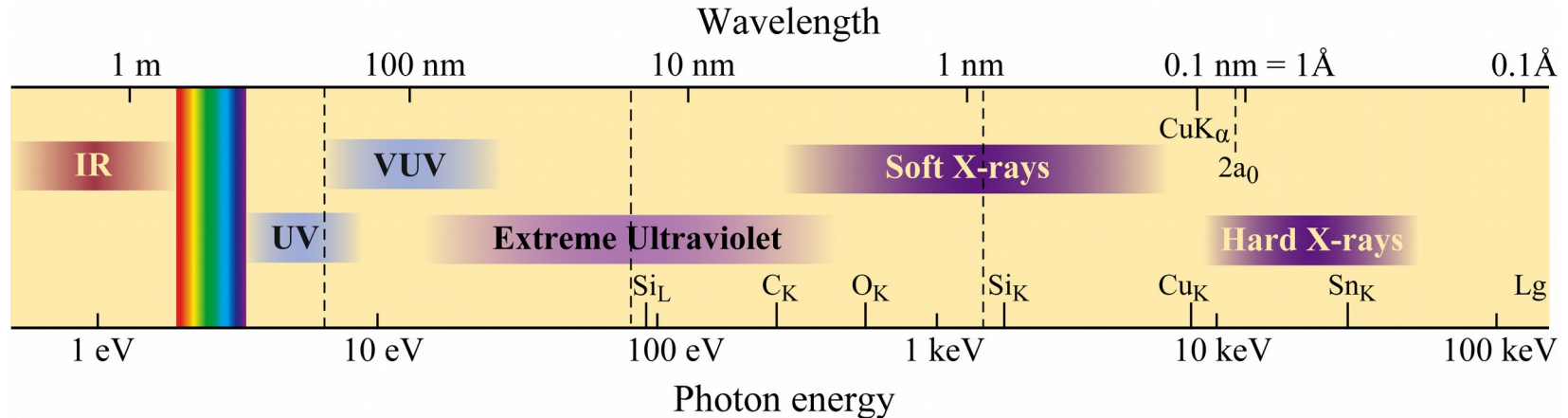




Introduction to Synchrotron Radiation

David Attwood
University of California, Berkeley

The short wavelength region of the electromagnetic spectrum



- Elemental and chemical sensitivity
- Penetrate visibly opaque objects
- See smaller features
- Write smaller patterns

Ch 01 F01 Feb2017 LG.ai

$$\hbar\omega \cdot \lambda = hc = 1239.842 \text{ eV nm}$$

$$n = 1 - \delta + i\beta \quad \delta, \beta \ll 1$$

Broadly tunable radiation is needed to probe the primary ($n = 1$ & $n = 2$) resonances of the elements



Periodic Table of the Elements

<div> <div>Group IA</div> <div>1 1.0079 H 1s¹ Hydrogen</div> <div>3 6.941 Li 1s² 2s¹ Lithium</div> <div>11 22.990 Na [Ne]3s¹ Sodium</div> <div>19 39.098 K [Ar]4s¹ Potassium</div> <div>37 85.47 Rb [Kr]5s¹ Rubidium</div> <div>55 132.91 Cs [Xe]6s¹ Cesium</div> <div>87 (223) Fr [Rn]7s¹ Francium</div> </div>																		<div>VIII</div> <div>2 4.003 He 1s² Helium</div> <div>10 20.180 Ne 1s² 2s² 2p⁶ Neon</div> <div>18 39.948 Ar [Ne]3s² 3p⁶ Argon</div> <div>36 83.80 Kr [Ar]3d¹⁰ 4s² 4p⁶ Krypton</div> <div>54 131.29 Xe [Kr]4d¹⁰ 5s² 5p⁶ Xenon</div> <div>86 (222) Rn [Xe]4f¹⁴ 5d¹⁰ 6s² 6p⁶ Radon</div>									
<div> <div>IIA</div> <div>4 9.012 Be 1s² 2s² Beryllium</div> <div>12 24.31 Mg [Ne]3s² Magnesium</div> <div>20 40.08 Ca [Ar]4s² Calcium</div> <div>38 87.62 Sr [Kr]5s² Strontium</div> <div>56 137.33 Ba [Xe]6s² Barium</div> <div>88 (226) Ra [Rn]7s² Radium</div> </div>																											
<div> <div>IIIB</div> <div>5 10.81 B 2s² 2s² 2p¹ Boron</div> <div>13 26.98 Al [Ne]3s² 3p¹ Aluminum</div> <div>21 39.098 Ga [Ar]3d¹⁰ 4s² 4p¹ Gallium</div> <div>31 69.72 In [Kr]4d¹⁰ 5s² 5p¹ Indium</div> <div>49 114.82 Tl [Xe]4f¹⁴ 5d¹⁰ 6s² 6p¹ Thallium</div> <div>81 204.38 Pb [Xe]4f¹⁴ 5d¹⁰ 6s² 6p² Lead</div> </div>																											
<div> <div>IVB</div> <div>6 12.011 C 1s² 2s² 2p² Carbon</div> <div>14 28.09 Si [Ne]3s² 3p² Silicon</div> <div>22 47.88 Ti [Ar]3d² 4s² Titanium</div> <div>30 69.72 Zn [Ar]3d¹⁰ 4s² Zinc</div> <div>48 112.41 Cd [Kr]4d¹⁰ 5s² Cadmium</div> <div>80 200.59 Hg [Xe]4f¹⁴ 5d¹⁰ 6s² Mercury</div> </div>																											
<div> <div>VB</div> <div>7 14.007 N 1s² 2s² 2p³ Nitrogen</div> <div>15 30.974 P [Ne]3s² 3p³ Phosphorus</div> <div>23 50.94 V [Ar]3d³ 4s² Vanadium</div> <div>31 69.72 Ga [Ar]3d¹⁰ 4s² 4p¹ Gallium</div> <div>49 114.82 Tl [Kr]4d¹⁰ 5s² 5p¹ Indium</div> <div>81 204.38 Pb [Xe]4f¹⁴ 5d¹⁰ 6s² 6p² Lead</div> </div>																											
<div> <div>VIB</div> <div>8 16 O 1s² 2s² 2p⁴ Oxygen</div> <div>16 32.066 S [Ne]3s² 3p⁴ Sulfur</div> <div>24 47.88 Cr [Ar]3d⁵ 4s¹ Chromium</div> <div>32 72.61 Ge [Ar]3d¹⁰ 4s² 4p² Germanium</div> <div>50 118.71 Sn [Kr]4d¹⁰ 5s² 5p² Tin</div> <div>82 207.2 Pb [Xe]4f¹⁴ 5d¹⁰ 6s² 6p² Lead</div> </div>																											
<div> <div>VII B</div> <div>9 19.00 F 1s² 2s² 2p⁵ Fluorine</div> <div>17 35.453 Cl [Ne]3s² 3p⁵ Chlorine</div> <div>25 50.94 Mn [Ar]3d⁵ 4s² Manganese</div> <div>33 74.92 As [Ar]3d¹⁰ 4s² 4p³ Arsenic</div> <div>51 127.60 Sb [Kr]4d¹⁰ 5s² 5p³ Antimony</div> <div>83 208.98 Bi [Xe]4f¹⁴ 5d¹⁰ 6s² 6p³ Bismuth</div> </div>																											
<div> <div>Key</div> <div>Atomic number → 14</div> <div>Atomic weight → 28.09</div> <div>Density (g/cm³) → 2.33</div> <div>Concentration (10²² atoms/cm³) → 4.99</div> <div>Nearest neighbor (Å) → 2.35</div> <div>Name → Silicon</div> <div>Oxidation states (Bold most stable) → 4</div> <div>Symbol → Si</div> <div>Electron configuration → [Ne]3s² 3p²</div> <div>State: Solid (black), Gas (blue), Liquid (green), Synthetically prepared (red)</div> </div>																											
<div> <div>References: International Tables for X-ray Crystallography (Reidel, London, 1983) (Ref. 33) and J.R. De Laeter and K.G. Heumann (Ref. 34, 1991); NIST Sept. 2014).</div> </div>																											
<div> <div>IIIB</div> <div>5 10.81 B 2s² 2s² 2p¹ Boron</div> <div>13 26.98 Al [Ne]3s² 3p¹ Aluminum</div> <div>21 39.098 Ga [Ar]3d¹⁰ 4s² 4p¹ Gallium</div> <div>31 69.72 In [Kr]4d¹⁰ 5s² 5p¹ Indium</div> <div>49 114.82 Tl [Xe]4f¹⁴ 5d¹⁰ 6s² 6p¹ Thallium</div> <div>81 204.38 Pb [Xe]4f¹⁴ 5d¹⁰ 6s² 6p² Lead</div> </div>																											
<div> <div>IVB</div> <div>6 12.011 C 1s² 2s² 2p² Carbon</div> <div>14 28.09 Si [Ne]3s² 3p² Silicon</div> <div>22 47.88 Ti [Ar]3d² 4s² Titanium</div> <div>30 69.72 Zn [Ar]3d¹⁰ 4s² Zinc</div> <div>48 112.41 Cd [Kr]4d¹⁰ 5s² Cadmium</div> <div>80 200.59 Hg [Xe]4f¹⁴ 5d¹⁰ 6s² Mercury</div> </div>																											
<div> <div>VB</div> <div>7 14.007 N 1s² 2s² 2p³ Nitrogen</div> <div>15 30.974 P [Ne]3s² 3p³ Phosphorus</div> <div>23 50.94 V [Ar]3d³ 4s² Vanadium</div> <div>31 69.72 Ga [Ar]3d¹⁰ 4s² 4p¹ Gallium</div> <div>49 114.82 Tl [Kr]4d¹⁰ 5s² 5p¹ Indium</div> <div>81 204.38 Pb [Xe]4f¹⁴ 5d¹⁰ 6s² 6p² Lead</div> </div>																											
<div> <div>VIB</div> <div>8 16 O 1s² 2s² 2p⁴ Oxygen</div> <div>16 32.066 S [Ne]3s² 3p⁴ Sulfur</div> <div>24 47.88 Cr [Ar]3d⁵ 4s¹ Chromium</div> <div>32 72.61 Ge [Ar]3d¹⁰ 4s² 4p² Germanium</div> <div>50 118.71 Sn [Kr]4d¹⁰ 5s² 5p² Tin</div> <div>82 207.2 Pb [Xe]4f¹⁴ 5d¹⁰ 6s² 6p² Lead</div> </div>																											
<div> <div>VII B</div> <div>9 19.00 F 1s² 2s² 2p⁵ Fluorine</div> <div>17 35.453 Cl [Ne]3s² 3p⁵ Chlorine</div> <div>25 50.94 Mn [Ar]3d⁵ 4s² Manganese</div> <div>33 74.92 As [Ar]3d¹⁰ 4s² 4p³ Arsenic</div> <div>51 127.60 Sb [Kr]4d¹⁰ 5s² 5p³ Antimony</div> <div>83 208.98 Bi [Xe]4f¹⁴ 5d¹⁰ 6s² 6p³ Bismuth</div> </div>																											
<div> <div>VIII</div> <div>10 20.180 Ne 1s² 2s² 2p⁶ Neon</div> <div>18 39.948 Ar [Ne]3s² 3p⁶ Argon</div> <div>36 83.80 Kr [Ar]3d¹⁰ 4s² 4p⁶ Krypton</div> <div>54 131.29 Xe [Kr]4d¹⁰ 5s² 5p⁶ Xenon</div> <div>86 (222) Rn [Xe]4f¹⁴ 5d¹⁰ 6s² 6p⁶ Radon</div> </div>																											

Lanthanide series

58 140.12 Ce [Xe]4f ¹ 5d ¹ 6s ² Cerium	59 140.91 Pr [Xe]4f ³ 6s ² Praseodymium	60 144.24 Nd [Xe]4f ⁴ 6s ² Neodymium	61 (145) Pm [Xe]4f ⁵ 6s ² Promethium	62 150.36 Sm [Xe]4f ⁶ 6s ² Samarium	63 152.0 Eu [Xe]4f ⁷ 6s ² Europium	64 157.25 Gd [Xe]4f ⁷ 5d ¹ 6s ² Gadolinium	65 158.93 Tb [Xe]4f ⁹ 6s ² Terbium	66 162.50 Dy [Xe]4f ¹⁰ 6s ² Dysprosium	67 164.93 Ho [Xe]4f ¹¹ 6s ² Holmium	68 167.26 Er [Xe]4f ¹² 6s ² Erbium	69 168.93 Tm [Xe]4f ¹³ 6s ² Thulium	70 173.04 Yb [Xe]4f ¹⁴ 6s ² Ytterbium	71 174.97 Lu [Xe]4f ¹⁴ 5d ¹ 6s ² Lutetium
--	--	---	---	--	---	--	---	---	--	---	--	--	---

Actinide series

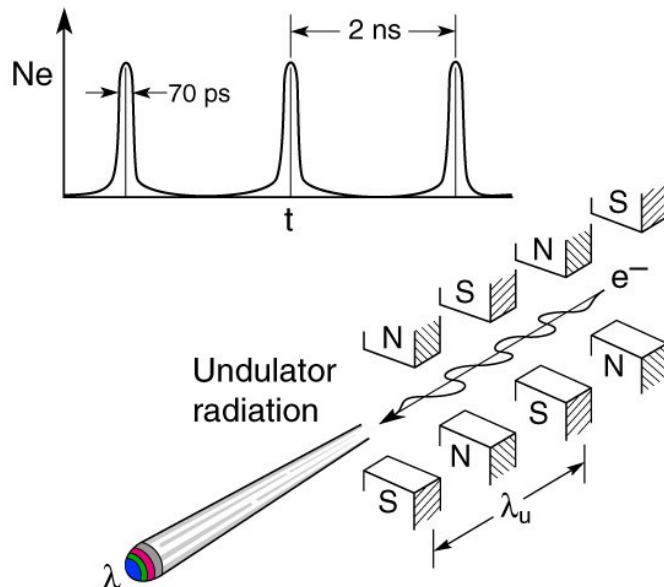
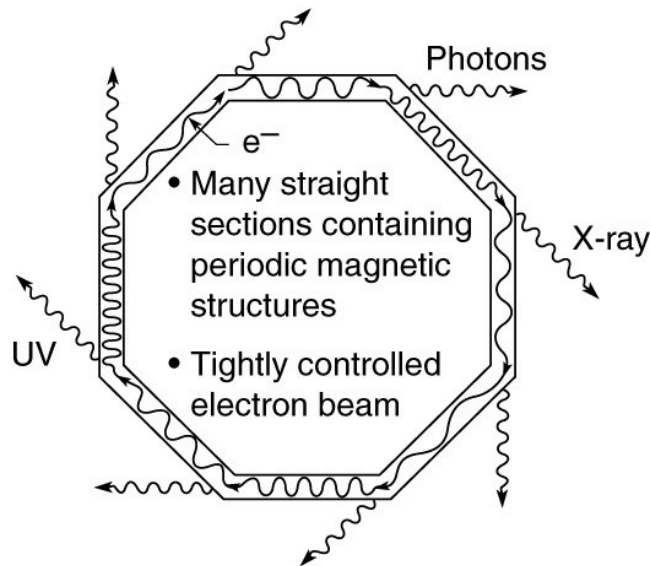
90 232.04 Th [Rn]6d ² 7s ² Thorium	91 231.04 Pa [Rn]5f ² 6d ¹ 7s ² Protactinium	92 238.03 U [Rn]5f ³ 6d ¹ 7s ² Uranium	93 (237) Np [Rn]5f ⁴ 6d ¹ 7s ² Neptunium	94 (244) Pu [Rn]5f ⁶ 7s ² Plutonium	95 (243) Am [Rn]5f ⁷ 7s ² Americium	96 (247) Cm [Rn]5f ⁷ 6d ¹ 7s ² Curium	97 (247) Bk [Rn]5f ⁹ 7s ² Berkelium	98 (251) Cf [Rn]5f ¹⁰ 7s ² Californium	99 (252) Es [Rn]5f ¹¹ 7s ² Einsteinium	100 (257) Fm [Rn]5f ¹² 7s ² Fermium	101 (258) Md [Rn]5f ¹³ 7s ² Mendelevium	102 (259) No [Rn]5f ¹⁴ 7s ² Nobelium	103 (262) Lr [Rn]5f ¹⁴ 6d ¹ 7s ² Lawrencium
---	--	--	--	--	--	---	--	---	---	--	--	---	---

Electron binding energies, in electron volts (eV), for the elements in their natural forms

