

Test of IMME in fp shell via direct mass measurements of $T_z = -3/2$ nuclides

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CSRe Mass Measurement Collaboration

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Outline

1. Introduction
2. Mass measurements in CSRe
3. Test the IMME in fp-shell nuclides
4. Summary

1. Introduction

Isospin

Isospin projection (good quantum number)

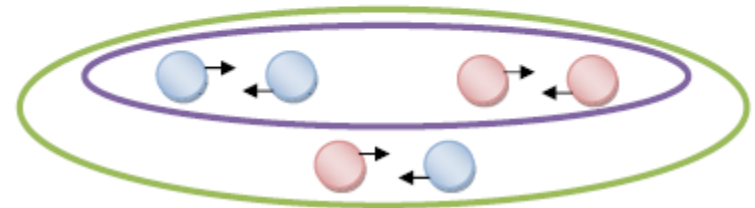
$$T_Z = \sum_{i=1}^A t_{z,i} = \frac{N-Z}{2}$$

Charge Symmetry: $V_{pp} = V_{nn}$

Charge Independence: $V_{pp} = V_{nn} = V_{pn}$

Isospin

$$\left| \frac{N-Z}{2} \right| \leq T \leq \frac{N+Z}{2} \quad \text{and } T \geq T_Z$$

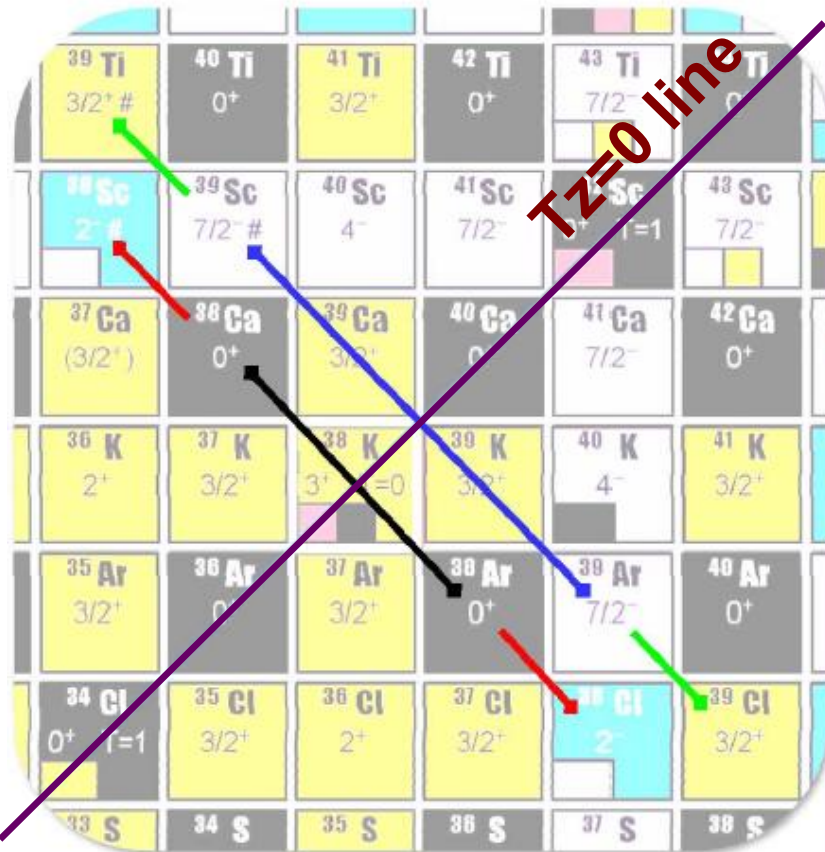


1932: Heisenberg applies the Pauli matrices to the problem of labelling the two charge states of the nucleon.

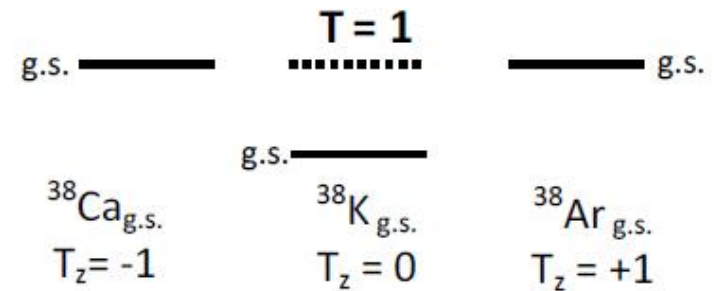
1937: Wigner points to isospin as a good quantum number to characterize isotopic multiplets (or isospin multiplets).

1. Introduction

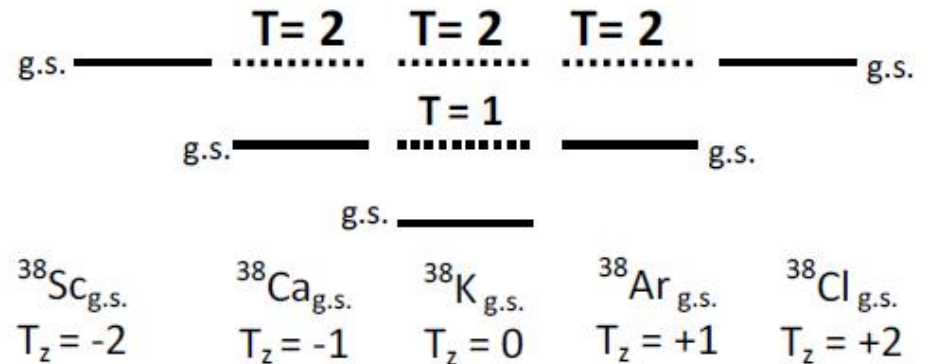
Isospin Multiplet



T=1 isobar multiplet members, IAS same spin-parity



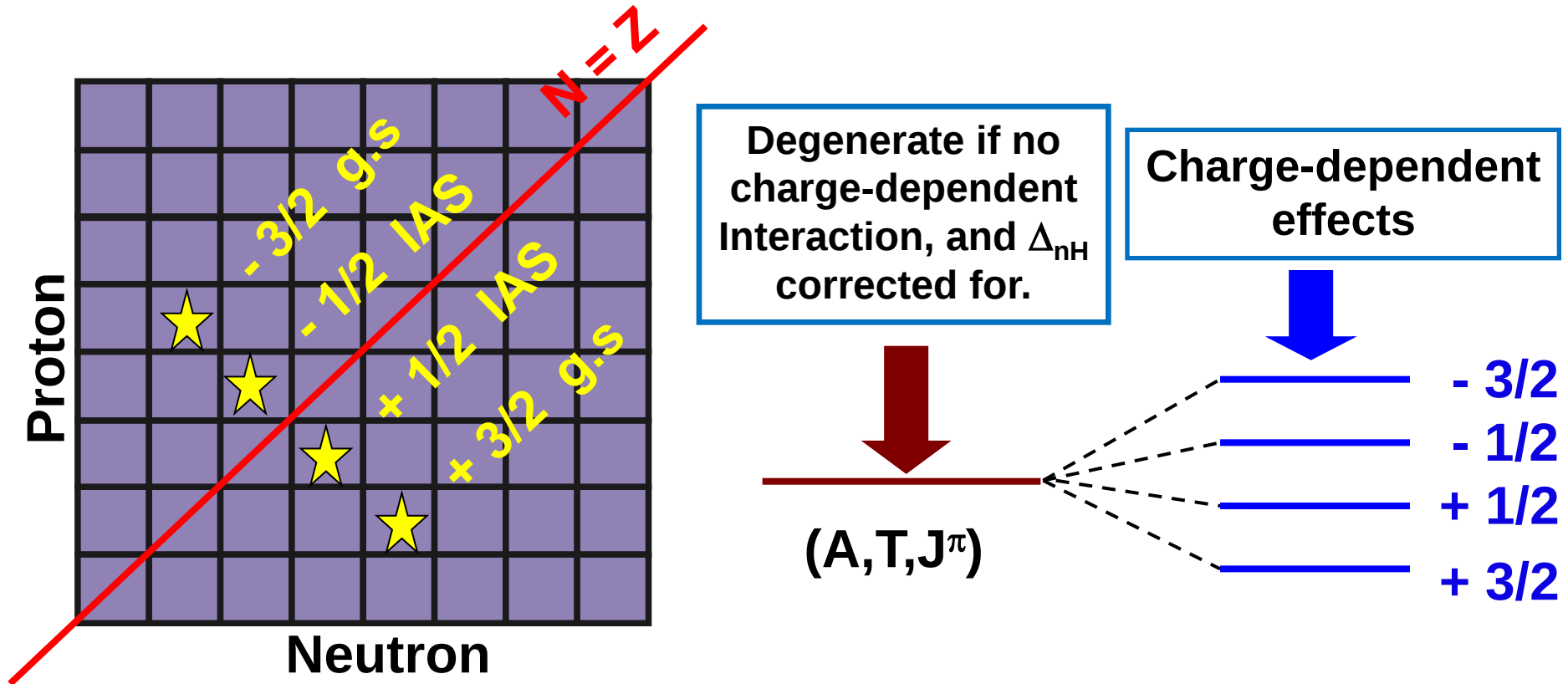
T=2 isobar multiplet members, IAS same spin-parity



