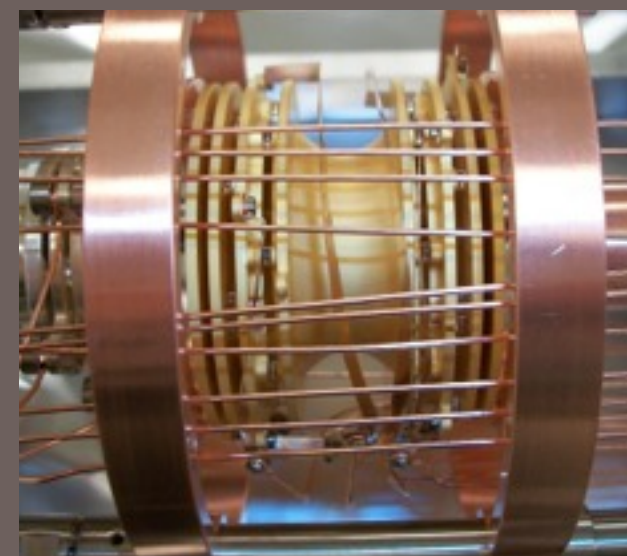


High Precision Mass Measurements of Rare Isotopes at TITAN

stephan malbrunot-ettenauer | TRIUMF / CERN

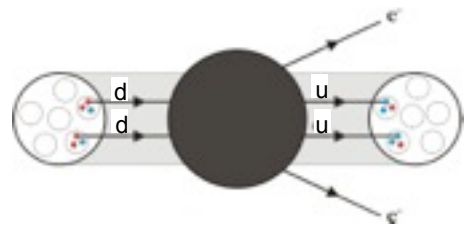


**weak
interaction**

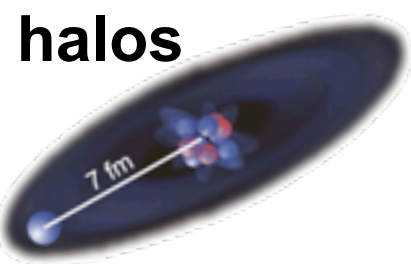
atomic masses

$\delta m/m \approx 10^{-8/9}$

neutrino physics



$0\nu\beta\beta$ -decay

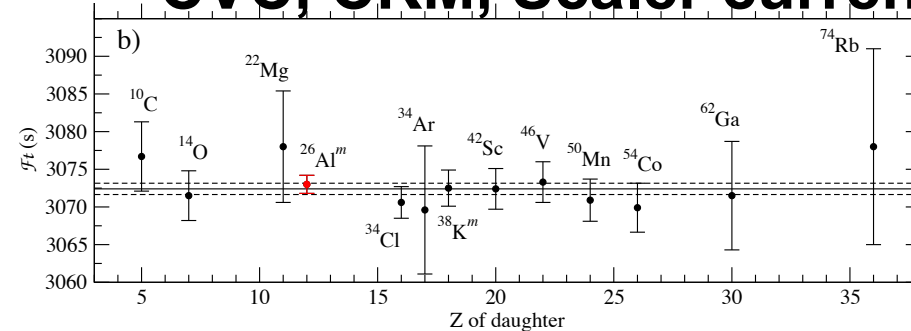


halos

previously@TITAN:

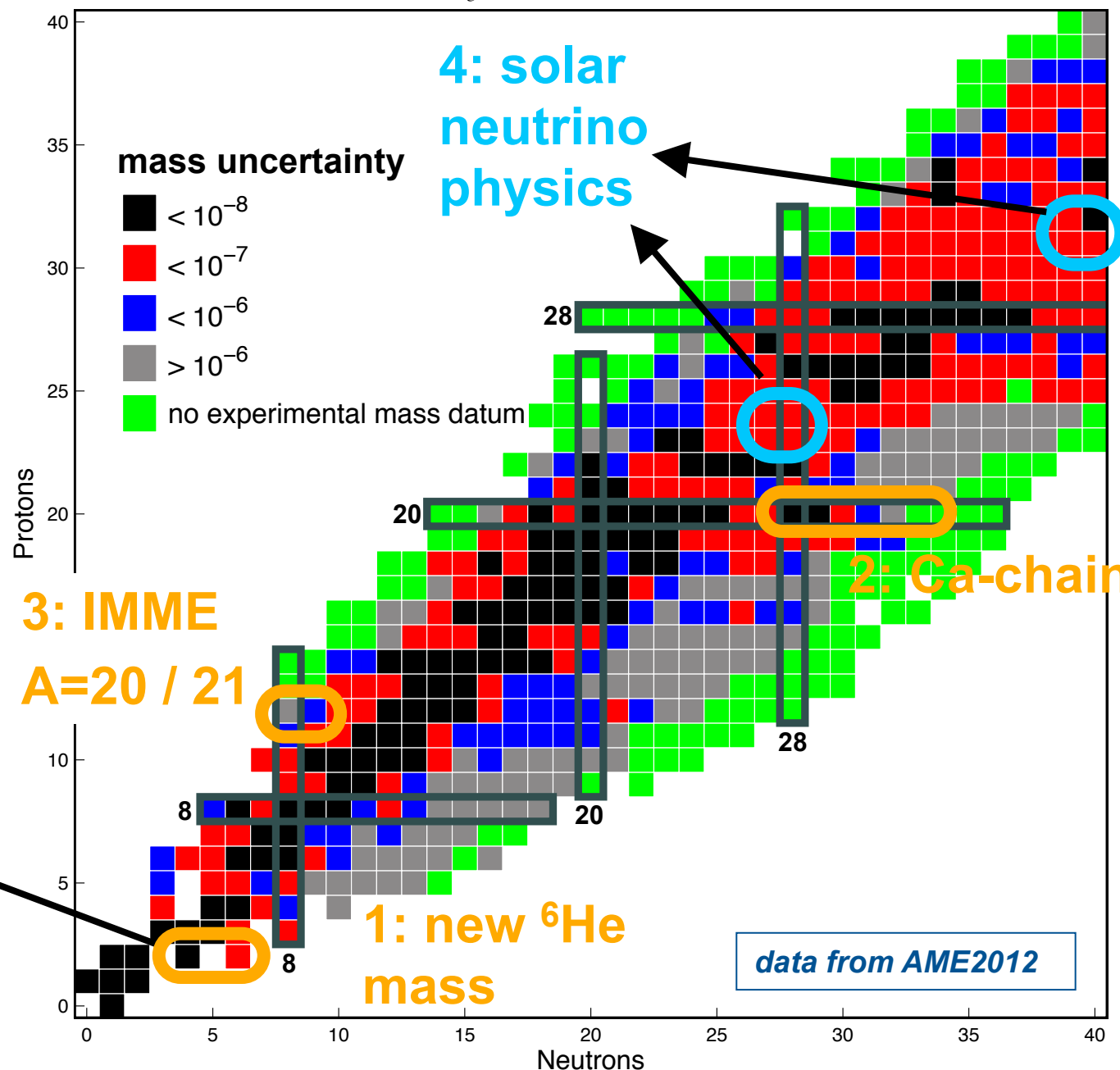
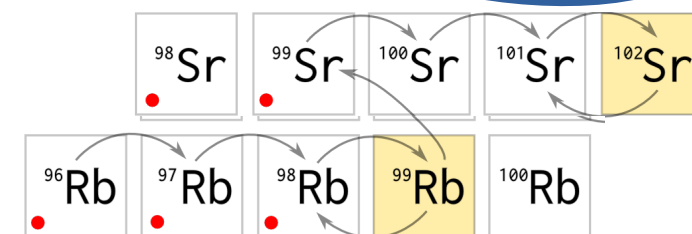
^{11}Li , ^{11}Be , ^8He

CVC, CKM, Scalar currents



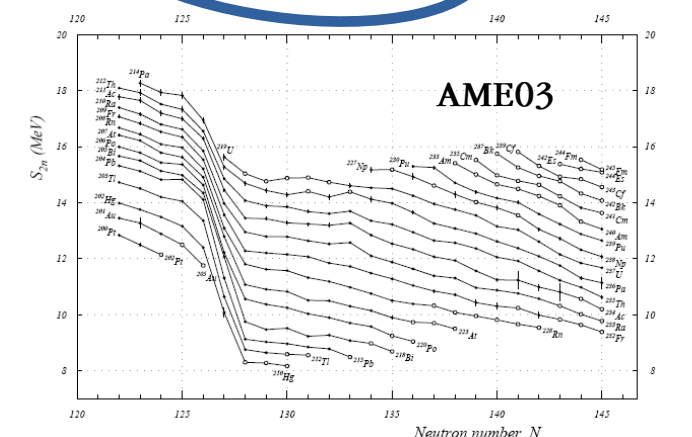
**Nuclear
Astrophysics**

$\delta m/m \approx 10^{-7}$



**Nuclear
Structure**

$\delta m/m \approx 10^{-6/7}$



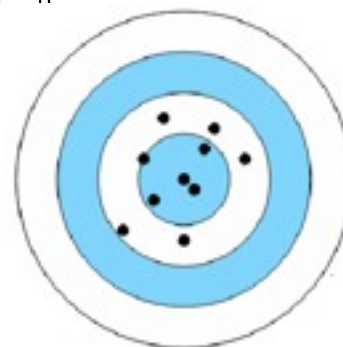
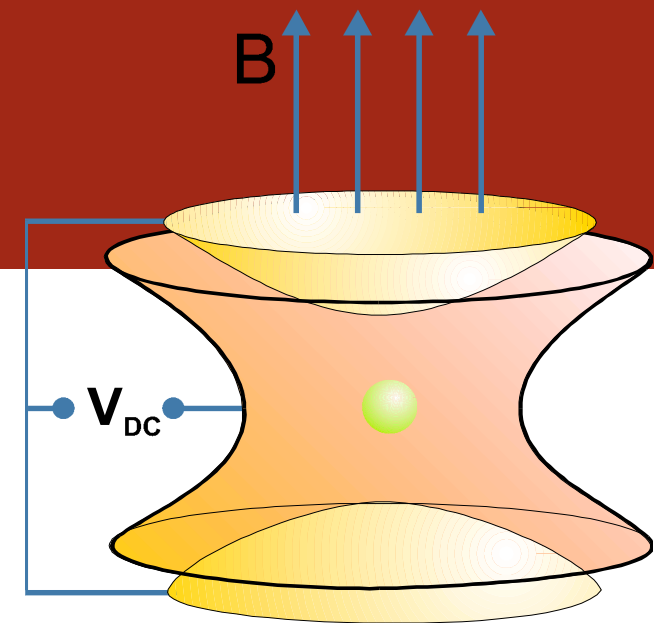
shell evolution

Penning traps

- ISOLTRAP
- JYFLTRAP
- LEBIT
- TITAN
- CPT
- SHIPTRAP

K. Blaum, INPC 2010

$$\nu_c = \frac{1}{2\pi} \frac{q}{m} B$$



accurate,
but not precise



precise,
but not accurate

Accuracy

- exact theoretical description

L.S. Brown and G. Gabrielse, *Rev. Mod. Phys.* 58, 233 (1986)
 G. Bollen et al., *J. Appl. Phys.* 88, 4355 (1990)
 M. König et al., *Int. J. Mass Spect.* 142, 95 (1995)
 M. Kretschmarr, *Int. J. Mass Spect.* 246, 122 (2007)

- even for non-ideal traps

G. Bollen et al., *J. Appl. Phys.* 88, 4355 (1990)

- off-line tests with stables

Precision

line-width (FWHM):

$$\Delta\nu \approx 1/T_{rf}$$

⇒ resolution:

$$R = \frac{m}{\Delta m} = \frac{\nu_c}{\Delta\nu_c} \approx \nu_c T_{rf}$$

$$\approx \frac{qBT_{rf}}{2\pi m}$$

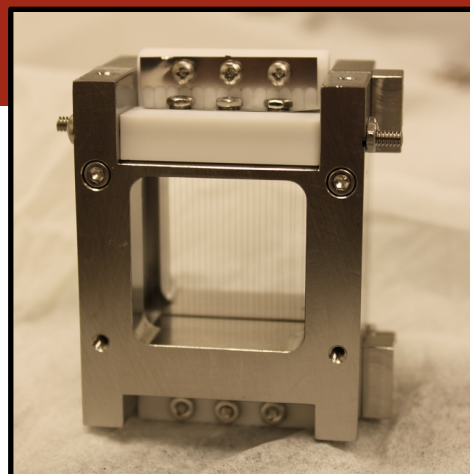
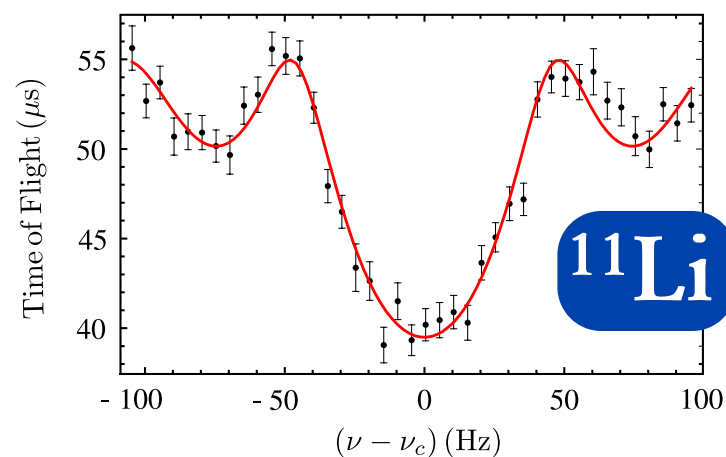
TITAN @ TRIUMF

Penning traps:

- highest precision
- down to $T_{1/2} < 10$ ms
(^{11}Li $T_{1/2} = 8.8$ ms @ TITAN)

M. Smith et al., PRL 101, 202501 (2008)

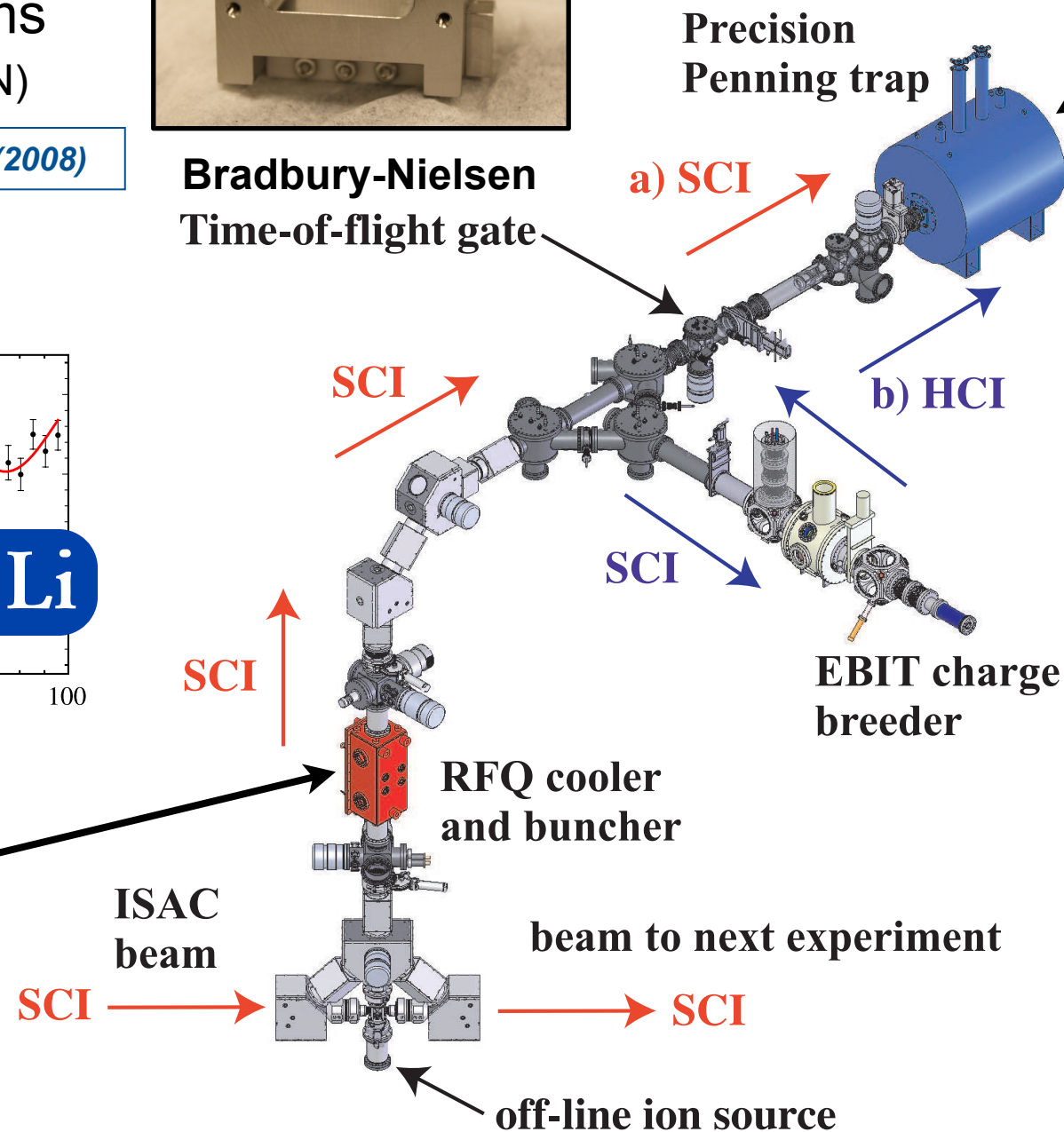
$$\nu_c = \frac{1}{2\pi} \frac{q}{m} B$$



**Bradbury-Nielsen
Time-of-flight gate**

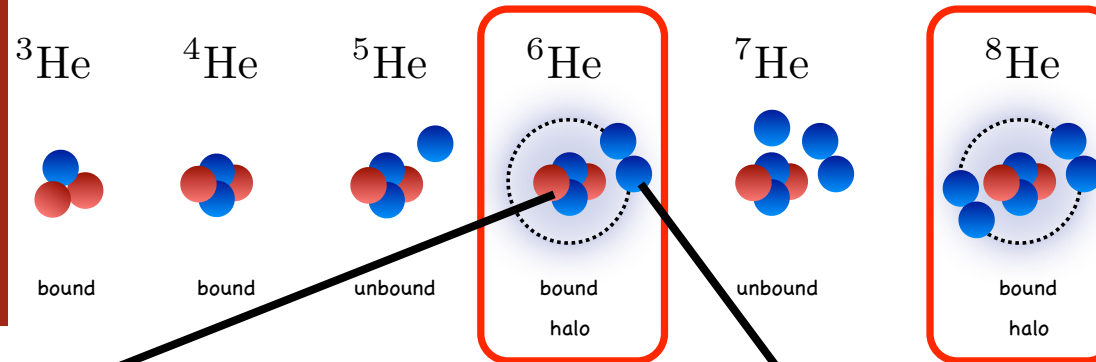


**Precision
Penning trap**



systematics: < 5 ppb possible

M. Brodeur et al, PRC 80, 044318 (2009)
M. Brodeur et al., IJMS 310, 20 (2012)

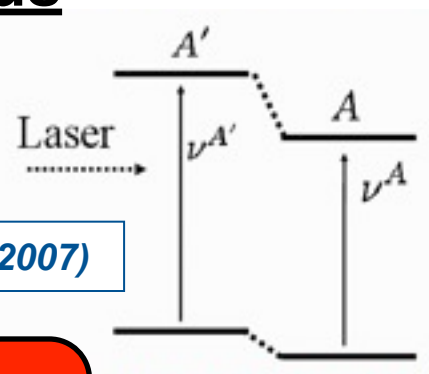


⁶He

core & charge radius

Isotope Shift

P. Mueller et al., PRL 99, 252501 (2007)

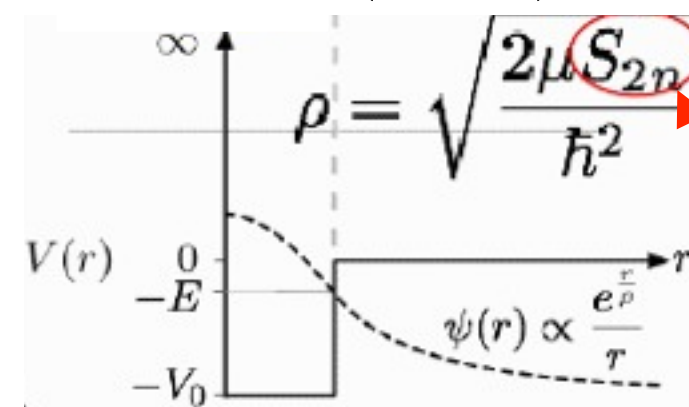


$$\delta\nu_{A,A'} = \delta_{A,A'}^{\text{MS}} + K_{\text{FS}} \delta \langle r_c^2 \rangle_{A,A'}$$

