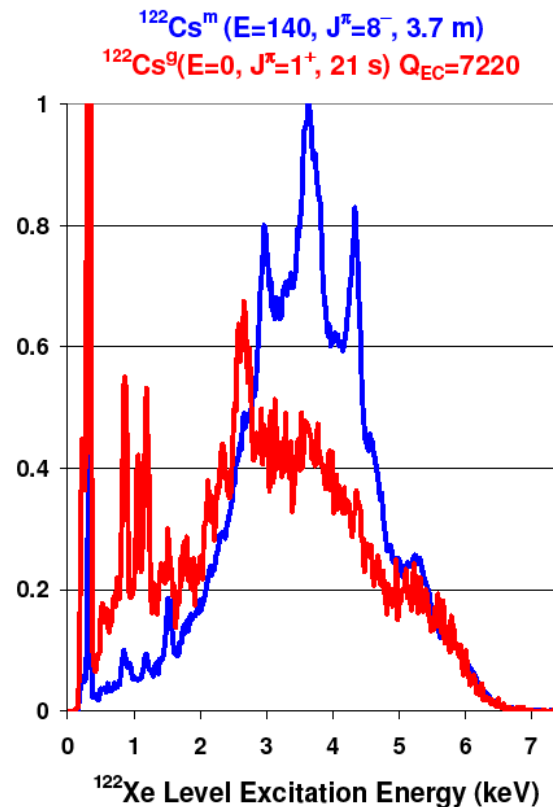


Failure of the Gross Theory of Beta Decay in Neutron Deficient Nuclei

Richard B. Firestone

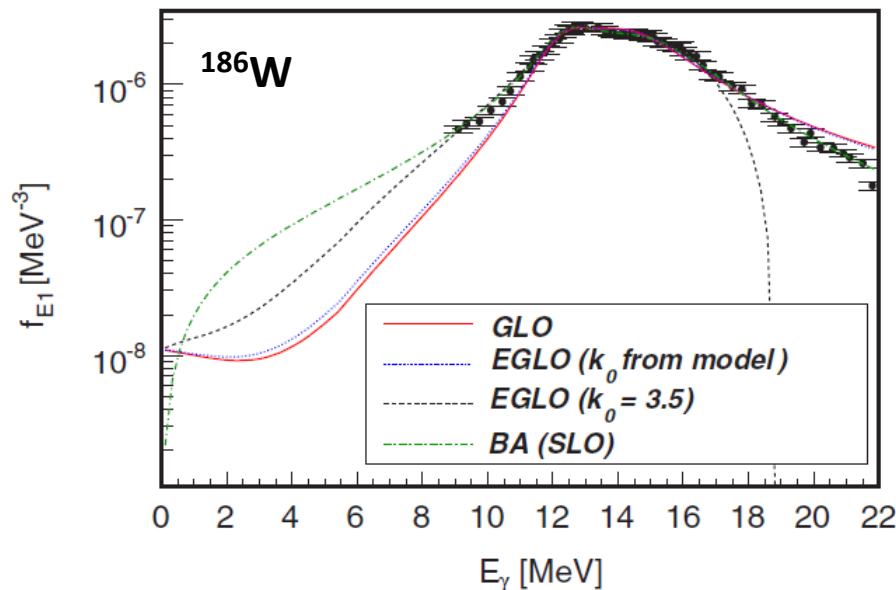
Lawrence Berkeley National Laboratory, Berkeley, CA 94720 USA



Photon Strength Statistical Models

Gamma Rays

E1: Brink-Axel and variations; based on the shape of the Giant Dipole Resonance (GDR).

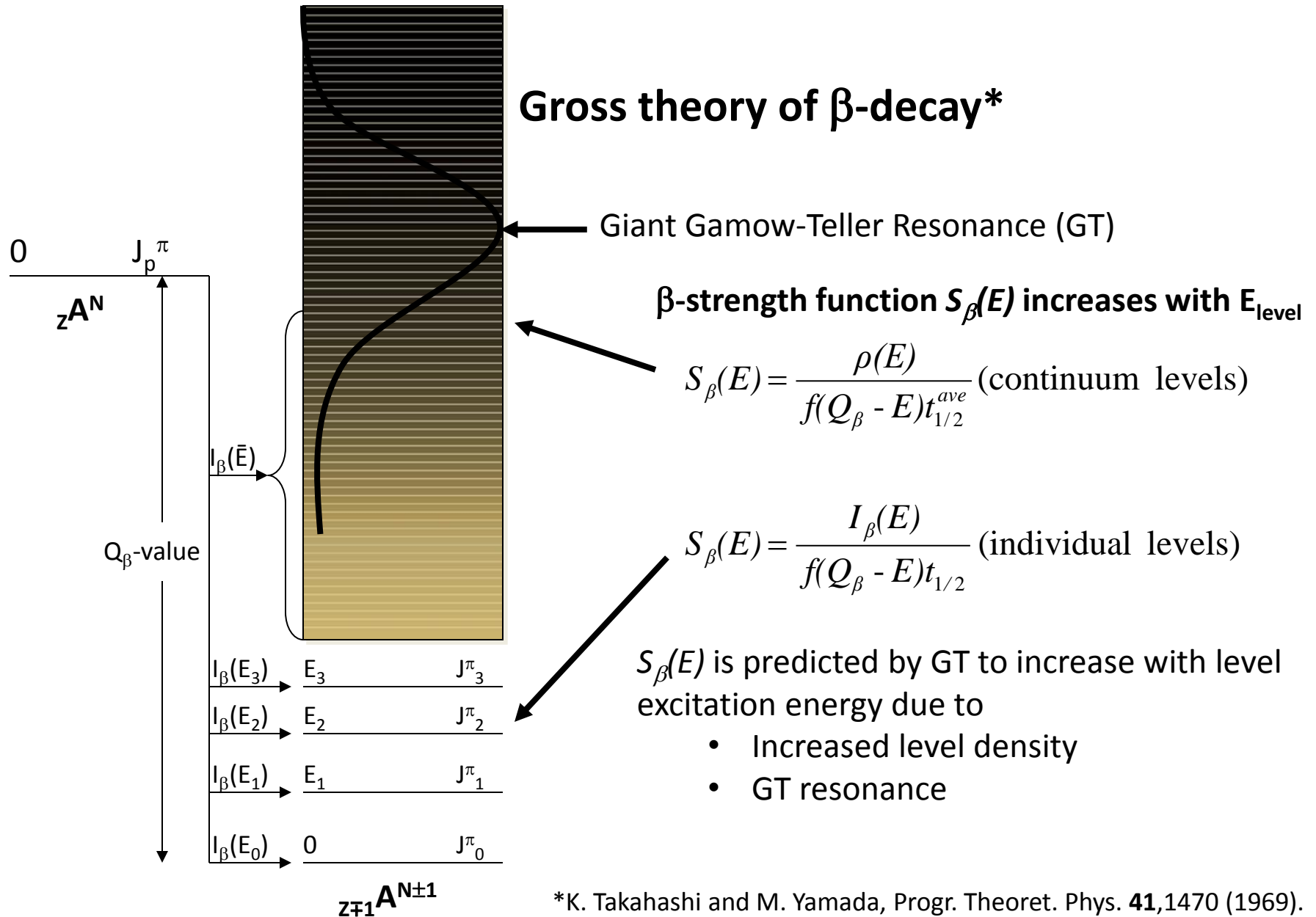


- Verified by photonuclear data *above the neutron separation energy*
- *Uncertain below the neutron separation energy S_n*
- ***Photon strength measured below S_n cannot reliably be compared to Brink-Axel.***

M1: No statistical model is available.