1. Introduction

$T=3/2$ quartet

Isospin Multiplet Mass Equation

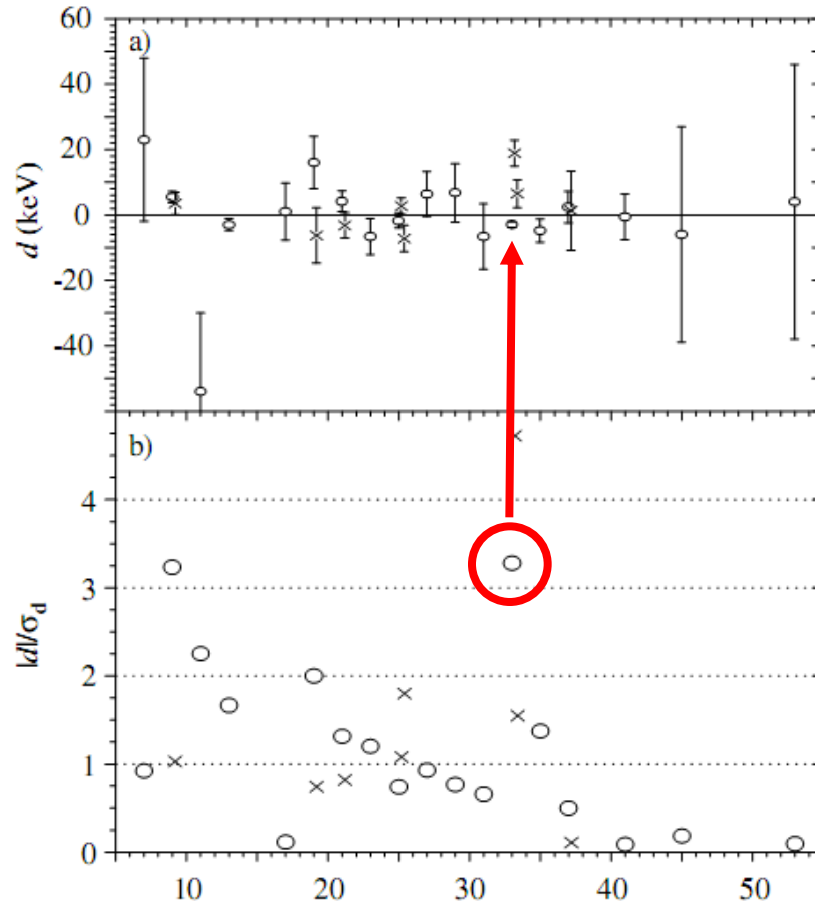


$$M(A, T, T_z) = a(A, T) + b(A, T)T_z + c(A, T)T_z^2$$

Any charge-dependent effects are two body interactions and be regarded as a perturbation.

Test the IMME: the case of $A=33, T=3/2$

$$M(T, A, T_3) = a(T, A) + b(T, A)T_3 + c(T, A)T_3^2 + d(T, A)T_3^3$$



Breakdown of the Isobaric Multiplet Mass Equation at $A=33, T=3/2$

F. Herfurth, [PhysRevLett.87.142501\(2001\)](#)

Related publications

Breakdown of the Isobaric Multiplet Mass Equation at $A=33$, $T=3/2$

F. Herfurth,^{1,3,*} J. Dilling,¹ A. Kellerbauer,^{2,5} G. Audi,⁴ D. Beck,^{6,1} G. Bollen,^{3,8}
H.-J. Kluge,¹ D. Lunney,⁴

DOI: [10.1103/PhysRevLett.87.142501](https://doi.org/10.1103/PhysRevLett.87.142501)(2001)

Revalidation of the Isobaric Multiplet Mass Equation

M. C. Pyle,¹ A. García,¹ E. Tatar,¹ J. Cox,¹ B. K. Nayak,¹ S. Triambak,¹ B.
Laughman,¹ A. Komives,¹ L. O. Lamm,¹

DOI: [10.1103/PhysRevLett.88.122501](https://doi.org/10.1103/PhysRevLett.88.122501) (2002)

Masses of ^{32}Ar and ^{33}Ar for Fundamental Tests

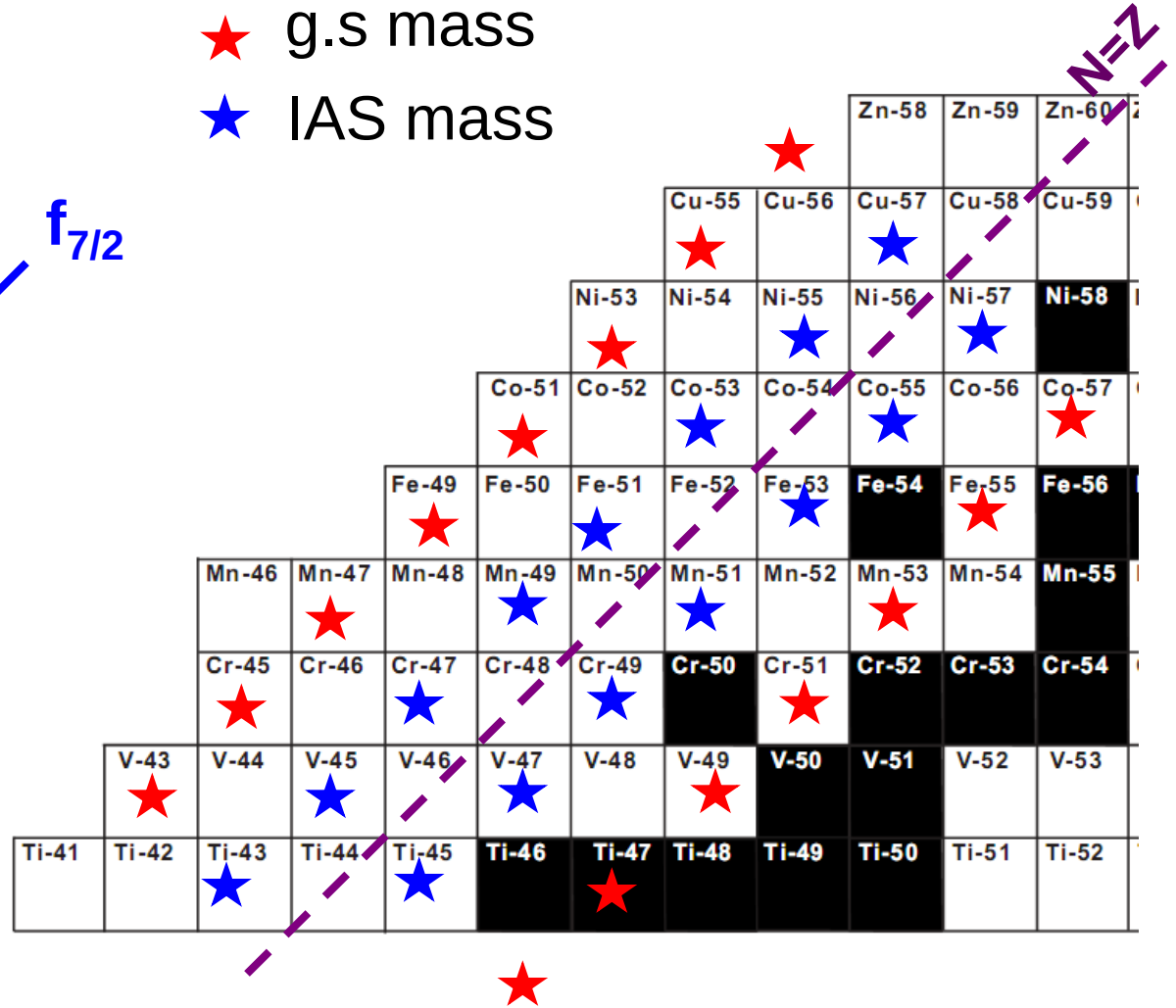
K. Blaum,^{1,2,*} G. Audi,³ D. Beck,² G. Bollen,⁴ F. Herfurth,¹ A. Kellerbauer,¹ H.-J.
[PhysRevLett.91.260801](https://doi.org/10.1103/PhysRevLett.91.260801) (2003)

[PHYSICAL REVIEW C 73, 054313 \(2006\)](#)

Mass of the lowest $T = 2$ state in ^{32}S : A test of the isobaric multiplet mass equation

[S.Triambak](#), [A.Garcia](#), [E.G.Adelberger](#), [G.J.P.Hodges](#), [D.Melconian](#), [H.E.Swanson](#),
[S.A.Hoedl](#), [S.K.L.Sjue](#), [A.L.Sallaska](#), [H.Iwamoto](#) [S.Triambak](#), [A.Garcia](#),
[E.G.Adelberger](#), [G.J.P.Hodges](#), [D.Melconian](#), [H.E.Swanson](#), [S.A.Hoedl](#), [S.K.L.Sjue](#),
[A.L.Sallaska](#), [H.Iwamoto](#)

- ★ g.s mass
- ★ IAS mass



2. Mass measurements in CSRe



SSC(K=450)

100 AMeV (H.I.), 110 MeV (p)

SFC (K=69)

