



A FAIR equation of state

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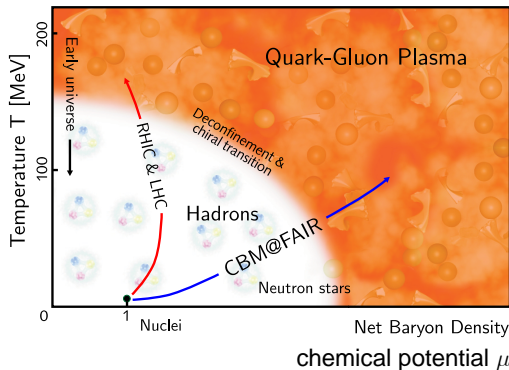
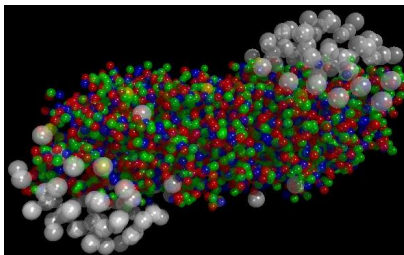
FZ Dresden-Rossendorf, FWKH

with B. Kämpfer

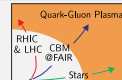
- quasiparticle model of quarks and gluons
- derivation of an equation of state (EOS)
- application of the EOS @ RHIC, FAIR and for pure quark stars

Introduction

- protons and neutrons consist of quarks and gluons
- heavy-ion collision experiments:
formation of quark-gluon plasma (QGP)

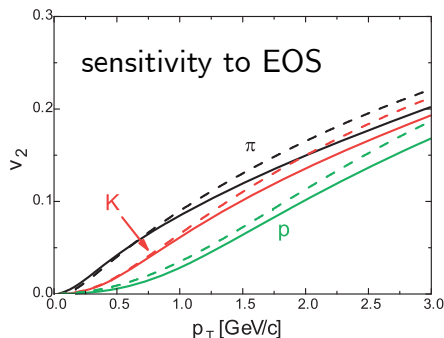
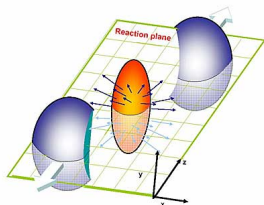


Introduction (2)



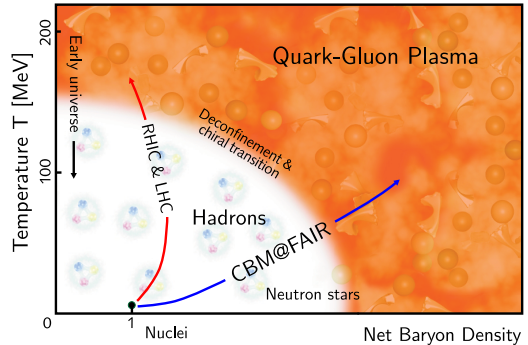
- fireball phase described using hydrodynamics
 → equation of state (EOS) of quark-gluon plasma is critical input
- example: azimuthal distribution v_2 @ RHIC

$$\frac{\partial N}{\partial \phi} = v_0 + v_1 \cos \phi + v_2 \cos 2\phi + \dots$$



Introduction (3)

- 1st principle evaluation of QCD difficult:
 - perturbative only if coupling weak
 - Monte-Carlo methods “on the lattice” only if baryon density low



→ quasiparticles to the rescue





The quasiparticle model

- quasiparticle model = thermodynamic system;
thermodynamic potential: pressure $p(T, \mu)$

→ other quantities follow

chemical potential

$$s = \frac{\partial p}{\partial T} \qquad n = \frac{\partial p}{\partial \mu}$$

- derived as approximation to actual QCD:
CJT formalism with 2-loop Γ_2 -functional

$$\Gamma_2 = \frac{1}{12} \text{ (loop 1)} + \frac{1}{8} \text{ (loop 2)} - \frac{1}{2} \text{ (loop 3)}$$

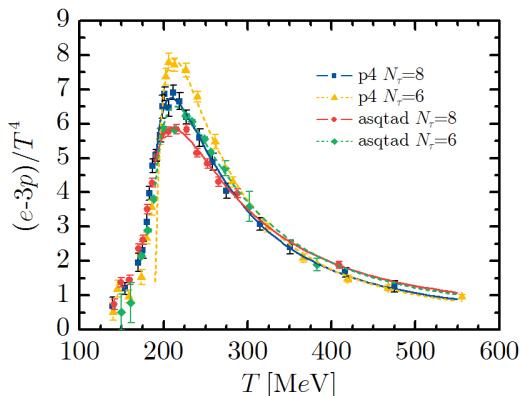


The quasiparticle model

- fundamental parameter:
running QCD coupling constant G^2

$$g^2(x^2) = \frac{16\pi^2}{\beta_0 \ln(x^2)} \quad x = \frac{\bar{\mu}}{\Lambda_{\text{QCD}}} \rightarrow \frac{T-T_s}{\lambda}$$

→ description of lattice results possible !