Mass Shift **Field Shift / Finite Size Shift**

extend of halo formation & S_{2n}

$$S_{2n} = m(Z, N - 2) + 2m_n - m(Z, N)$$



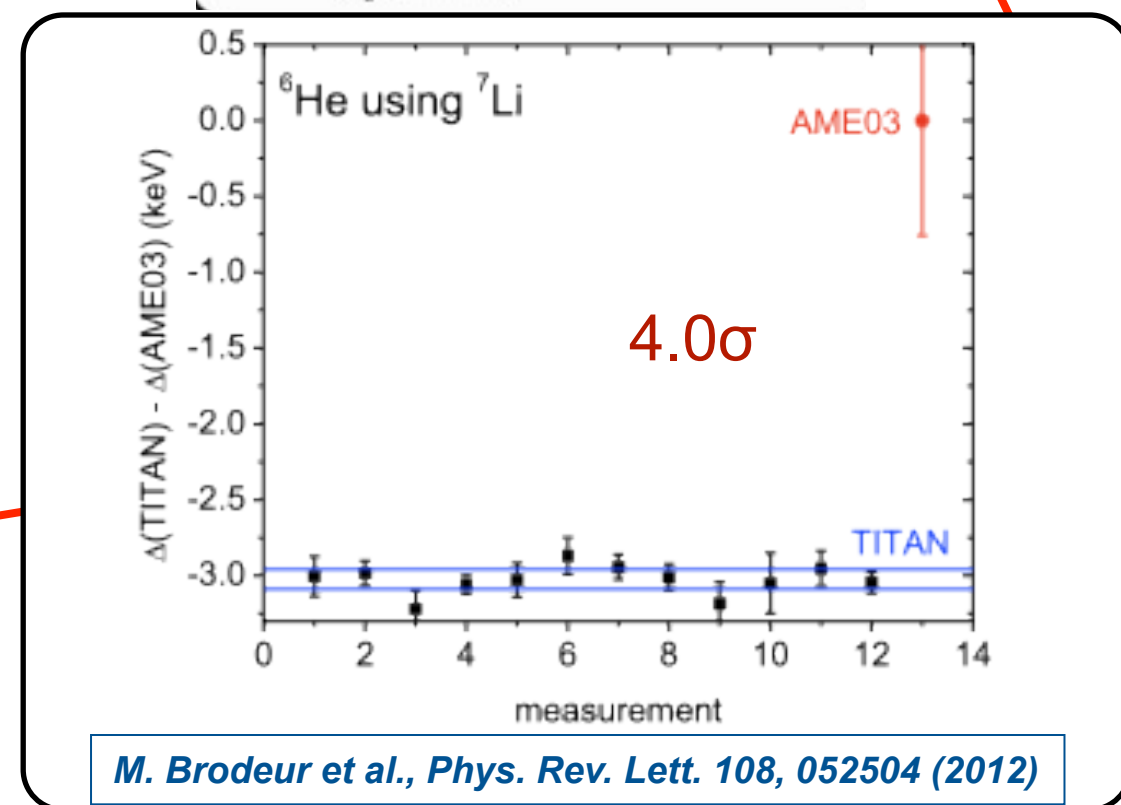
high precision atomic physics calculation

G. W. F. Drake, Nucl. Phys. A737, 25 (2004)
Z.-C. Yan et al., PRL 100, 243002 (2008)

$$E = \mathcal{E}_{\text{NR}}^{(0)} + \lambda \mathcal{E}_{\text{NR}}^{(1)} + \lambda^2 \mathcal{E}_{\text{NR}}^{(2)} + \alpha^2 (\mathcal{E}_{\text{rel}}^{(0)} + \lambda \mathcal{E}_{\text{rel}}^{(1)}) + \alpha^3 (\mathcal{E}_{\text{QED}}^{(0)} + \lambda \mathcal{E}_{\text{QED}}^{(1)}) + \alpha^4 (\mathcal{E}_{\text{ho}}^{(0)} + \lambda \mathcal{E}_{\text{ho}}^{(1)}) + \bar{r}_c^2 (\mathcal{E}_{\text{nuc}}^{(0)} + \lambda \mathcal{E}_{\text{nuc}}^{(1)}) + \dots$$

with $\lambda = \frac{\mu}{M} = \frac{m_e}{m_e + M}$

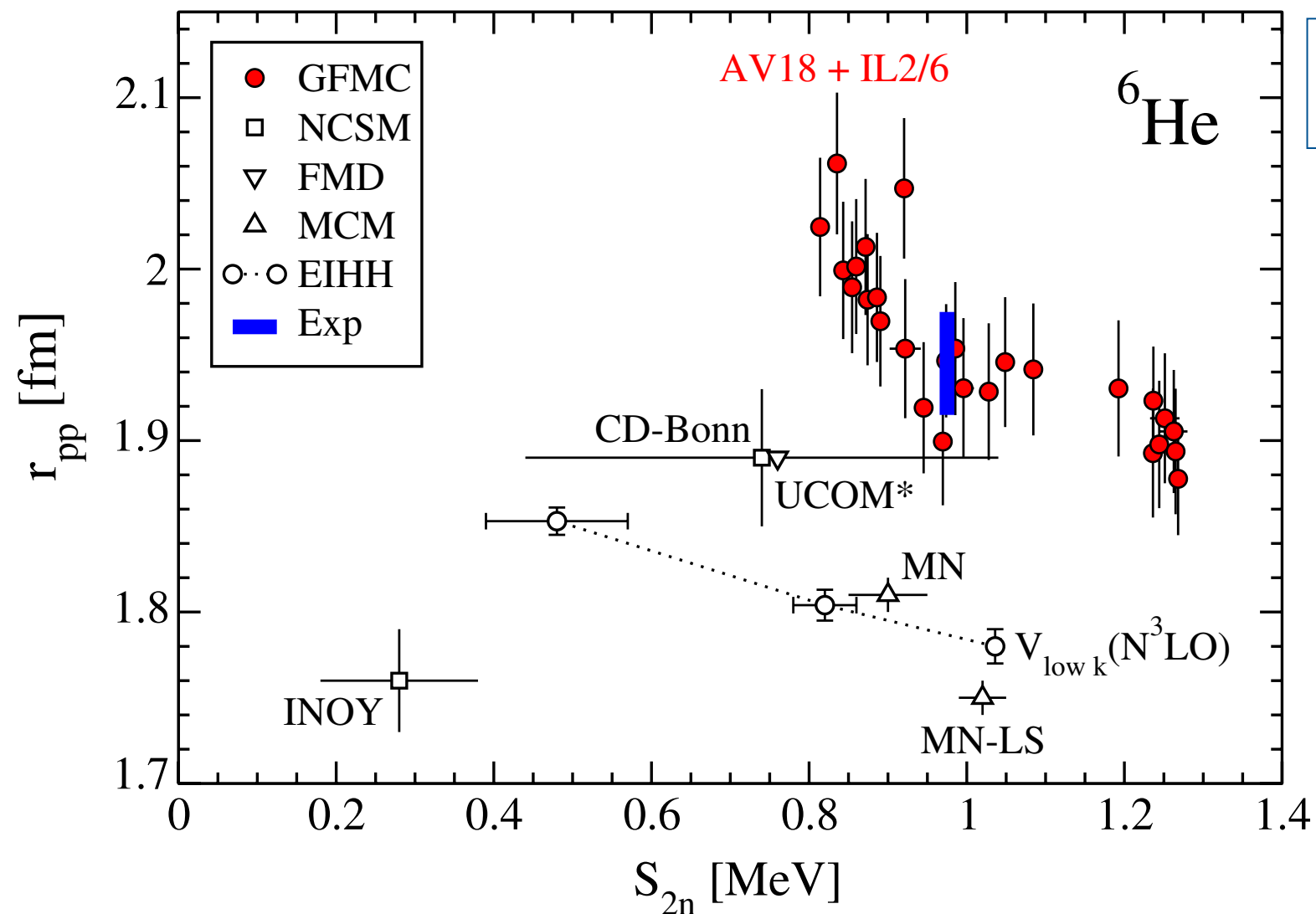
nuclear mass:
 $\delta m < 1 \text{ keV}$



M. Brodeur et al., Phys. Rev. Lett. 108, 052504 (2012)

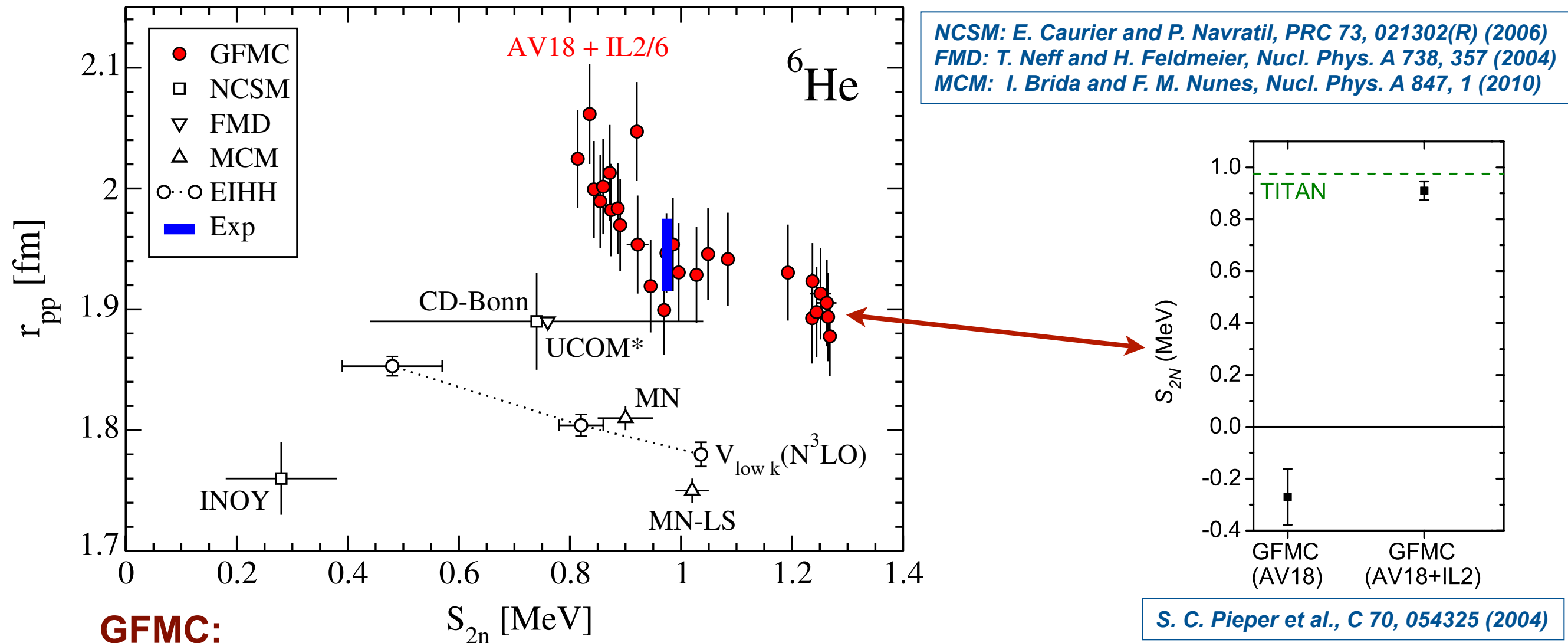
see talks Friday morning

comparison to ab-initio calculations



NCSM: E. Caurier and P. Navratil, PRC 73, 021302(R) (2006)
 FMD: T. Neff and H. Feldmeier, Nucl. Phys. A 738, 357 (2004)
 MCM: I. Brida and F. M. Nunes, Nucl. Phys. A 847, 1 (2010)

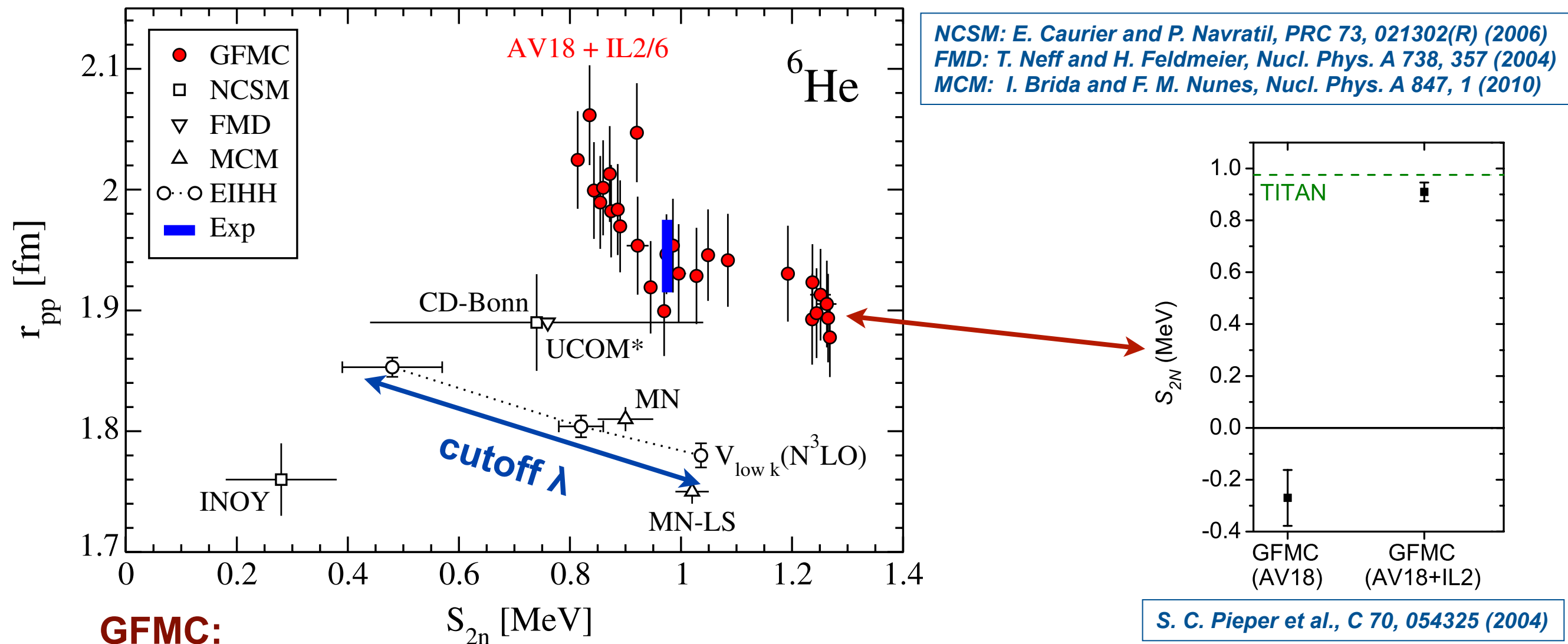
comparison to ab-initio calculations



GFMC:

- only calculation with 3N forces
- phenomenological forces

comparison to ab-initio calculations



GFMC:

- only calculation with 3N forces
- phenomenological forces

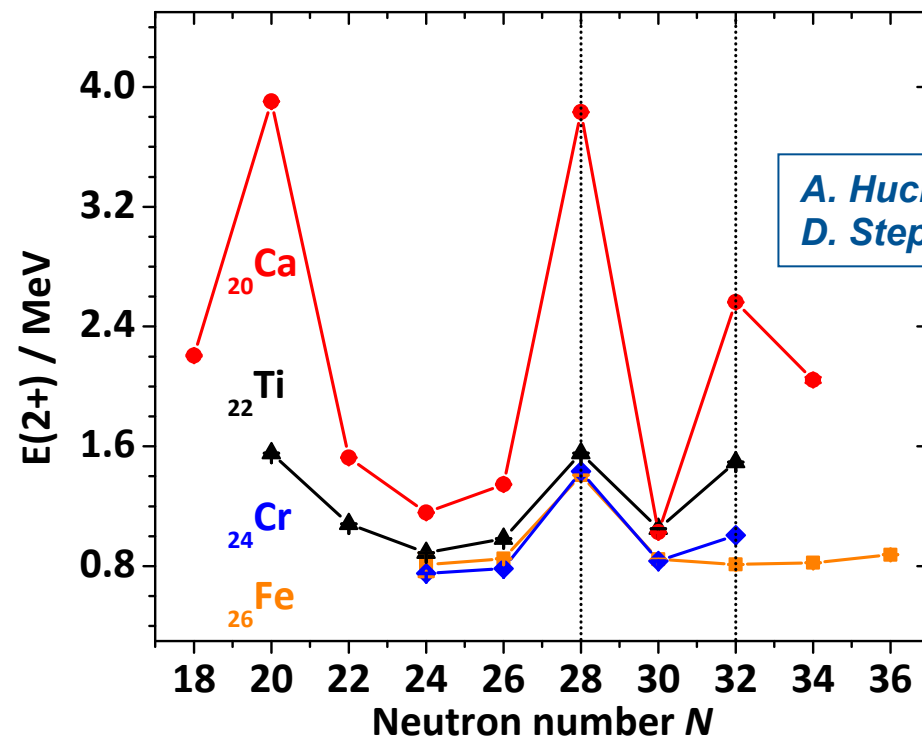
S. C. Pieper, Riv. Nuovo Cimento 31, 709 (2008), [arXiv:0711.1500](https://arxiv.org/abs/0711.1500)

hyper-spherical harmonics

- chiral EFT, but without 3N forces
- running of observables with $\lambda \leftrightarrow$ no many-body forces (analog to Tjon line)

M. Brodeur et al., Phys. Rev. Lett. 108, 052504 (2012)
S. Bacca et al., PRC 86, 034321 (2012)

Ca-chain: magic numbers $N=32 / 34$?