10 AMeV (H.I.), 17~35 MeV (p)



RIBLL1

RIBs at tens of AMeV

CSRe

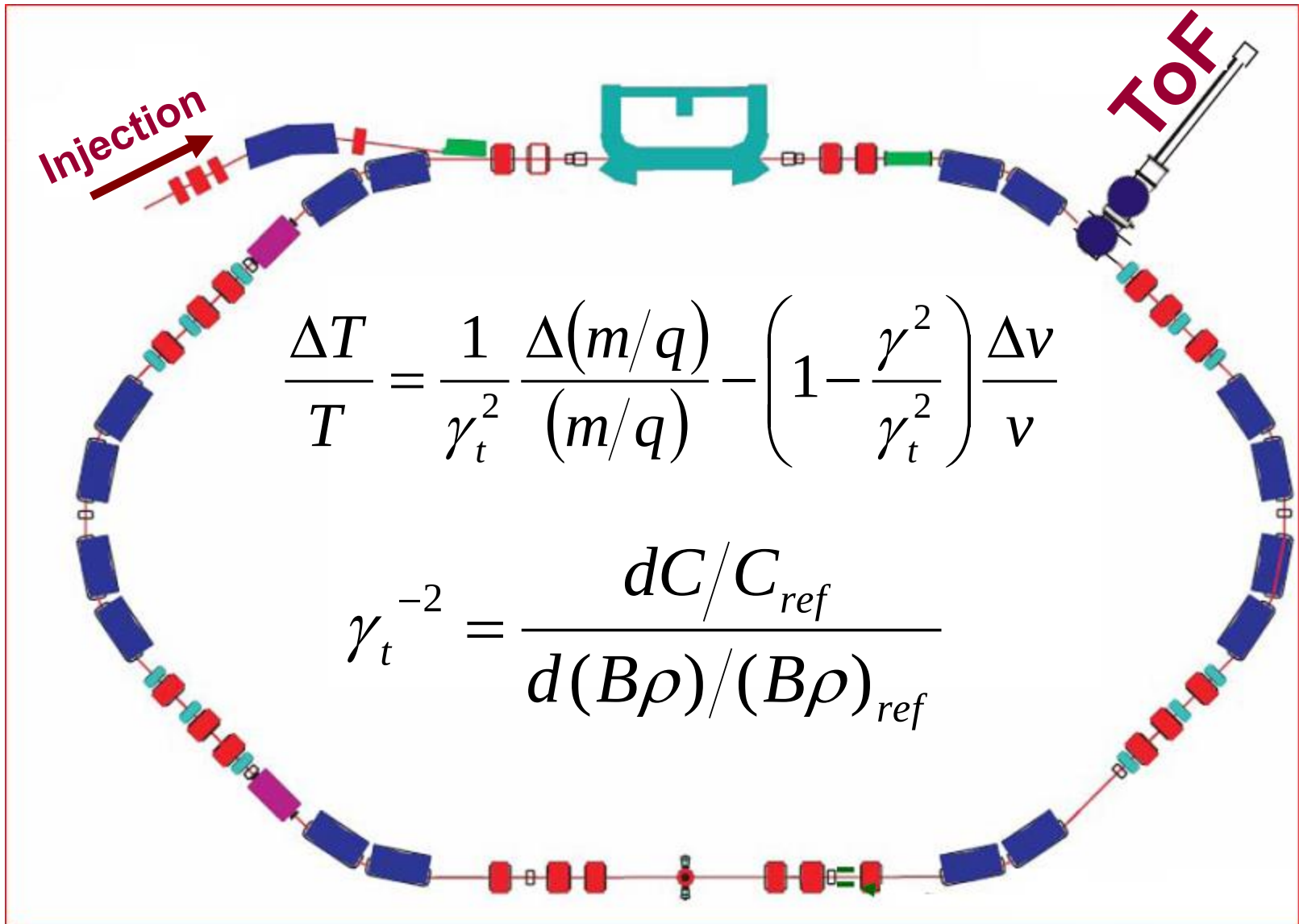
RIBLL2

RIBs at hundreds of AMeV

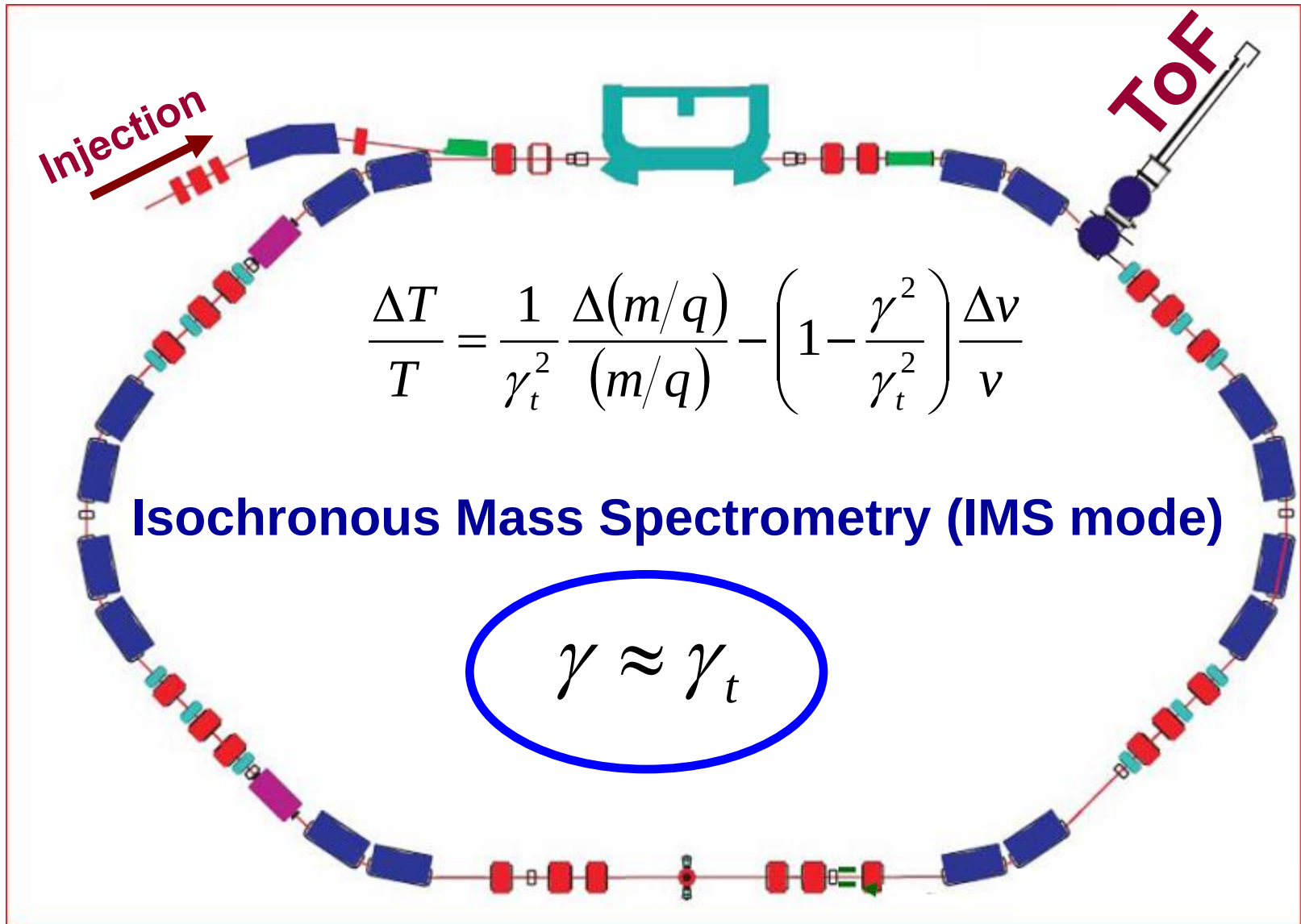
CSRm

1000 AMeV (H.I.), ≤ 2.8 GeV (p)

Principle of mass measurement in CSRe

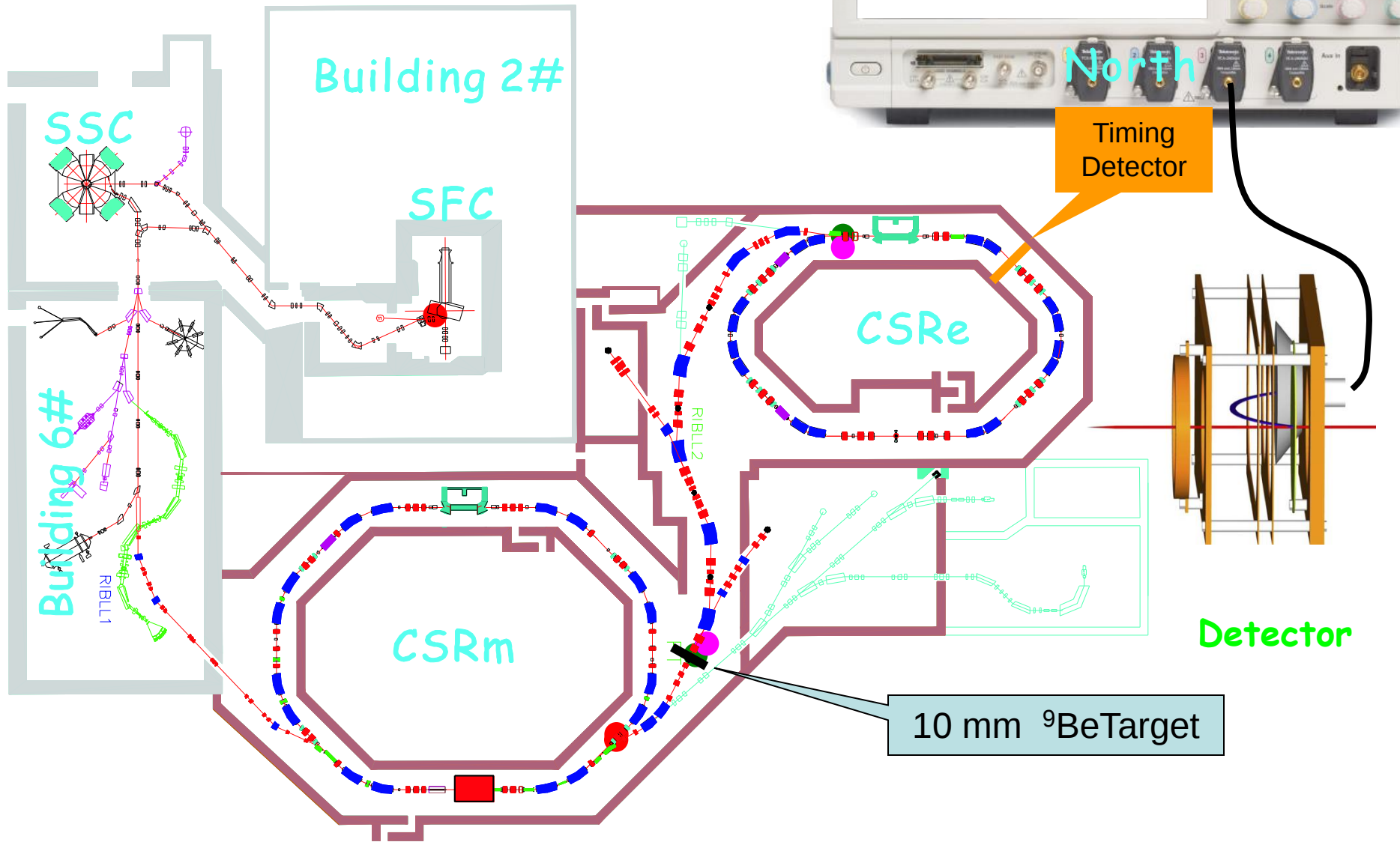