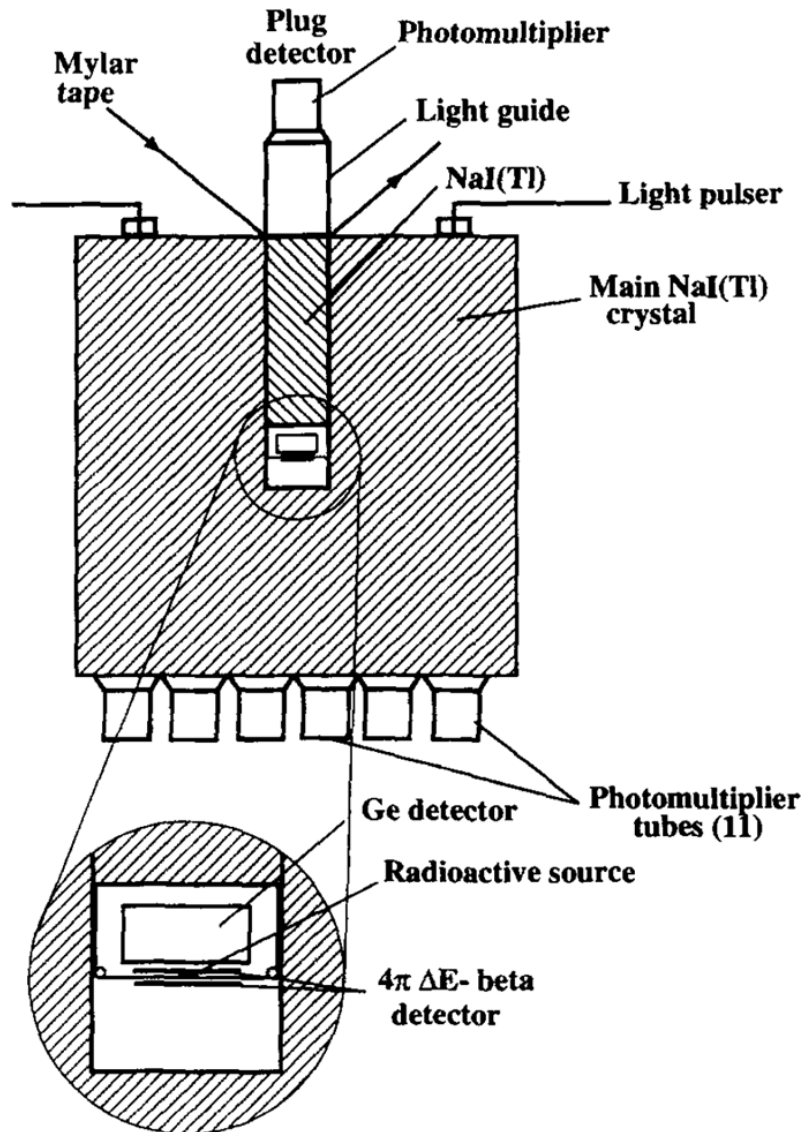
- *Single particle and scissors models may be applicable at low energies*
- *Success of Brink-Axel above S_n , where E1 is dominant, suggests that **M1 strength is very weak at high energies.***

Beta Decay Statistical Model



*K. Takahashi and M. Yamada, Progr. Theoret. Phys. **41**,1470 (1969).

LBNL Total Absorption Spectrometer (TAS)*



Measurement of β -strength with TAS

The TAS detector consisted of

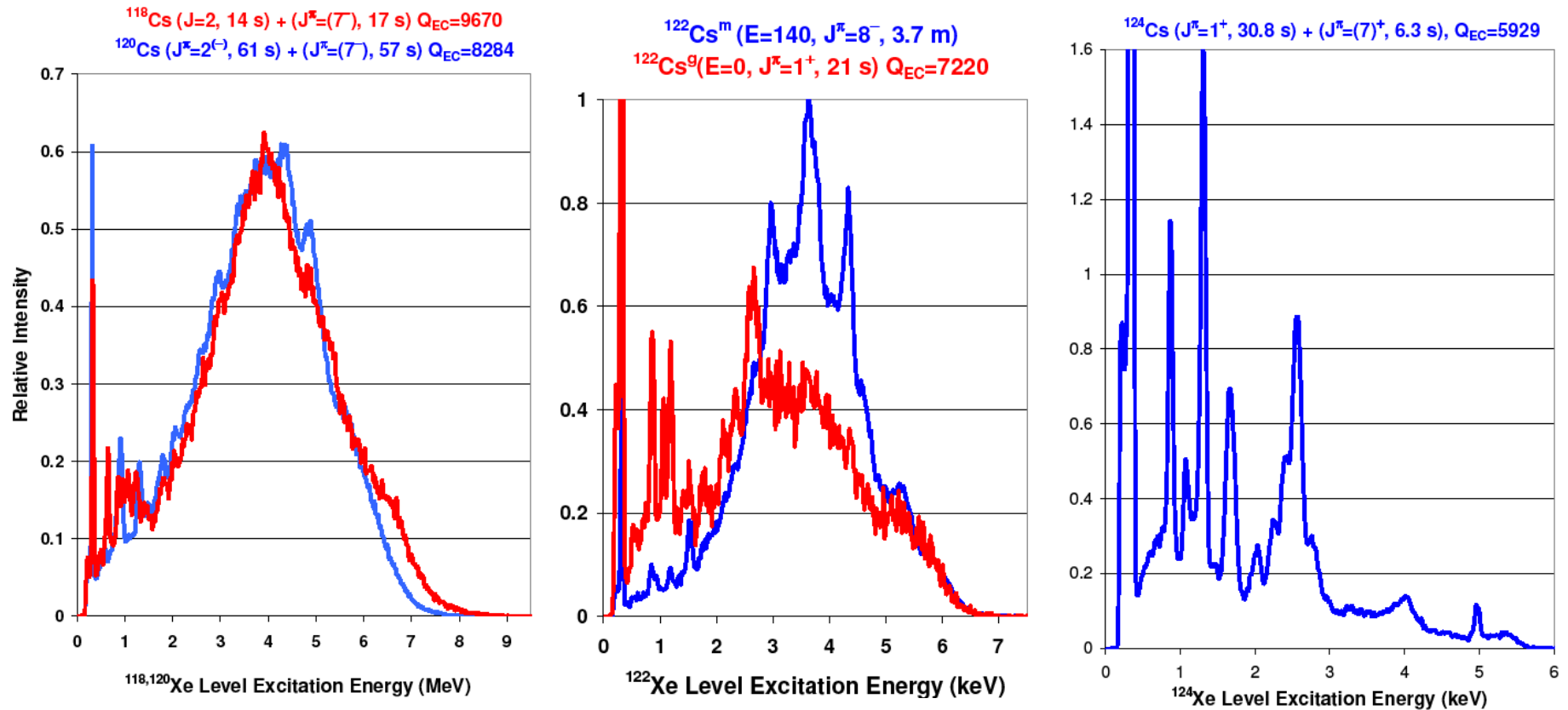
- 36×36 cm NaI(Tl) well detector with a 4×15 cm plug detector for measuring the sum γ -ray energy following decay.
- 1.6×1 cm Ge x-ray detector
- Two 1.8×0.1 Si beta detectors

