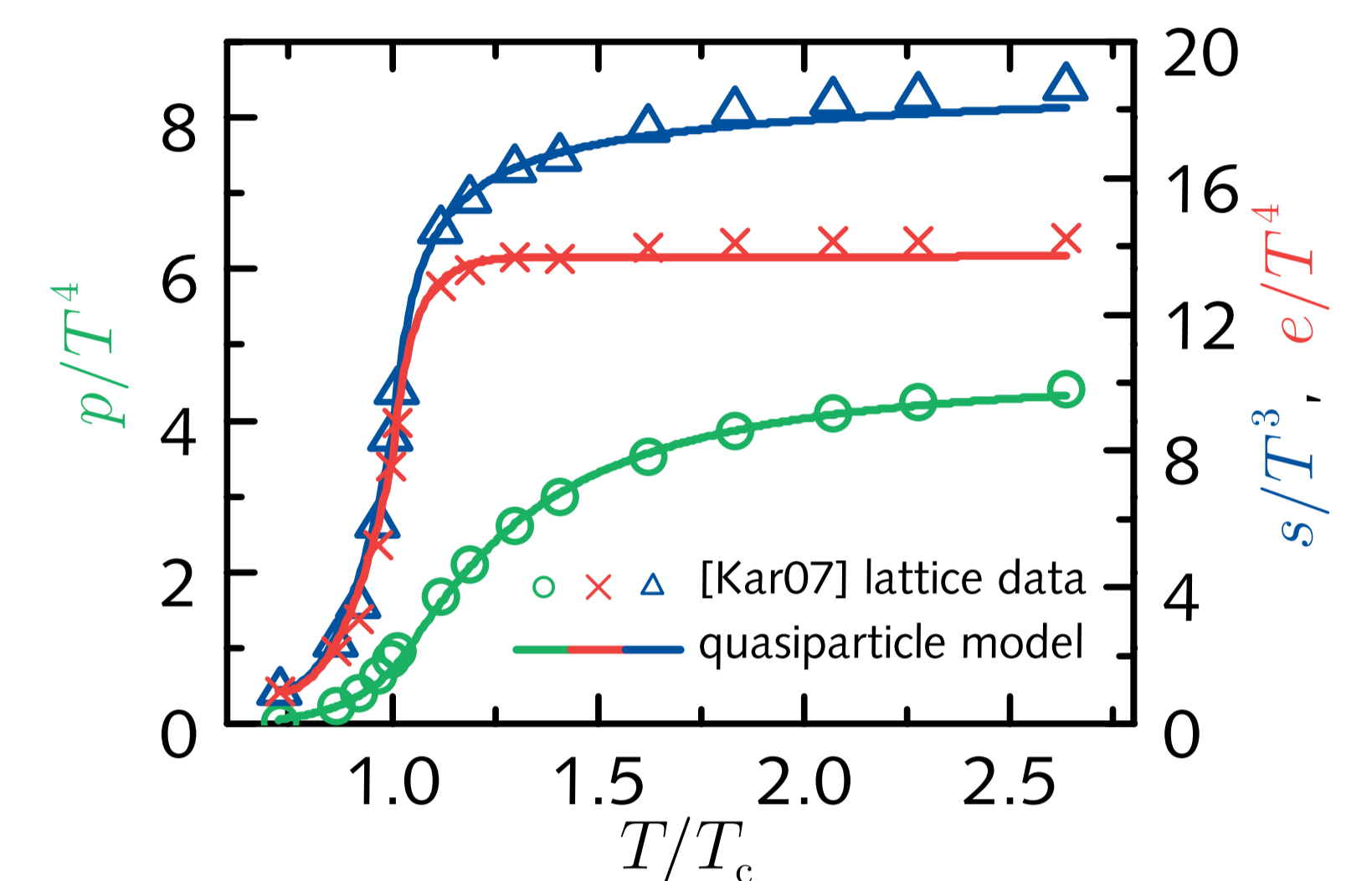
$$s := \frac{\partial \Gamma}{\partial T} = s_{g,T} + s_{g,L} + s_{q,Pt} + s_{q,P1} + s' \quad s' \approx 0$$

$$s_{g,T} \sim \int \frac{d^4k}{(2\pi)^4} \left\{ \underbrace{\pi \varepsilon(\omega) \Theta(-\text{Re} D_i^{-1})}_{\text{quasiparticle contribution}} + \underbrace{\text{Re} D_i \text{Im} \Pi_i - \text{atan} \left(\frac{\text{Im} \Pi_i}{\text{Re} D_i} \right)}_{\text{Landau damping}} \right\}$$