Principle of mass measurement in CSRe



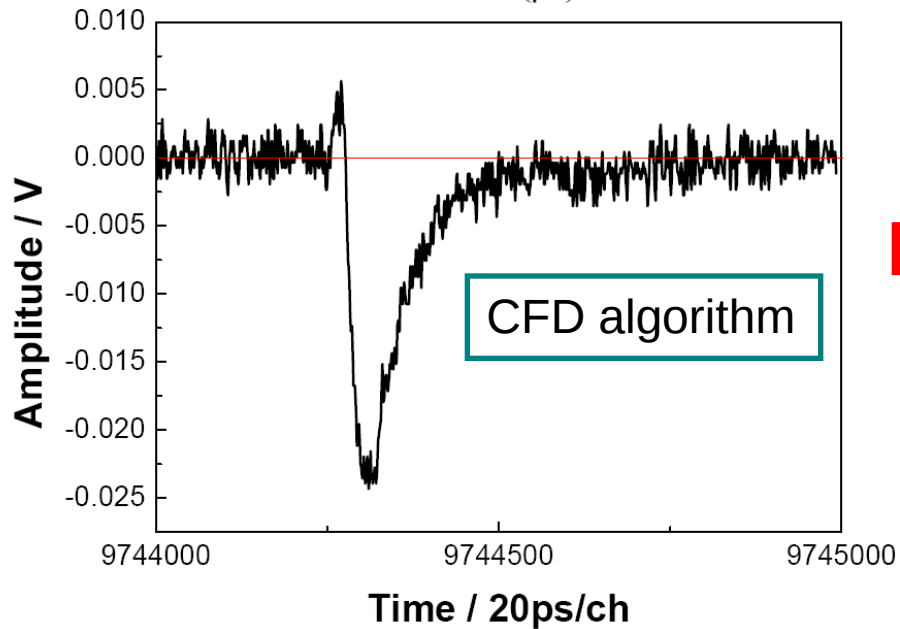
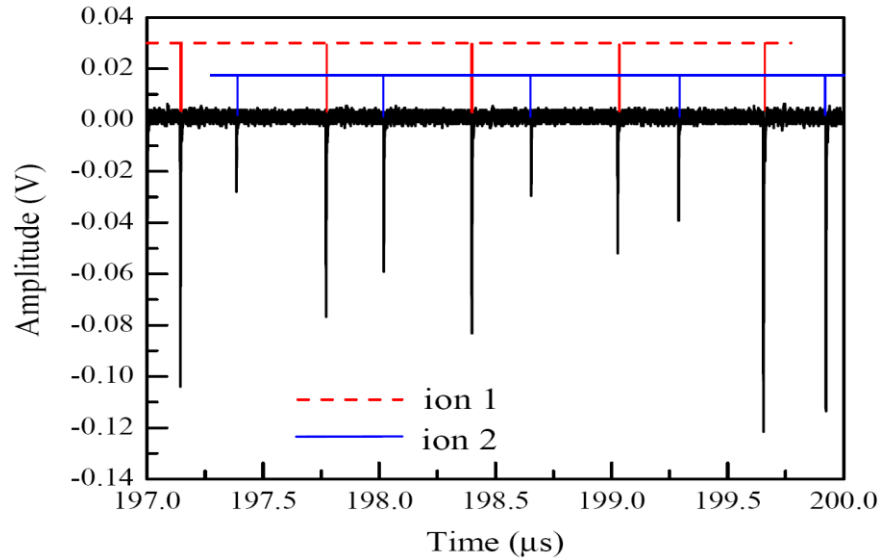
Measurement

$$\gamma_t = 1.395 \text{ --- } 460 \text{ MeV/u}$$

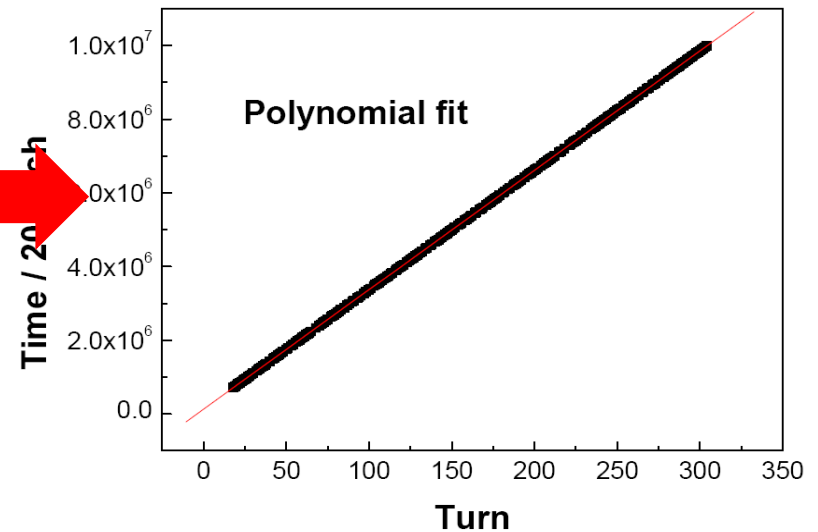
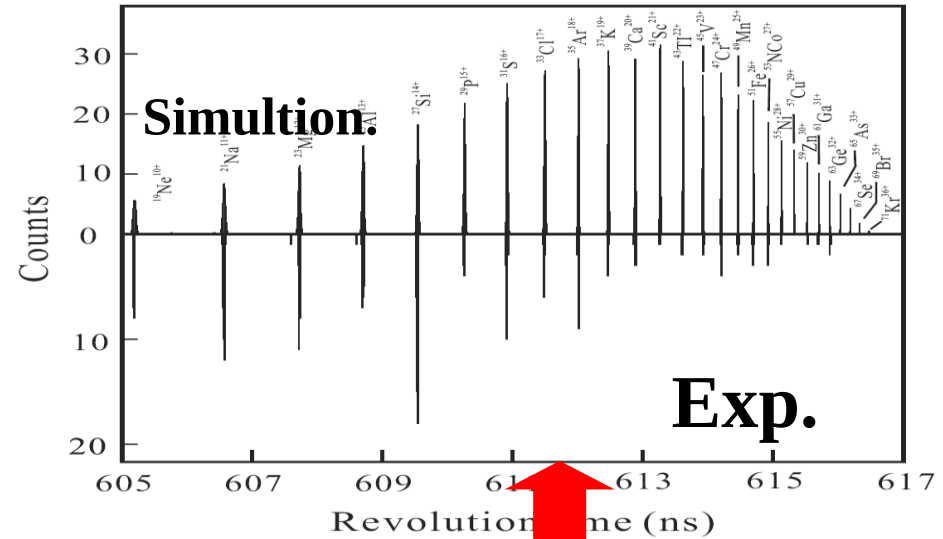