Element	K 1s	L ₁ 2s	L ₂ 2p _{1/2}	L ₃ 2p _{3/2}	M ₁ 3s	M ₂ 3p _{1/2}	M ₃ 3p _{3/2}	M ₄ 3d _{3/2}	M ₅ 3d _{5/2}	N ₁ 4s	N ₂ 4p _{1/2}	N ₃ 4p _{3/2}
1 H	13.6											
2 He	24.6 ^b											
3 Li	54.7 ^b											
4 Be	111.5 ^b											
5 B	188 ^b											
6 C	284.2 ^b											
7 N	409.9 ^b	37.3 ^b										
8 O	543.1 ^b	41.6 ^b										
9 F	696.7 ^b											
10 Ne	870.2 ^b	48.5 ^b	21.7 ^b	21.6 ^b								
11 Na	1070.8 ^c	63.5 ^c	30.4 ^c	30.5 ^b								
12 Mg	1303.0 ^c	88.6 ^b	49.6 ^c	49.2 ^c								
13 Al	1559.6	117.8 ^b	72.9 ^b	72.5 ^b								
14 Si	1838.9	149.7 ^b	99.8 ^b	99.2 ^b								
15 P	2145.5	189 ^b	136 ^b	135 ^b								
16 S	2472	230.9 ^b	163.6 ^b	162.5 ^b								
17 Cl	2822.4	270.2 ^b	202 ^b	200 ^b								
18 Ar	3205.9 ^b	326.3 ^b	250.6 ^b	248.4 ^b	29.3 ^b	15.9 ^b	15.7 ^b					
19 K	3608.4 ^b	378.6 ^b	297.3 ^b	294.6 ^b	34.8 ^b	18.3 ^b	18.3 ^b					
20 Ca	4038.5 ^b	438.4 ^c	349.7 ^c	346.2 ^c	44.3 ^c	25.4 ^c	25.4 ^c					
21 Sc	4492.8	498.0 ^b	403.6 ^b	398.7 ^b	51.1 ^b	28.3 ^b	28.3 ^b					
22 Ti	4966.4	560.9 ^c	461.2 ^c	453.8 ^c	58.7 ^c	32.6 ^c	32.6 ^c					
23 V	5465.1	626.7 ^c	519.8 ^c	512.1 ^c	66.3 ^c	37.2 ^c	37.2 ^c					
24 Cr	5989.2	695.7 ^c	583.8 ^c	574.1 ^c	74.1 ^c	42.2 ^c	42.2 ^c					
25 Mn	6539.0	769.1 ^c	649.9 ^c	638.7 ^c	82.3 ^c	47.2 ^c	47.2 ^c					
26 Fe	7112.0	844.6 ^c	719.9 ^c	706.8 ^c	91.3 ^c	52.7 ^c	52.7 ^c					
27 Co	7708.9	925.1 ^c	793.3 ^c	778.1 ^c	101.0 ^c	58.9 ^c	58.9 ^c					
28 Ni	8332.8	1008.6 ^c	870.0 ^c	852.7 ^c	110.8 ^c	68.0 ^c	66.2 ^c					
29 Cu	8978.9	1096.7 ^c	952.3 ^c	932.5 ^c	122.5 ^c	77.3 ^c	75.1 ^c					
30 Zn	9658.6	1196.2 ^b	1044.9 ^b	1021.8 ^b	139.8 ^b	91.4 ^b	88.6 ^b	10.2 ^b	10.1 ^b			
31 Ga	10367.1	1299.0 ^b	1143.2 ^c	1116.4 ^c	159.5 ^c	103.5 ^c	103.5 ^c	18.7 ^c	18.7 ^c			
32 Ge	11103.1	1414.6 ^b	1248.1 ^b	1217.0 ^b	180.1 ^b	124.9 ^b	120.8 ^b	29.0 ^b	29.0 ^b			
33 As	11866.7	1527.0 ^b	1359.1 ^b	1323.6 ^b	204.7 ^b	146.2 ^b	141.2 ^b	41.7 ^b	41.7 ^b			
34 Se	12657.8	1652.0 ^b	1474.3 ^b	1433.9 ^b	229.6 ^b	166.5 ^b	160.7 ^b	55.5 ^b	54.6 ^b			
35 Br	13473.7	1782.0 ^b	1596.0 ^b	1549.9 ^b	257 ^b	189 ^b	182 ^b	70 ^b	69 ^b			
36 Kr	14325.6	1921.0	1730.9 ^b	1678.4 ^b	292.8 ^b	222.2 ^b	214.4	95.0 ^b	93.8 ^b	27.5 ^b	14.1 ^b	14.1 ^b
37 Rb	15199.7	2065.1	1863.9	1804.4	326.7 ^b	248.7 ^b	239.1 ^b	113.0 ^b	112 ^b	30.5 ^b	16.3 ^b	15.3 ^b
38 Sr	16104.6	2216.3	2006.8	1939.6	358.7 ^c	280.3 ^c	270.0 ^c	136.0 ^c	134.2 ^c	38.9 ^c	20.3 ^c	20.3 ^c
39 Y	17038.4	2372.5	2155.5	2080.0	392.0 ^b	310.6 ^b	298.8 ^b	157.7 ^c	155.8 ^c	43.8 ^b	24.4 ^b	23.1 ^b
40 Zr	17997.6	2531.6	2306.7	2222.3	430.3 ^c	343.5 ^c	329.8 ^c	181.1 ^c	178.8 ^c	50.6 ^c	28.5 ^c	27.7 ^c
41 Nb	18985.6	2697.7	2464.7	2370.5	466.6 ^c	376.1 ^c	360.6 ^c	205.0 ^c	202.3 ^c	56.4 ^c	32.6 ^c	30.8 ^c
42 Mo	19999.5	2865.5	2625.1	2520.2	506.3 ^c	411.6 ^c	394.0 ^c	231.1 ^c	227.9 ^c	63.2 ^c	37.6 ^c	35.5 ^c
43 Tc	21044.0	3042.5	2793.2	2676.9	544 ^b	445 ^b	425 ^b	257 ^b	253 ^b	68 ^b	39 ^c	39 ^c
44 Ru	22117.2	3224.0	2966.9	2837.9	586.2 ^c	483.5 ^c	461.4 ^c	284.2 ^c	280.0 ^c	75.0 ^c	46.5 ^c	43.2 ^c
45 Rh	23219.9	3411.9	3146.1	3003.8	628.1 ^c	521.3 ^c	496.5 ^c	311.9 ^c	307.2 ^c	81.4 ^b	50.5 ^c	47.3 ^c
46 Pd	24350.3	3604.3	3330.3	3173.3	671.6 ^c	559.9 ^c	532.3 ^c	340.5 ^c	335.2 ^c	87.6 ^b	55.7 ^c	50.9 ^c
47 Ag	25514.0	3805.8	3523.7	3351.1	719.0 ^c	603.8 ^c	573.0 ^c	374.0 ^c	368.0 ^c	97.0 ^c	63.7 ^c	58.3 ^c

www.cxro.lbl.gov

Synchrotron radiation



Bending Magnet:

$$\hbar\omega_c = \frac{3e\hbar B\gamma^2}{2m} \quad (5.7)$$

Wiggler:

$$\hbar\omega_c = \frac{3e\hbar B\gamma^2}{2m} \quad (5.80)$$

$$n_c = \frac{3K}{4} \left(1 + \frac{K^2}{2}\right) \quad (5.82)$$

$$P_T = \frac{\pi e K^2 \gamma^2 I N}{3\epsilon_0 \lambda_u} \quad (5.85)$$

Undulator:

$$\lambda = \frac{\lambda_u}{2\gamma^2} \left(1 + \frac{K^2}{2} + \gamma^2 \theta^2\right) \quad (5.28)$$

$$K = \frac{e B_0 \lambda_u}{2\pi m c} \quad (5.18)$$

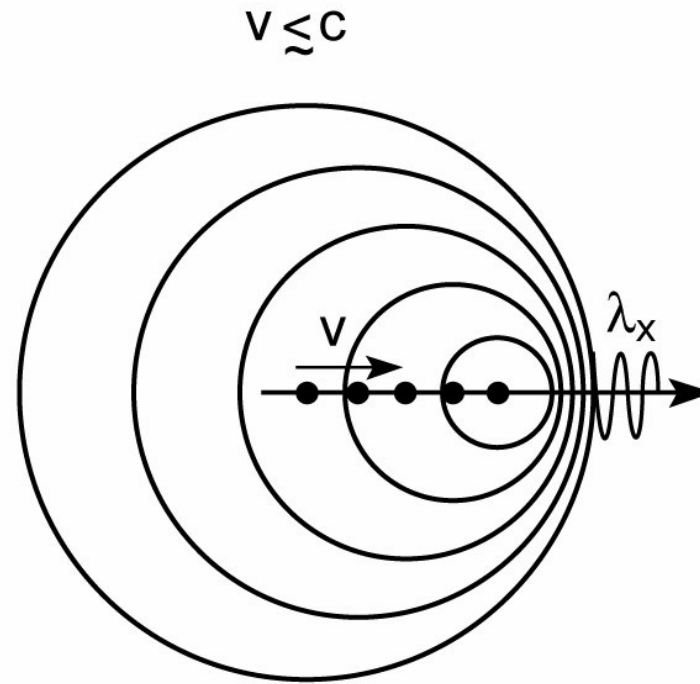
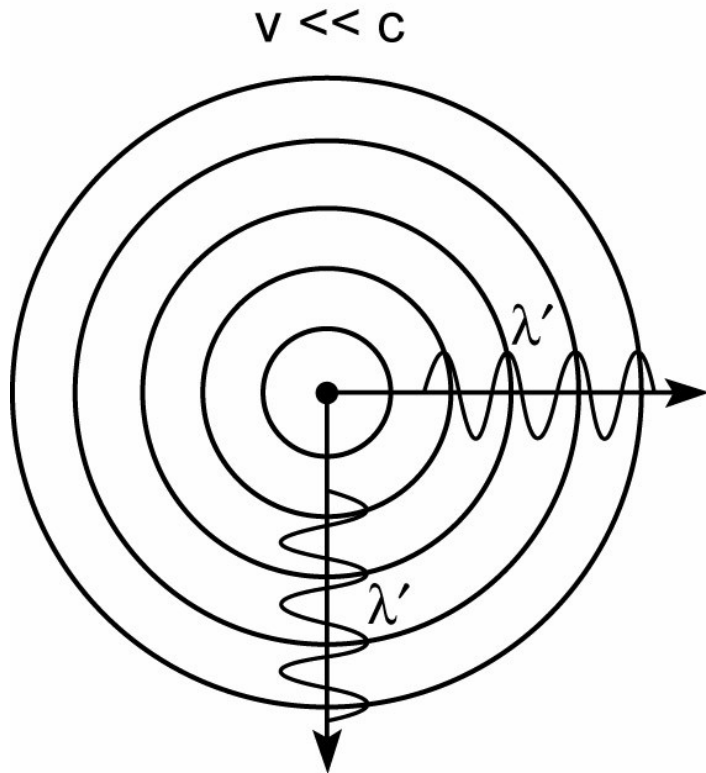
$$\theta_{\text{cen}} = \frac{1}{\gamma^* \sqrt{N}} \quad (5.15)$$

$$\left. \frac{\Delta\lambda}{\lambda} \right|_{\text{cen}} = \frac{1}{N} \quad (5.14)$$

$$\bar{P}_{\text{cen}} = \frac{\pi e \gamma^2 I}{\epsilon_0 \lambda_u} \frac{K^2}{\left(1 + \frac{K^2}{2}\right)^2} [\text{JJ}]^2 \quad (5.41)$$

Ch05_F00VG_Jan06.ai

Synchrotron radiation from relativistic electrons



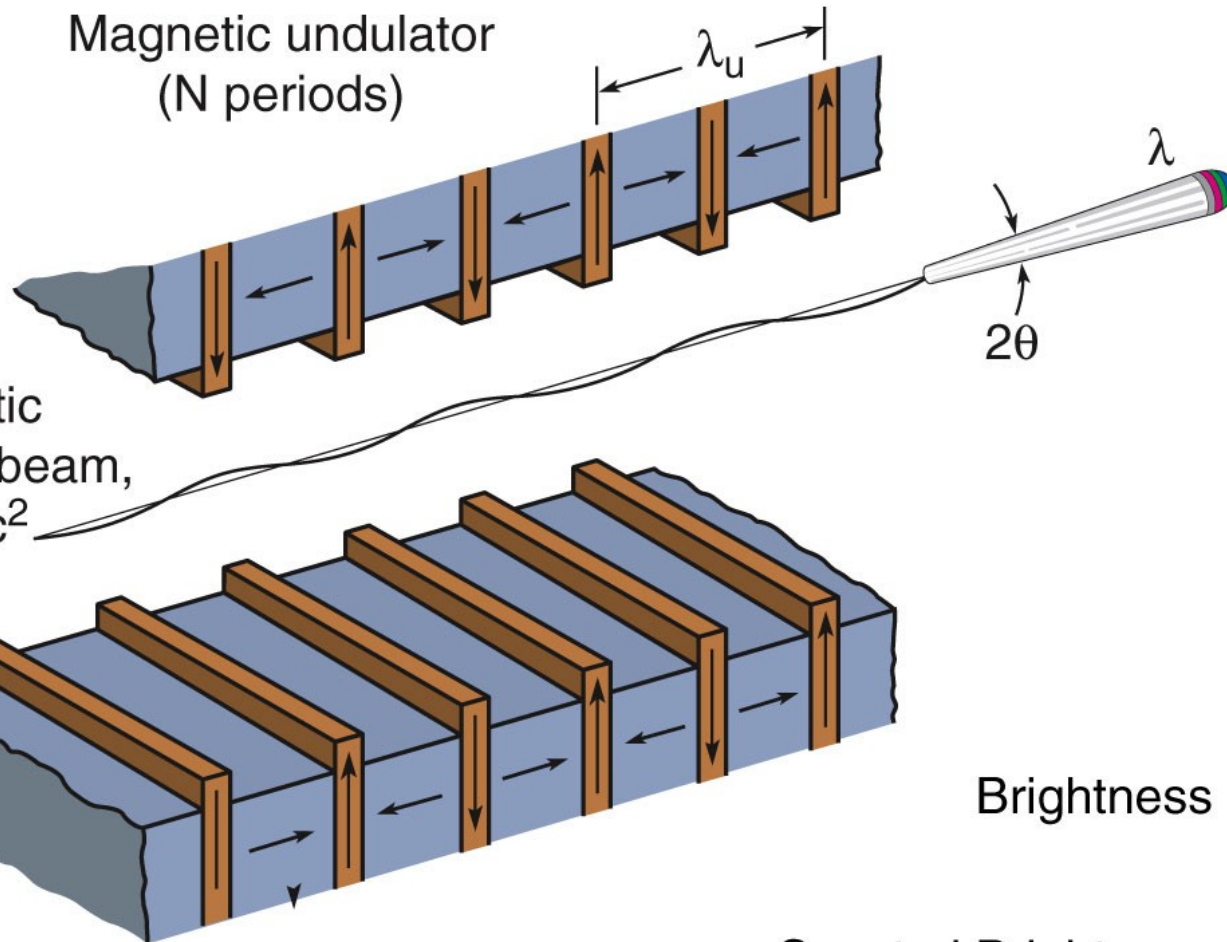
Note: Angle-dependent doppler shift

$$\lambda = \lambda' \left(1 - \frac{v}{c} \cos\theta\right) \quad \lambda = \lambda' \gamma \left(1 - \frac{v}{c} \cos\theta\right)$$

$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$$

Following John Madey

Undulator radiation from a small electron beam radiating into a narrow forward cone is very bright



$$\lambda \approx \frac{\lambda_u}{2\gamma^2}$$

$$\theta_{\text{cen}} \approx \frac{1}{\gamma \sqrt{N}}$$

$$\left[\frac{\Delta\lambda}{\lambda} \right]_{\text{cen}} = \frac{1}{N}$$

$$\text{Brightness} = \frac{\text{photon flux}}{(\Delta A) (\Delta\Omega)}$$

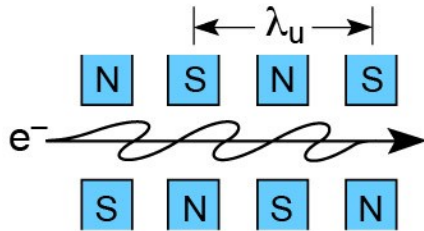
$$\text{Spectral Brightness} = \frac{\text{photon flux}}{(\Delta A) (\Delta\Omega) (\Delta\lambda/\lambda)}$$