A. Huck et al., *Phys. Rev. C* 31, 2226–2237 (1985)
D. Steppenbeck et al., *Nature* 502, 207–210 (2013)

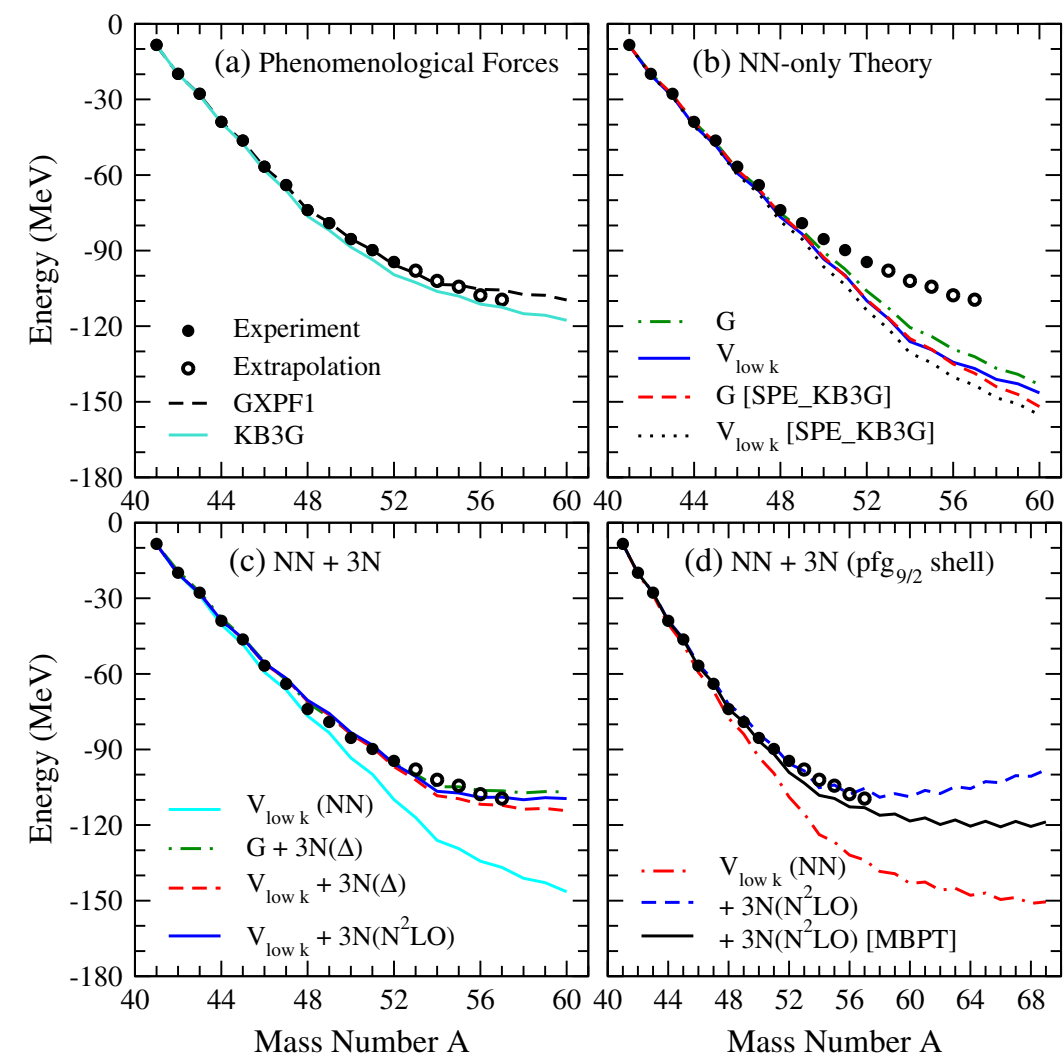
GXPFI/GXPFI A:

predicts shell closure at $N=34$

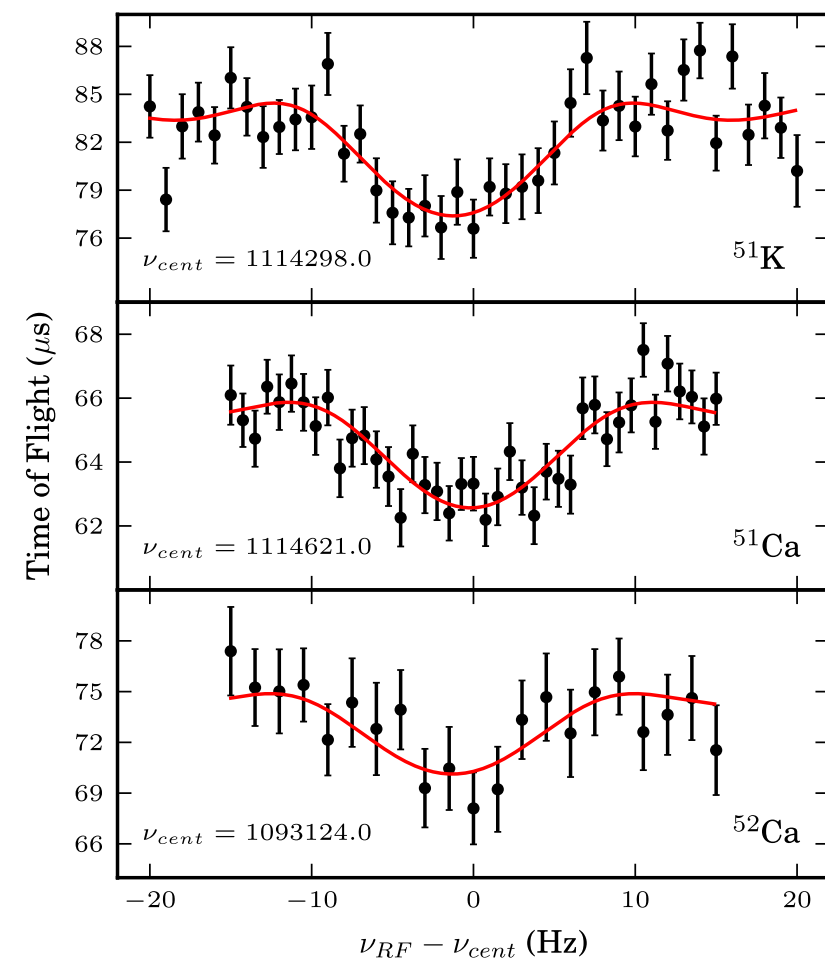
M. Honma et al., *Phys. Rev. C* 65, 061301(R) (2002).
M. Honma et al., *Eur. Phys. J. A* 25, 499 (2005).

J. D. Holt et al., *J. Phys. G: Nucl. Part. Phys.* 39 085111 (2012)

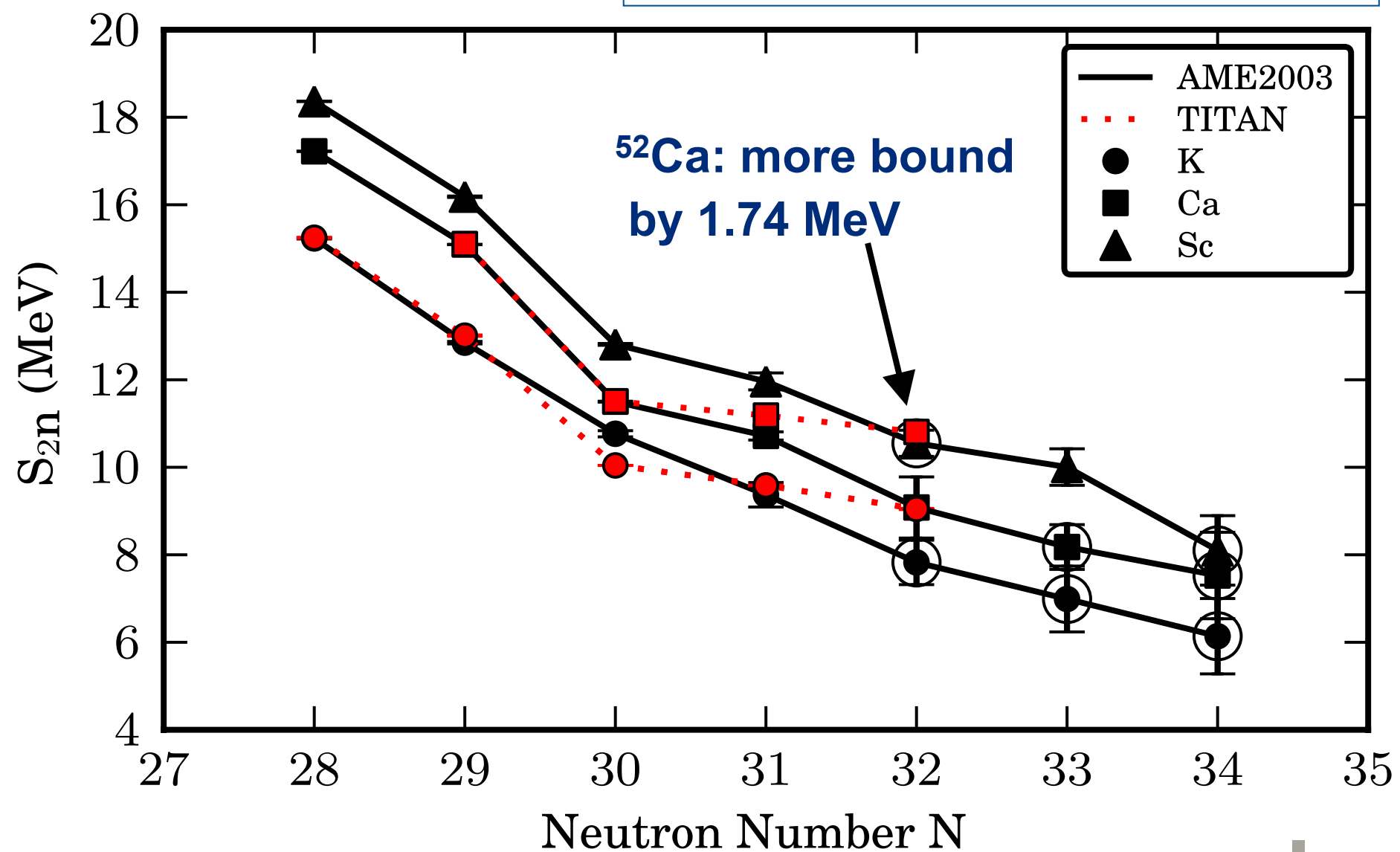
shell model with chiral 3N forces



TITAN- measurements

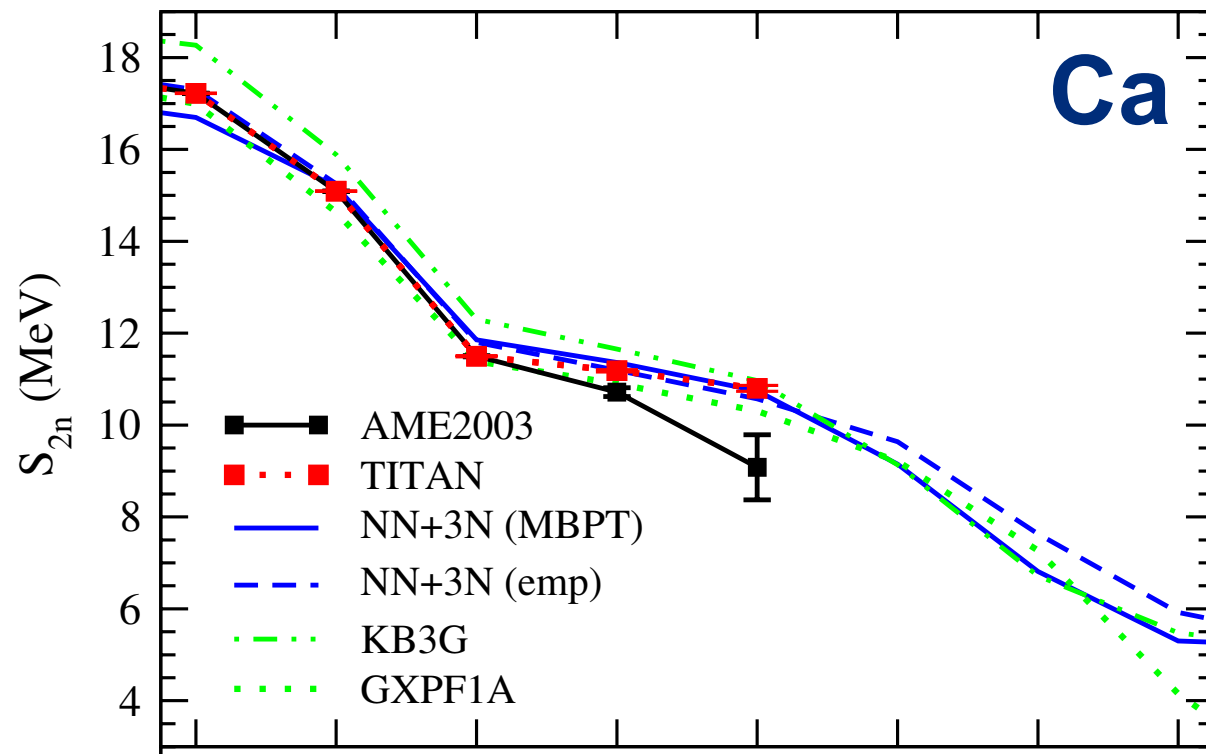


A. T. Gallant et al., Phys. Rev. Lett. 109, 032506 (2012)
A. Lapierre et al., Phys. Rev. C 85, 024317 (2012)



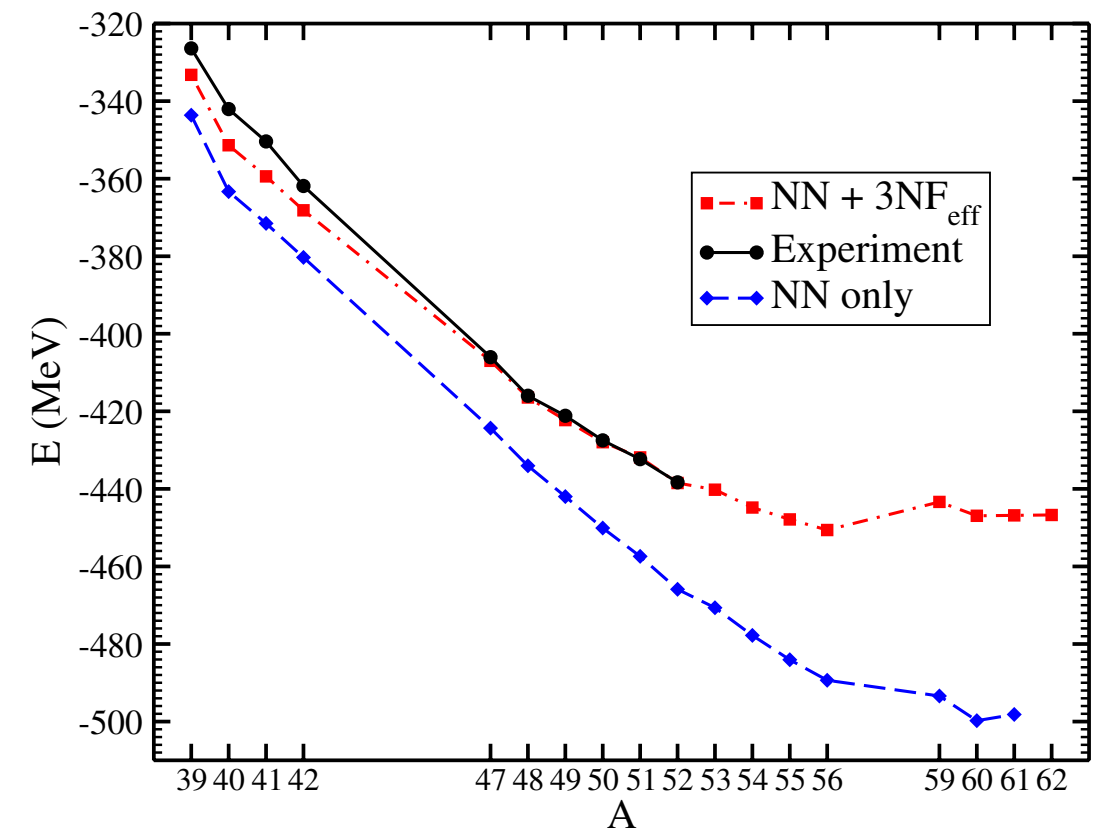
Ca: comparison to theory

shell model + chiral forces



A. T. Gallant et al., *Phys. Rev. Lett.* 109, 032506 (2012)
J. D. Holt et al., *J. Phys. G* 39, 085111 (2012).

coupled-cluster method + chiral NN forces + phenomenological 3n forces

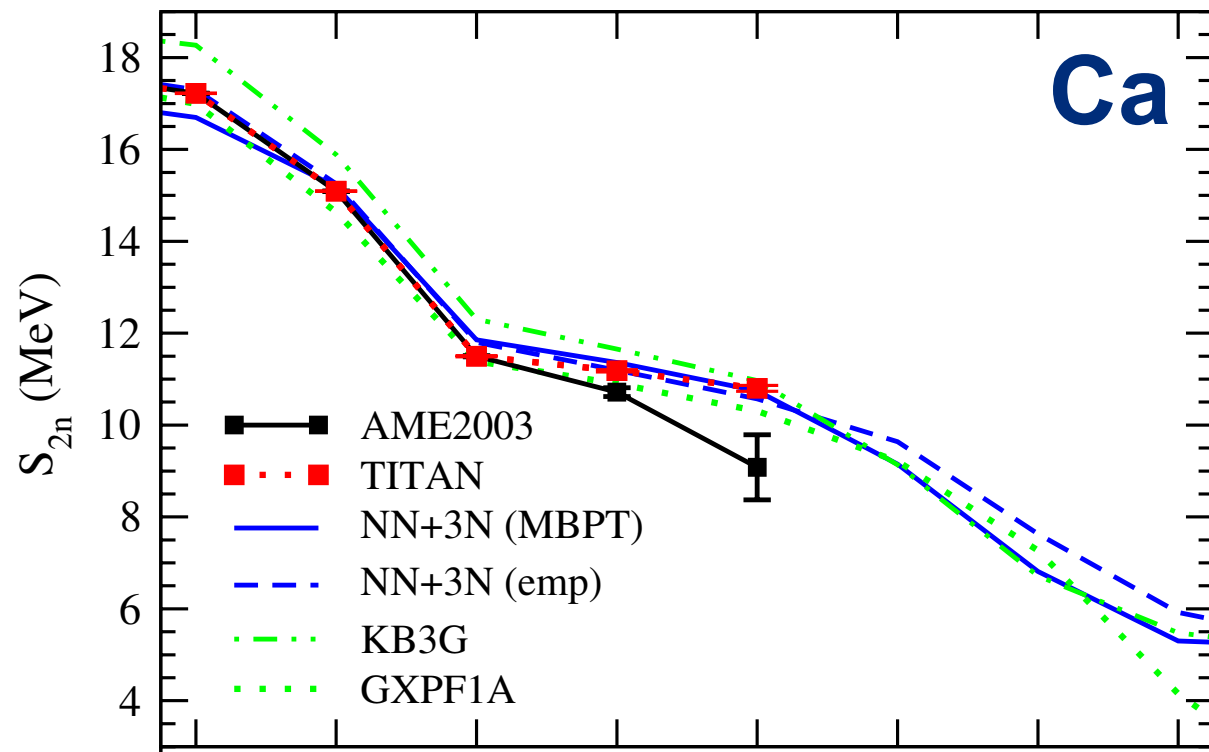


G. Hagen et al., *Phys. Rev. Lett.* 109, 032502 (2012)

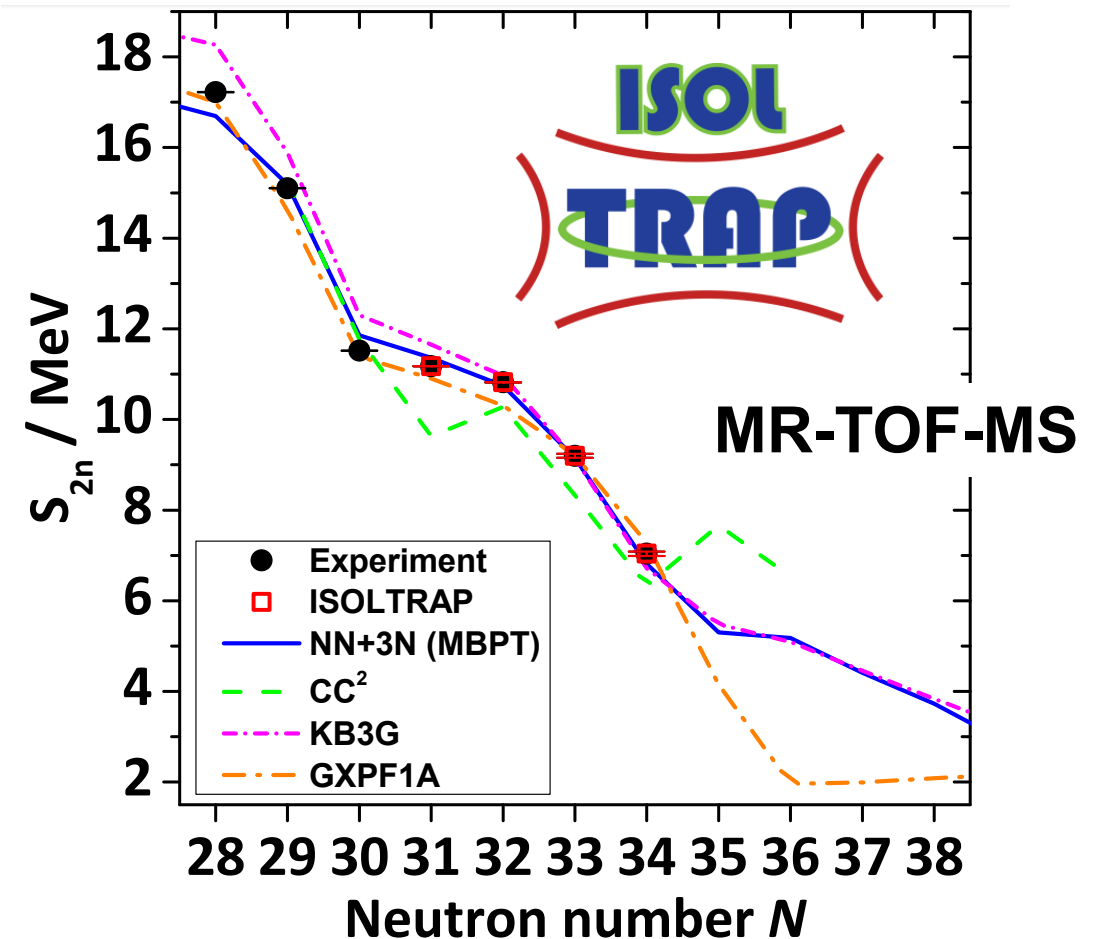
excellent agreement between experiment and theory