The only TAS experiment at the LBNL SuperHILAC was performed in 1990. A ^{28}Si beam bombarded a $^{\text{nat}}\text{Mo}$ target to produce the isotopes $^{117-121}\text{Xe}$, $^{117-124}\text{Cs}$, and $^{122-124}\text{Ba}$.

- A identification by OASIS mass separator
- Z identification by coincident EC x-rays

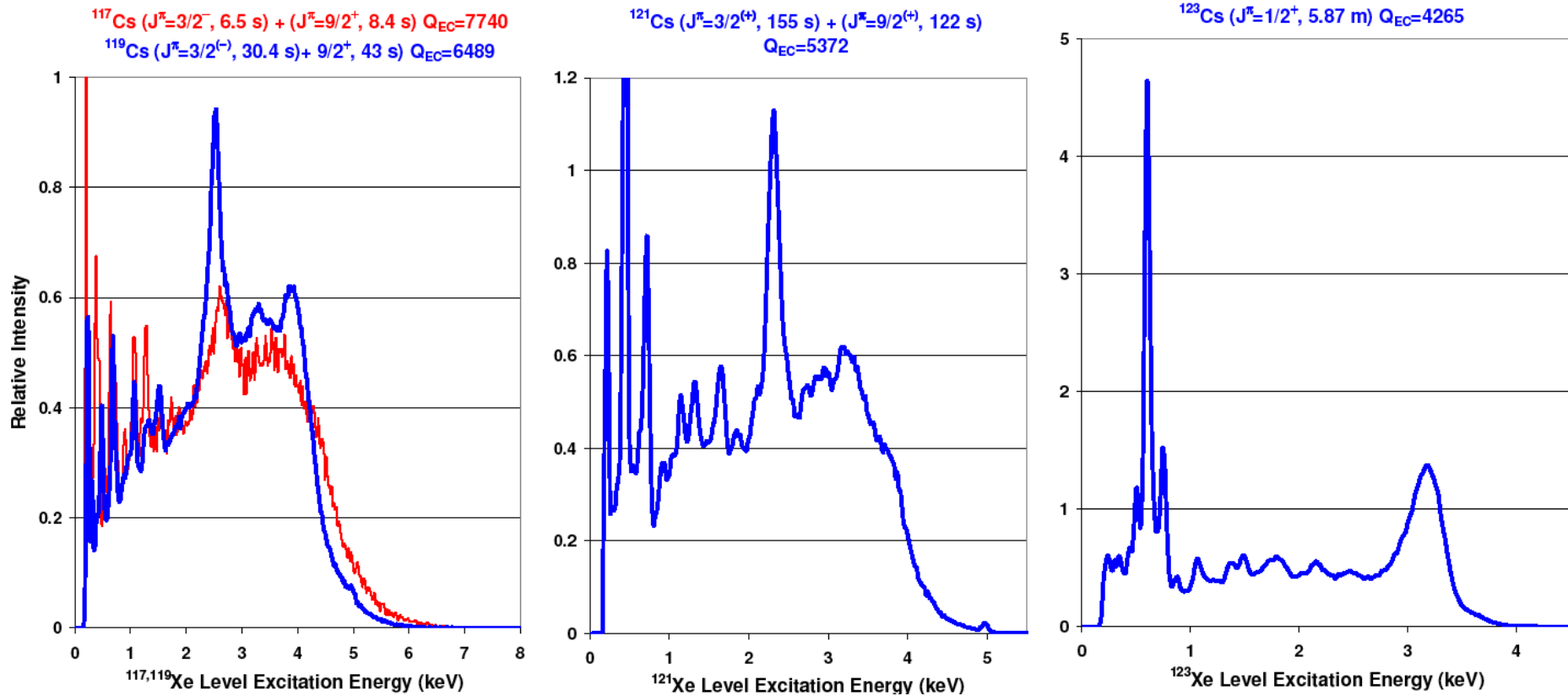
* Designed by J.M. Nitschke, TAS was moved to GSI shortly after this experiment and now lies in pieces in Berkeley.