Ch05_F08VG_1.04.ai

Undulator radiation



Laboratory Frame of Reference

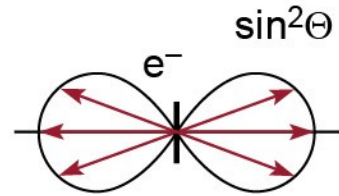


$$E = \gamma mc^2$$

$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$$

$N = \#$ periods

Frame of Moving e^-



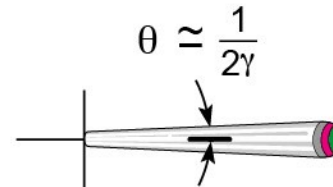
e^- radiates at the Lorentz contracted wavelength:

$$\lambda' = \frac{\lambda_u}{\gamma}$$

Bandwidth:

$$\frac{\lambda'}{\Delta\lambda'} \simeq N$$

Frame of Observer



Doppler shortened wavelength on axis:

$$\lambda = \lambda' \gamma (1 - \beta \cos \theta)$$

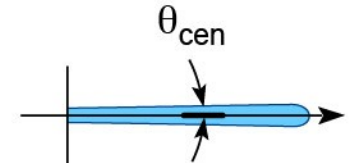
$$\lambda = \frac{\lambda_u}{2\gamma^2} (1 + \gamma^2 \theta^2)$$

Accounting for transverse motion due to the periodic magnetic field:

$$\lambda = \frac{\lambda_u}{2\gamma^2} \left(1 + \frac{K^2}{2} + \gamma^2 \theta^2 \right)$$

where $K = eB_0\lambda_u / 2\pi mc$

Following Monochromator



For $\frac{\Delta\lambda}{\lambda} \simeq \frac{1}{N}$

$$\theta_{\text{cen}} \simeq \frac{1}{\gamma \sqrt{N}}$$

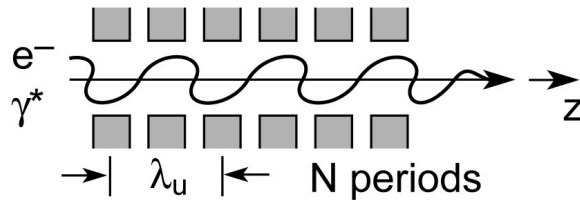
typically

$$\theta_{\text{cen}} \simeq 10\text{-}30 \text{ } \mu\text{rad}$$

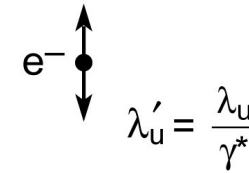
Calculating Power in the Central Radiation Cone: Using the well known “dipole radiation” formula by transforming to the frame of reference moving with the electrons



x, z, t laboratory frame of reference



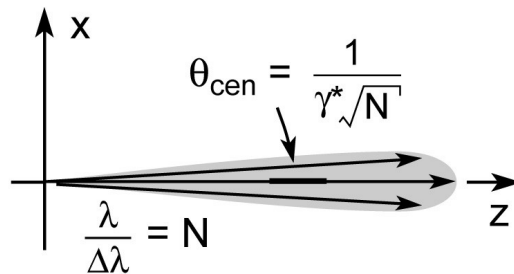
x', z', t' frame of reference moving with the average velocity of the electron



Lorentz transformation

Determine x, z, t motion:

$$\frac{d\mathbf{p}}{dt} = -e (\mathbf{E} + \mathbf{v} \times \mathbf{B})$$

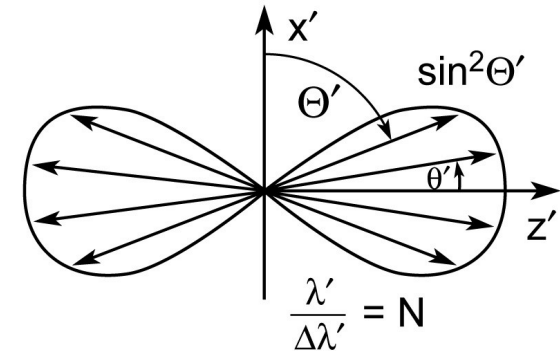


Lorentz transformation

$$\bar{P}_{\text{cen}} = \frac{\pi e \gamma^2 I}{\epsilon_0 \lambda_u} \frac{K^2}{(1 + K^2/2)^2}$$

Dipole radiation:

$$\frac{dP'}{d\Omega'} = \frac{e^2 a'^2 \sin^2 \Theta'}{16\pi^2 \epsilon_0 c^3}$$



$$\frac{dP'}{d\Omega'} = \frac{e^2 c \gamma^2}{4\epsilon_0 \lambda_u^2} \frac{K^2}{(1 + K^2/2)^2} (1 - \sin^2 \theta' \cos^2 \phi') \cos^2 \omega'_u t'$$

Power in the central radiation cone



$$\lambda_x = \frac{\lambda_u}{2\gamma^2} \left(1 + \frac{K^2}{2} + \gamma^2 \theta^2\right)$$

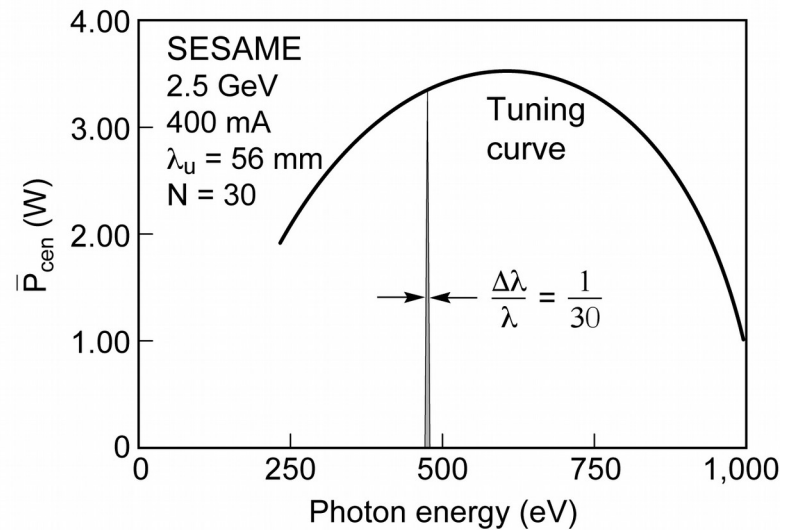
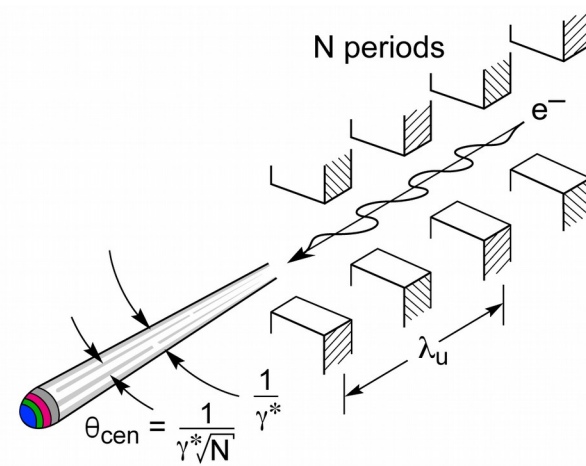
$$\bar{P}_{\text{cen}} = \frac{\pi e \gamma^2 I}{\epsilon_0 \lambda_u} \frac{K^2}{\left(1 + \frac{K^2}{2}\right)^2} [JJ]^2$$

$$\theta_{\text{cen}} = \frac{1}{\gamma^* \sqrt{N}}$$

$$\left(\frac{\Delta\lambda}{\lambda}\right)_{\text{cen}} = \frac{1}{N}$$

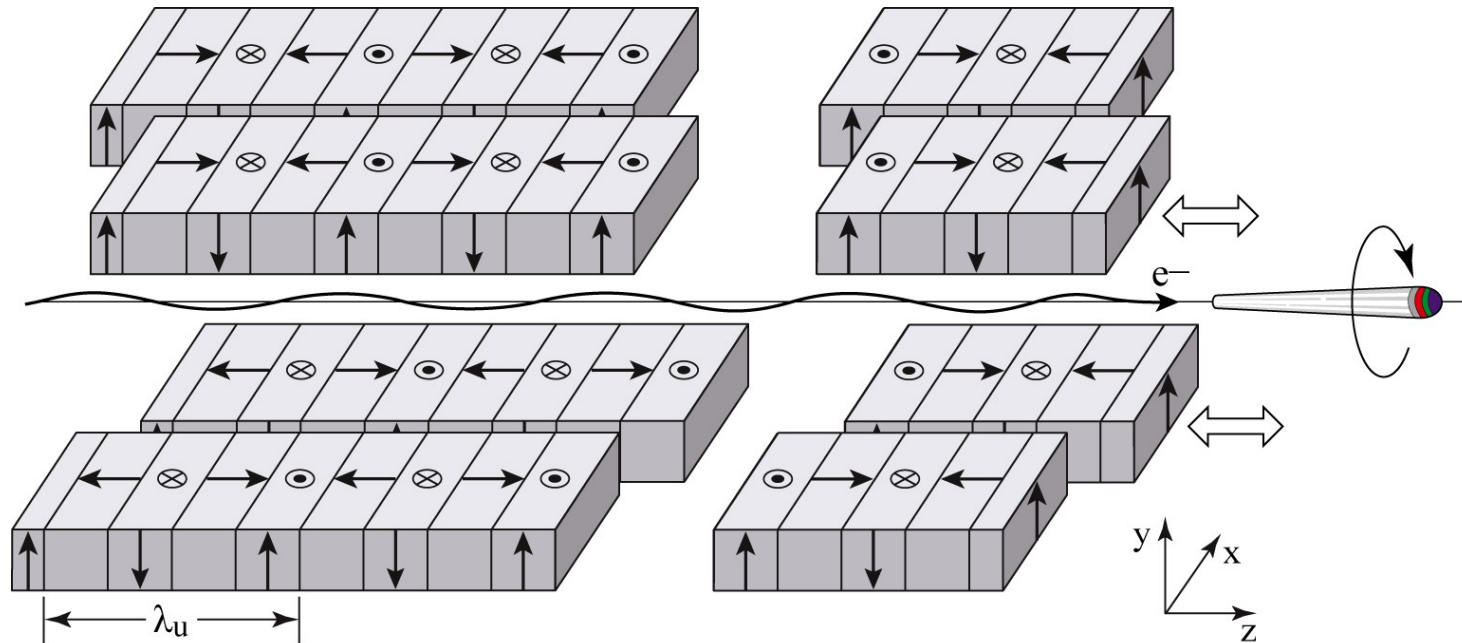
$$K = \frac{eB_0 \lambda_u}{2\pi m_0 c}$$

$$\gamma^* = \gamma / \sqrt{1 + \frac{K^2}{2}}$$



PowerCentralCone_SESAMEx.ai

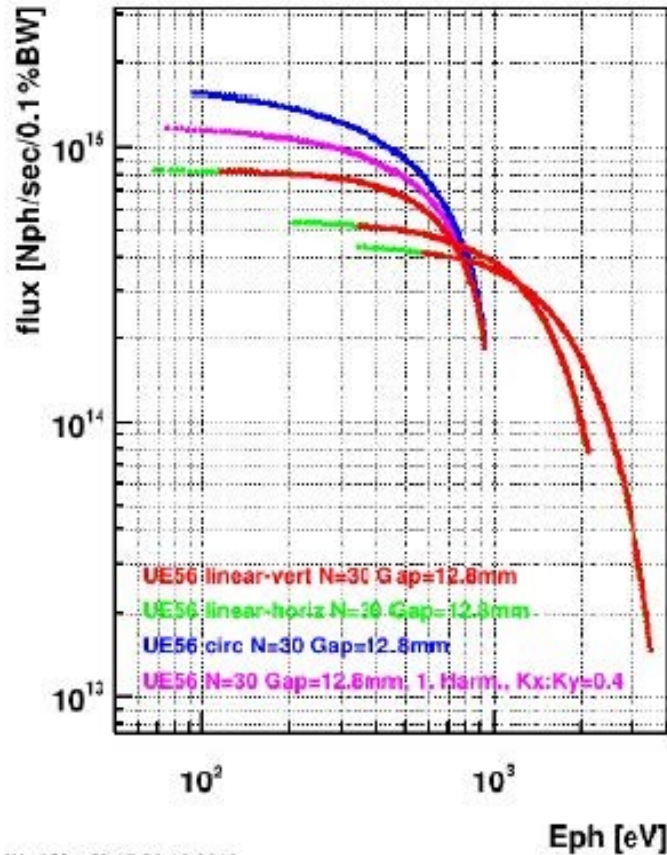
APPLE II Elliptically Polarizing Undulator (EPU)



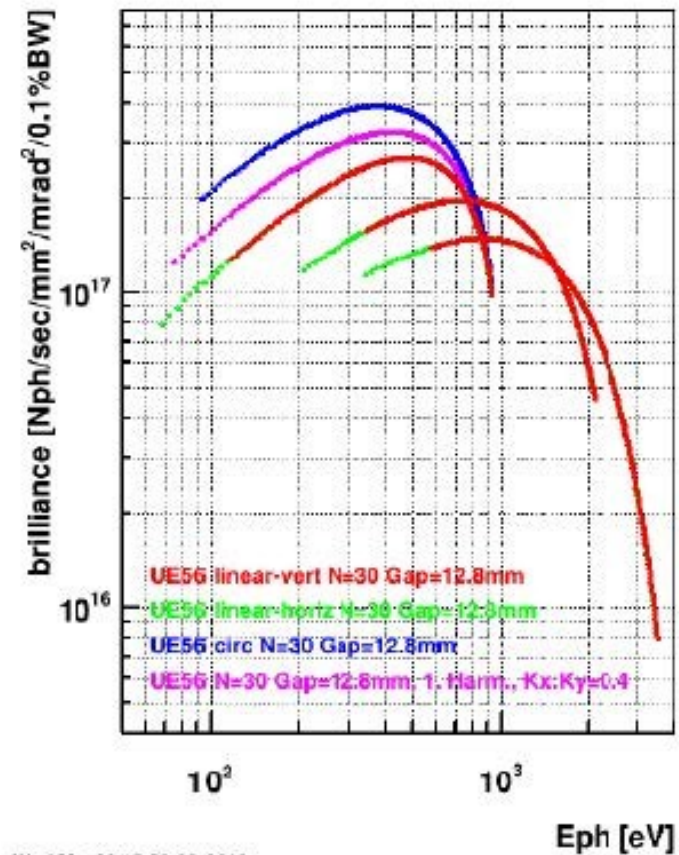


Add Si, C, Fe to both

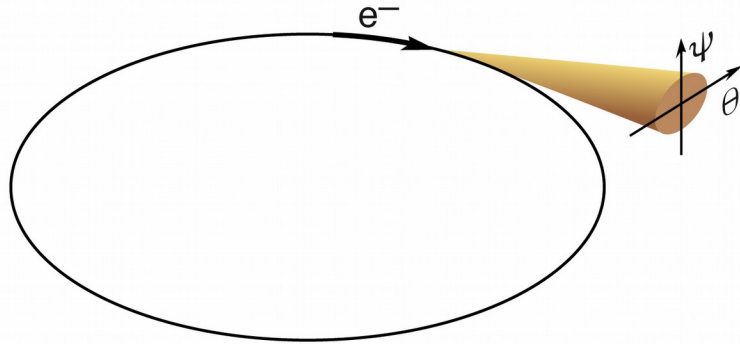
Flux, 2.5 GeV, 400 mA



Brilliance, 2.5 GeV, 400 mA



Bending magnet radiation covers a broad region of the spectrum, including the primary absorption edges of most elements



$$E_c = \hbar\omega_c = \frac{3e\hbar\gamma^2}{2m} \quad (5.7a)$$

$$E_c[\text{keV}] = 0.6650 E_e^2[\text{GeV}] B[\text{T}] \quad (5.7b)$$

$$F_{1\text{mrad}, 0.1\% \text{BW}} = 2.46 \times 10^{13} E_e[\text{GeV}] I[\text{A}] G_1(E/E_c) \text{ ph/sec} \quad (5.8)$$