Procedure of Data analysis

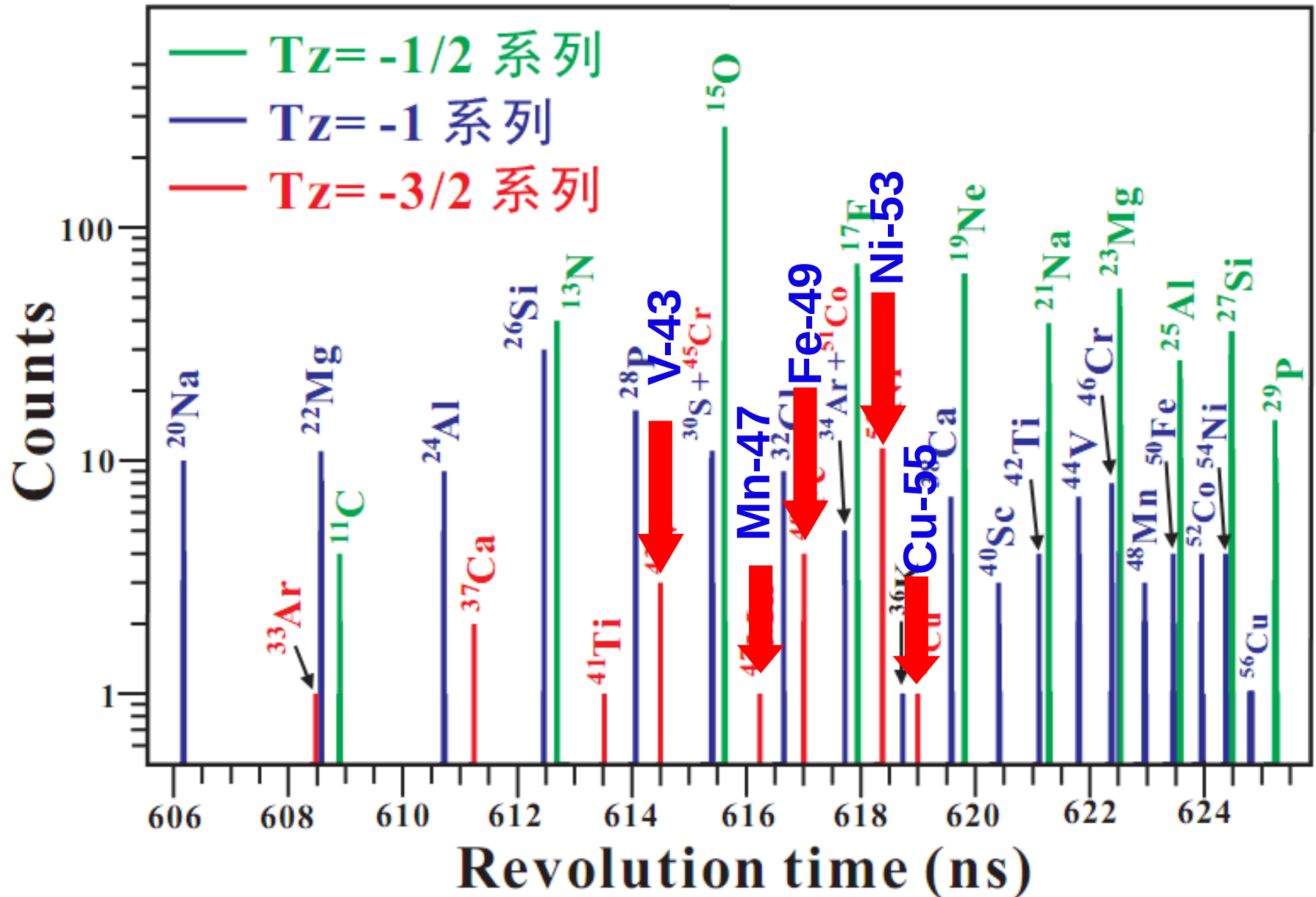
Signals in Oscilloscope



Ions Identification



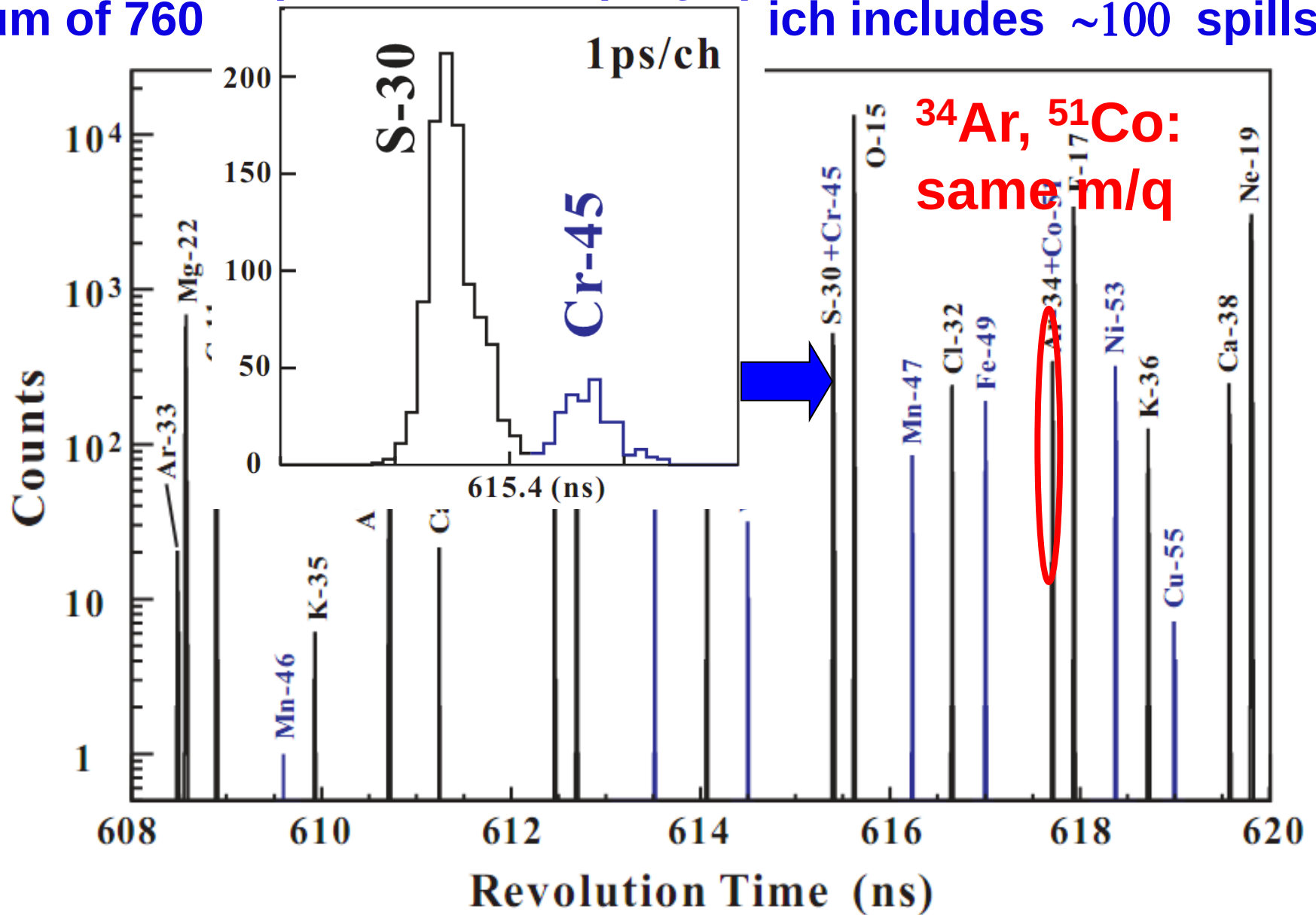
^{58}Ni beam: Revolution Time Spectrum



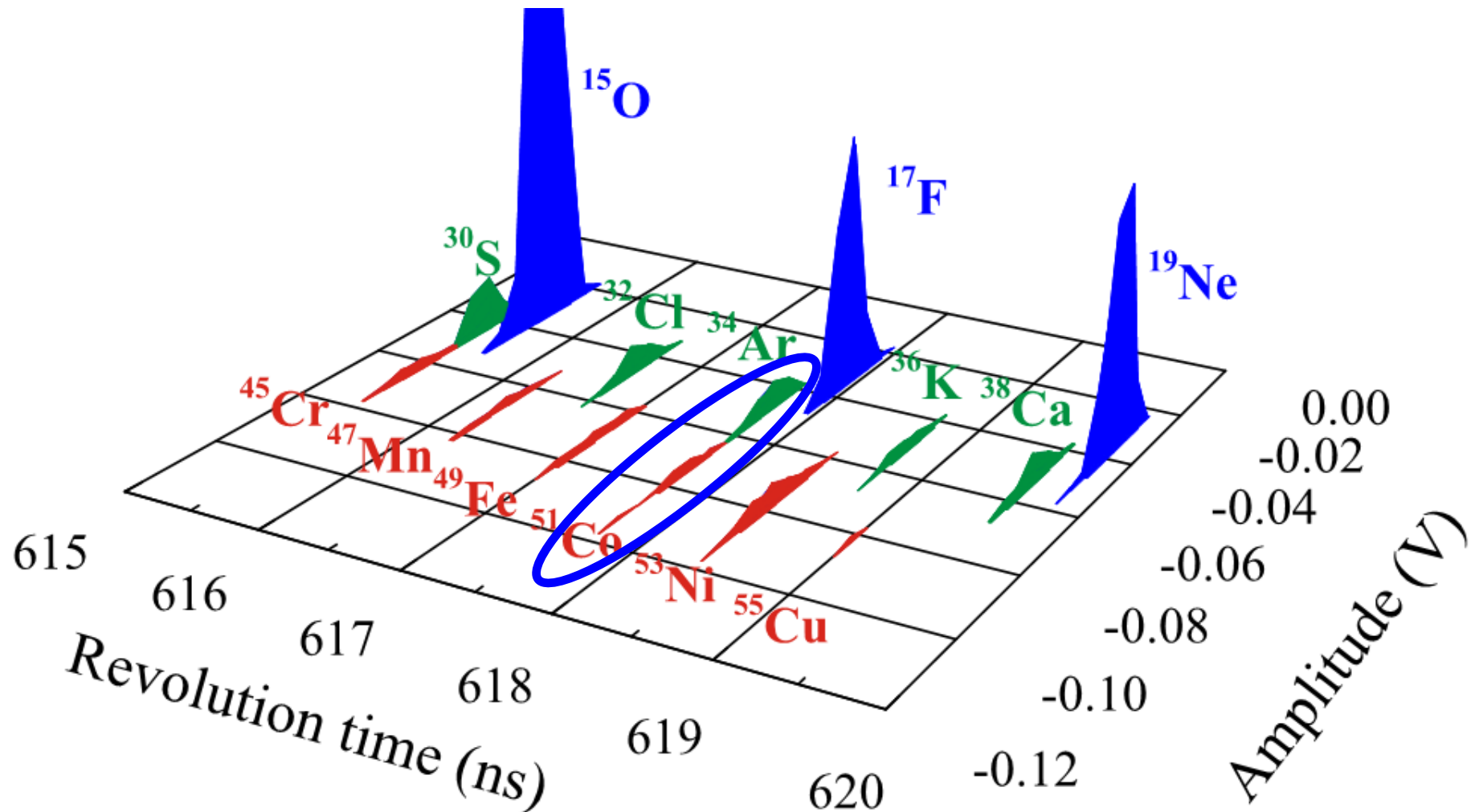
^{58}Ni beam: Revolution Time Spectrum

Sum of 760

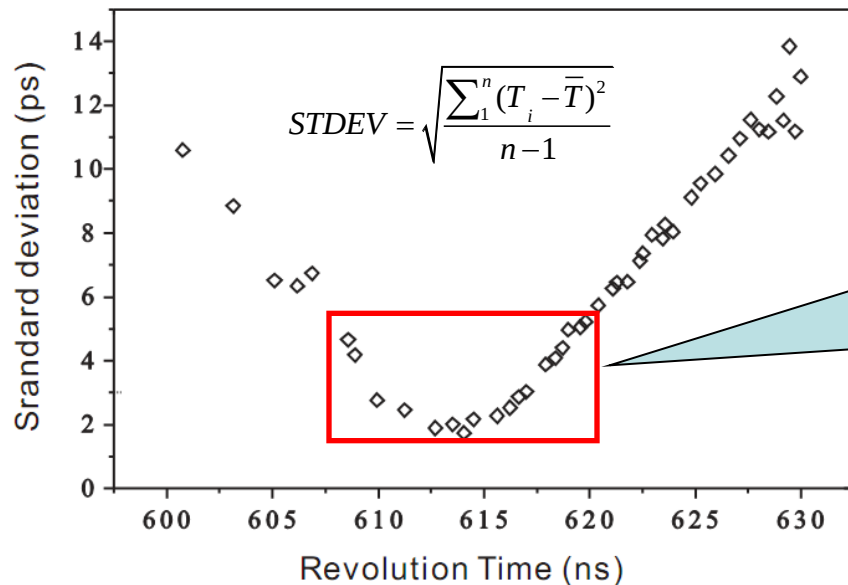
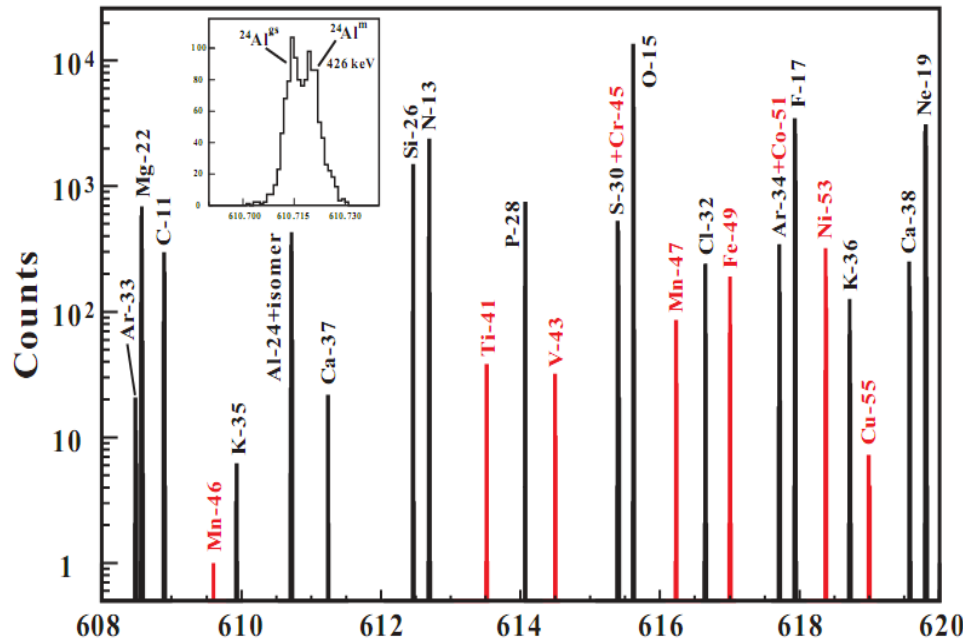
ich includes ~100 spills