Ca: comparison to theory

shell model + chiral forces



A. T. Gallant et al., *Phys. Rev. Lett.* 109, 032506 (2012)
J. D. Holt et al., *J. Phys. G* 39, 085111 (2012).



F. Wienholtz et al., *Nature* 498, 346 (2013)

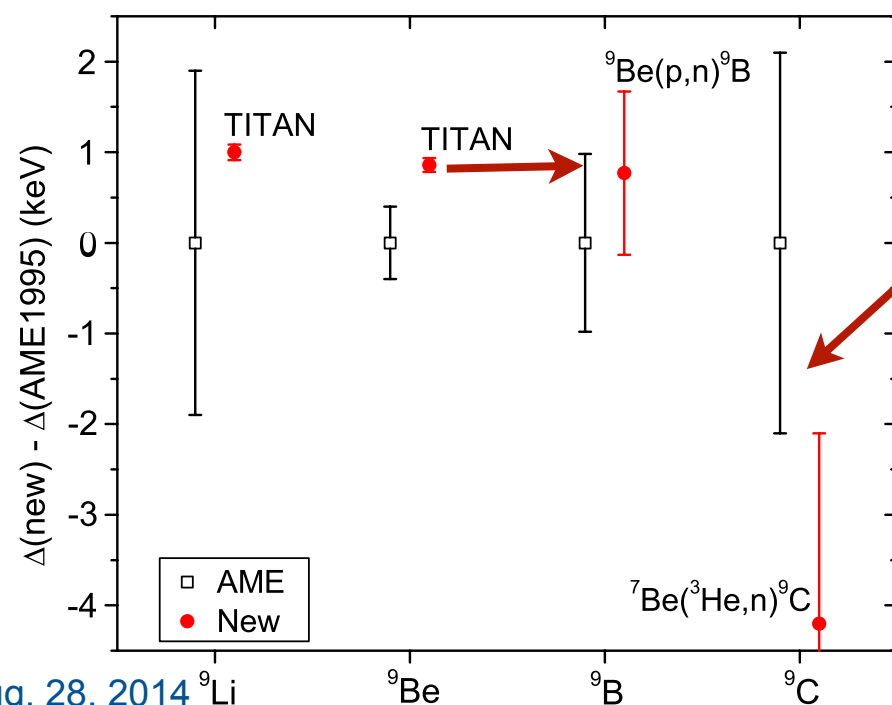
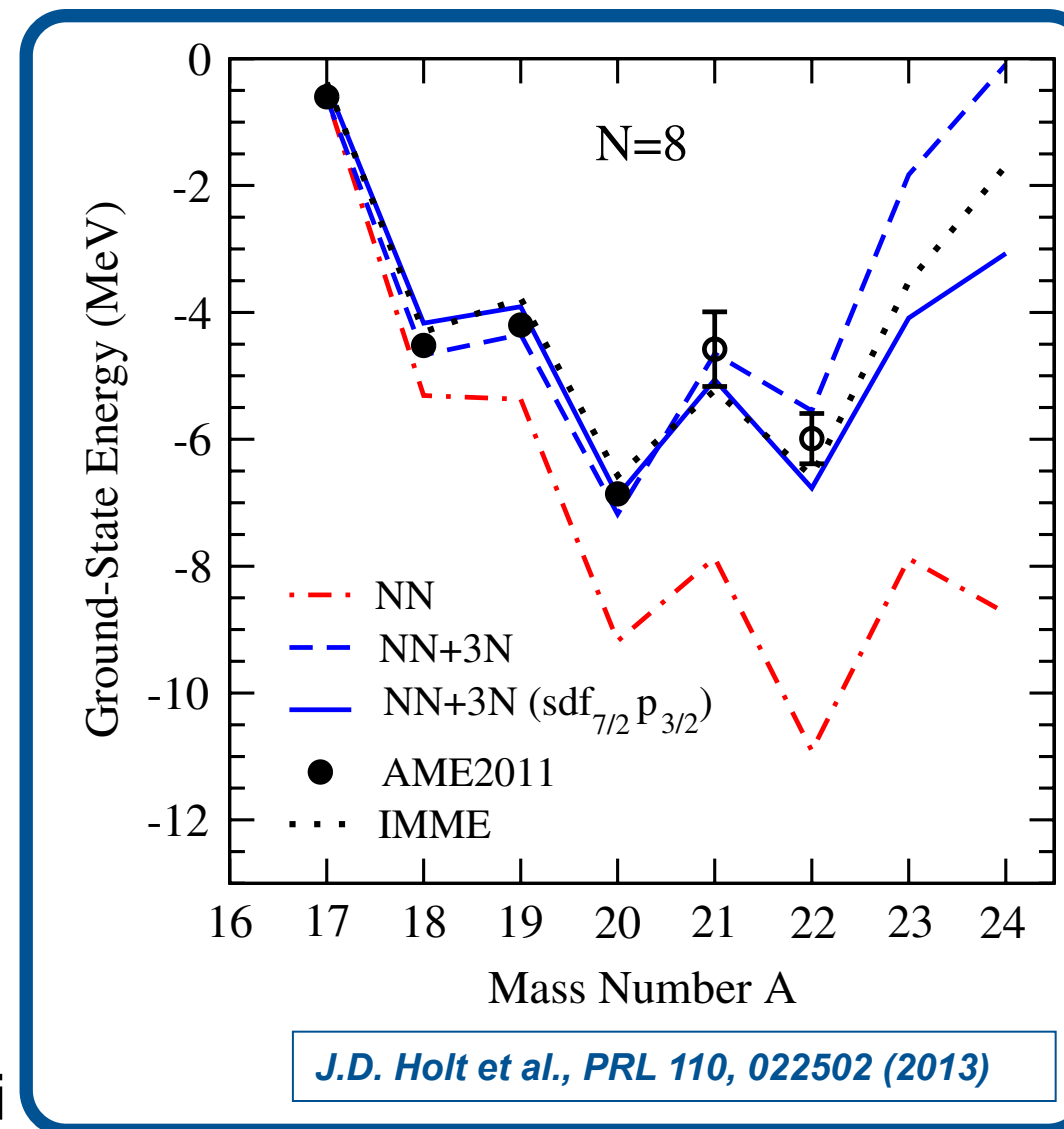
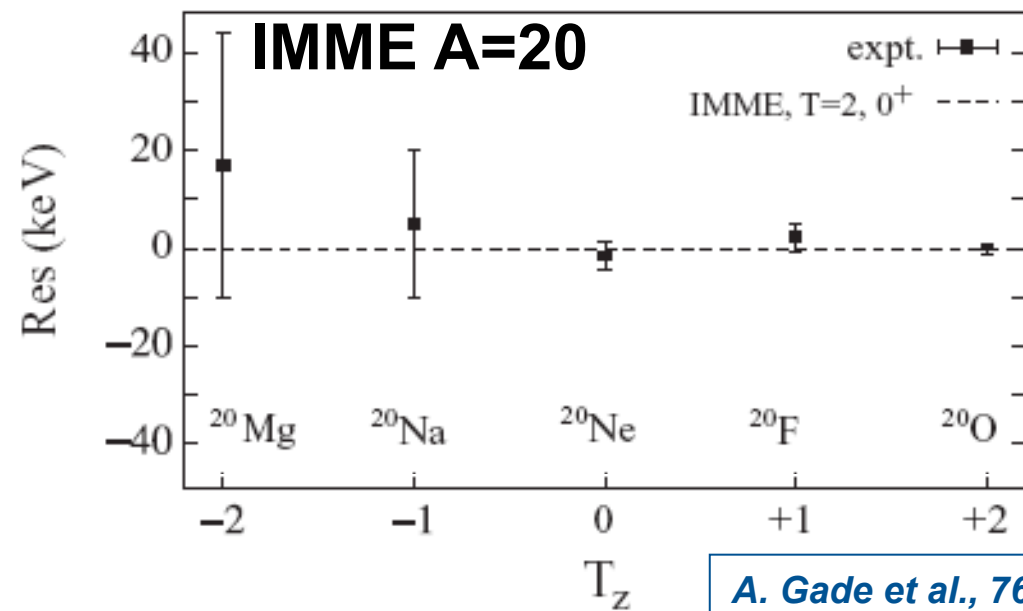
see talk by F. Wienholtz

excellent agreement between experiment and theory

IMME, 3N-forces & proton rich nuclei

IMME

$$M(A, T, T_z) = a(A, T) + b(A, T) \cdot T_z + c(A, T) \cdot T_z^2$$



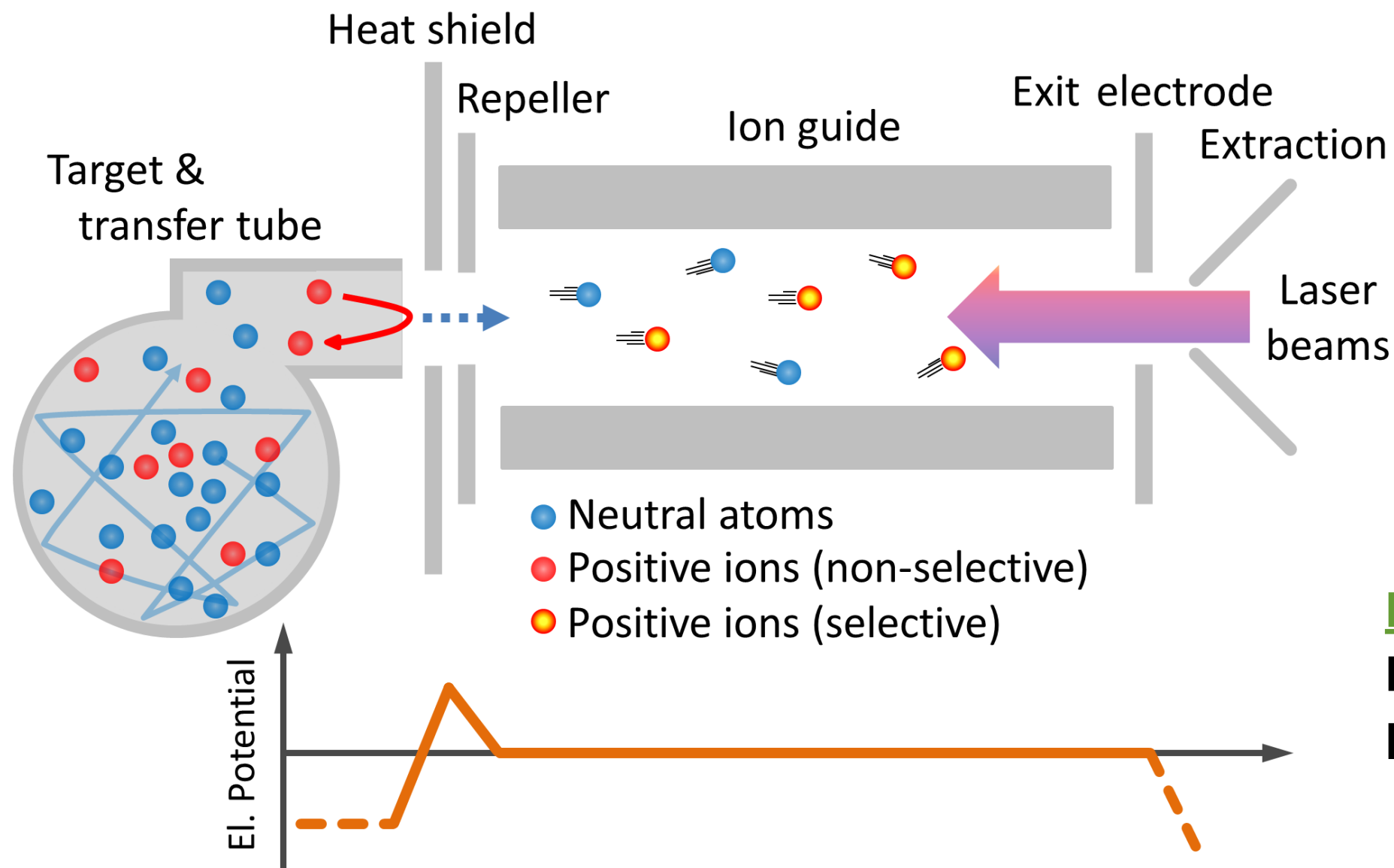
$^7\text{Li}(p, n)^7\text{Be}$
& new mass of ^7Li
(SMILETRAP)

IMME breakdown at $A=9$ explained by
isospin mixing with neighboring states in
 ^9Be and ^9B (SM by B. A. Brown)

M. Brodeur et al., PRL 108, 212501 (2012)

Ion Guide Laser Ion Source (IG-LIS)

Laser ion source group: TRIUMF, Laval, U Manitoba, Oldenburg
J. Lassen, H. Heggen, A. Teigelhoefer et al.

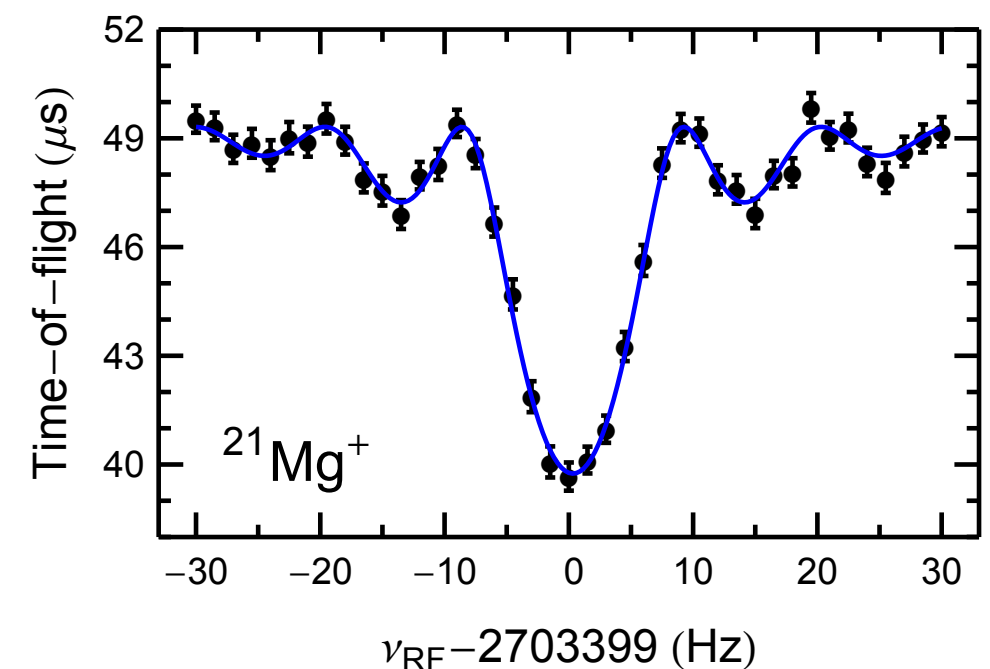
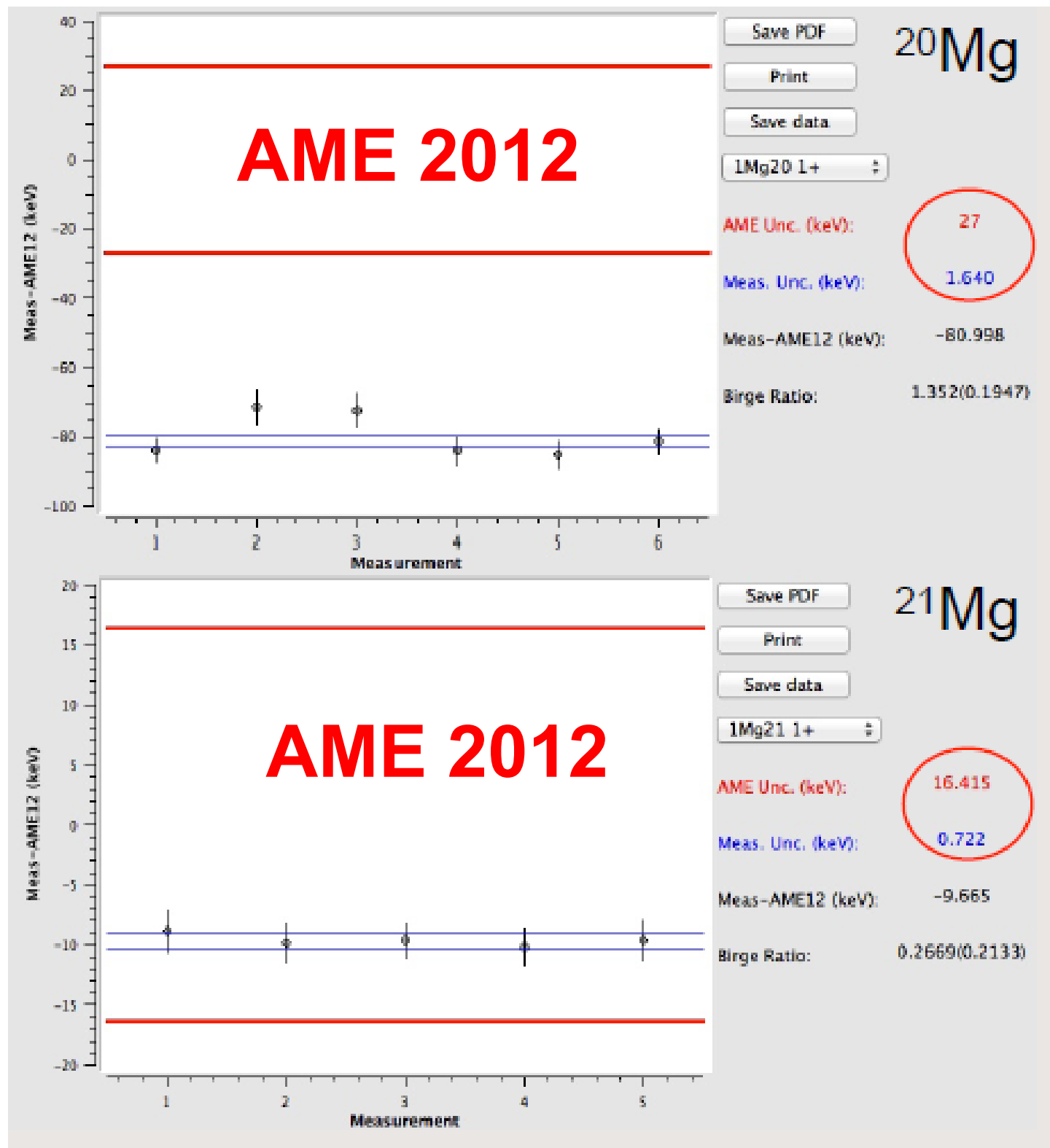


Na-contamination

Na suppressed by 10^6
Mg reduced by 50

A. T. Gallant et al., PRL 113, 082501 (2014)

$^{20,21}\text{Mg}$ measurement at TITAN



Nuclide	Exp.	USDA	USDB	NN + 3N
^{20}Mg	-6.94	-6.71	-6.83	-6.89
^{21}Mg	-21.59	-21.79	-21.81	-23.18

A. T. Gallant et al., PRL 113, 082501 (2014)

IMME: A=20 / 21 multiplets

Nuclide	T_z	ME(g.s.) (keV)	E_x (keV)
$A = 20, J^\pi = 0^+, T = 2$			
^{20}O	+2	3796.17 (89)	0.0
^{20}F	+1	-17.45 (3)	6519.0 (30)
^{20}Ne	0	-7041.9306 (16)	16732.9 (27)
^{20}Na	-1	6850.6 (11)	6524.0 (97) ^a
^{20}Mg	-2	17477.7 (18) ^b	0.0
Fit	d (keV)	e (keV)	χ^2
Quadratic	-	-	10.4
Cubic	2.8 (11)	-	3.7
Quartic Only	-	0.89 (12)	9.9
Quartic	5.4 (17)	-3.5 (18)	-
USDA	-0.1	-	
USDA	-	-1.7	
USDB	-0.1	-	
MBPT	-18		
$A = 21, J^\pi = 5/2^+, T = 3/2$			
^{21}F	+3/2	-47.6 (18)	0.0
^{21}Ne	+1/2	-5731.78 (4)	8859.2 (14)
^{21}Na	-1/2	-2184.6 (3)	8976.0 (20)
^{21}Mg	-3/2	10903.85 (74) ^b	0.0
Fit	d (keV)	χ^2	
Quadratic	-	28	
Cubic	6.7 (13)	-	
USDA	-0.3		
USDB	0.3		
MBPT	-38		

again breakdown of the IMME

prediction of required cubic d
coefficients:
challenge for shell-model
calculations