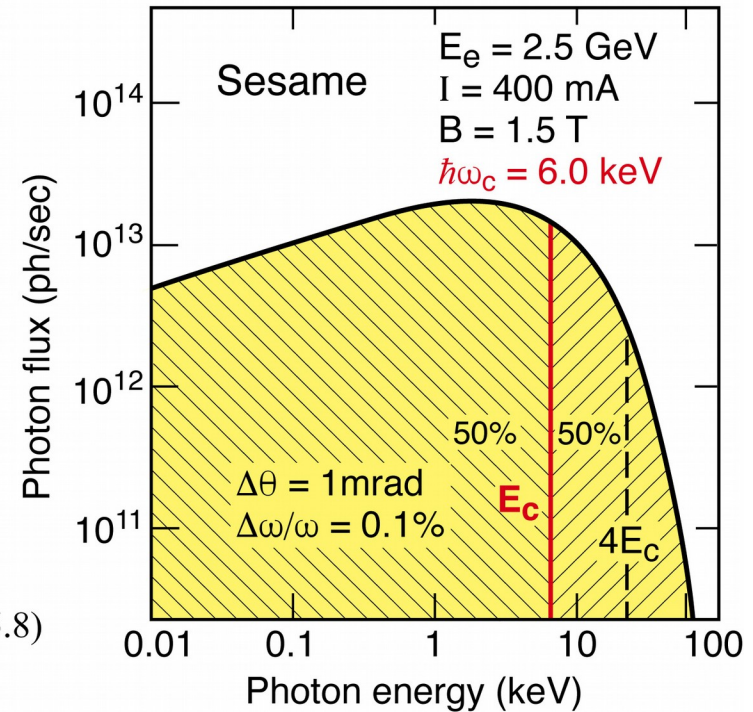
where $G_1(1) = 0.6514$

Advantages:

- covers broad spectral range
- least expensive
- most accessible

Disadvantages:

- not as bright as an undulator

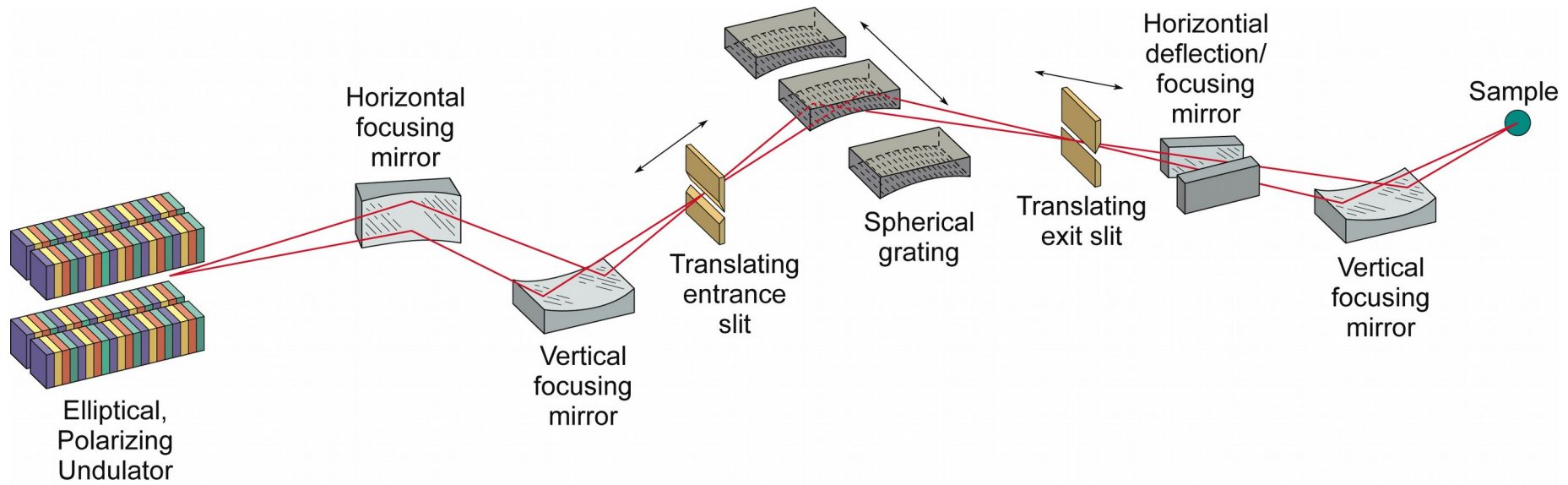


$$E_c = 6 \text{ keV}$$

$$4E_c = 24 \text{ keV}$$

Ch05_F07_Sesame.ai

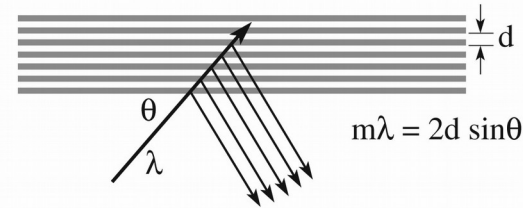
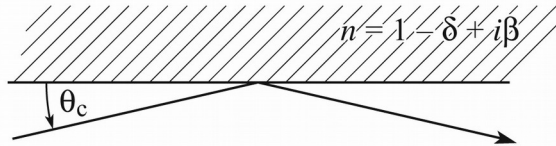
A typical beamline: A monochromator plus glancing incidence optics deliver radiation to the sample



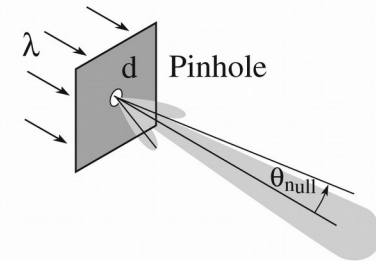
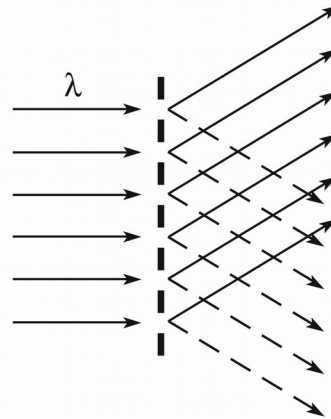
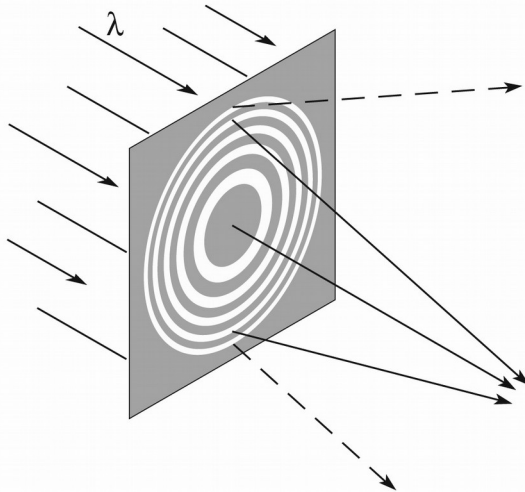
Available Optical Techniques for Soft X-Rays and EUV



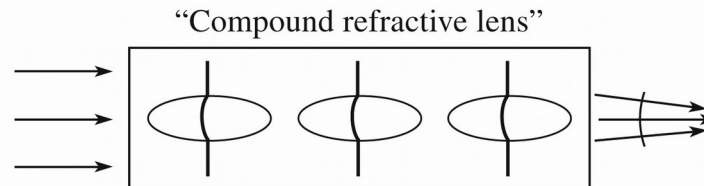
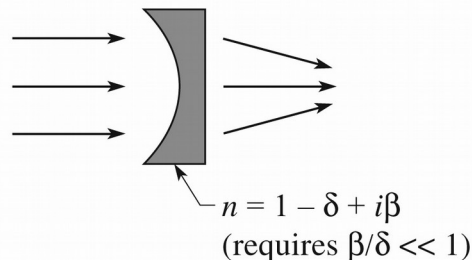
- Reflection (glancing incidence or multilayer coatings)



- Diffraction (zone plates, gratings, pinholes)



- Refraction (only for hard x-rays, > 20 keV)



A. Snigerev et al., *Nature* **384**, 49 (7Nov.1996)

B. Lengeler et al., *J. Appl. Phys.* **84**, 5855 (1Dec.1998)

AvaiOpticTechSXREUV.ai

Refractive index at x-ray wavelengths



Based on a simple, semi-classical oscillator in the presence of an electric field $E = E_0 \cos \omega t$

$$n(\omega) = 1 - \frac{1}{2} \frac{e^2 n_a}{\epsilon_0 m} \sum_s \frac{g_s}{(\omega^2 - \omega_s^2) + i\gamma\omega} \quad (3.8)$$

Expressed in terms of atomic scattering factors:

$$n(\omega) = 1 - \frac{n_a r_e \lambda^2}{2\pi} \left[f_1^0(\omega) - i f_2^0(\omega) \right] \quad (3.9)$$

which we can write simply as

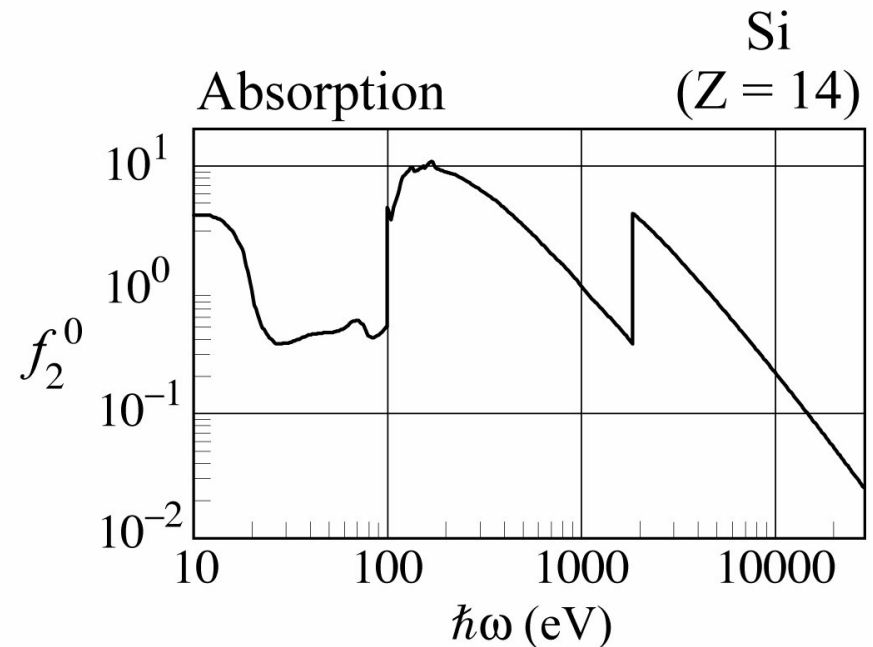
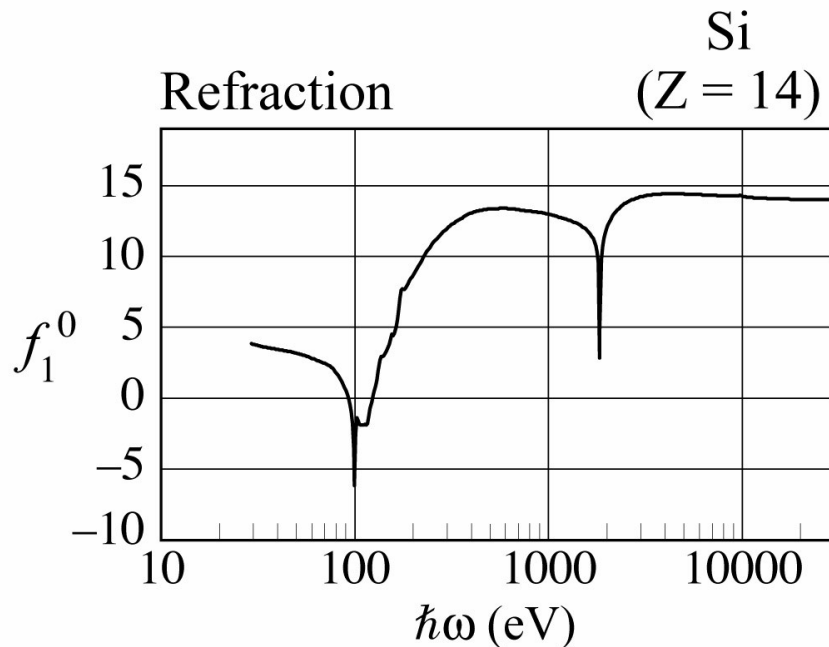
$$n(\omega) = 1 - \delta + i\beta \quad (3.12)$$

Refractive index at nanometer wavelengths

Refractive Index

$$n = 1 - \delta + i\beta = 1 - \frac{n_a r_e \lambda^2}{2\pi} (f_1^0 - i f_2^0)$$

Atomic scattering factors



[www.cxro.LBL.gov/optical_constants](http://www.cxro.lbl.gov/optical_constants)

ScattngRefracIndex_June2009.ai

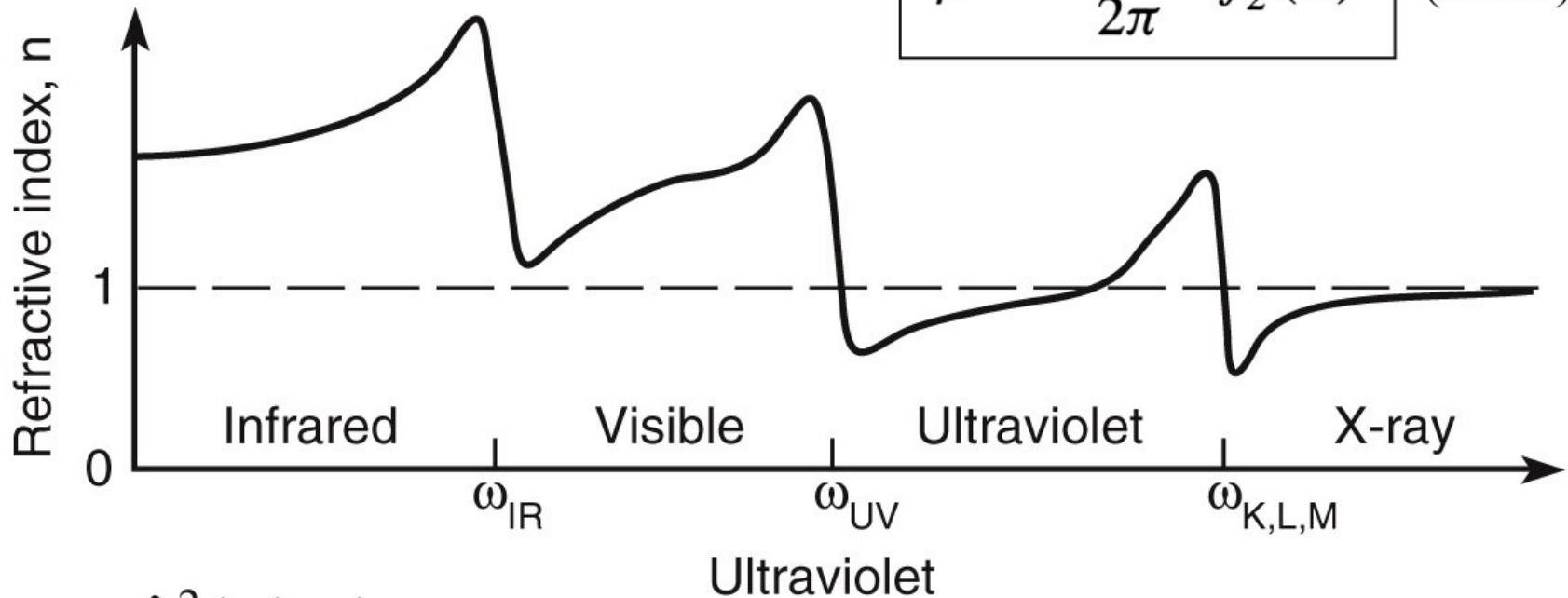
Refractive index from the IR to x-ray spectral region



$$n(\omega) = 1 - \delta + i\beta \quad (3.12)$$

$$\delta = \frac{n_a r_e \lambda^2}{2\pi} f_1^0(\omega) \quad (3.13a)$$

$$\beta = \frac{n_a r_e \lambda^2}{2\pi} f_2^0(\omega) \quad (3.13b)$$



- λ^2 behavior
- $\delta \ \& \ \beta \ll 1$
- δ -crossover



Normal incidence reflection of x-rays is very small

$$R_s = \frac{|\cos \phi - \sqrt{n^2 - \sin^2 \phi}|^2}{|\cos \phi + \sqrt{n^2 - \sin^2 \phi}|^2} \quad (3.49)$$

at $\phi = 0$:

$$R_{s,\perp} = \frac{|1 - n|^2}{|1 + n|^2} = \frac{(1 - n)(1 - n^*)}{(1 + n)(1 + n^*)}$$