- neglecting collective excitations and Landau damping leads to previous simple model (eQP)

- non-perturbative effects of QCD are accommodated by means of an **effective coupling** G^2 replacing running coupling entering HTL self-energies

- adjustment of model parameters in G^2 to **first principle** lattice QCD calculations of pressure and entropy density from Karsch, 2007 at $n=0$



Equation of State

- self-consistent model allows **mapping to nonzero baryon densities** using Maxwell's relation

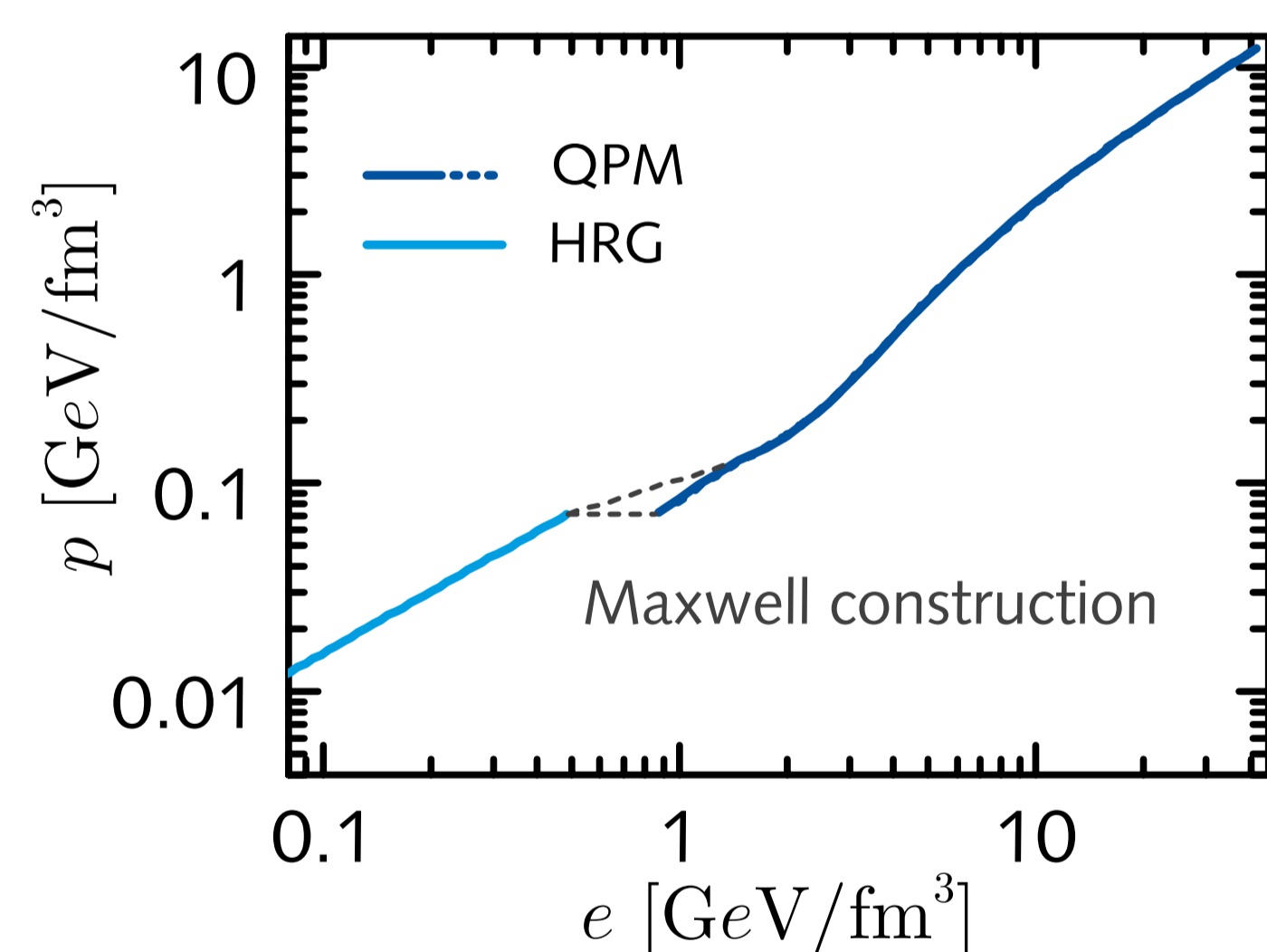
$$\frac{\partial s}{\partial \mu} = \frac{\partial n}{\partial T}$$