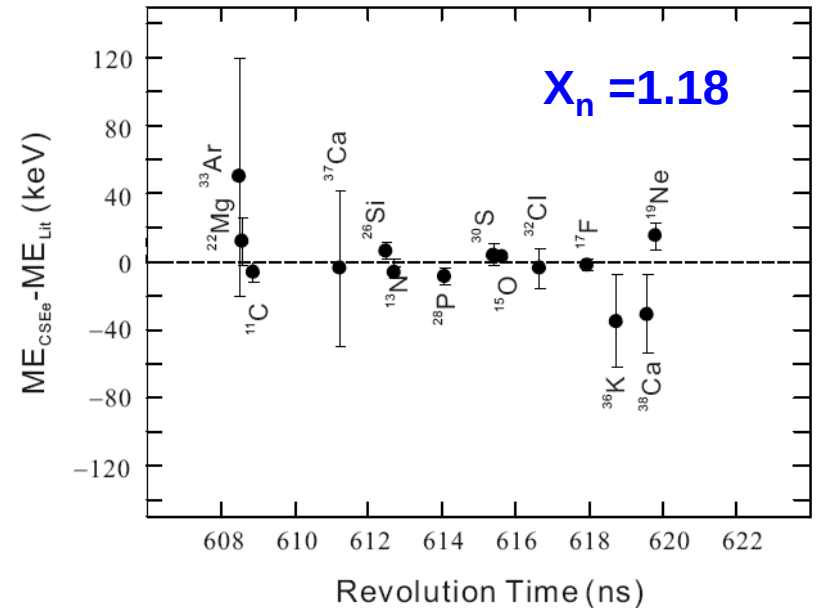
Ion-amplitude identification: ^{51}Co



Mass excesses for the nuclides of interest (^{58}Ni beam)



$$M/q = a + b T + c T^2 + d T^3$$



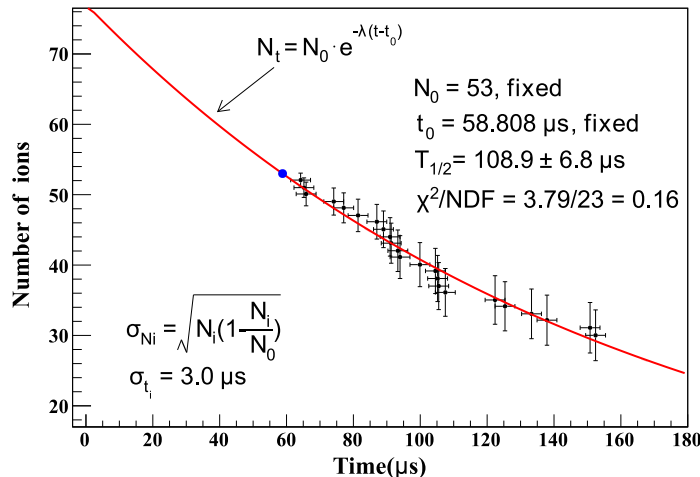
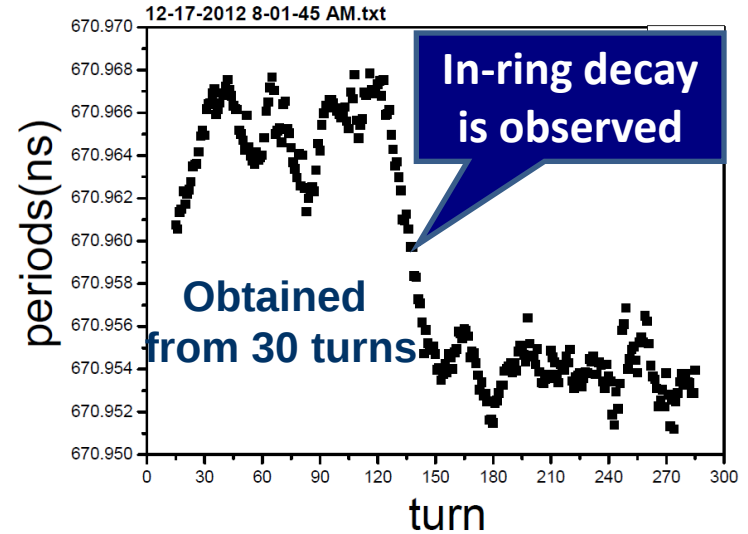
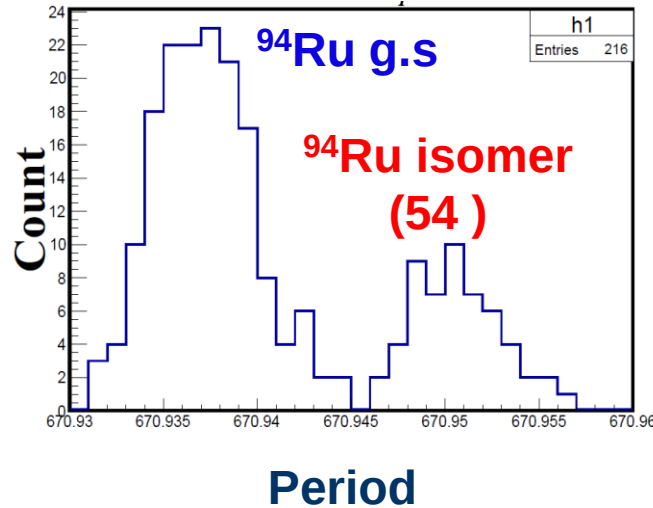
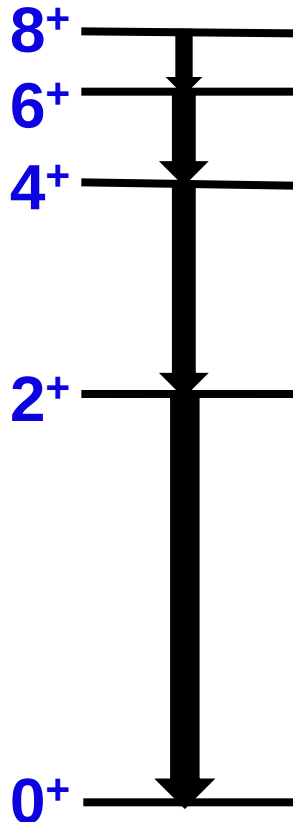
Nuclides for Calibration:

Nuclides used for M/q calibration are within a time window which is not far from the isochronous condition.

Mass and $T_{1/2}$ of short-lived Isomers in ^{94}Ru

$$T_{1/2} = 71 \mu\text{s}$$

$$E_x = 2645 \text{ KeV}$$



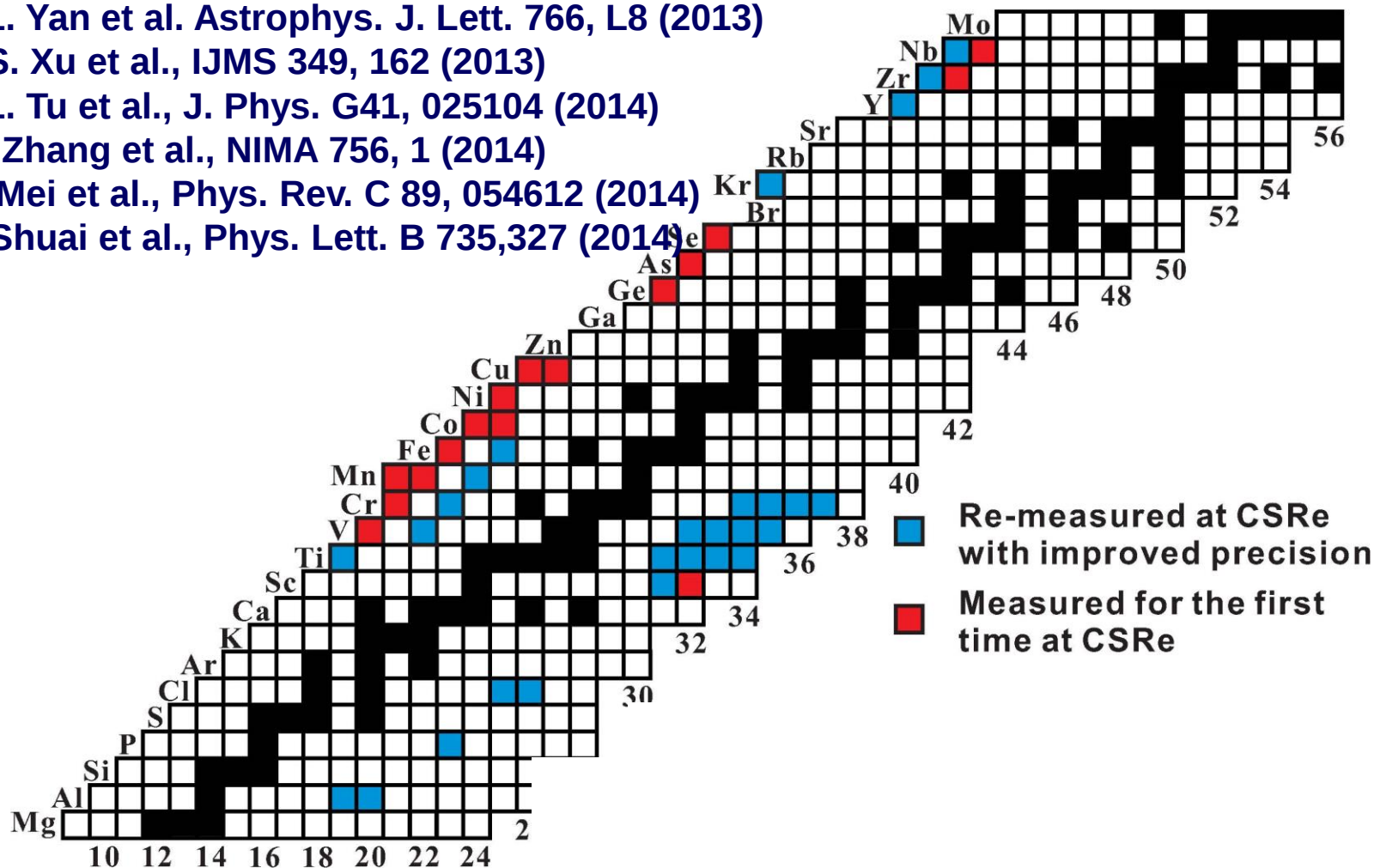
Using $\gamma = 1.3$, we have
partial $T_{1/2} = 84 (5) \mu\text{s}$