For $n = 1 - \delta + i\beta$

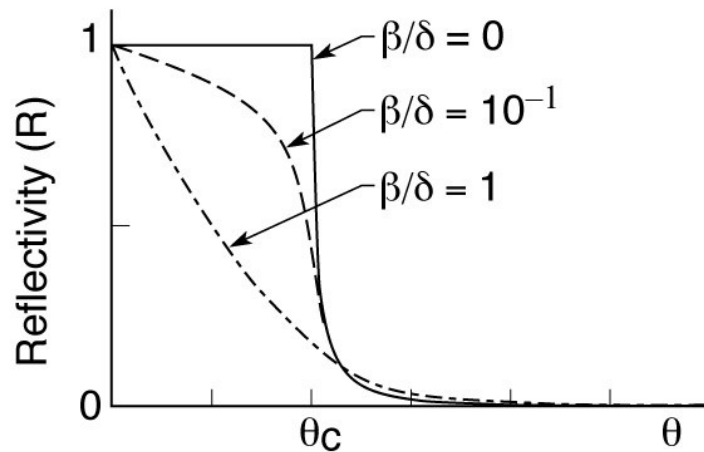
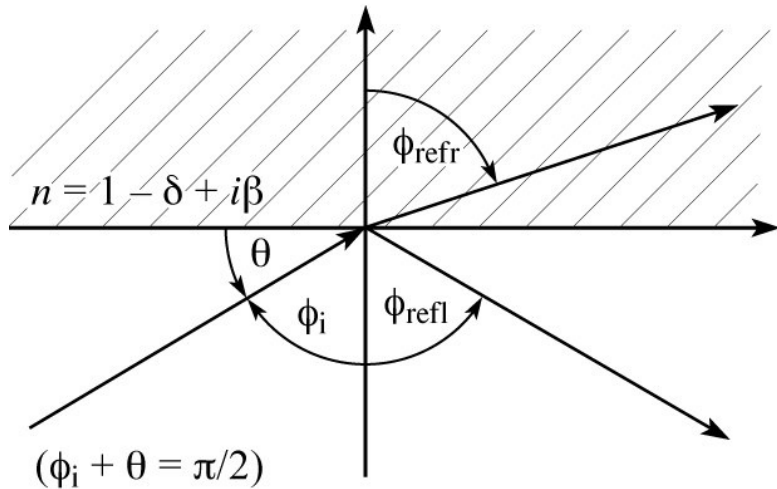
$$R_{s,\perp} = \frac{(\delta - i\beta)(\delta + i\beta)}{(2 - \delta + i\beta)(2 - \delta - i\beta)} = \frac{\delta^2 + \beta^2}{(2 - \delta)^2 + \beta^2}$$

Reflectivity for x-ray and EUV radiation at normal incidence ($\phi = 0$):

$$R_{s,\perp} \simeq \frac{\delta^2 + \beta^2}{4} \quad (3.50)$$

Example: Nickel @ 300 eV (4.13 nm) $\left. \begin{array}{ll} f_1^\circ = 17.8 & f_2^\circ = 7.70 \\ \delta = 0.0124 & \beta = 0.00538 \end{array} \right\} R_\perp = 4.58 \times 10^{-5} \text{ [@ 300 eV]} \\ [\sim 10^{-8} \text{ at 3 keV}]$

Glancing Incidence Optics



Snell's Law: $\sin \phi_{\text{refr.}} = \frac{\sin \phi_i}{n}$

Total external Reflection:

$$\phi_{\text{refr.}} \rightarrow \frac{\pi}{2} \text{ as } \phi_i \rightarrow \phi_{\text{critical}}$$

$$\text{Snell's Law: } 1 = \frac{\sin \phi_c}{1 - \delta}$$

$$\sin(90^\circ - \theta_c) = 1 - \delta$$

$$\cos \theta_c = 1 - \delta$$

$$1 - \frac{\theta_c^2}{2} = 1 - \delta$$

$$\theta_c = \sqrt{2\delta}$$

For gold at 1 keV

$$\delta = 2.1 \times 10^{-3}$$

$$\theta_c = 3.7^\circ$$

(www.cxro.lbl.gov ;
 "X-ray properties of the elements"
 "X-ray interaction with matter")

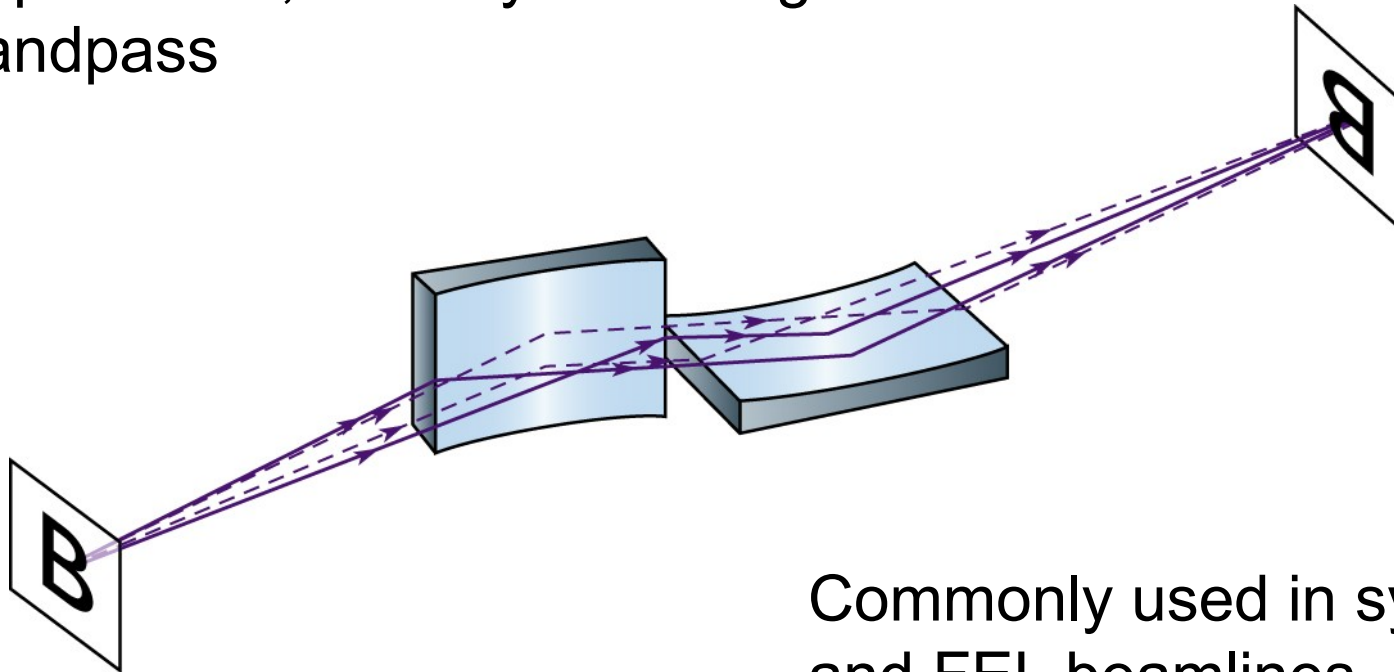
Kirkpatrick-Baez Mirror Pair



Orthogonal mirrors cancel astigmatism

Elliptical surfaces for point to point imaging

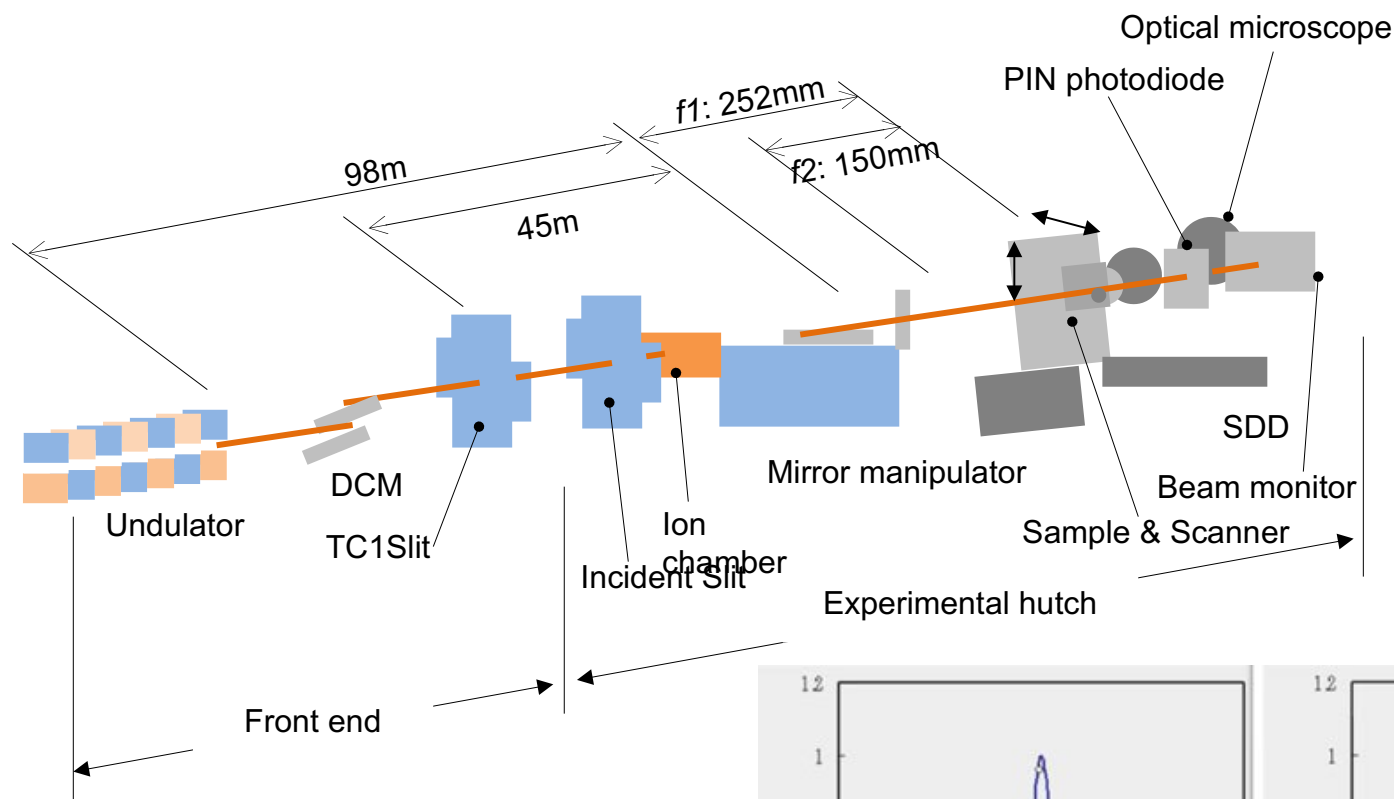
Glancing incidence coatings for broad band applications, multilayer coatings for fixed bandpass



Courtesy of J. Underwood, LBNL

Commonly used in synchrotron and FEL beamlines, and in plasma diagnostics

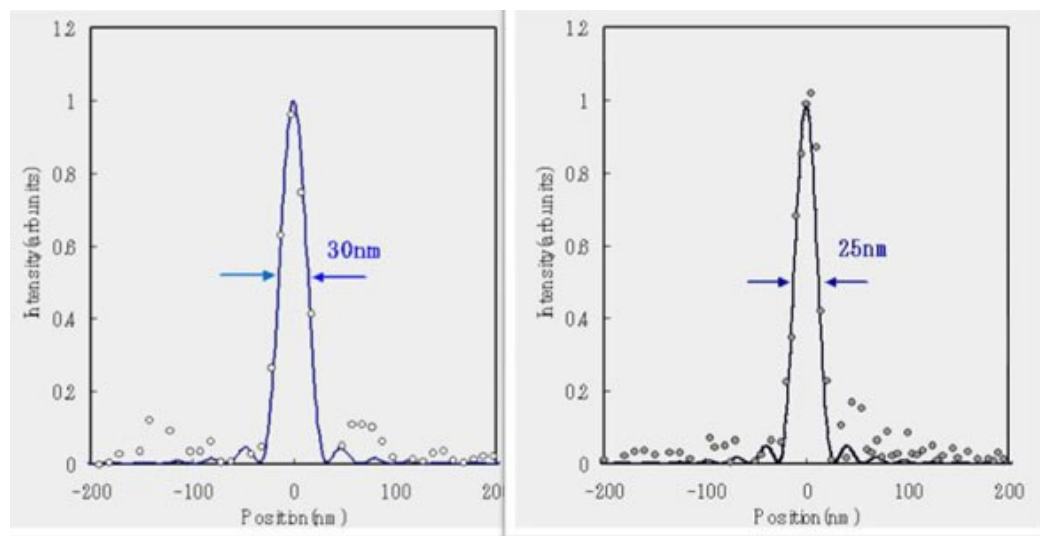
X-ray microprobe at SPring-8



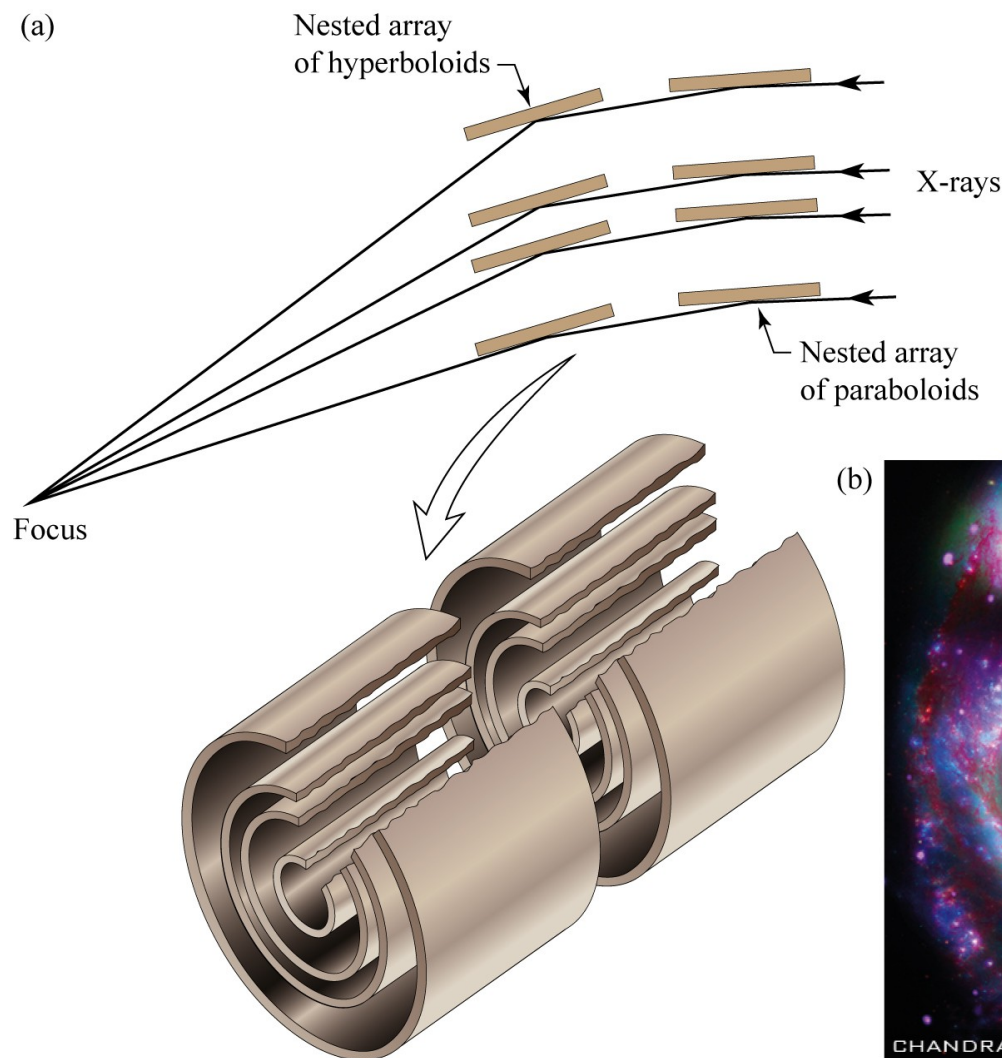
**Now focused
to 7 nm**

S. Matsuyama et al.,
Rev. Sci. Instrum.
77, 103102 (2006)

Courtesy of Professor Kazuto Yamauchi,
Osaka University and Spring-8



Nested pairs of Wolter type 1 reflective x-ray optics for the orbiting Chandra X-ray Observatory



Composite view of the M51 "Whirlpool Galaxy"