TAS Spectra Even-A Cs Isotopes



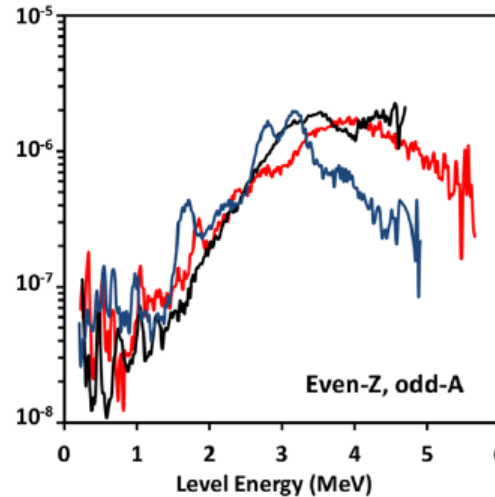
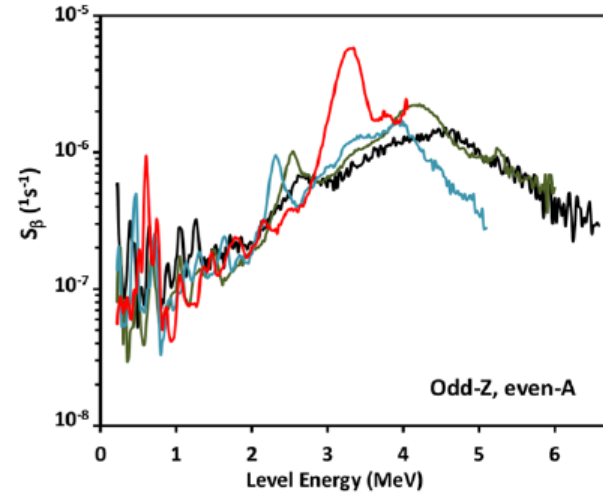
Typical spectra for $^{118-124}\text{Cs}$ decays. The TAS γ -ray spectra correspond to β -decay feeding intensities after correction for the detector response and EC/EC+ β^+ ratio. Total detection efficiency ranged from 95% (0.3 MeV) to 55% (5 MeV).

TAS Spectra Odd-A Cs Isotopes



Typical spectra for $^{117-123}\text{Cs}$ decays.

Photon Strength Functions



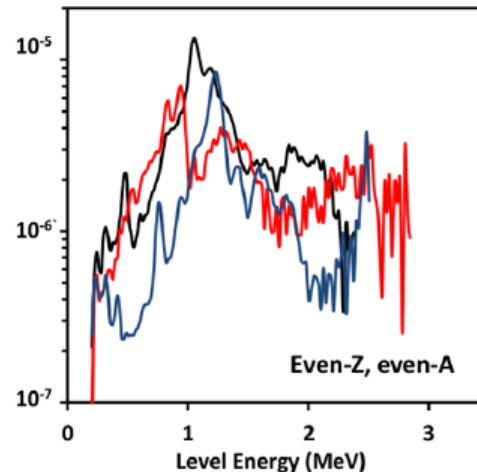
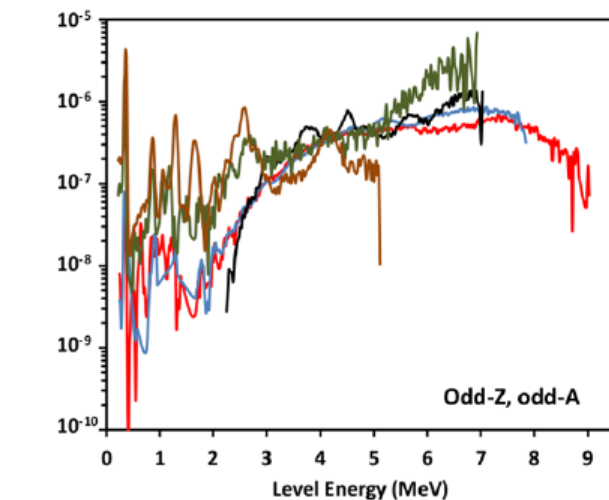
The 19 keV binned experimental strengths are comparable for each group of nuclides.

$$S_{\beta}(E) = 1/f t_{1/2}(E)$$

Note that the strength falls off dramatically above

— 117Cs (9/2+) — 119Cs (9/2+) — 121Cs (9/2+) — 123Cs (1/2+)

— 117Xe (5/2+) — 119Xe (5/2+) — 123Ba (5/2+)



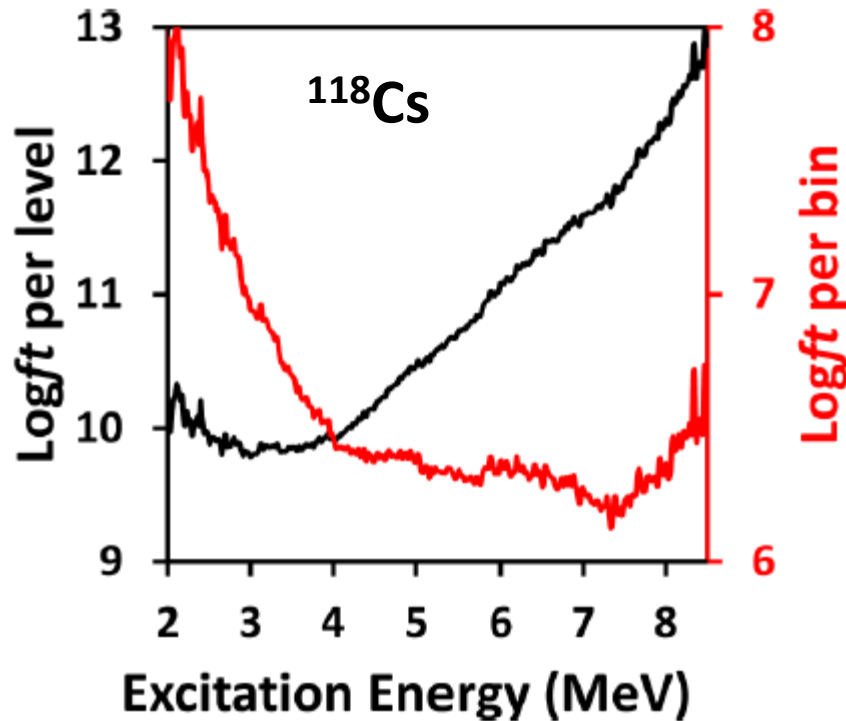
- 1 MeV: even-Z, even-N
- 3-4 MeV: even-Z, odd-N
- 4-5 MeV: odd-Z, even-N
- 7-8 MeV: odd-Z, odd-N

These results contradict the simple predictions of Gross Theory.