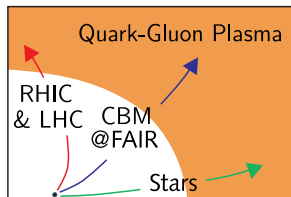
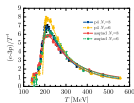
state variables $s, n, p, (e-3p), \dots$



effective coupling G^2 (+ pressure constant B_0)



@ $\mu = 0$:



@ $\mu \neq 0$:

??



Into the T - μ -plane

- the BIG trick: $\mu > 0$: thermodynamic model = self-consistent

$$\frac{\partial^2 p}{\partial T \partial \mu} = \frac{\partial^2 p}{\partial \mu \partial T}$$

↓

$$\frac{\partial s}{\partial \mu} = \frac{\partial n}{\partial T}$$

↓

$$a_T \frac{\partial G^2}{\partial T} + a_\mu \frac{\partial G^2}{\partial \mu} = b$$

Maxwell's relation

= in a self-consistent system,
information in T -direction
contains knowledge about
 μ -direction

flow equation

= Cauchy problem

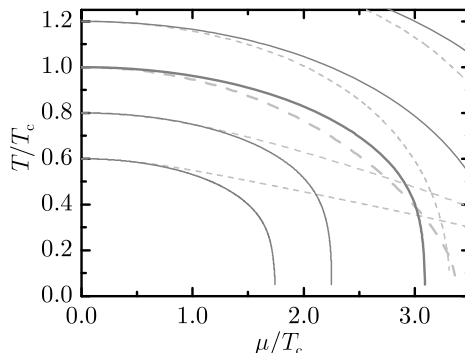
Peshier, Kämpfer, Soff: PRC'00, PRD'02
Blum, Kämpfer, RS, Seipt: EPJC'07



Into the T - μ -plane

- solution of the flow equation using method of characteristics
- effective QPM: crossing characteristics
→ area of ambiguous results
- full HTL QPM:
crossings resolved
→ large μ , e.g. for FAIR accessible

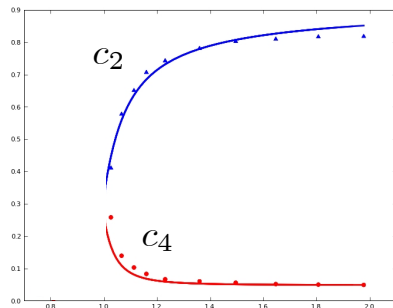
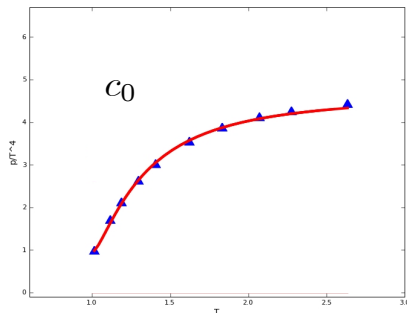
RS, Bluhm, Kämpfer: EPJ ST'08



Small chemical potential

- successful test with $p(T, \mu \gtrsim 0)$ lattice data

$$p = T^4 \sum_n c_n(T) \left(\frac{\mu}{T}\right)^n \quad c_n(T) = \frac{1}{n!} \frac{\partial^n (p/T^4)}{\partial (\mu/T)^n}$$

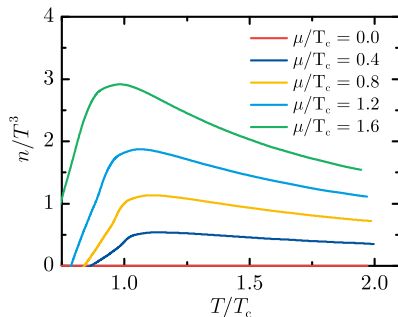
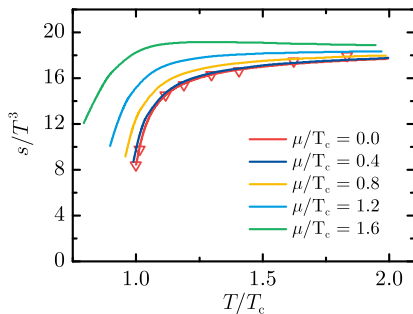


symbols = lattice QCD from Allton et al. (2001)