theoretical ICC = 0.334,
then we deduce
 $T_{1/2} (^{94m}\text{Ru}) = 63 (4) \mu\text{s}$

Results from CSRe mass measurements

1. B. Mei et al., NIMA A 624, 109 (2010)
2. X.L. Tu et al., PRL 106, 112501 (2011)
3. X.L. Tu et al., NIMA A 654, 213 (2011)
4. Y.H. Zhang et al., PRL 109, 102501 (2012)
5. X.L. Yan et al. Astrophys. J. Lett. 766, L8 (2013)
6. H.S. Xu et al., IJMS 349, 162 (2013)
7. X.L. Tu et al., J. Phys. G41, 025104 (2014)
8. W. Zhang et al., NIMA 756, 1 (2014)
9. B. Mei et al., Phys. Rev. C 89, 054612 (2014)
10. P. Shuai et al., Phys. Lett. B 735, 327 (2014)

Beams: ^{56}Ni , ^{78}Kr , ^{86}Kr , ^{112}Sn

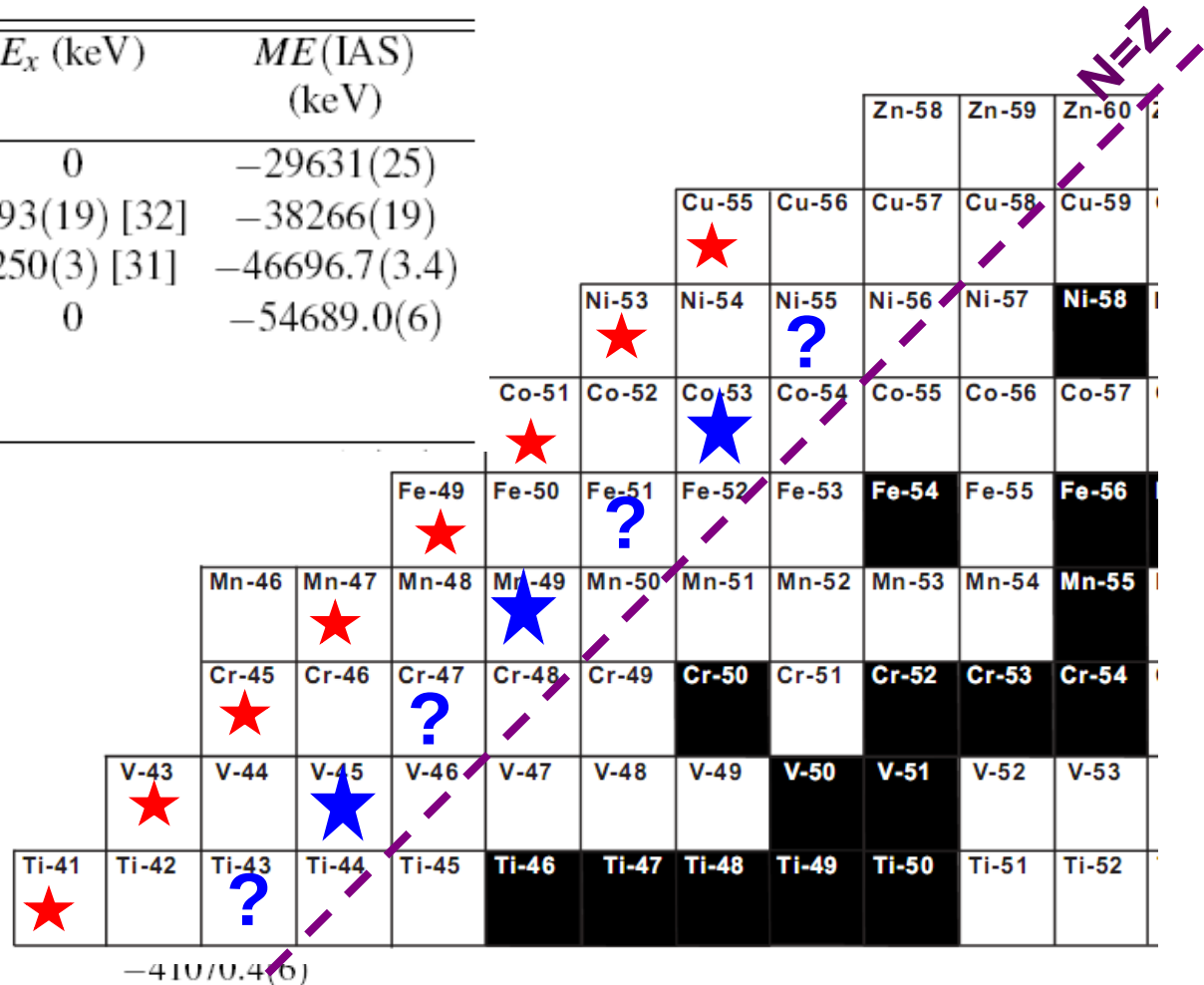


3. Test the IMME in fp shell nuclides

$$M(A,T,T_3)=a(A,T)+b(A,T)T_3+c(A,T)T_3^2 + d(A,T)T_3^3$$

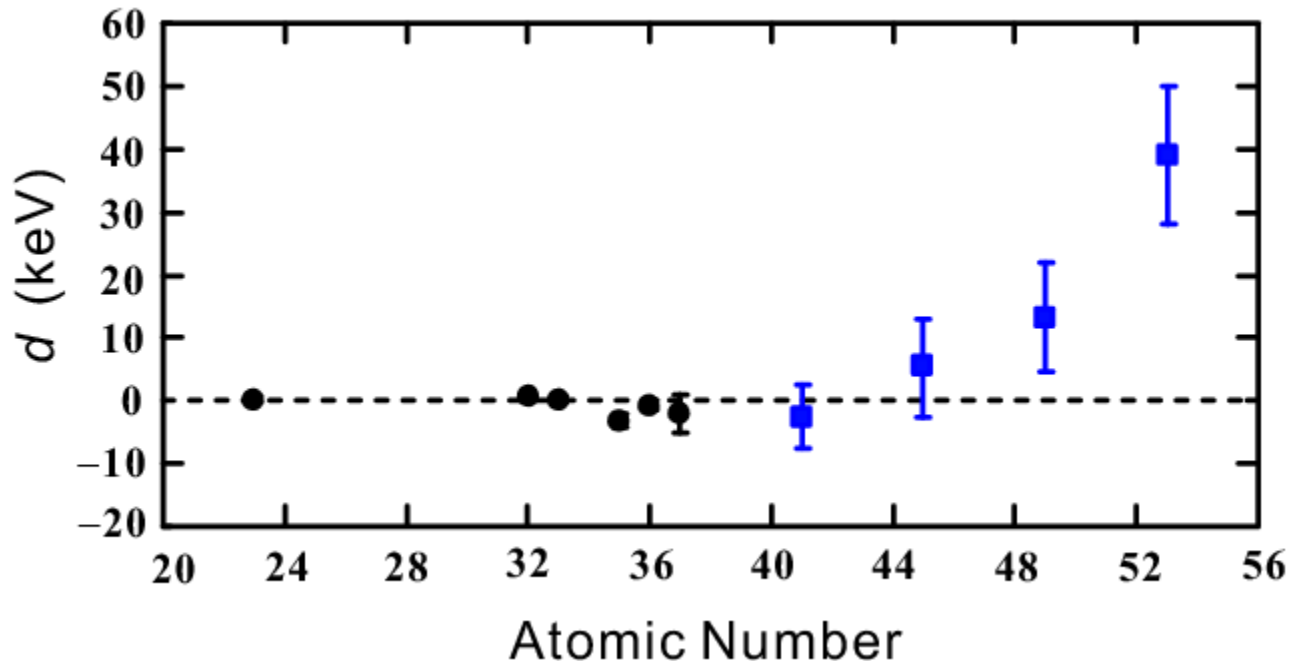
Atom	T_z	$ME(g. s)$ (keV)	E_x (keV)	$ME(IAS)$ (keV)
^{53}Ni	-3/2	-29631(25)**	0	-29631(25)
^{53}Co	-1/2	-42658.6(1.7) [26]	4393(19) [32]	-38266(19)
^{53}Fe	+1/2	-50946.7(1.7) [26]	4250(3) [31]	-46696.7(3.4)
^{53}Mn	+3/2	-54689.0(6) [26]	0	-54689.0(6)
Quadratic fit: $\chi^2/n = 13.6$				
Cubic fit: $d = 39(11)$				

^{49}Fe	-3/2	-24751(24)**	0
^{49}Mn	-1/2	-37615(24) [26]	4809(2)
^{49}Cr	+1/2	-45333(2) [26]	4764(5)
^{49}V	+3/2	-47961.0(9) [26]	0
Quadratic fit: $\chi^2/n = 2.2$			
Cubic fit: $d = 13.2(8.7)$			
^{45}Cr	-3/2	-19515(35)**	0
^{45}V	-1/2	-31880(17) [26]	4791(1)
^{45}Ti	+1/2	-39008.3(8) [26]	4723(7)
^{45}Sc	+3/2	-41070.4(6) [26]	0
Quadratic fit: $\chi^2/n = 0.5$			
Cubic fit: $d = 5.4(7.9)$			



Test the IMME in **fp** shell nuclei

$$M(T, A, T_3) = a(T, A,) + b(T, A)T_3 + c(T, A)T_3^2 + d(T, A)T_3^3$$



d coefficients increase gradually up to $A=53$ for which **d** is 3.5σ deviated from zero.