— 118Cs (2+) — 120Cs (2+) — 122Cs (8-)
— 122Cs (1+) — 124Cs (1+)

— 118Xe (0+) — 122Ba (0+) — 124Ba (0+)

Logft Variation

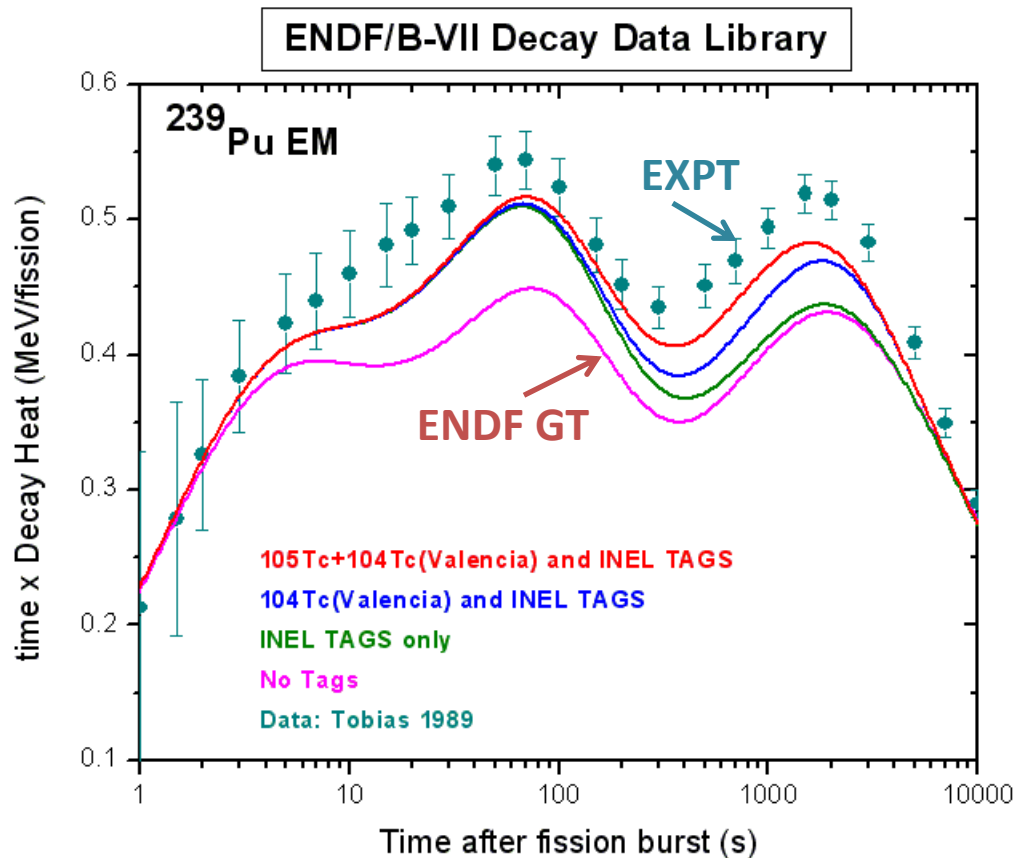


The average $\log ft$ per 19 keV energy bin increases rapidly above 7 MeV to $\log ft \approx 6.5$ at 8.5 MeV.

Correcting for the level density, the average $\log ft$ per level increases rapidly above 3 MeV to $\log ft \approx 13$ at 8.5 MeV.

These results disagree with predictions from Gross Theory

Decay Heat and Total Absorption γ -ray data



Decay heat calculations are dramatically improved by replacing ENDF Gross Theory based data with TAGS measurements from INEL (Greenwood *et al**) and Valencia (Algora *et al*#).

* NIM A, 317 (1992)

J. Korean Phys. Soc. 59,1479 (2011).

Poor agreement of the Gross Theory of β -decay with TAS and decay heat data cast doubt on the validity of this theory!

A Shell Model Approach to β -decay

The $ft_{1/2}$ value is defined as

$$ft_{1/2} = 6144 / |M|^2$$

where

$$|M|^2 = \left| \int 1 \right|^2 + \left(\frac{C_A}{C_V} \right)^2 \left| \int \sigma \right|^2$$

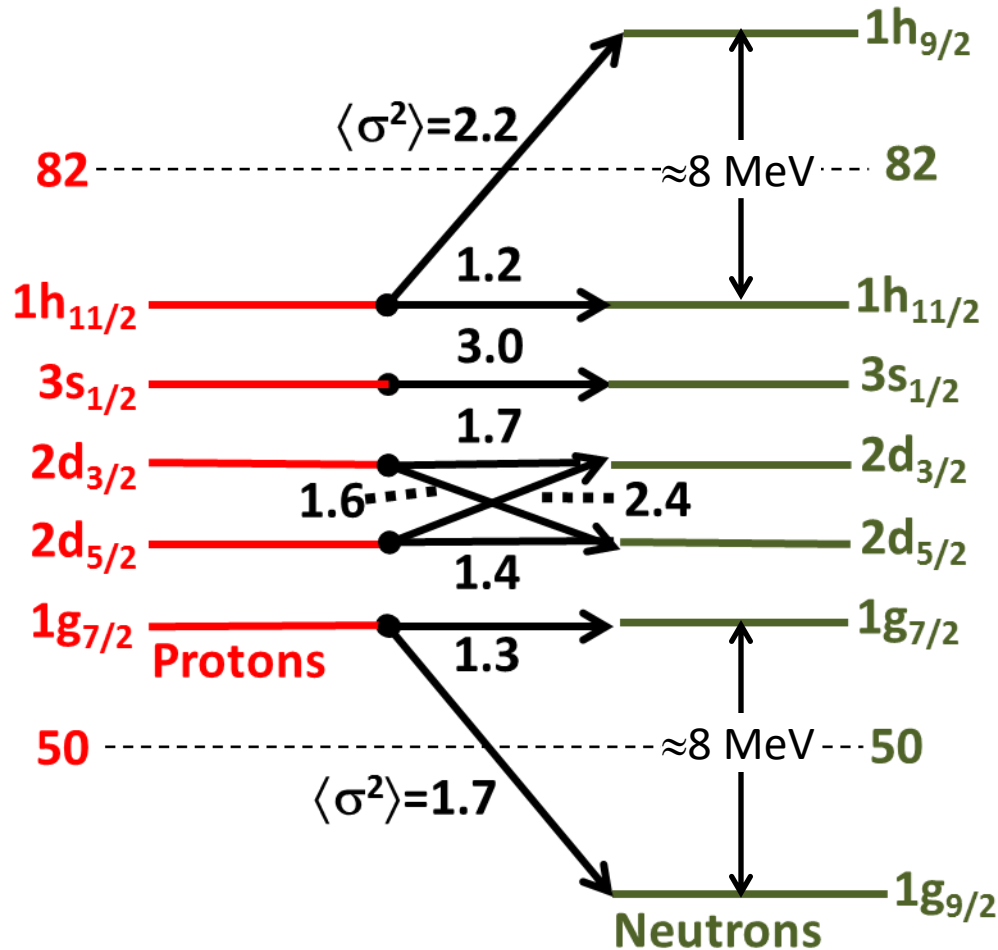
For mirror transitions, $\left| \int 1 \right|^2 = 1$, and for $0^+ \rightarrow 0^+$ transitions, $\left| \int 1 \right|^2 = 2$,

From the Shell Model

$$\left| \int \sigma \right|^2 = \left[\frac{j+1}{j} \right]^{\pm 1} \quad j_i = j_f = l \pm 1/2$$

$$\left| \int \sigma \right|^2 = \left[\frac{l + 1/2 \mp 1/2}{2l + 1} \right]^{\pm 1} \quad j_i = l \mp \frac{1}{2}, \quad j_f = l \pm 1/2$$

Shell Model



Fast Shell Model transitions available in the $4\pi\hbar$ oscillator shell to Xe, Cs, and Ba.