- 1st order partial differential equation for G^2 (dubbed "**flow equation**")

$$a_T(\mu, T) \frac{\partial G^2}{\partial T} + a_\mu(\mu, T) \frac{\partial G^2}{\partial \mu} = b(\mu, T, G^2)$$

- method of characteristics – free of ambiguities found for eQP close to deconfinement transition

- connect to **hadron resonance gas** (HRG) below the phase transition – Maxwell construction for all state variables



- both, real phase transition (1st+ order) or simple crossover possible

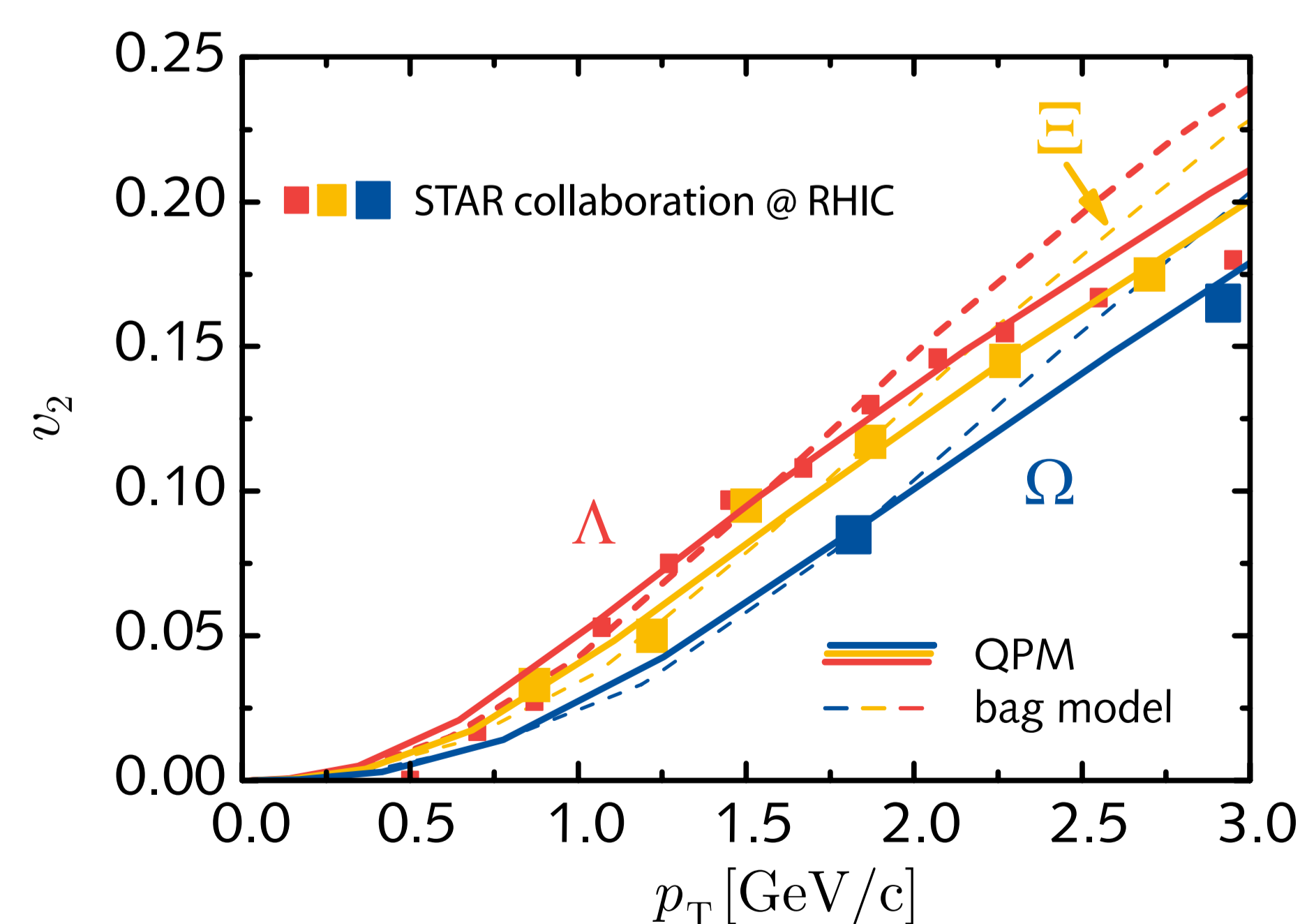
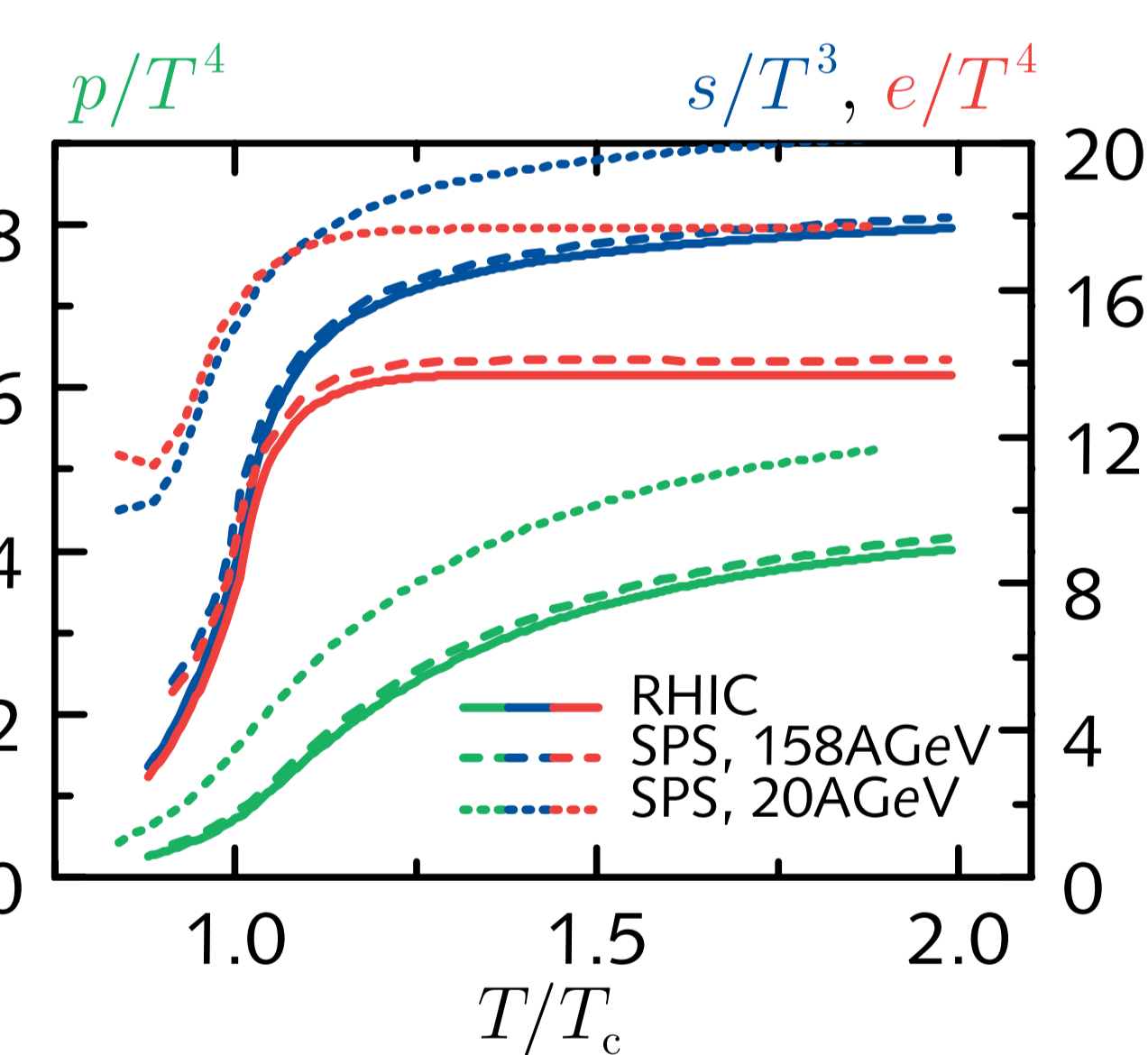
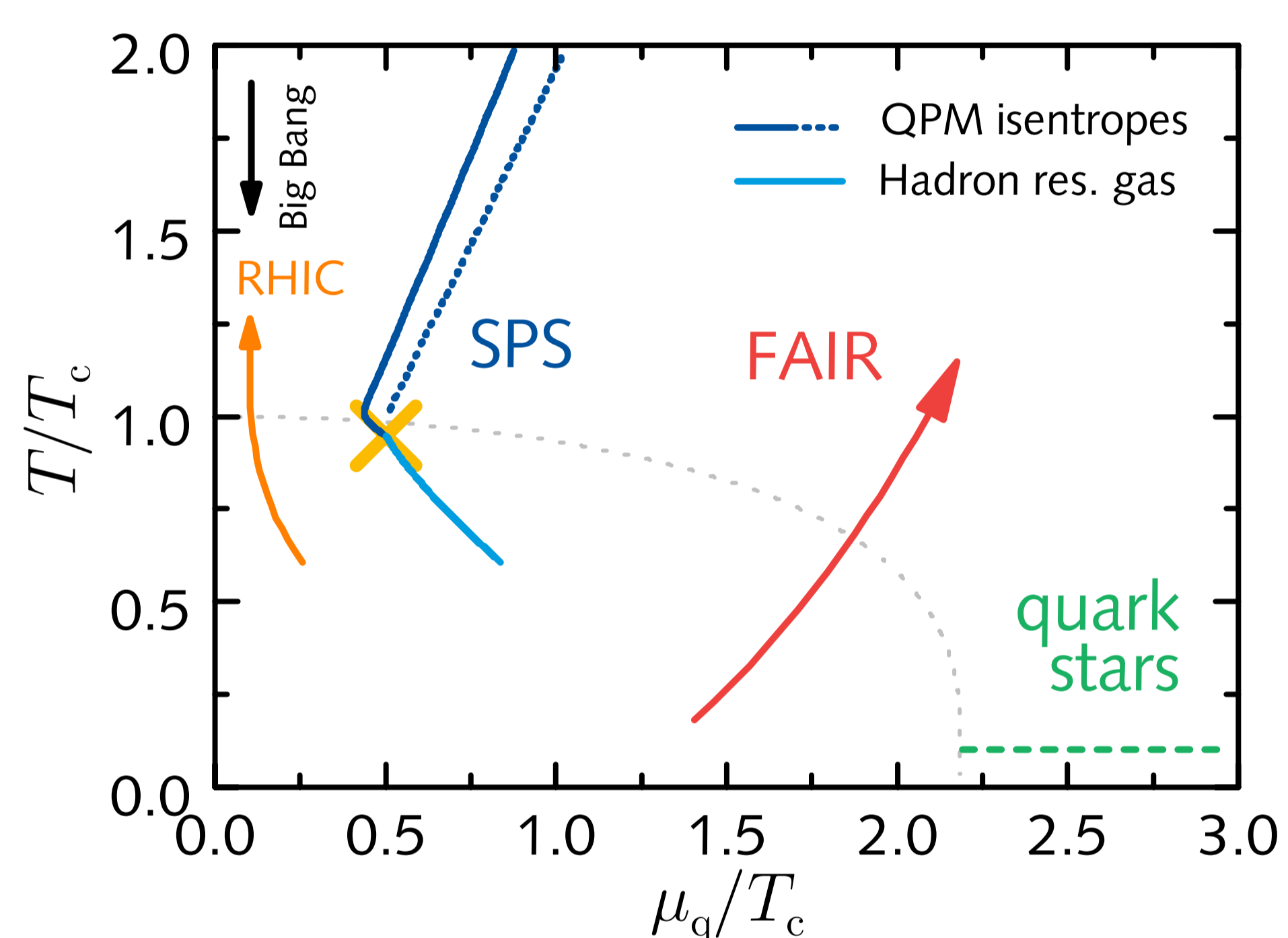
- Equation of State for heavy-ion collision experiments as well as compact stellar matter available