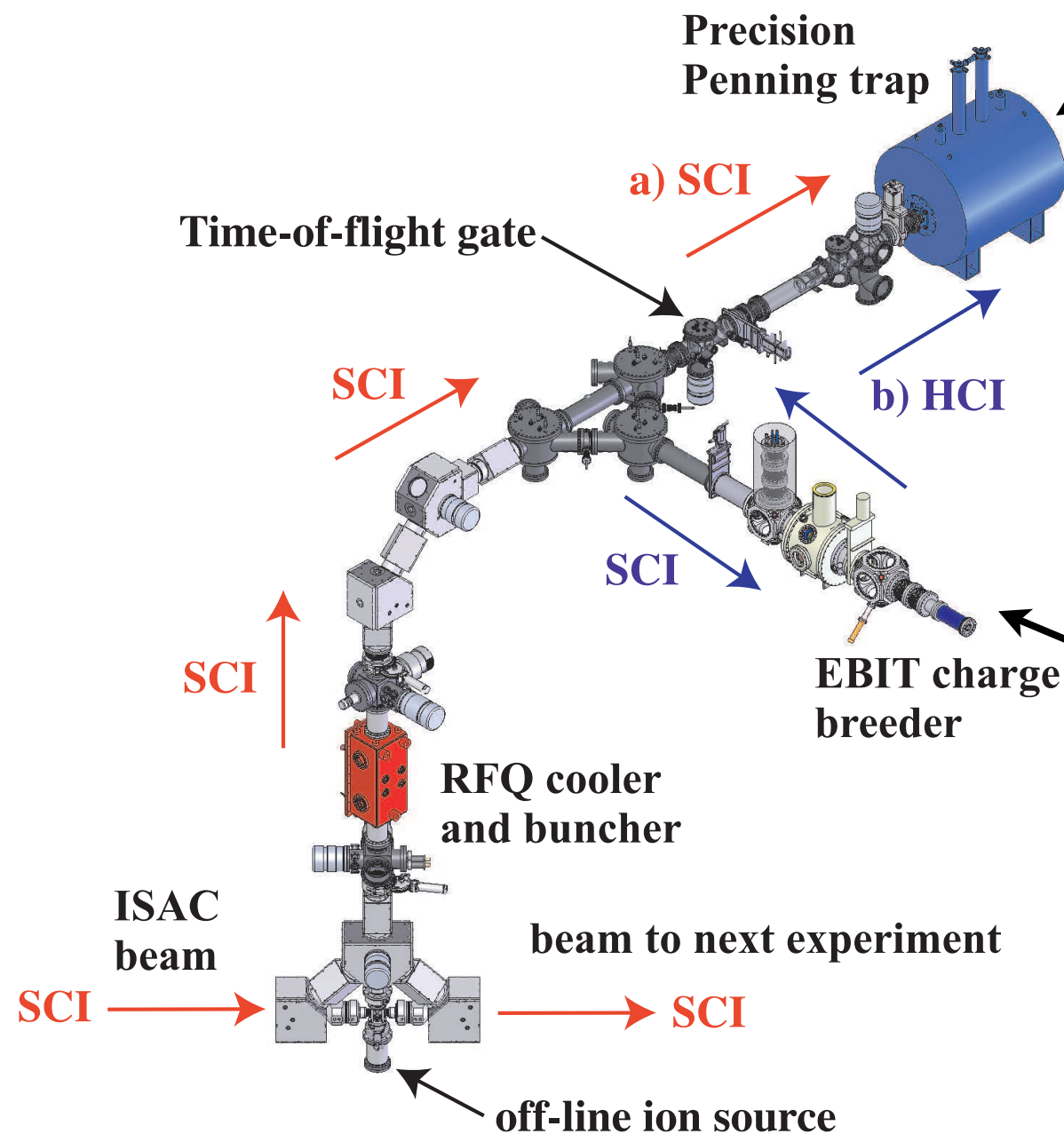
A. T. Gallant et al., PRL 113, 082501 (2014)

highly charged ions @ TITAN

$$\frac{\delta m}{m} \propto \frac{m}{q} \frac{1}{BTN^{1/2}}$$

Advantages:

- ➡ precision
- ➡ resolving power
- ➡ new separation schemes

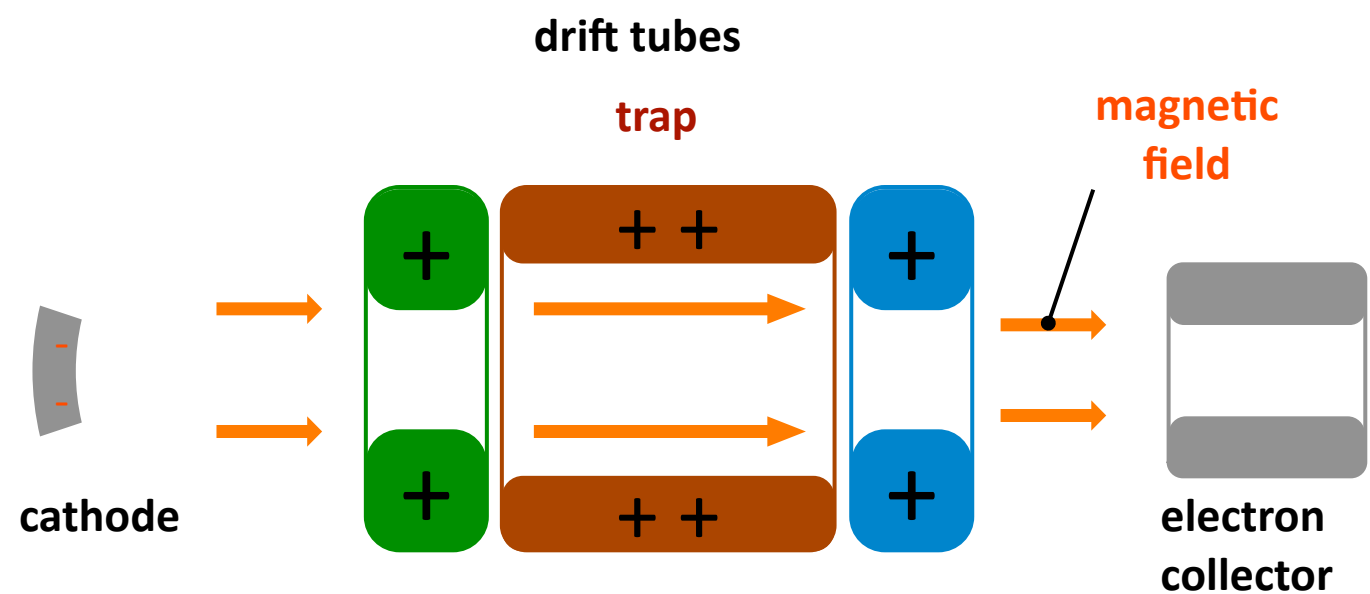
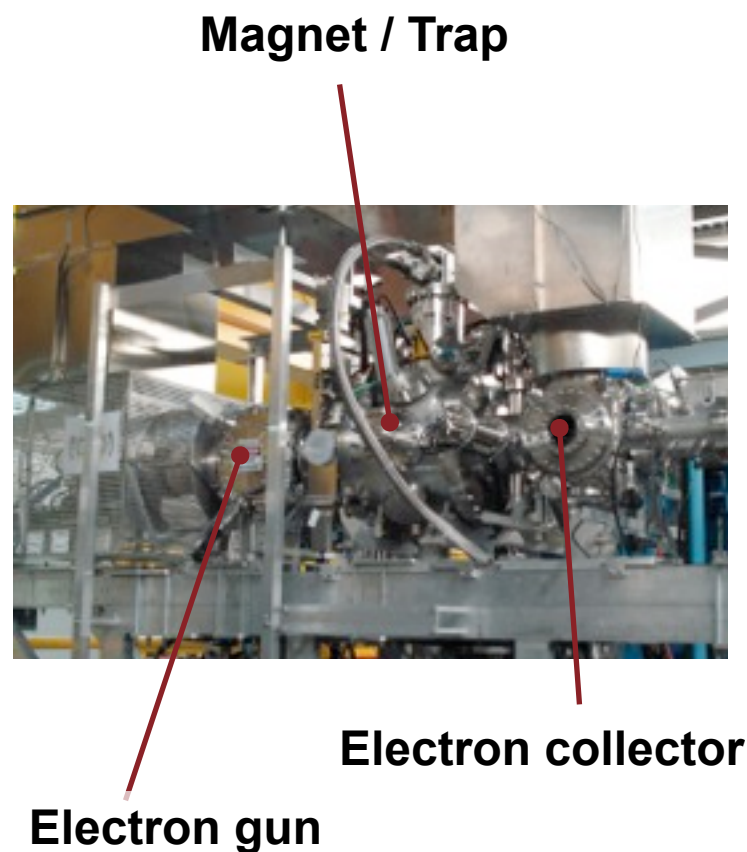


first demonstrated with ^{74}Rb ($T_{1/2}=65$ ms)

S. Ettenauer et al., PRL 107, 272501 (2011)



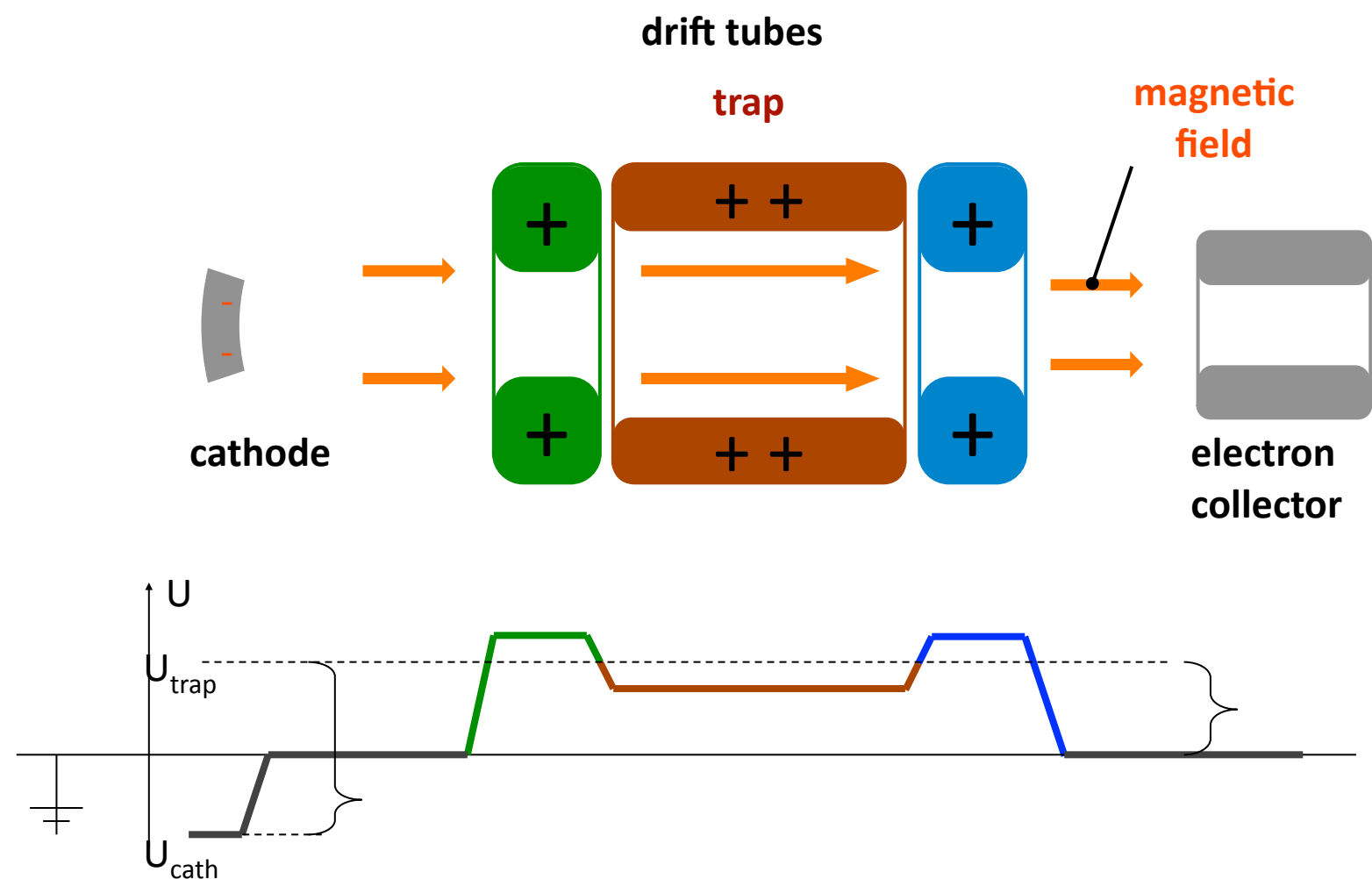
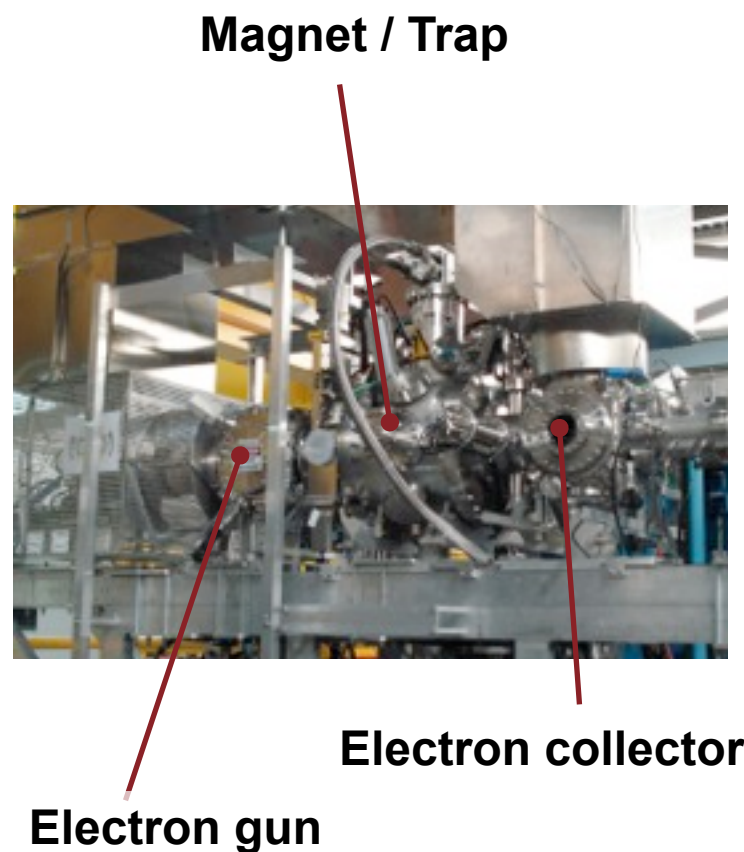
Electron Beam Ion Trap



requirements for charge breeding:

- efficient
- fast

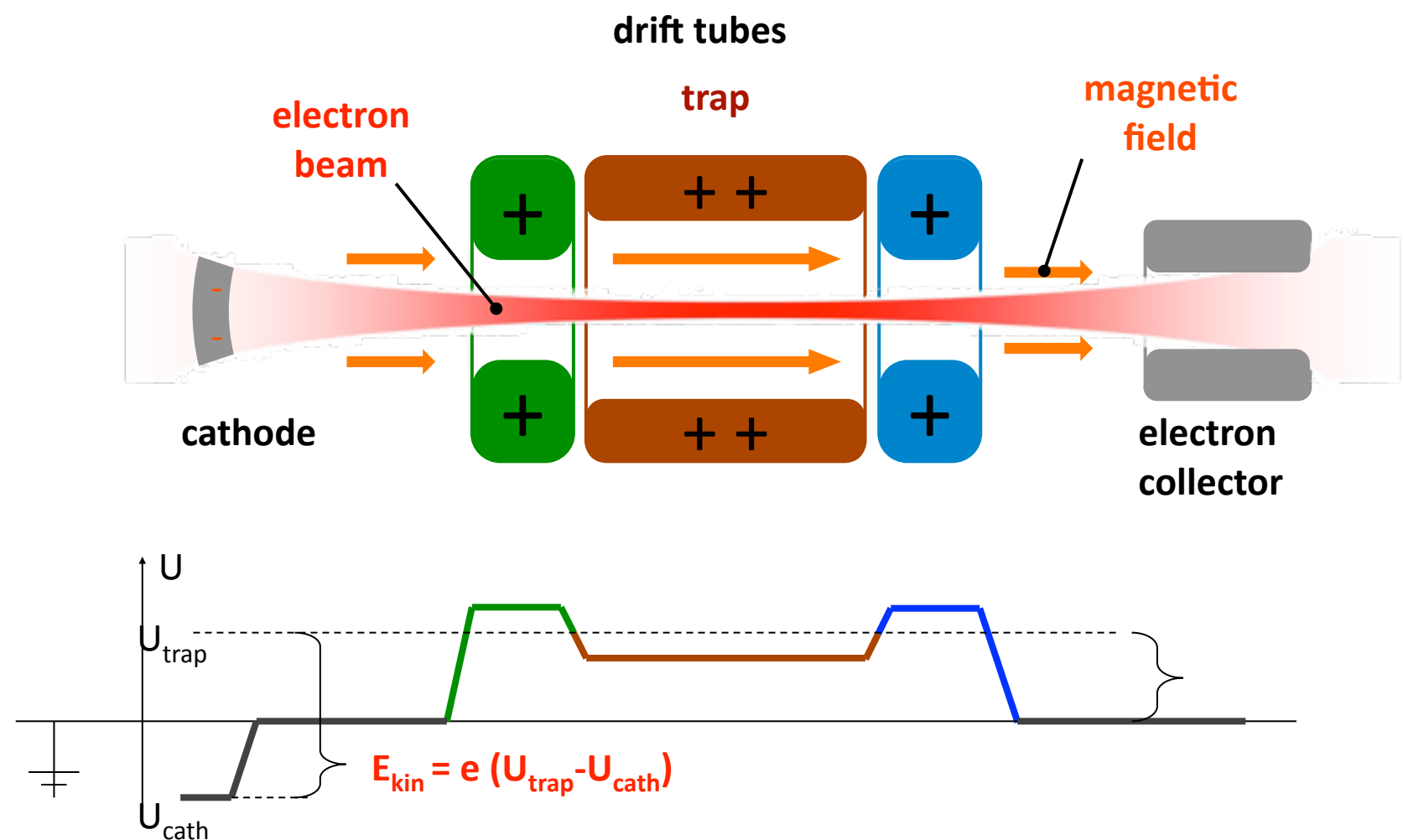
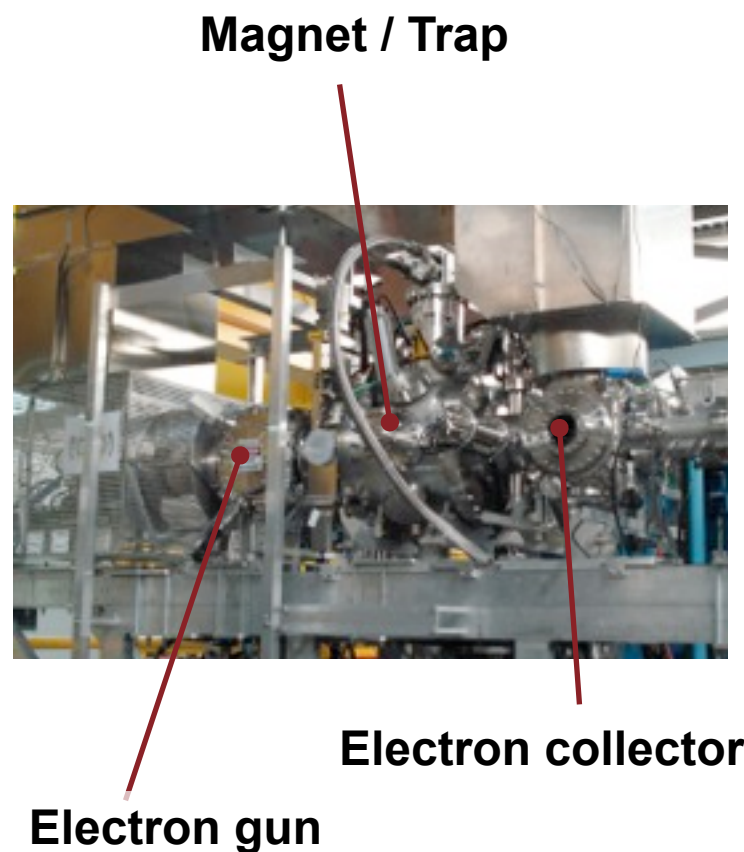
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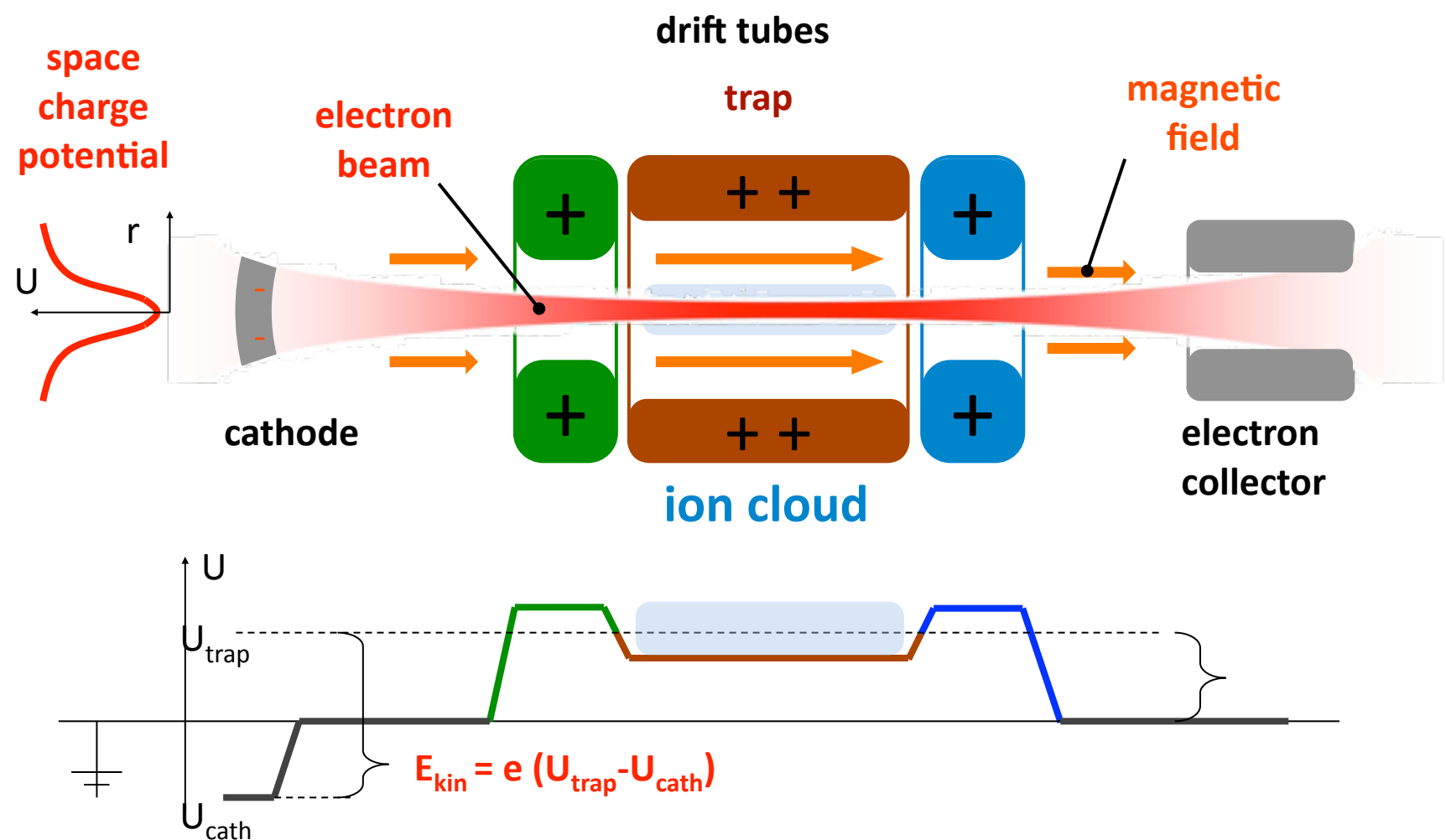
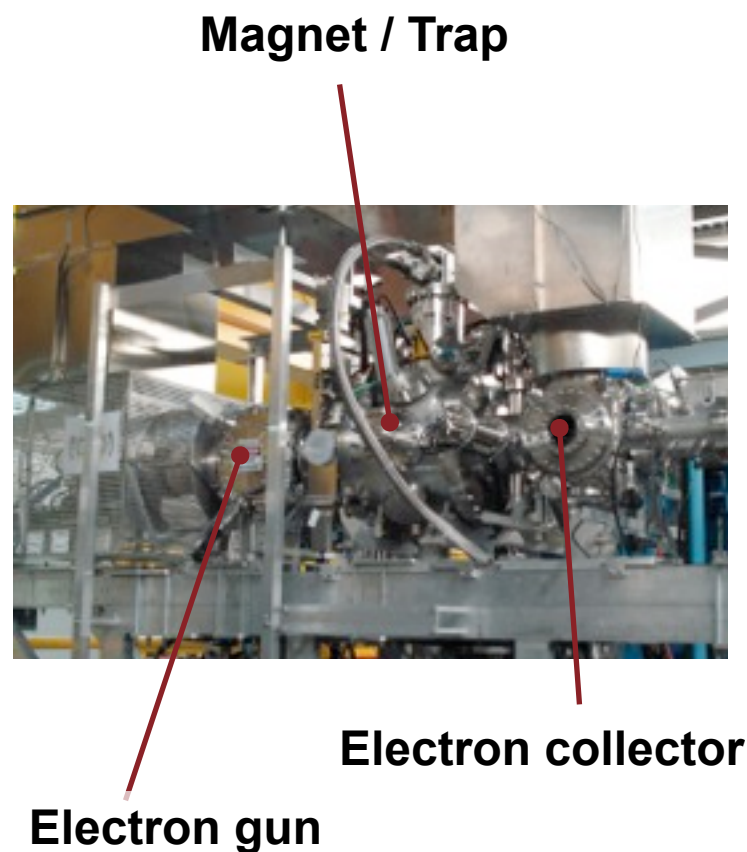
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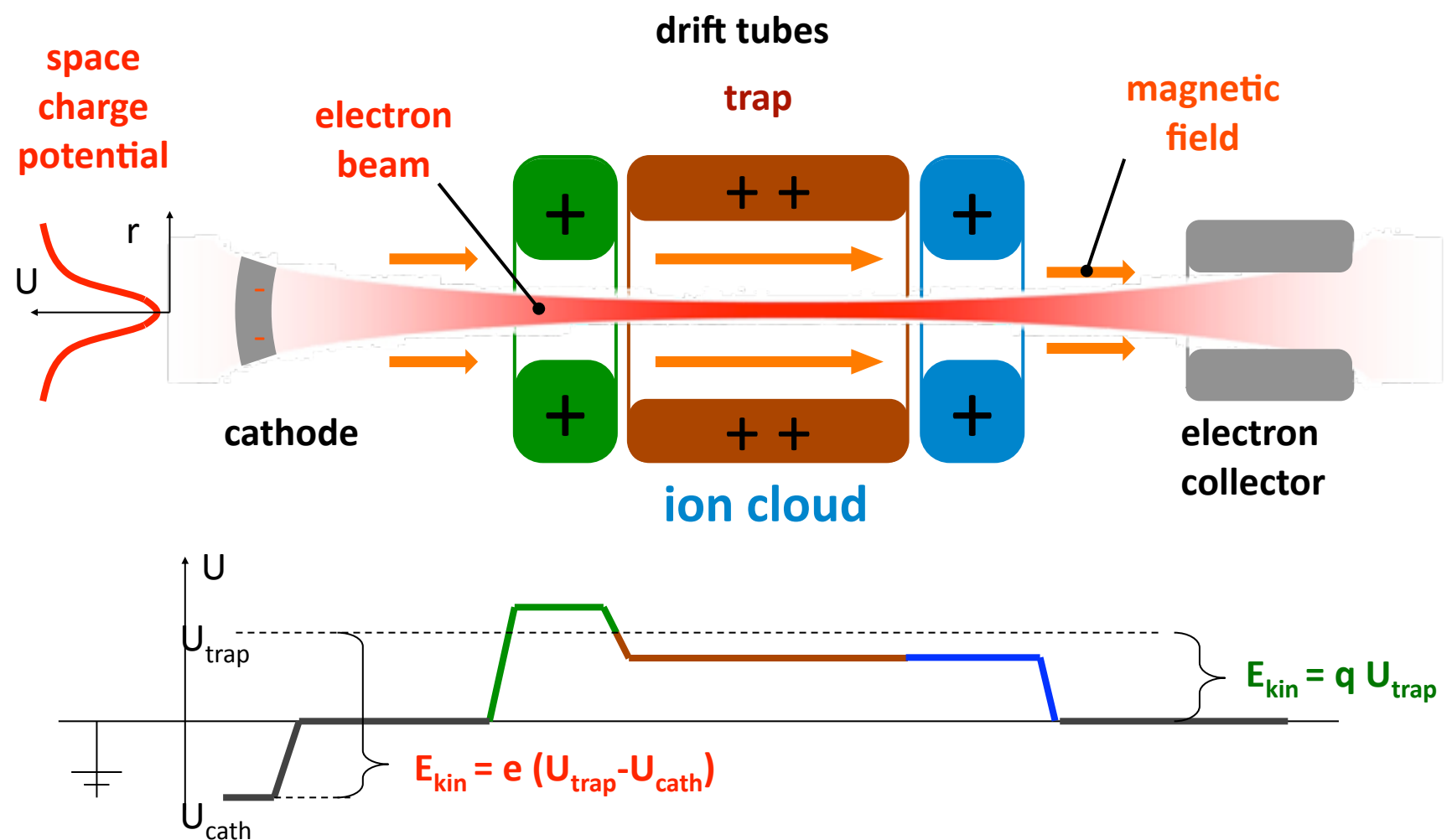
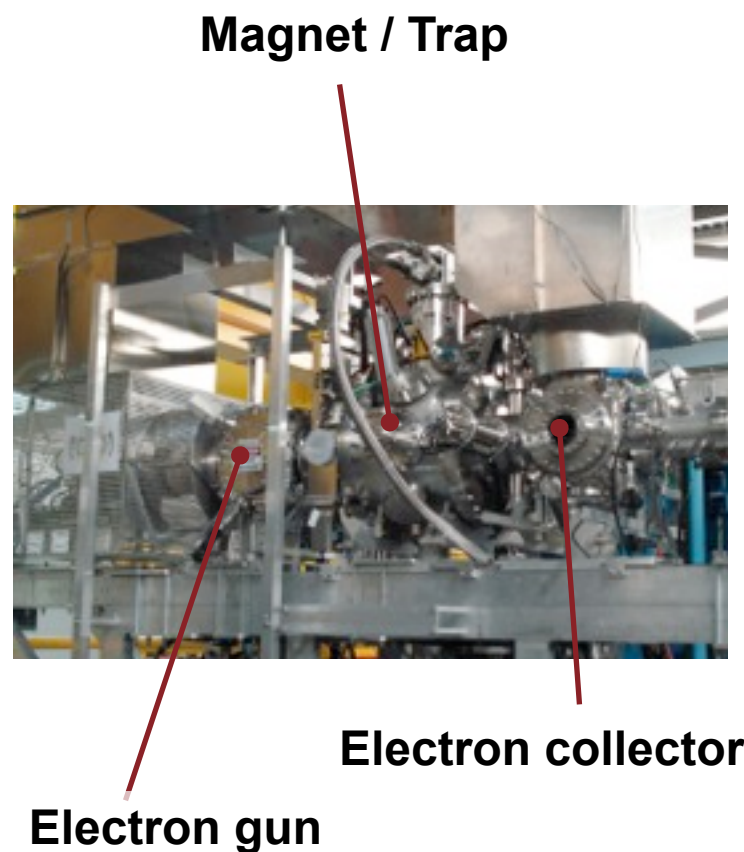
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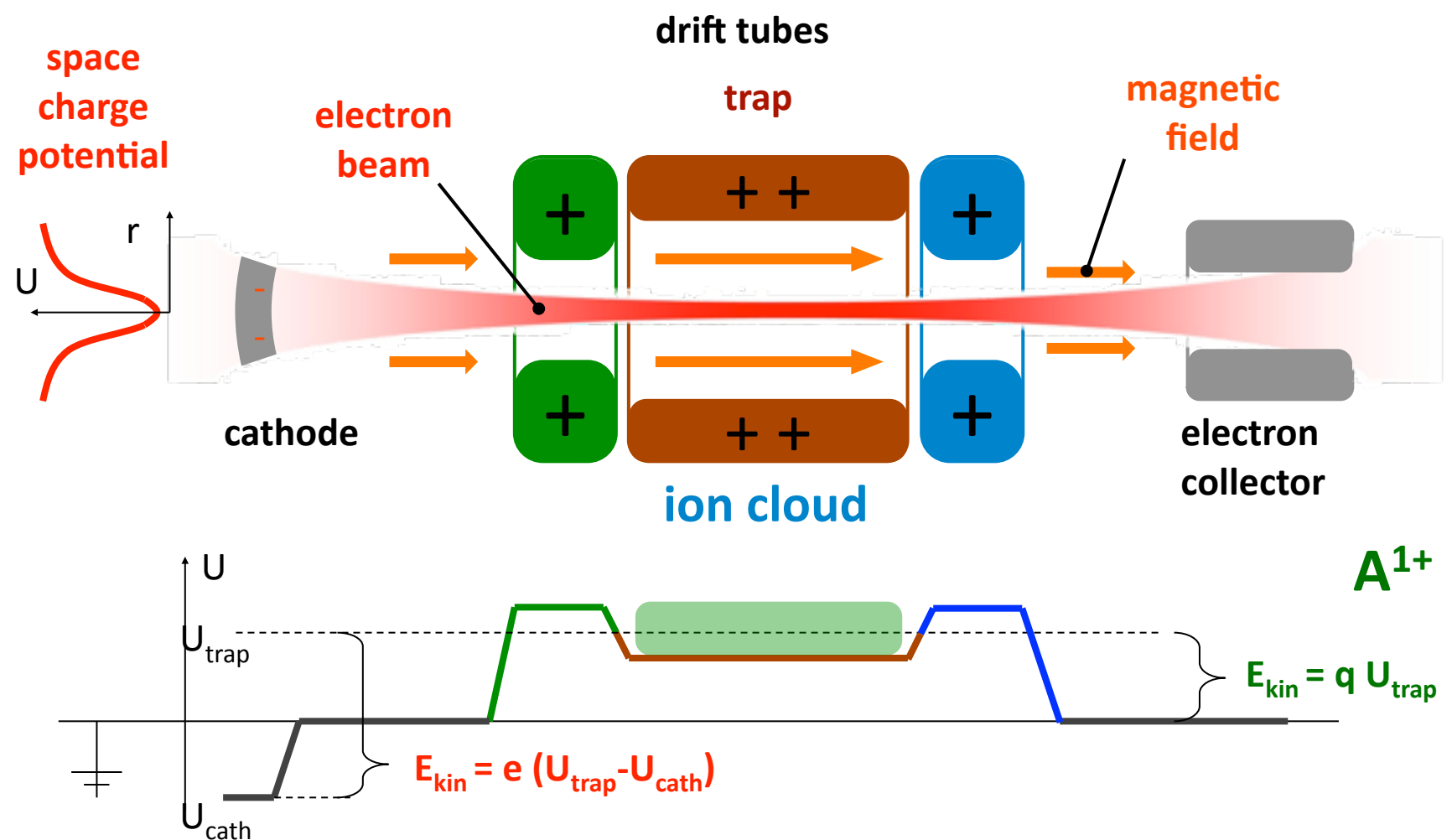
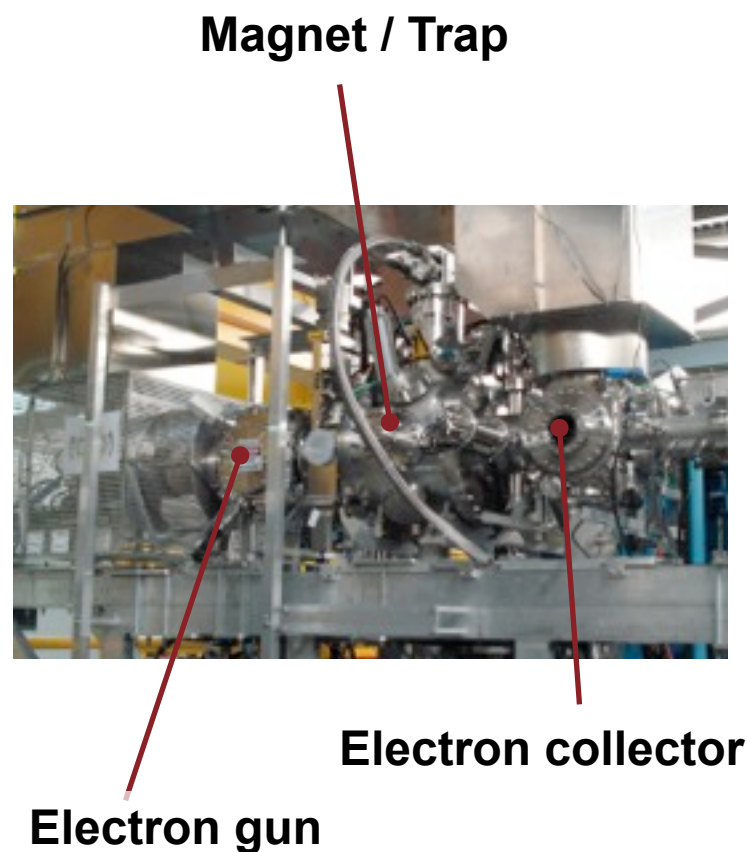
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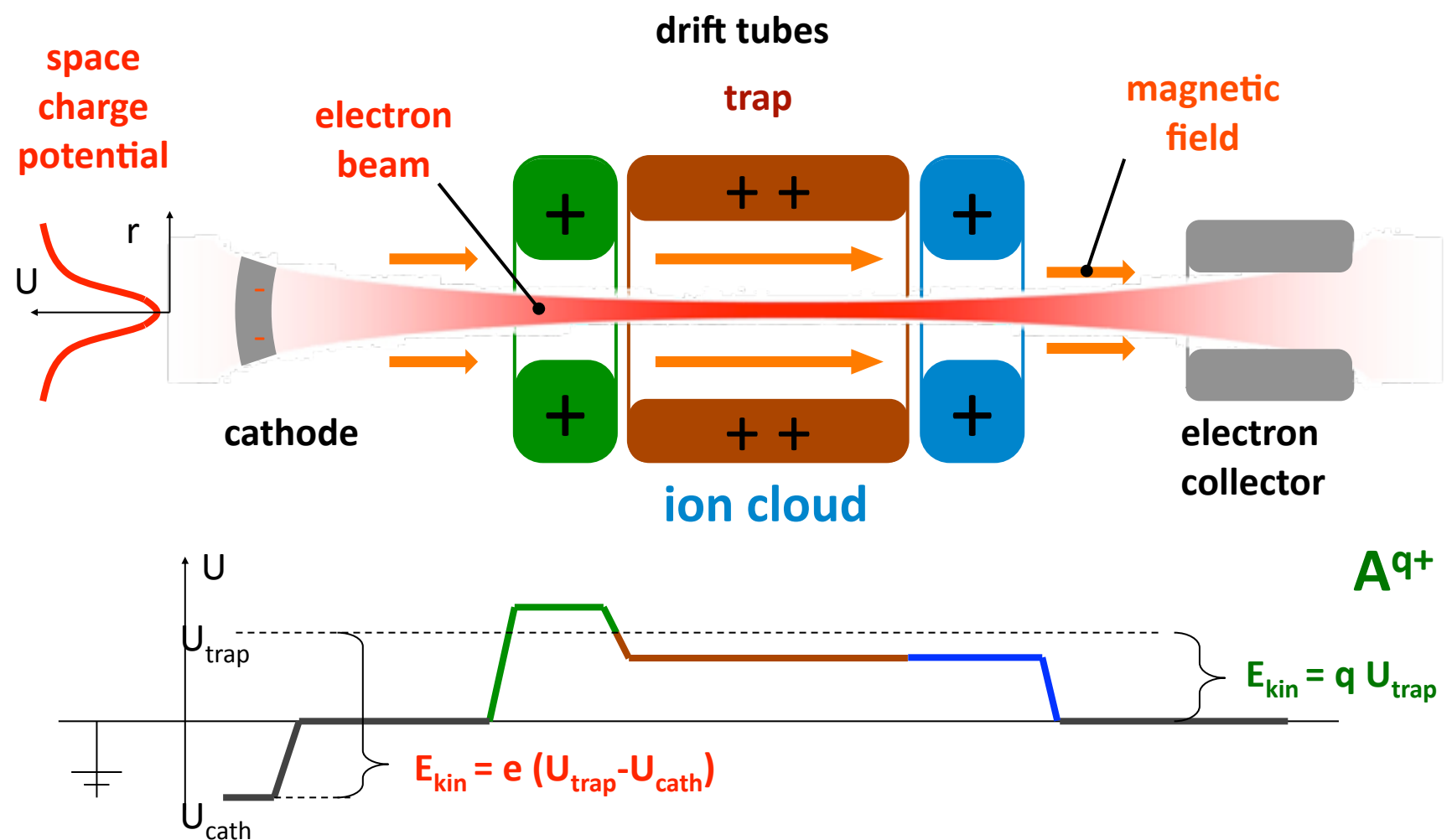
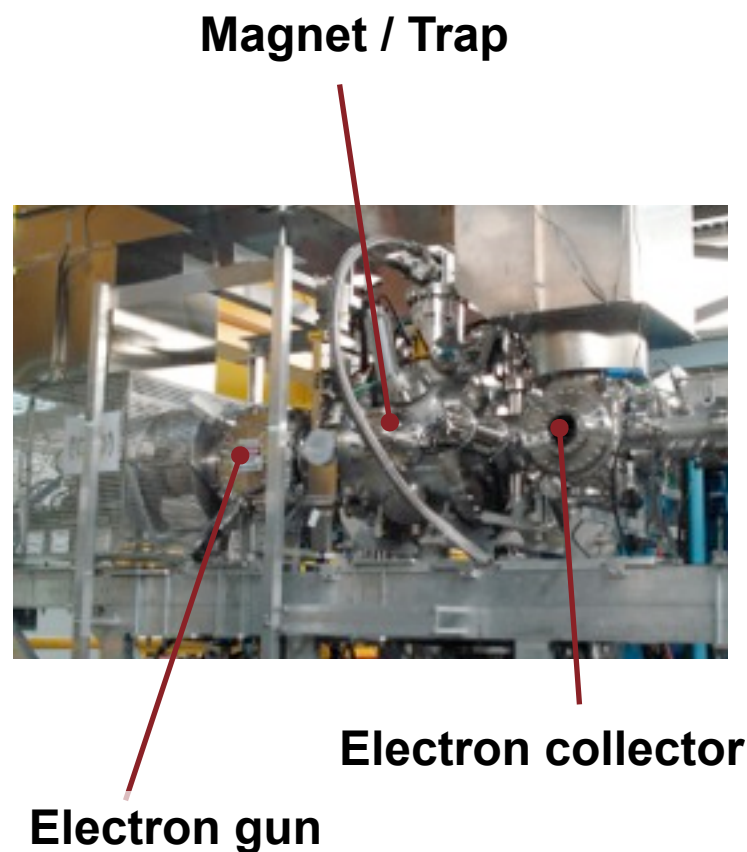
Electron Beam Ion Trap