For light isotopes $|C_A/C_v|=1.24$ and the superallowed β -decays give

$$0^+ \rightarrow 0^+, T=1: ft_{1/2} = 3072$$

$$\text{Mirror}, T=1/2: ft_{1/2} \approx 4000-6000$$

Hypothesis: *If the superallowed β -decay to low-lying levels dominates the β -decay of light isotopes, then similar strength should be observed to low-lying levels in heavier isotopes.*

- *Strength mixed to lower levels*
- *No strength to higher levels*

For heavier nuclei we can define

$$\overline{ft}_{1/2} = \sum_{E=0}^{Q_{EC}} [S_{\beta}(E)]^{-1}$$

Results from LBNL TAS Data

A_Z	J^π	$t_{1/2}$ (s)	Q_{EC}^a (keV)	GS Feeding	Isomer ^b $J^\pi, t_{1/2}$	$[\sum S_\beta(E)]^{-1}$ ($\equiv ft$)
¹¹⁷ Xe	5/2 ⁺	61	6251	10% ^c		5900
¹¹⁷ Cs	9/2 ⁺	8.4	7690		3/2 ⁺ , 6.5 s	5800
¹¹⁸ Xe	0 ⁺	216	2892	12% ^c		2800
¹¹⁸ Cs	2 ⁺	14	9670		7 ⁻ , 17 s	10000
¹¹⁹ Xe	5/2 ⁺	348	4971	16% ^d		6200
¹¹⁹ Cs	9/2 ⁺	43	6489		3/2 ⁺ , 30.4 s	5300
¹²⁰ Xe	0 ⁺	2400	1581	38%		7100
¹²⁰ Cs	2 ⁺	61.3	8284		7 ⁻ , 57 s	9700
¹²¹ Xe	5/2 ⁺	2400	3771	28%		10800
¹²¹ Cs	9/2 ⁺	122	5445		3/2 ⁺ , 155 s	7600
¹²² Cs	1 ⁺	21.2	7070 ^e	37%		5400
¹²² Cs	8 ⁻	222	7210 ^e			9900
¹²² Ba	0 ⁺	117	3540	13% ^f		3400
¹²³ Cs	1/2 ⁺	353	4205	33%		5500
¹²³ Ba	5/2 ⁺	162	5389	12% ^c		9100
¹²⁴ Cs	1 ⁺	30.9	5930	34%		12800
¹²⁴ Ba	0 ⁺	660	2642	17% ^f		5900

Comparison of Xe, Cs, and Ba decays with superallowed/mirror decays

For isotopes with the largest Q_{EC} values, where most of the shell model β -strength is energetically accessible we find

Odd-Z, even-N Cs isotopes: $\overline{ft}_{1/2} = 5300 - 5800, \quad |M|^2 = 1.1 - 1.2$

Odd-Z, odd-N Cs isotopes: $\overline{ft}_{1/2} = 5400 - 10000, \quad |M|^2 = 0.6 - 1.1$

Even-Z, odd-N Xe isotopes: $\overline{ft}_{1/2} = 5900 - 6200, \quad |M|^2 = 1.0$

For mirror β -decays, $|M|^2 = 1.0 - 1.5$

Even-Z, even-N Xe, Ba isotopes: $\overline{ft}_{1/2} = 2800 - 3400, \quad |M|^2 = 1.8 - 2.2$

For $0^+ \rightarrow 0^+$ β -decays, $|M|^2 = 2.0$

The LBNL TAS measurements yield total beta strengths consistent with the strengths of superallowed/mirror decays in lighter isotopes.

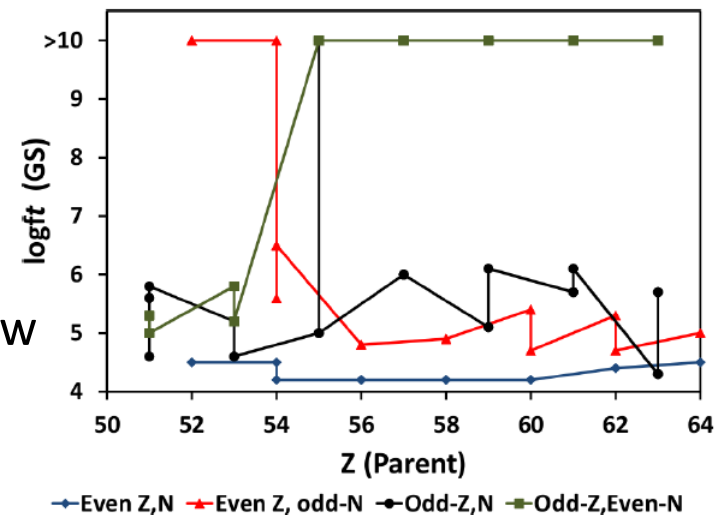
Calculation of half-lives near the proton drip line

Gross Theory is often used to calculate the half-lives of nuclei far from stability. Can the TAS β -strength data obtain similar results?