Shell model calculations

TABLE III: $b_{3,1}$, $b_{3,3}$ and d coefficients for $A = 53$.

	b_{33} (keV)	b_{31} (keV)	d (keV)
Experiment	8353(8)	8431(19)	39(12)
Theory ($f_{7/2}$ model)	8366	8365	-0.5
Theory (full pf model)	8292	8290	-1.0

The second result is obtained for the full ($f_{7/2}$, $f_{5/2}$, $p_{3/2}$, $p_{1/2}$) (pf) model space. The Hamiltonian is composed of the GPFX1A isospin conserving Hamiltonian [34–36] plus the Ormand-Brown (OB) isospin non-conserving Hamiltonian [37]. Details of the GPFX1A part and its applications to many pf shell data are given in Refs. [34–36]. The OB part was

Mass Excesses

uncertainty: 0.6 keV 25 keV 3.4 keV 19 keV
 ⁵³Mn gs ⁵³Ni gs ⁵³Fe IAS ⁵³Co IAS

$$d = \frac{1}{6} \{ [\text{ME}_{(+\frac{3}{2})} - \text{ME}_{(-\frac{3}{2})}] - 3[\text{ME}_{(+\frac{1}{2})} - \text{ME}_{(-\frac{1}{2})}] \}.$$

More attention should be paid to the excitation Energies of IAS's in ⁵³Co & ⁵³Fe since the errors are three times as important as those of the g.s masses of ⁵³N and ⁵³Mn for an evaluation of *d* & in checking the validity of the IMME.

Previous results

Result from: C. Dossat et al., Nucl. Phys. A792 (2007) 18-86

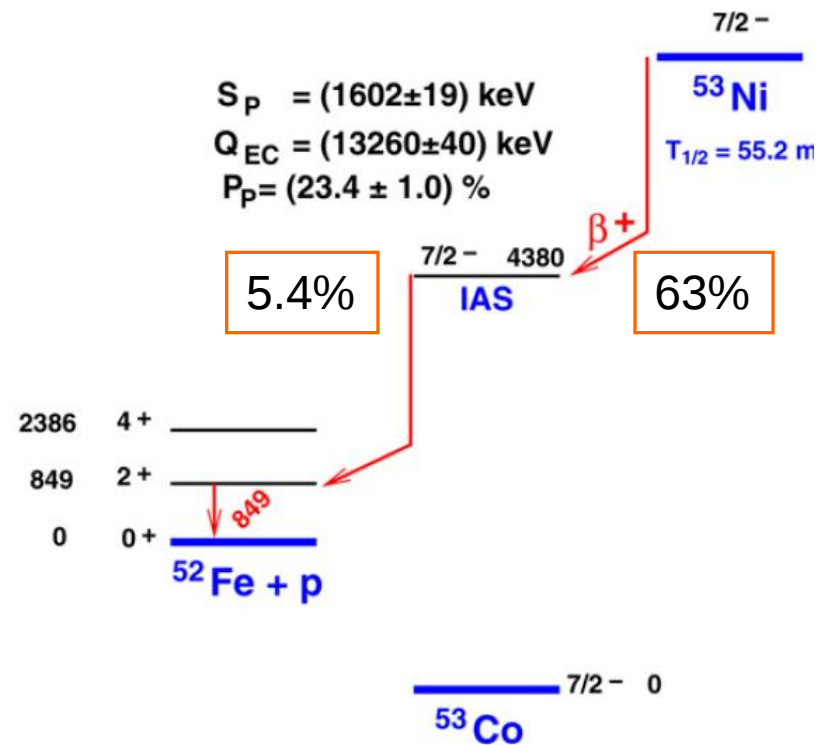
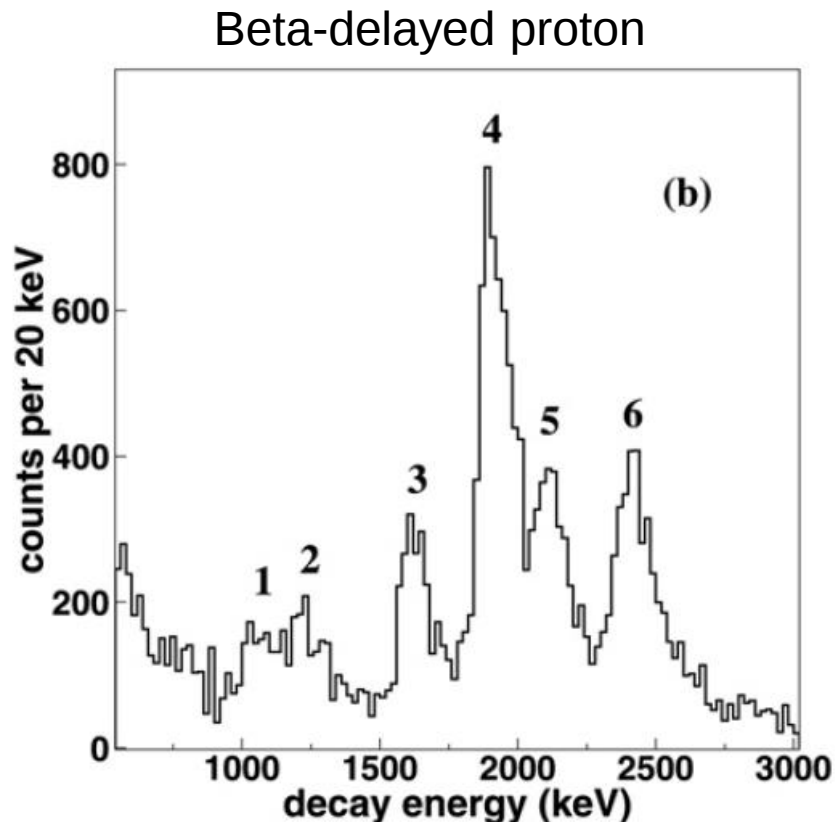


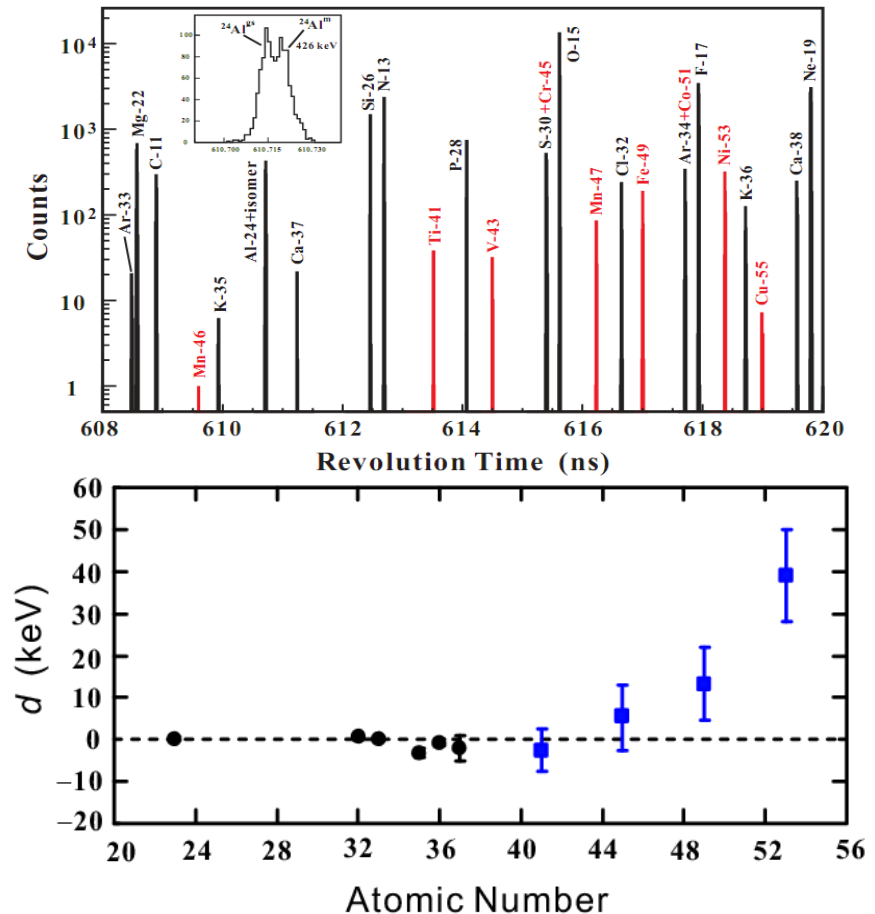
Fig. 41. Partial decay scheme for the β decay of ^{53}Ni .

4. Summary

1) CSRe IMS + interpolation
Masses of $T_3 = -3/2$ nuclei
measured.

2) Breakdown of quadratic
form of IMME found for
 $A=53$, $T=3/2$ quartet

3) More precise mass measurements of (^{53}Ni ; gs) and (^{53}Co ; IAS) are needed in order to check the validity of IMME in the pf-shell nuclides.



**Thank you for your attention and
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