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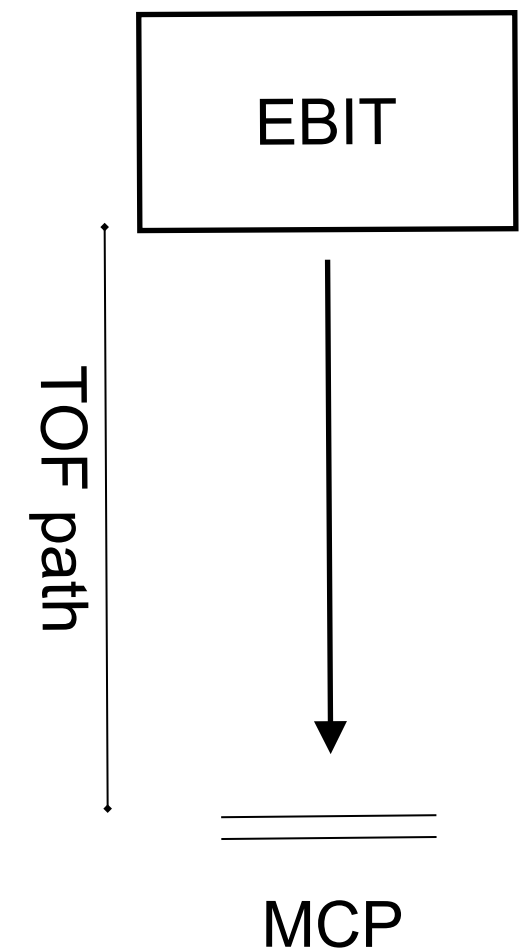
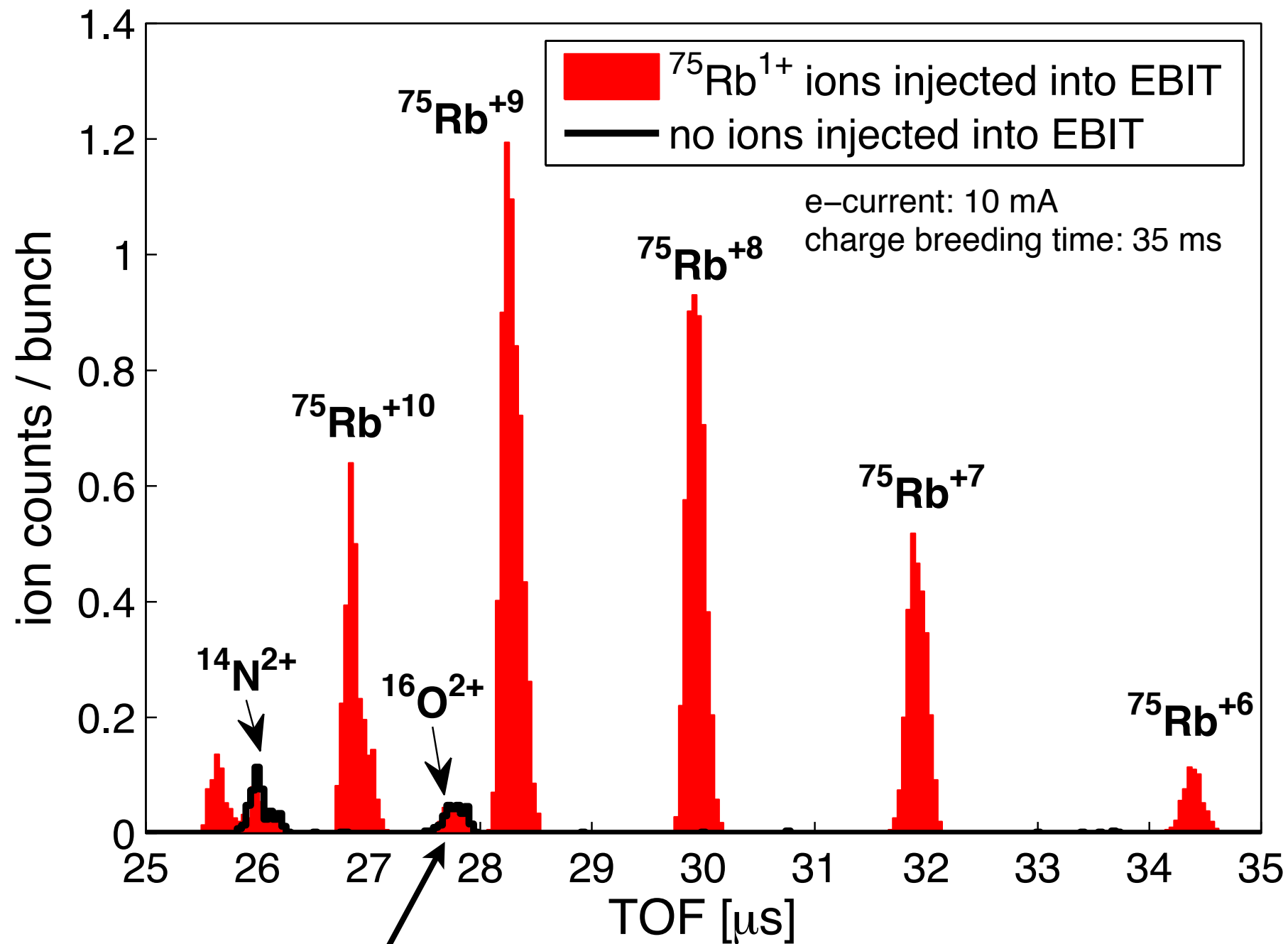
Electron Beam Ion Trap



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- efficient
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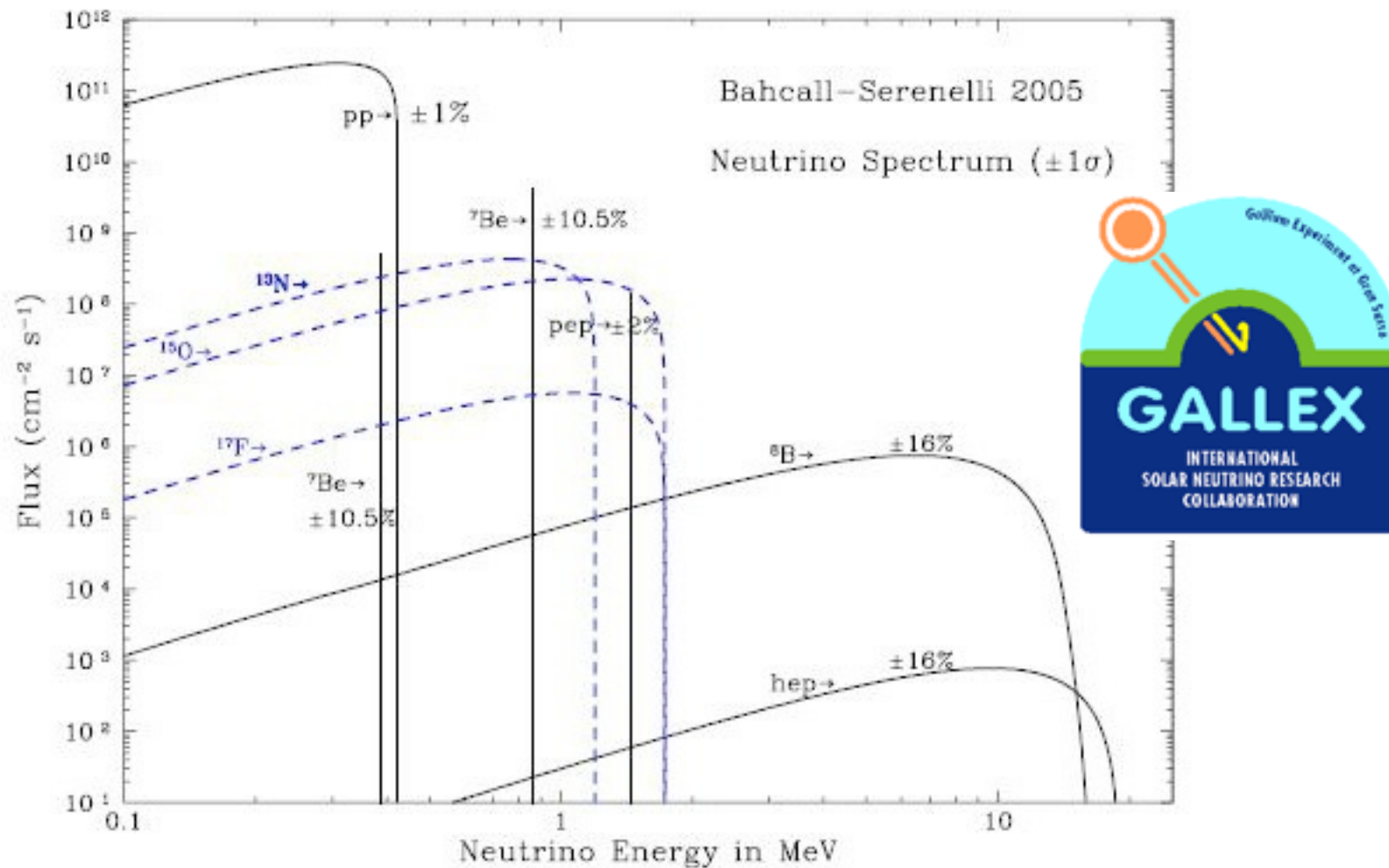
charge breeding of ^{75}Rb



charge bred residual gas

*S. Ettenauer et al.,
PRL 107, 272501 (2011)
Int. J. Mass Spectrom. 349, 74 (2013)*

Solar Neutrino Physics



Exp.	source	ratio
GALLEX	^{51}Cr -1	0.95 ± 0.11
GALLEX	^{51}Cr -2	0.81 ± 0.11
SAGE	^{51}Cr	0.95 ± 0.12
SAGE	^{37}Ar	0.79 ± 0.10
Average	$^{51}\text{Cr}, ^{37}\text{Ar}$	0.87 ± 0.05

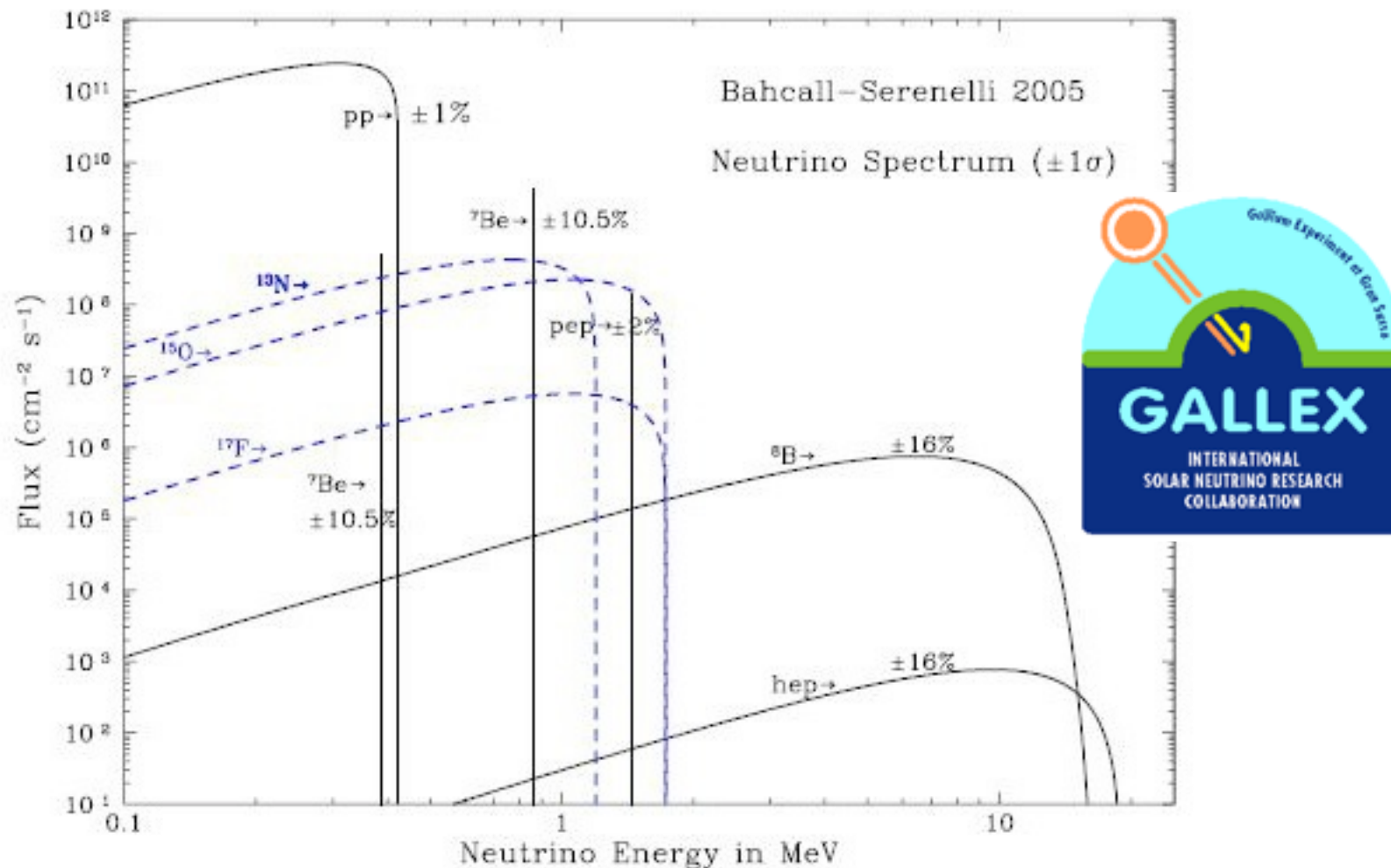
measured to expected events ?!?

cross section depends
on Q_{EC} of ^{71}Ge !