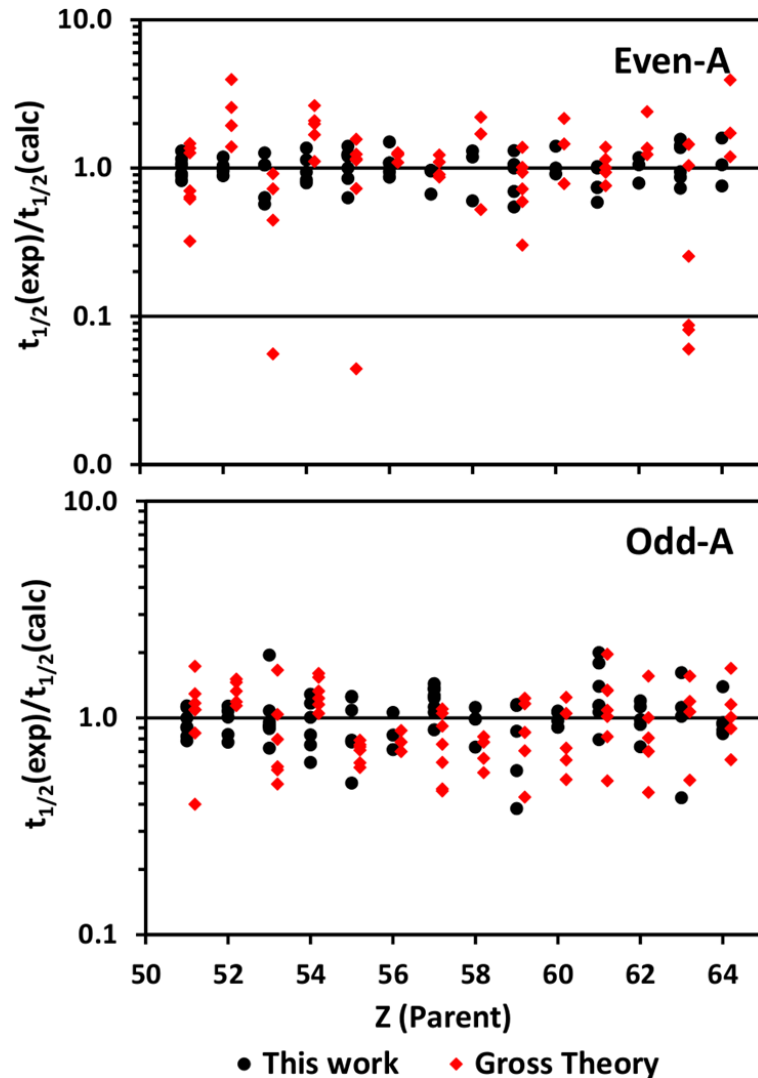
Assumption 1: The measured β -strengths from ^{117}Xe , ^{117}Cs , ^{118}Cs , and ^{122}Ba can be used as standard β -strength templates for all odd-even, odd-odd, and even-even neutron deficient isotopes with $N < 82$ and $Z = 50-64$.

Assumption 2: An additional parameter is needed for the strong β -strength to low lying levels. (note that this feeding is also needed for the Gross Theory model).

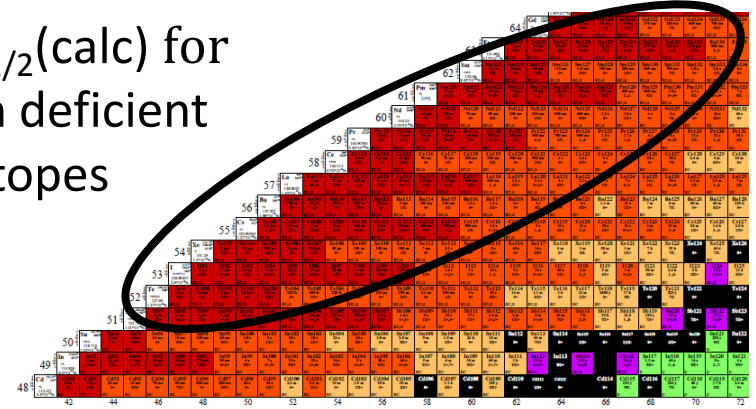
For odd-N or odd-Z isotopes the $ft_{1/2}$ to low lying levels varies with the Shell Model configuration of the GS.



Comparison of TAS Strength and Gross Theory Half-life Calculations



$t_{1/2}(\text{expt})/t_{1/2}(\text{calc})$ for
143 neutron deficient
Z=51-64 isotopes



TAS β -strength

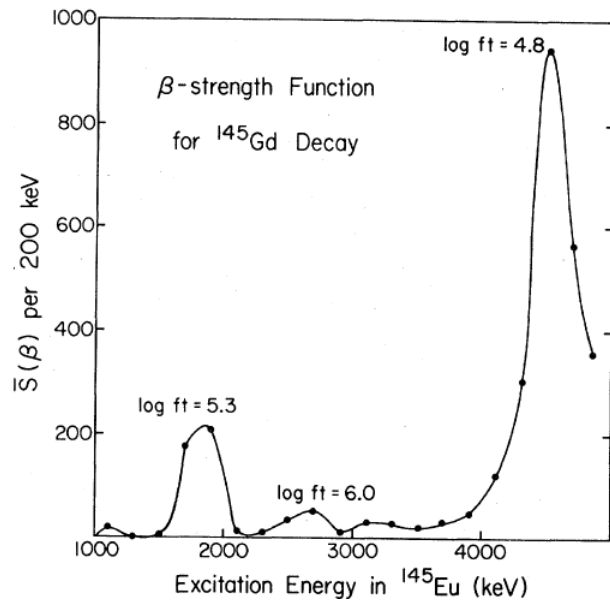
$\chi^2/f=1.0$ assuming a theoretical
uncertainty of **20%** for all isotopes.

Gross Theory β -strength*

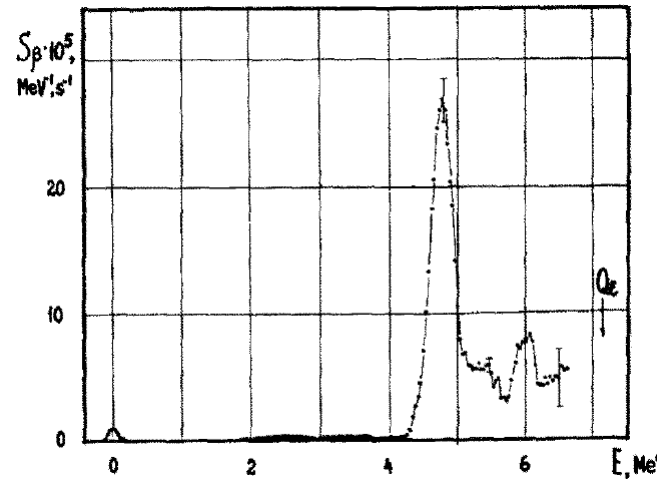
$\chi^2/f=1.0$ assuming a theoretical
uncertainty of **33%** for odd-A nuclei
and **73%** for even-A nuclei.

*Nuclear Data Center JAEA, 2013

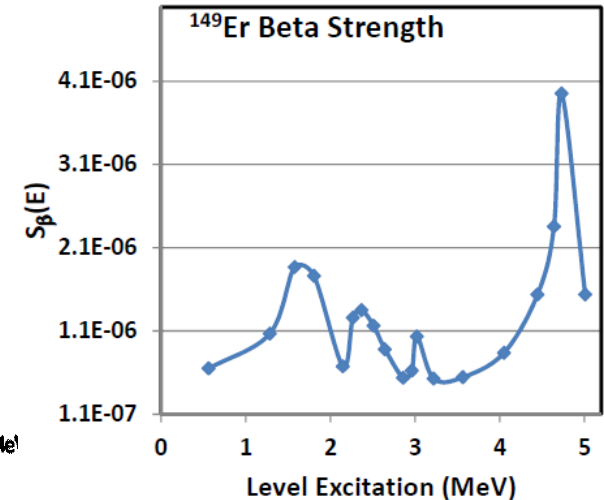
Application of template method to heavier isotopes