RS: unpublished

Thermodynamic bulk variables

- entropy density and net quark density

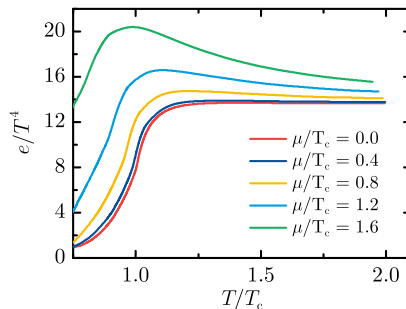
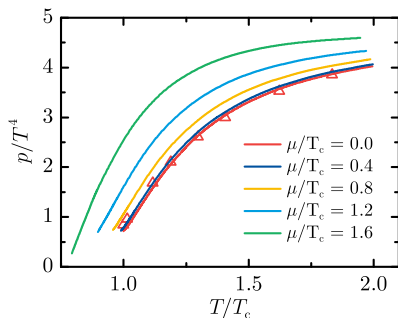


RS, Bluhm, Kämpfer: PPNP'09

- increase with chemical potential

Thermodynamic bulk variables

- pressure and energy density



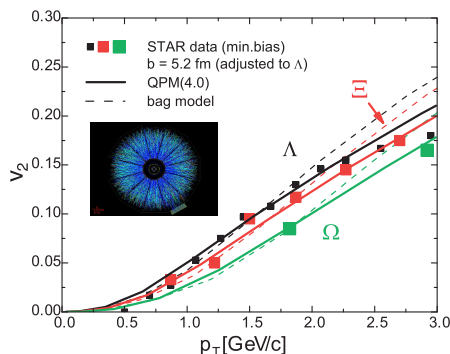
- small area of negative pressure
 - no problems for EOS @ RHIC, LHC, SPS, FAIR
 - natural limit of stability for quark stars

RS, Bluhm, Kämpfer: PPNP'09



Comparison with the experiment

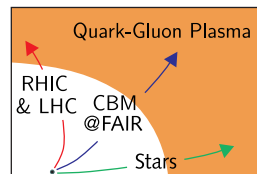
- calculate elliptic flow using relativistic hydro code using QPM equation of state
- compare with experimental data (RHIC)



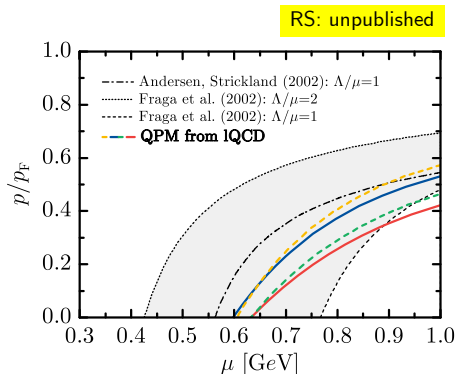
Bluhm, Kämpfer, RS, Seipt, Heinz: PRC'07

At $T=0$

- going all the way: quarks stars
→ solve TOV equations using
QPM equation of state

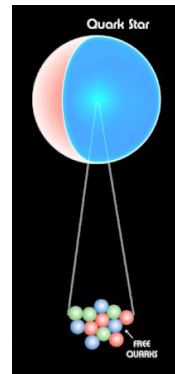
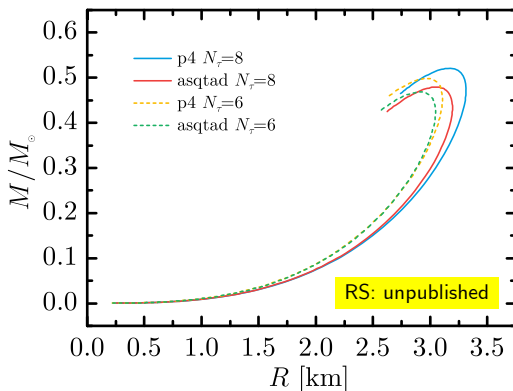


- perturbative predictions for
general pressure behavior
→ agreement
→ our estimate =
1st to give an actual
order of magnitude



Quark stars

- solutions of the TOV equations



- quark stars quite small and light
- no twins of neutron stars

Summary & Outlook

- EOS adjusted to numerical QCD evaluation
- sound extrapolation to very dense matter
- quark stars with rather smaller radii
- method applicable to EOS of electron-positron plasma for laser-induced hot dense matter
- outlook: EOS for FAIR/CBM:
combination with hadron EOS