- evolution of state variables with increasing particle densities is shown in right panel

- pressure p , entropy density s , energy density e , baryon density n_{Ba} and interaction measure $e-3p$ increase with baryo-chemical potential

- quantities obey standard thermodynamic relations such as Nernst's law

- EoS applied in hydrodynamic descriptions of HIC – comparison with **experimental results** from STAR collaboration: elliptic flow v_2 (measure of azimuthal distribution of emitted hadrons) as function of transverse momentum p_T



Quark stars

- EoS for small temperatures and large baryon densities can be parametrized as a Bag-like system

$$e = \alpha p + 4\tilde{B}$$

where α is found to be approximately 4 as opposed to 3 from previous quasiparticle models

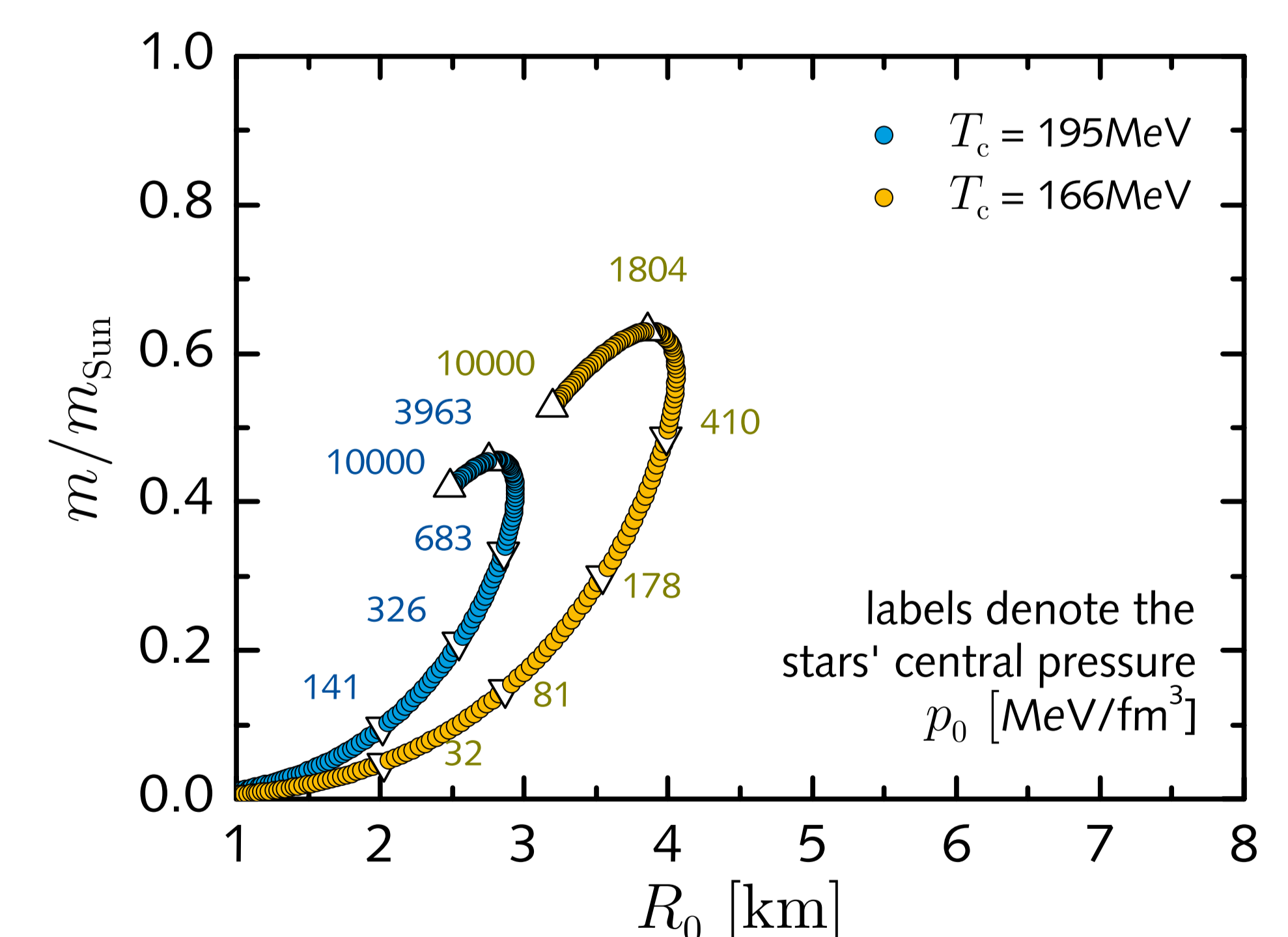
- β -equilibrium between quarks, gluons and leptons maintained by weak processes

$$d, s \leftrightarrow u, l, \nu_l$$

- lepton chemical potential follows directly from electric charge neutrality

- Tolman-Oppenheimer-Volkov** equations give dependence of radius and mass of quarks stars on the central pressure

- strong dependence of star radii on value of critical temperature T_c observed



References:

Schulze, Kämpfer – PPNP, to be published
Schulze, Bluhm, Kämpfer – EPJ ST, 2008
Bluhm, Kämpfer, Schulze, Seipt, Heinz – PRC, 2007