Firestone et al, PRC25, 527(1982)
 $Q_{\text{EC}}=5068$, $\overline{ft}_{1/2}=39,000$



Alkhozov et al, NPA 438, 482 (1985)
 $Q_{\text{EC}}=6546$, $\overline{ft}_{1/2}=10,000$

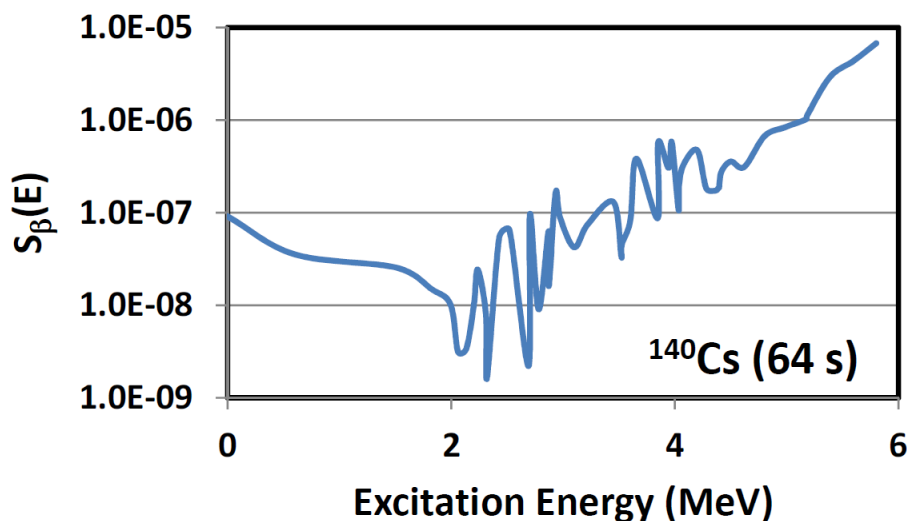


Firestone et al, PRC39, 219 (1988)
 $Q_{\text{EC}}=7920$, $\overline{ft}_{1/2}=13000$

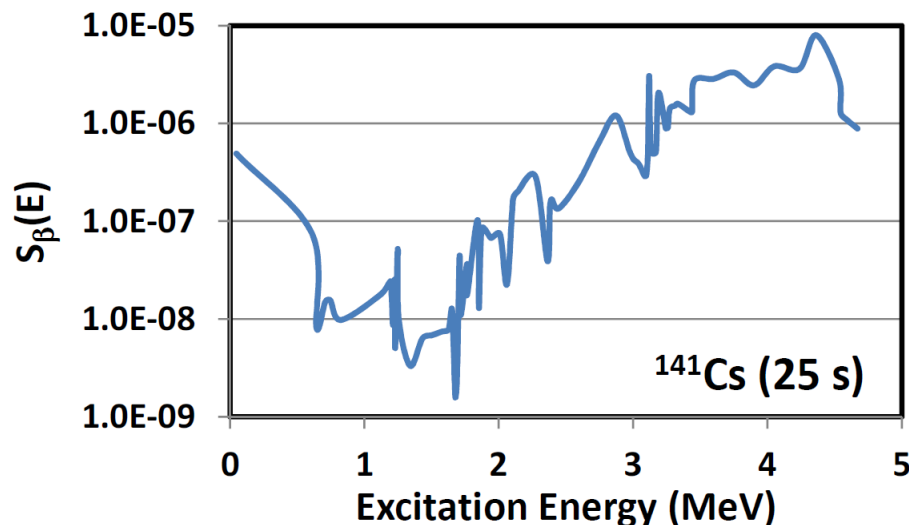
N=81: The only allowed decay channel open is the $\pi h_{11/2} \rightarrow \nu h_{9/2}$ spin flip transition. Single particle $\overline{ft}_{1/2}=2900$ is much lower than observed values.

Missing strength at higher excitations? Higher energy template needed?

Neutron Rich Cs Isotopes



$$\overline{ft}_{1/2} = 25,000$$



$$\overline{ft}_{1/2} = 18,000$$

Data from INEL Total Absorption Gamma Spectrometer (TAGS)*

Experimental β -strengths do not peak within experimental energy window. These data would be incomplete templates for extrapolation to heavier Cs isotopes.

*R.G. Helmer et al, NIMA 339, 189 (1994).

Calculation of Cs Half-lives

1. Extrapolate standard $S_\beta(E)$ to higher energies with a broad peak at 7 MeV with $S_\beta(E)_{\max} = 2.5 \times 10^{-5}$, 1 MeV fwhm for odd- and even-A Cs isotopes

2. Calculate half-life

$$t_{1/2} = c \sum_{E=0}^{Q_{EC}} (1/S_\beta(E)): \quad c(^{140}\text{Cs})=0.29, \quad c(^{141}\text{Cs})=0.23$$

The reason for renormalization of $S_\beta(E)$ is unknown.

Isotope	J^π	$t_{1/2}(\text{expt})$	$t_{1/2}(\text{calc})$	$t_{1/2}(\text{GT})$
^{142}Cs	0^-	1.684(14) s	3.9 s	3.3 s
^{143}Cs	$3/2^+$	1.791(7) s	1.9 s	3.1 s
^{144}Cs	$1^{(-)}$	0.994(6) s	0.97 s	1.6 s
^{145}Cs	$3/2^+$	0.587(5) s	0.51 s	1.2 s
^{146}Cs	1^-	0.321(2) s	0.36 s	0.68 s
^{147}Cs	$(3/2^+)$	0.230(1) s	0.24 s	0.27 s
^{148}Cs		0.146(6) s	0.13 s	0.16 s
^{149}Cs		>50 ms	101 ms	94 ms
^{150}Cs		>50 ms	47 ms	85 ms

For the $^{144-148}\text{Cs}$ calculations

This work: $\chi^2/f=1$ for $\Delta t_{1/2}=9\%$

Gross Theory: $\chi^2/f=1$ for $\Delta t_{1/2}=37\%$

Conclusions

- β -strength measurements with the LBNL TAS spectrometer for neutron deficient Xe, Cs, and Ba isotopes are inconsistent with predictions of the Gross Theory of β -decay
- Total β -strengths for neutron deficient isotopes are consistent with shell model predictions.
- Half-lives of neutron deficient isotopes can be calculated with good accuracy using measured TAS templates.
- Total β -strengths for neutron rich isotopes are consistent with decay across shell gaps
- Half-lives of neutron rich isotopes may be calculated with good accuracy using TAS templates that are extrapolated to higher energies
- ***Lessons from β -strength analysis should apply to M1 γ -rays.***