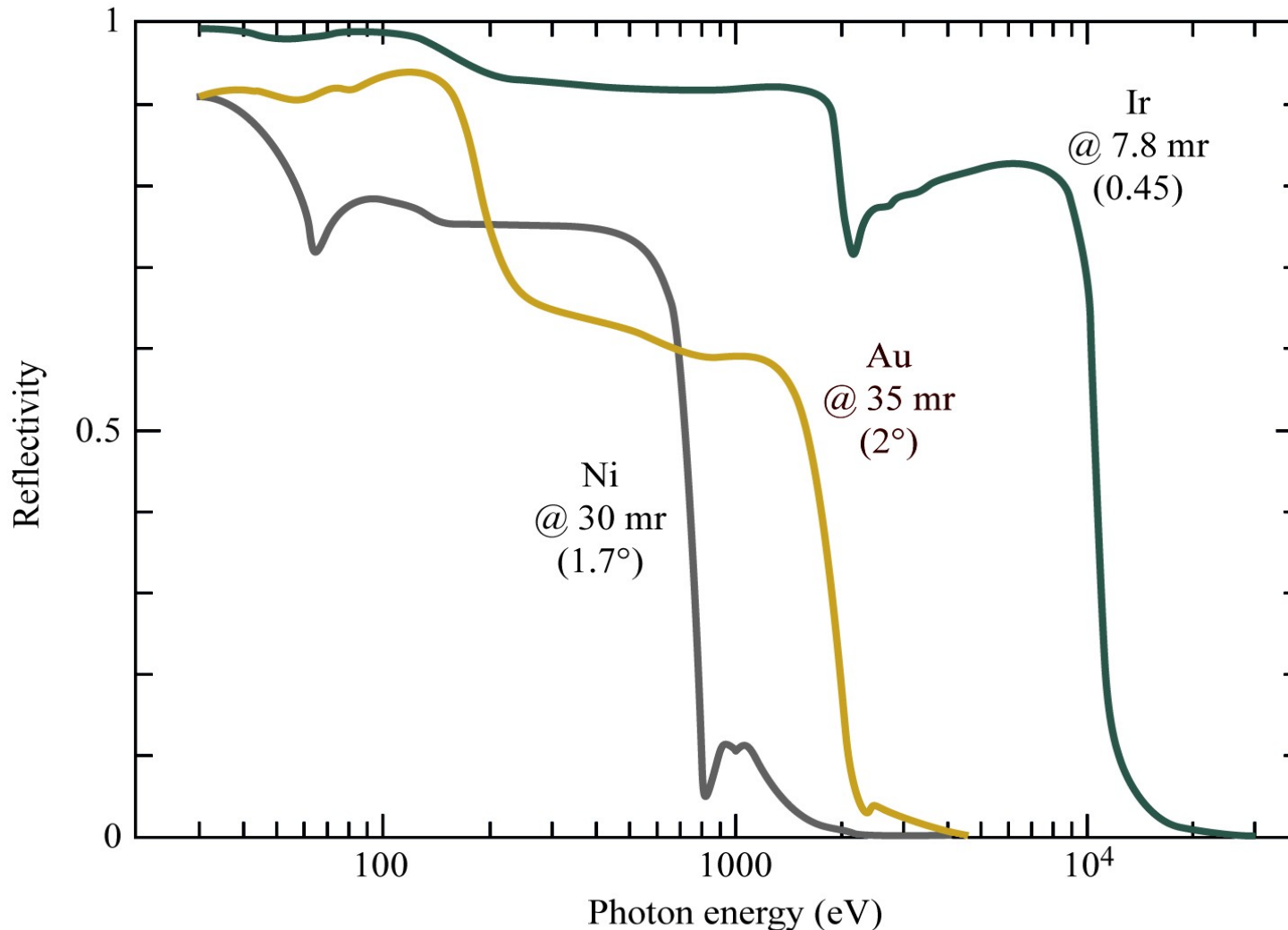


Courtesy of D. Schwartz (Harvard-Smithsonian Center for Astrophysics) and NASA

Single surface mirrors for x-ray astronomy

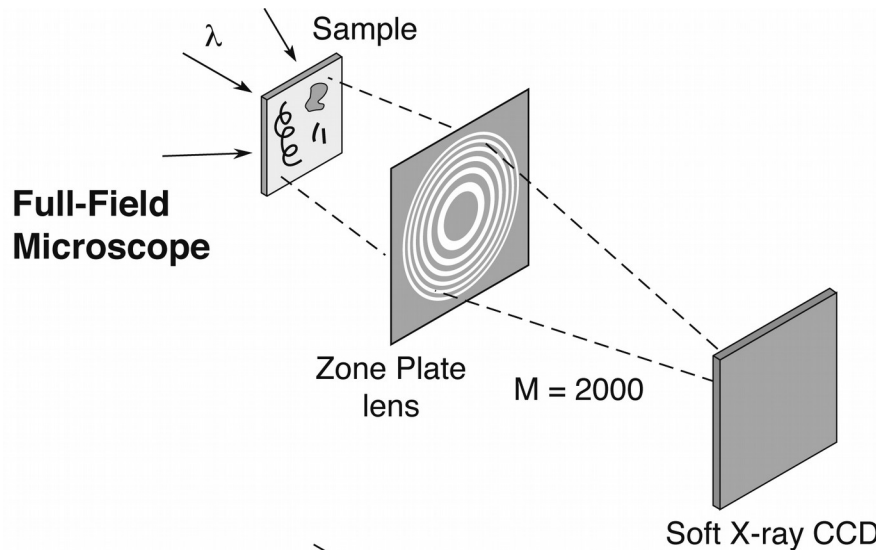


Sharp cutoffs at 700 eV, 2 keV and 10 keV

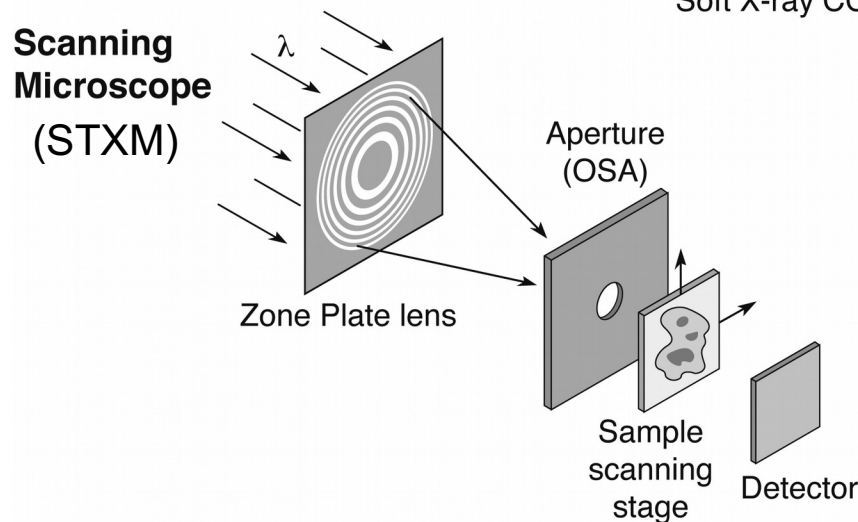


Courtesy of R. Soufli, LLNL, and E. Gullikson, LBL; www.cxro.LBL.gov/ical_constants

Two common zone plate x-ray microscopes

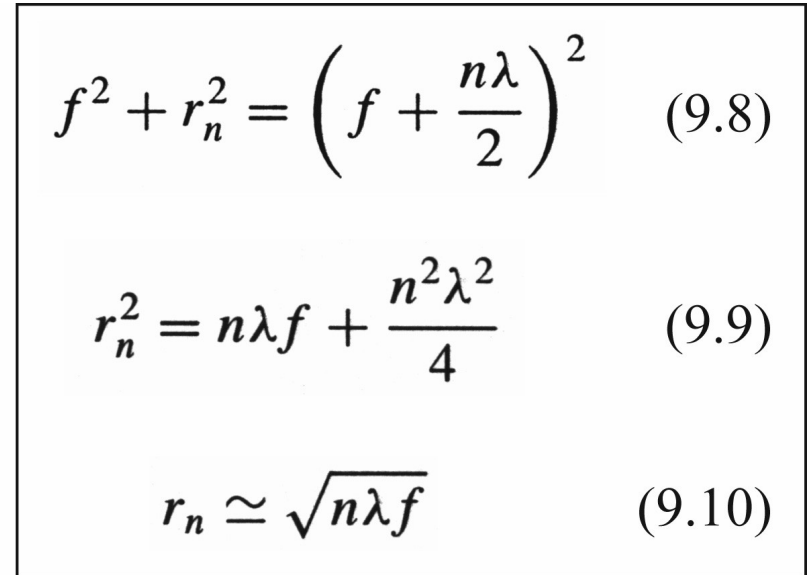


- 10–20 nm spatial resolution
- High spectral resolution
- Seconds exposure time
- Bending magnet, or undulator
- Higher radiation dose
- Flexible sample environment (wet, cryo, labeled magnetic fields, electric fields, cement, ...)



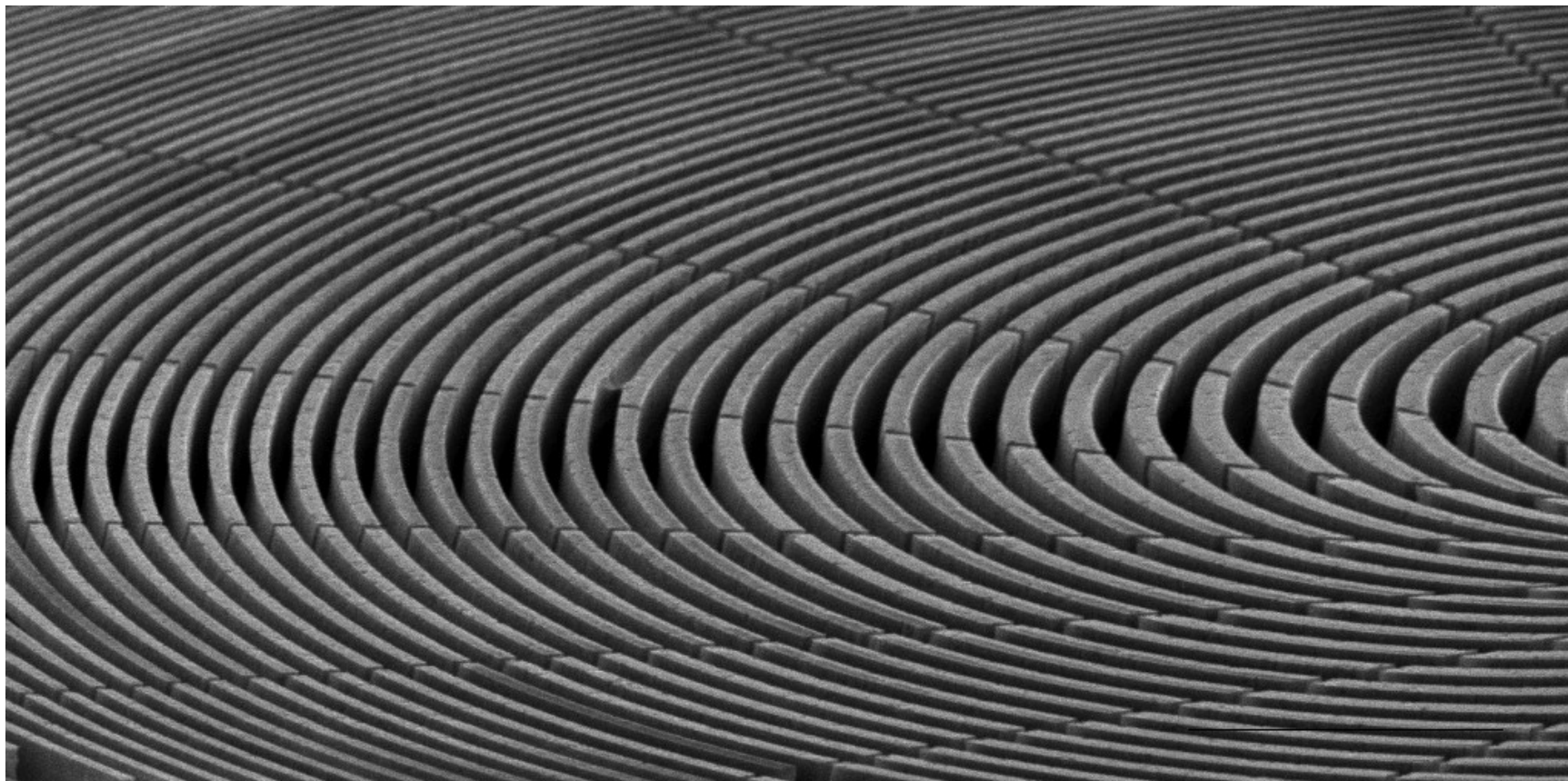
- 10–20 nm spatial resolution
- Least radiation dose
- High spectral resolution
- Requires spatially coherent radiation
- Minutes exposure time
- Flexible sample environment
- Photoemission, fluorescence imaging

Ch09_F21_Feb2017.ai



Ch09_F05VG.ai

X-ray Fresnel zone plate lens can be used for imaging at high spatial resolution

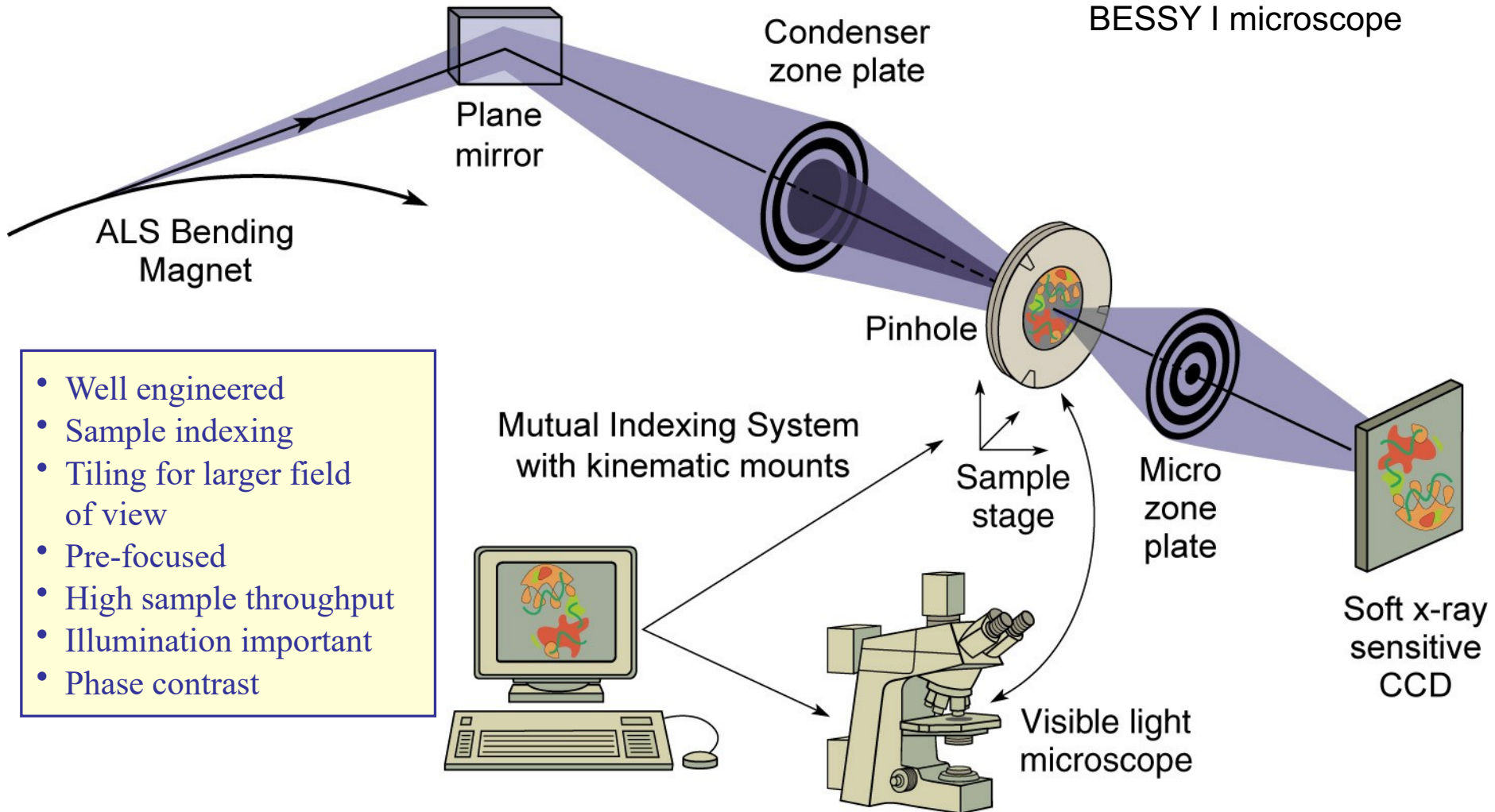


Courtesy of A. Sakdinawat and Chieh Chang (SLAC/ Stanford)