Detection reaction: $\nu_e + ^{71}\text{Ga} \rightarrow ^{71}\text{Ge} + e^-$

Detector calibration: EC of ^{51}Cr and ^{37}Ar

Solar Neutrino Physics



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Detection reaction: $\nu_e + ^{71}\text{Ga} \rightarrow ^{71}\text{Ge} + e^-$

Detector calibration: EC of ^{51}Cr and ^{37}Ar

HCl measurement of Q_{EC} of ^{51}Cr & ^{71}Ge

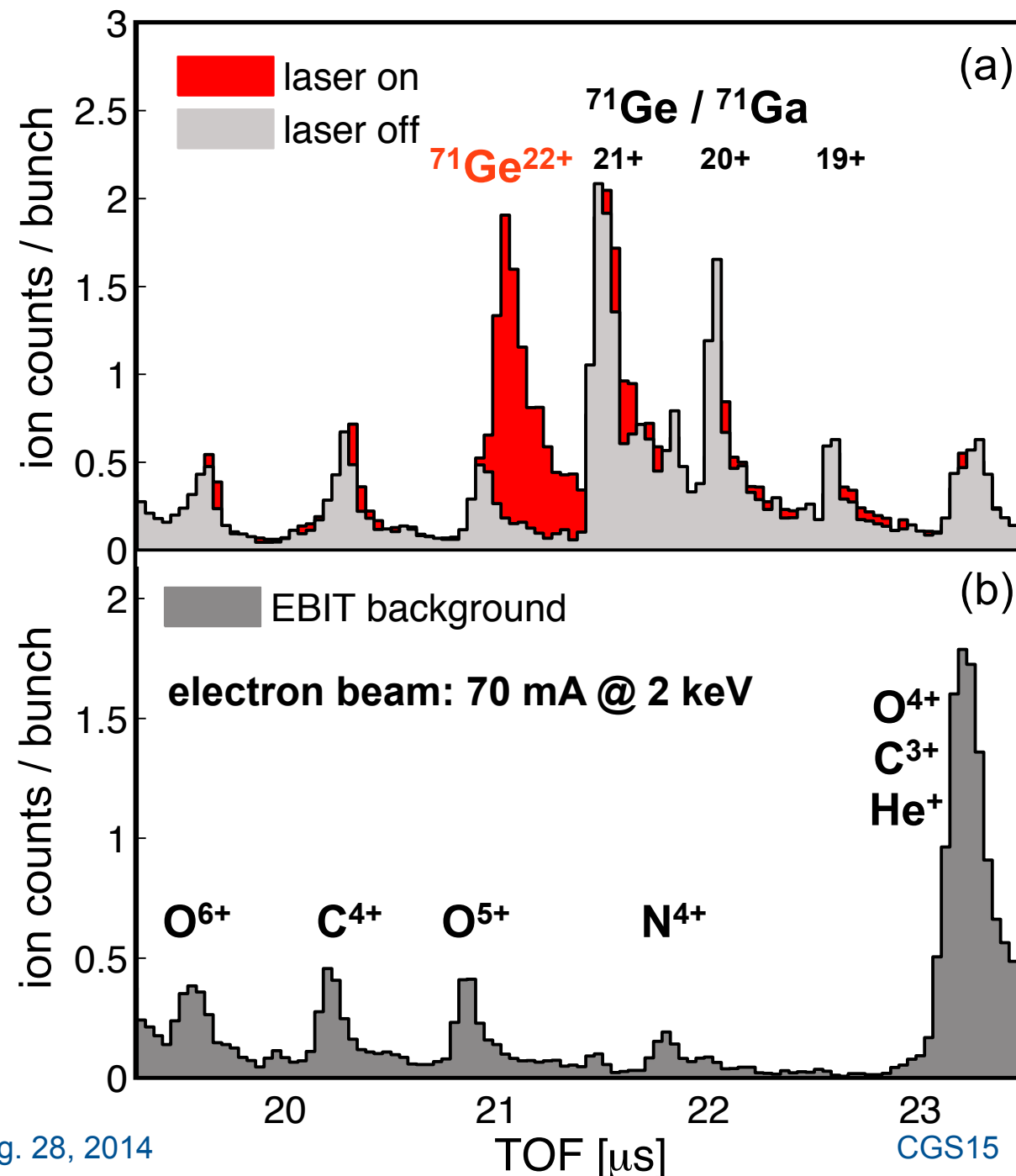
other nuclear physics uncertainties already excluded in [D. Frekers et al., Phys. Lett. B 706, 134 \(2011\)](#)

isobaric separation of ^{71}Ga - ^{71}Ge

Ge delivery from ISAC required Laser Ionization:

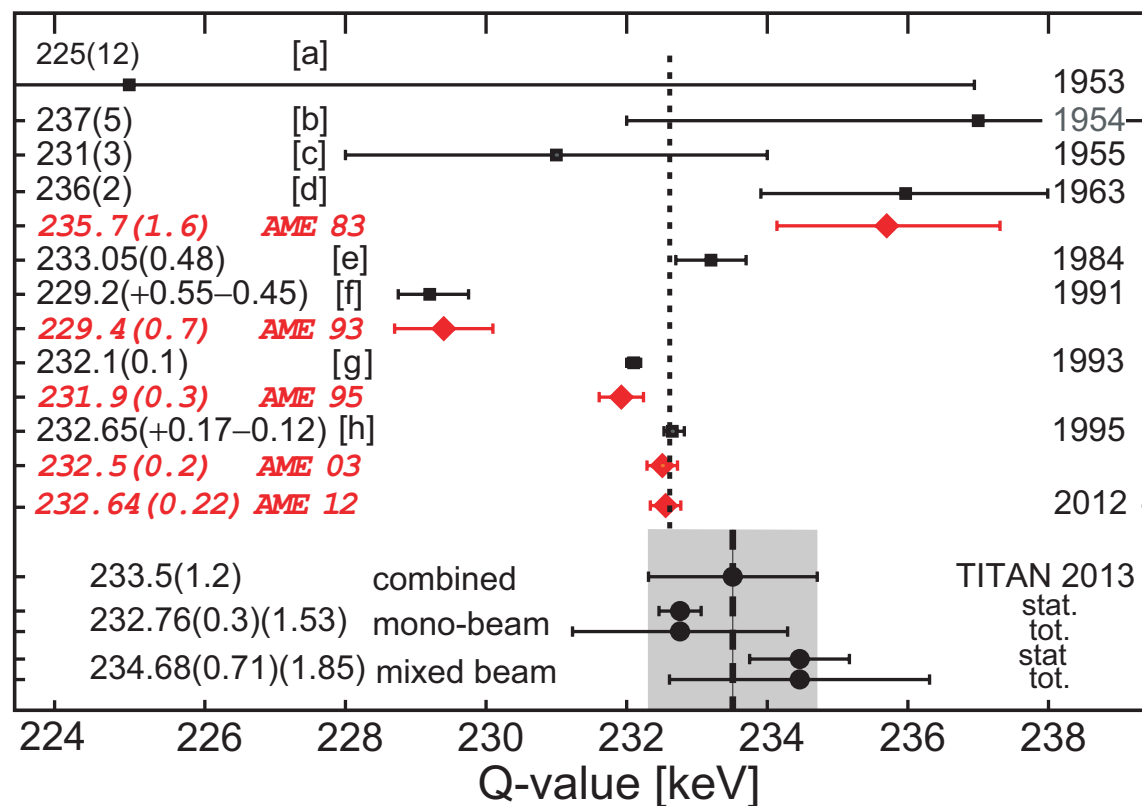
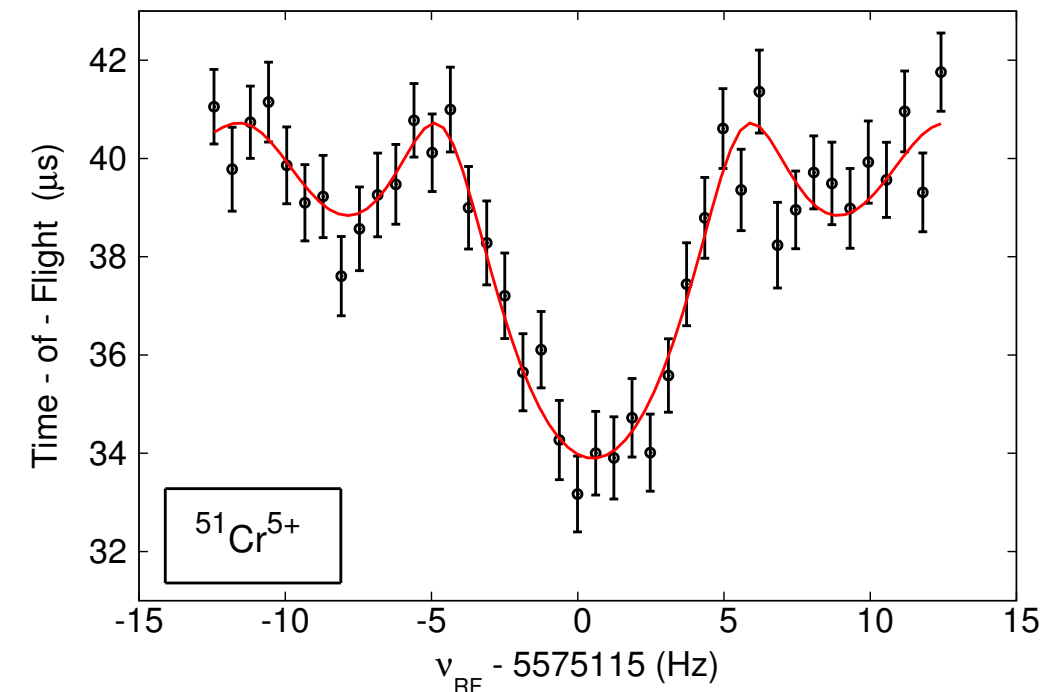
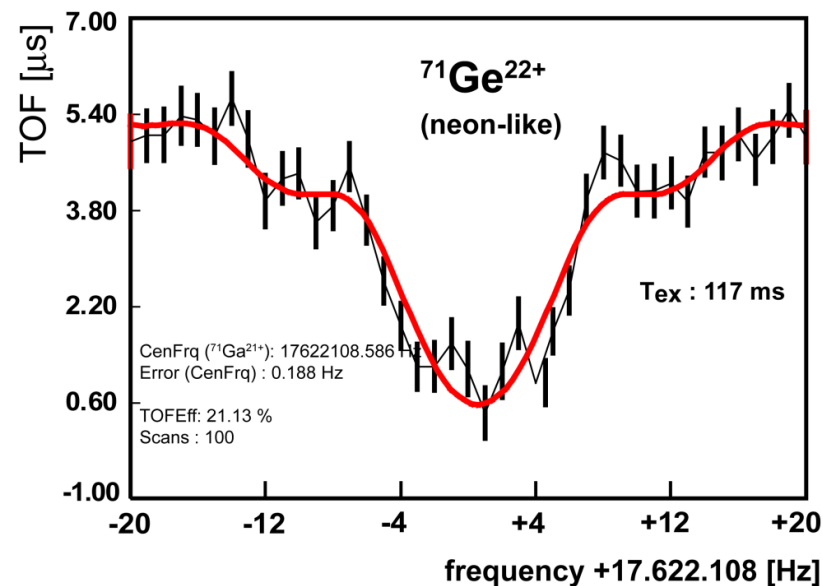
clean $^{71}\text{Ga}^{21+}$ if Laser OFF (Ga produced through surface ionization)

clean $^{71}\text{Ge}^{22+}$ if Laser ON (Ga not bred to $q=22+$)



→ separation based on atomic properties
→ no $\delta m/m$ -limit in resolving power

D. Frekers et al., Physics Letters B 722, 233 (2013)



Ion	Ref.	$R = \tilde{\nu}_c^V / \nu_c^{Cr}$	Q-value (keV)
$^{51}\text{Cr}^{5+}$	$^{51}\text{V}^{5+}$	1.000015851(14)	752.14(64)
$^{51}\text{Cr}^{6+}$	$^{51}\text{V}^{6+}$	1.000015827(23)	751.05(108)
Average Q-value:			751.86(55)
AME:			752.63(24)

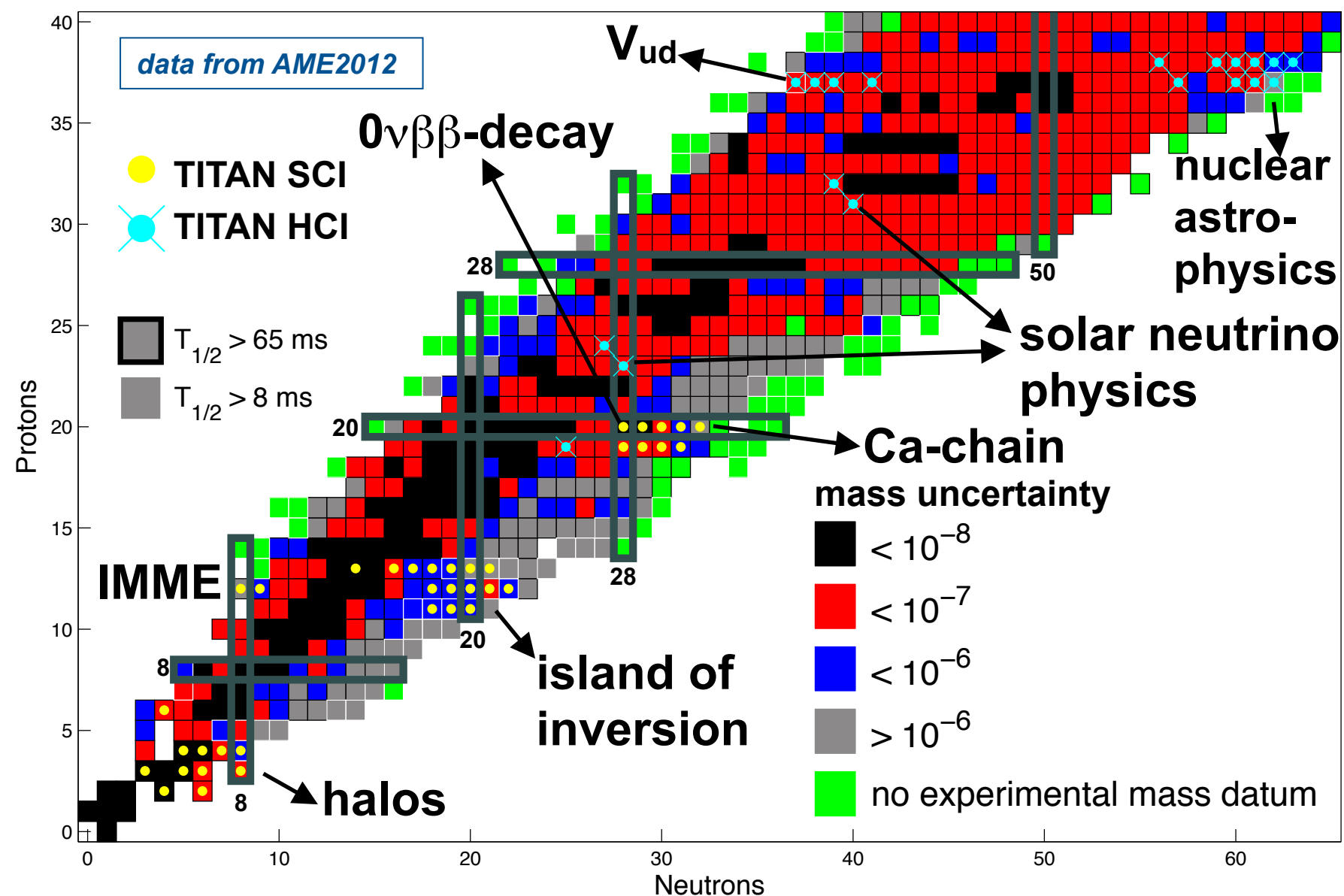
D. Frekers et al., Physics Letters B 722, 233 (2013)
T. D. Macdonald et al., Phys. Rev. C 89, 044318 (2014)

confirms previous Q_{EC} measurements

⇒ GALEX - SAGE discrepancy unresolved!

TITAN:

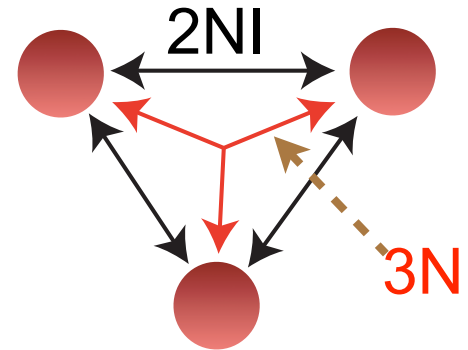
- ➡ only PT for nuclides with $T_{1/2}=10$ ms
- ➡ unique in use of radioactive HCl
 - precision
 - resolution
 - separation



summary

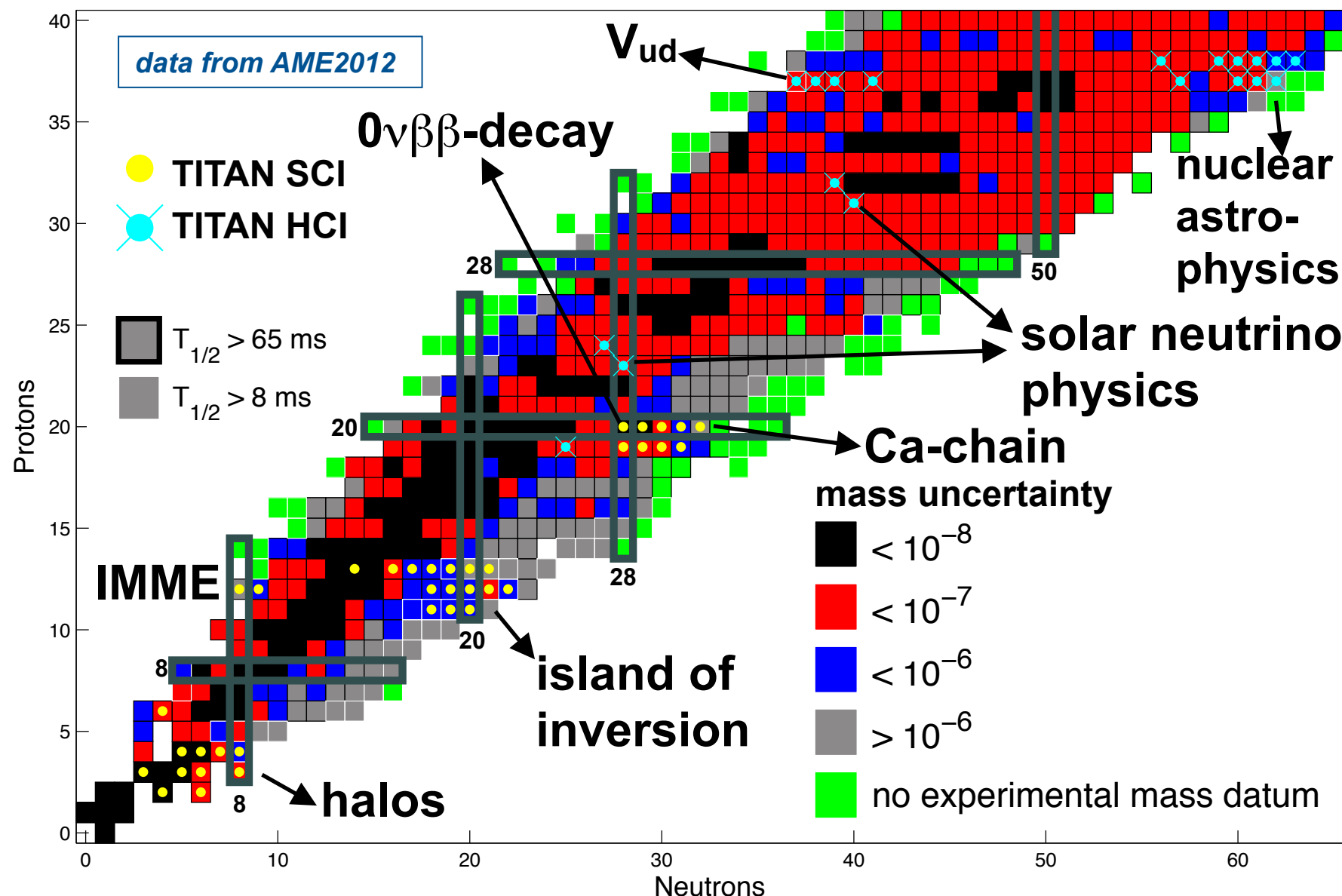
TITAN:

- ➡ only PT for nuclides with $T_{1/2}=10$ ms
- ➡ unique in use of radioactive HCl
 - precision
 - resolution
 - separation



3-body forces:

- new mass of ${}^6\text{He}$
 - masses of Ca-isotopes
 - ${}^{20,21}\text{Mg}$ for tests of IMME
- ➡ highlights successes and challenges of theory

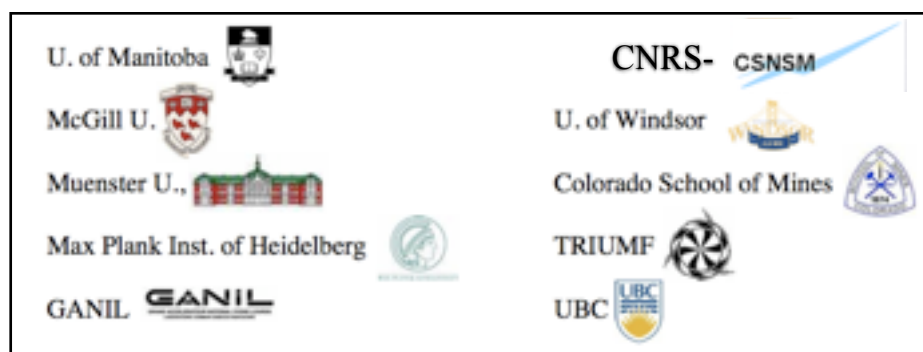


Ga-anomaly:

- confirmed Q_{EC} -values of ${}^{51}\text{Cr}$ & ${}^{71}\text{Ge}$
- ➡ discrepancy unresolved
- ➡ eliminates nuclear physics uncertainties

- ❖ **The TITAN Group:** Jens Dilling, Dieter Frekers, Gerald Gwinner, Melvin Good, Alain Lapierre, David Lunney, Mathew Pearson, Ryan Ringle, Corina Andreoiu, **Maxime Brodeur**, **Thomas Brunner**, **Ankur Chaudhuri**, **Stephan Malbrunot-Ettenauer**, **Alexander Grossheim**, **Ania Kwiatkowski**, **Kyle Leach** **Ernesto Mané**, **Brad Schultz**, **Martin C. Simon**, **Usman Chowdhury**, **Benjamin Eberhart**, **Aaron Gallant**, **R. Klawitter**, **Annika Lennarz**, **Tegan Macdonald**, **Vanessa Simon**, **Mathew Smith**
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And the rest of the TITAN collaboration....



- ❖ **Theory Calculations:** S. Bacca, G. W. F. Drake, J. D. Holt, J. Menéndez, J. Simonis, A. Schwenk, B. A. Brown