High resolution zone plate microscopy

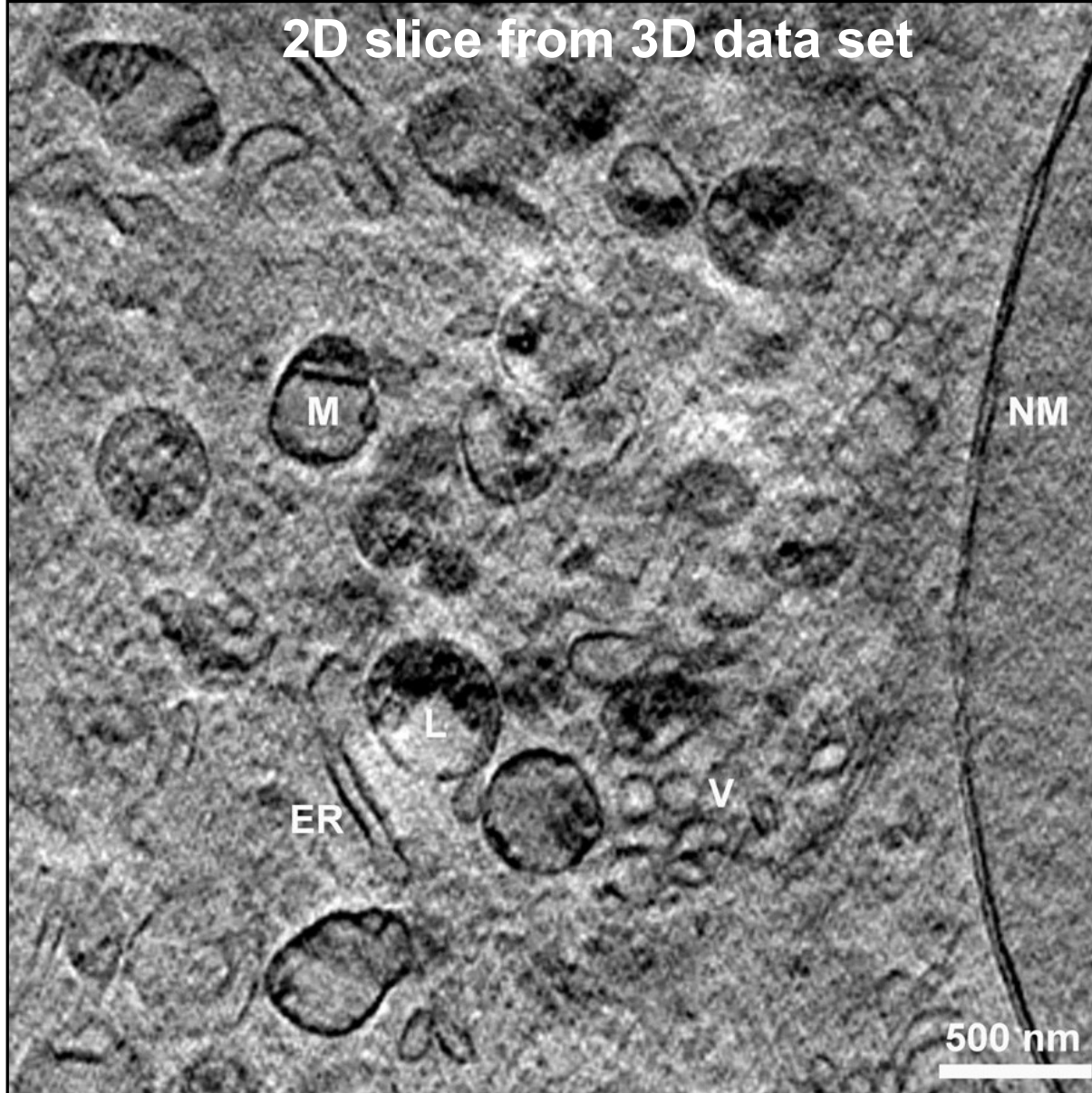


A near clone of the
BESSY I microscope



HiResZPMicrXM1Biology_Jan08.ai

2D slice from 3D data set



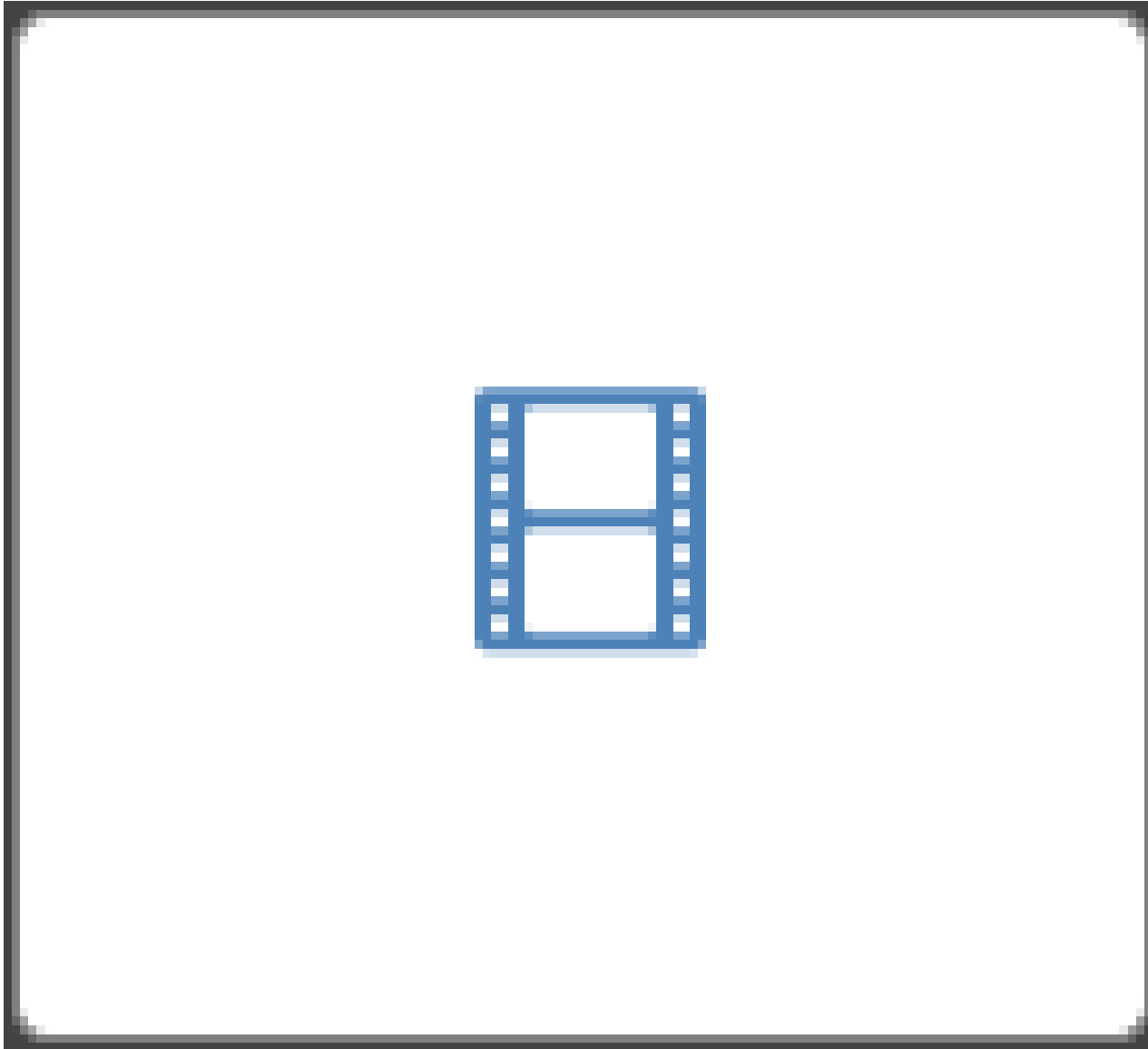
510 eV (2.43 nm)
 $\Delta r = 25$ nm,
 1° intervals, $\pm 60^\circ$
36 nm nuclear
double membrane.
Exposure ~ 5 minutes

Endoplasmic Reticulum
(ER)
Mitochondria (M)
Nuclear Membrane (NM)
Lysosomes (L)
Vesicles (V)
Nuclear pores (NP)

Courtesy of Gerd Schneider,
BESSYII and James McNally,
NIH.

Nature Methods 7, 985 (2010).

X-ray computed tomography of a single biological cell

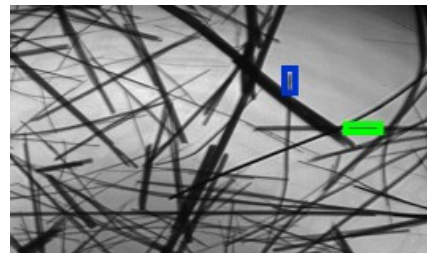
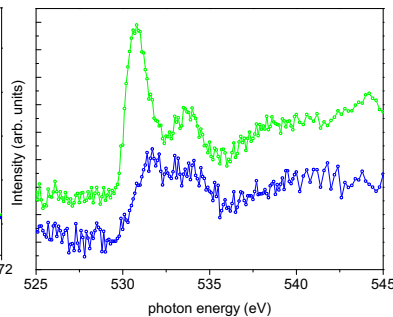
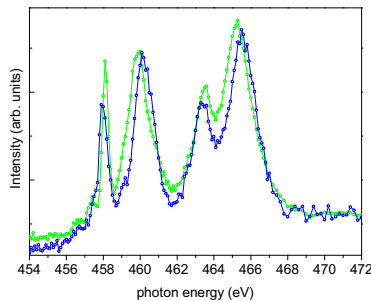
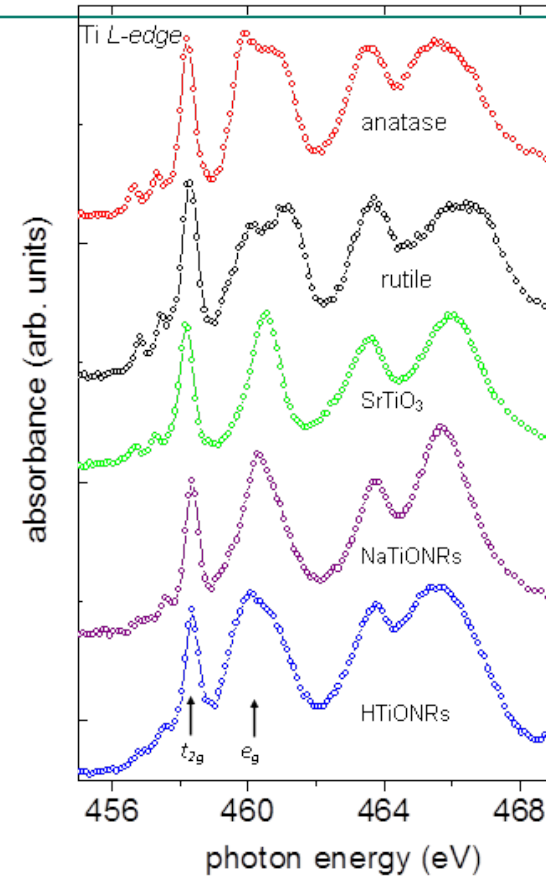
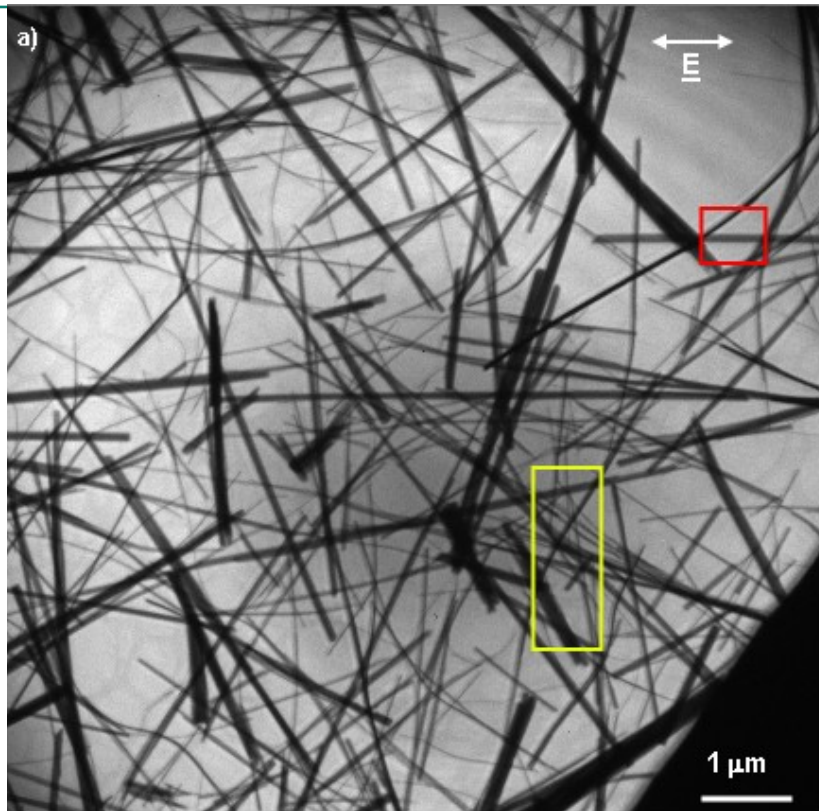


Courtesy of Gerd Schneider, BESSYII and James McNally, NIH.

Nano-spectroscopy of sodium titanate nanoribbons



In collaboration with:
C. Bittencourt,
U. Antwerp, Belgium

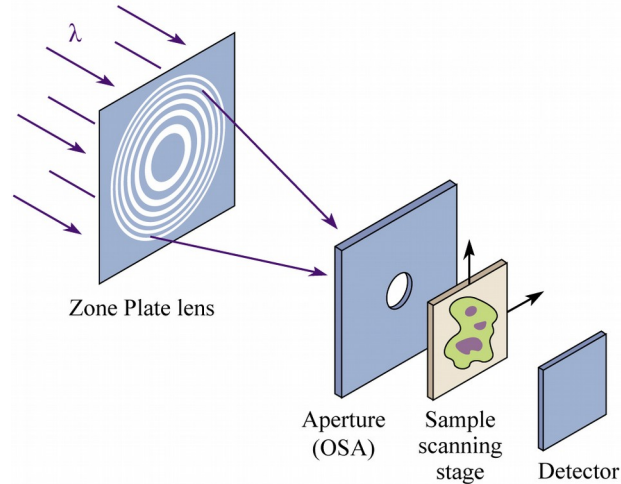


P. Guttman et al., *Nature Photonics*
(Dec. 2011).

Scanning Transmission X-ray Microscope (STXM)

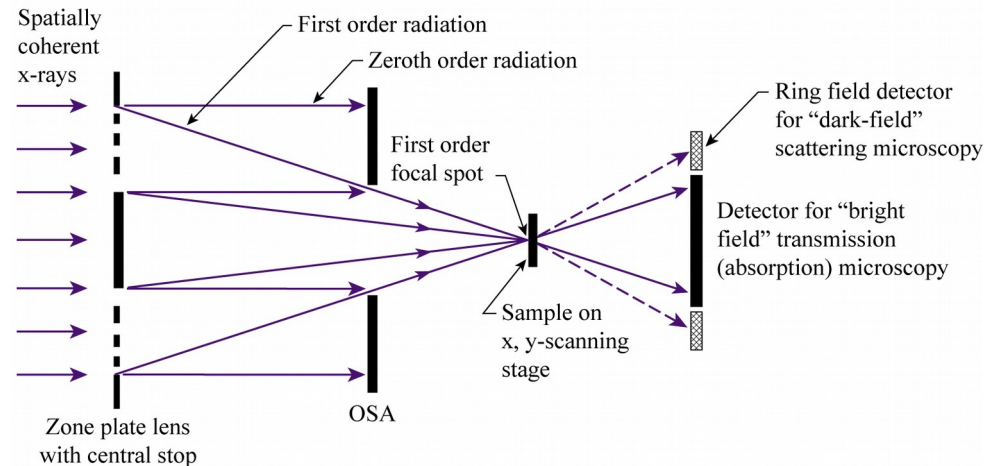


(a) Scanning Transmission X-ray Microscope



Especially useful for
spectromicroscopy
of radiation sensitive
samples

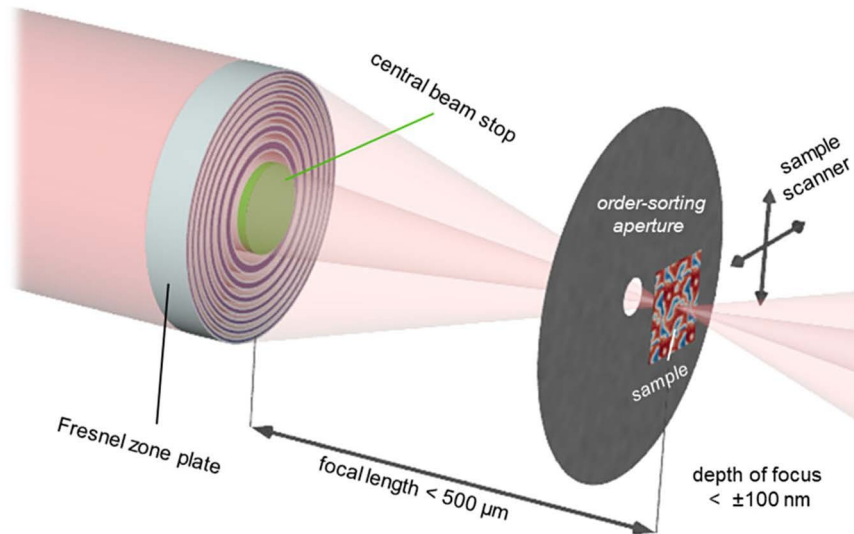
(b)



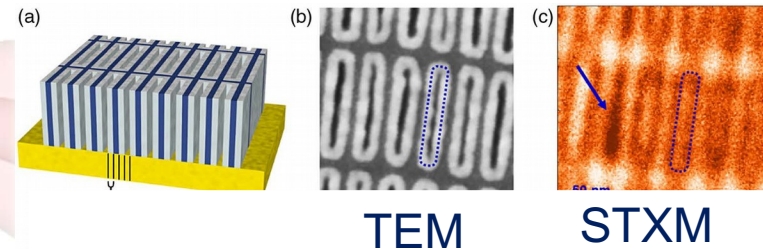
Soft x-ray microscopy with 7 nm resolution



Scanning Transmission X-ray Microscope (STXM)
PSI, Swiss Light Source



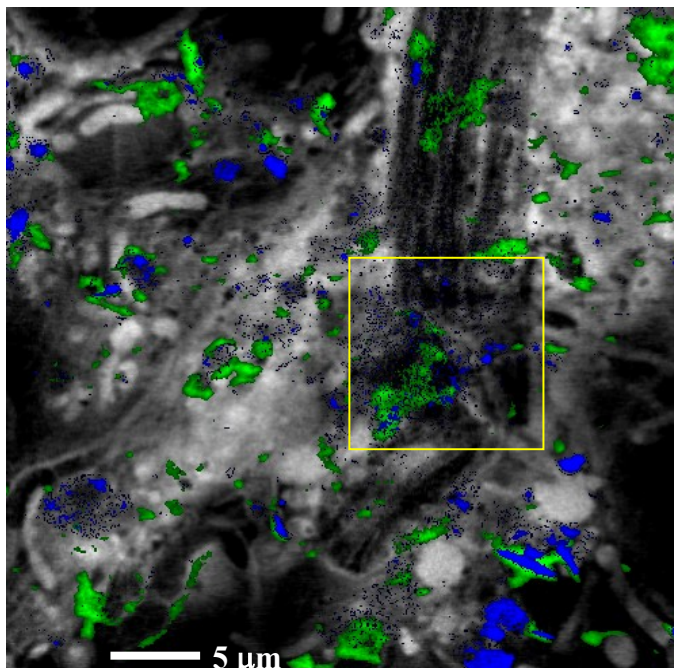
Magnetic nanostructure



B. Rosner,* S. Finizio, F. Koch, F. Doring, V.A. Guzenko, M. Langer, E. Kirk, B. Watts, M. Meyer, J. Lorona Ornelas, A. Spath, S. Stanescu, S. Swaraj, R. Belkhou, T. Ishikawa, T.F. Keller, B. Gross, M. Poggio, R.H. Fink, J. Raabe, A. Kleibert, AND Christian David **Optica** 7, 1602 (November 2020).

PSI, ETH, Erlangen-Nurnberg, Soleil, DESY, U. Hamburg, U. Basel

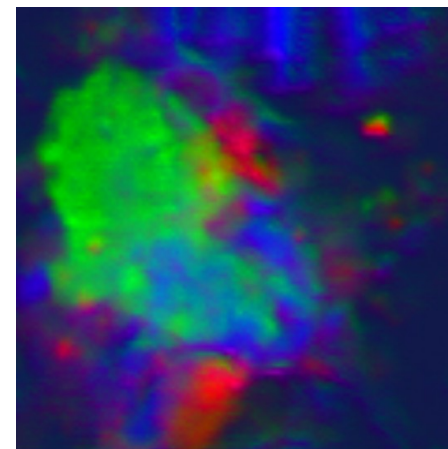
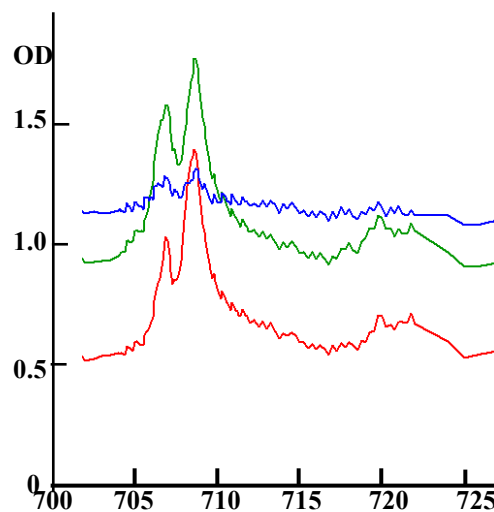
Environmental study: Biofilm from Saskatoon River



Protein (gray), Ca, K

RESULTS

- Ni, Fe, Mn, Ca, K, O, C elemental map, (there was no sign of Cr.)
- Different oxidation states for Fe and Ni



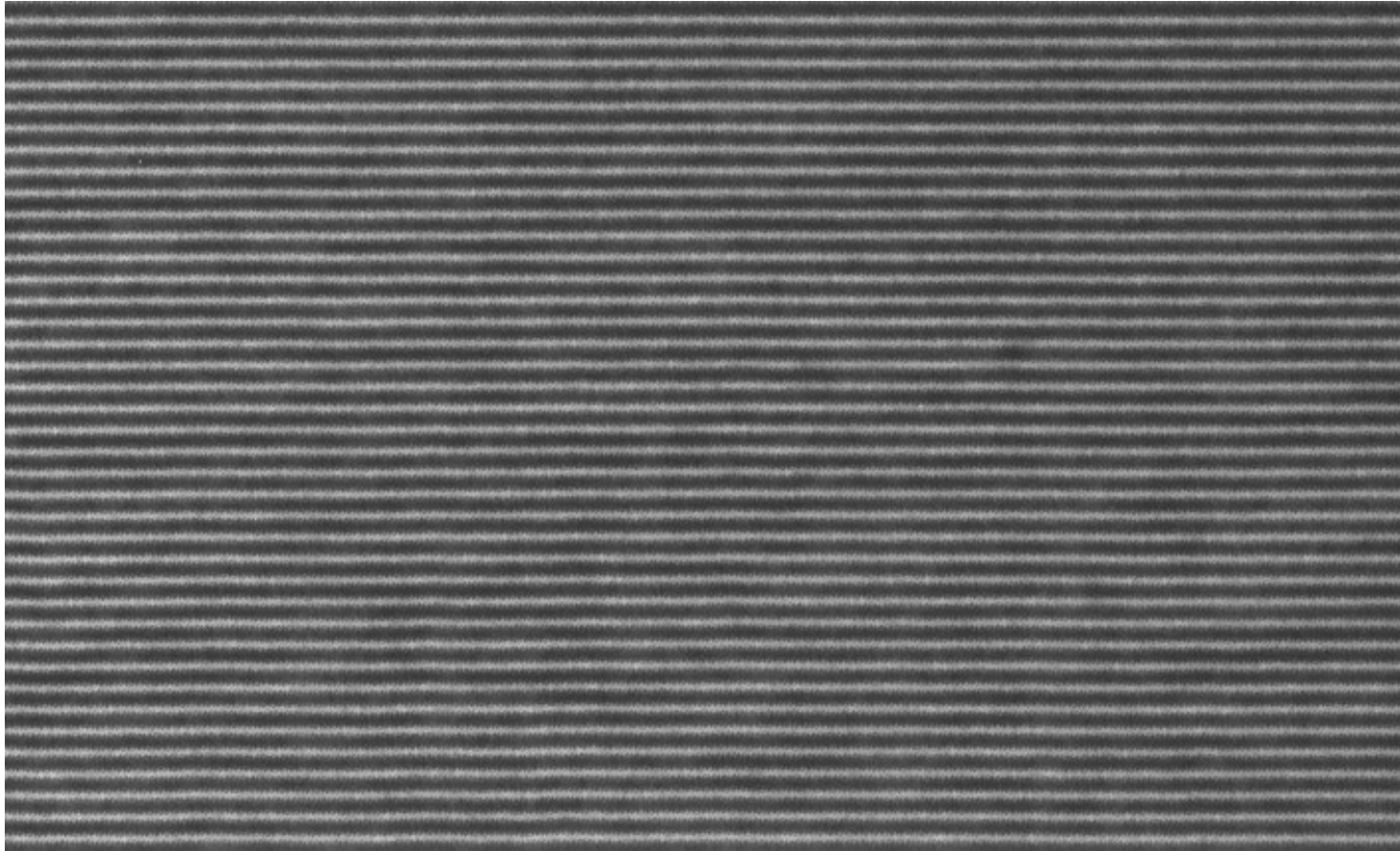
Different oxidation states (minerals) found for Fe & Ni

Courtesy of Tohru Araki, Adam Hitchcock (McMaster University) and Tolek Tyliczszak, LBNL; Sample from: John Lawrence, George Swerhone (NWRI-Saskatoon) and Gary Leppard (NWRI-CCIW)

A High Quality Mo/Si Multilayer Mirror can Achieve 70% Normal Incidence Reflectivity in the EUV



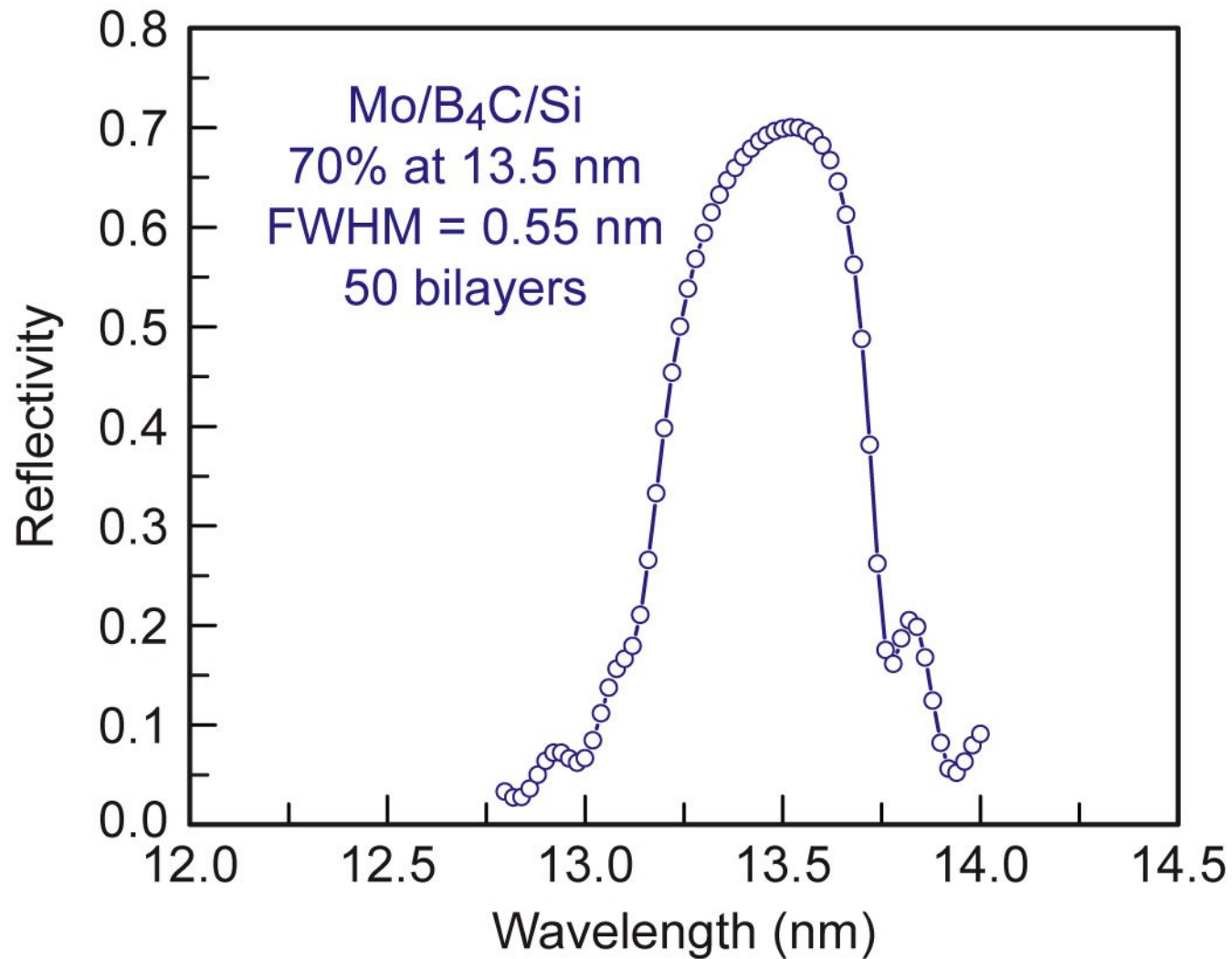
Small reflections at many interfaces add in phase at the Bragg angle.
In the EUV δ and β are relatively large (dependence)



$N = 40$
 $d = 6.7$
 $\lambda = 13.5 \text{ nm}$
(92.5 eV)

Courtesy of Saa Bajt (CFEL/DESY)

Multilayer mirrors have achieved a reflectivity of 70% in the extreme ultraviolet (EUV) ... an unusual result



Courtesy of Saša Bajt (LLNL)

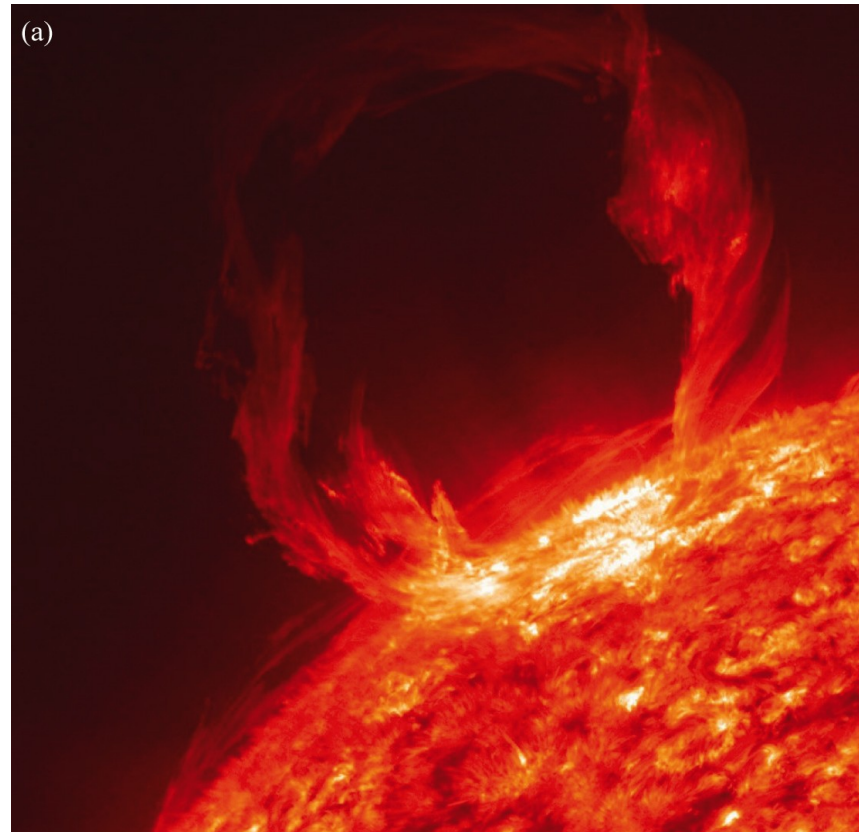
Ch04_ReflectCurv70.ai

EUV Image obtained with Mo/Si coated optics: coronal loop of magnetized plasma at the sun's surface



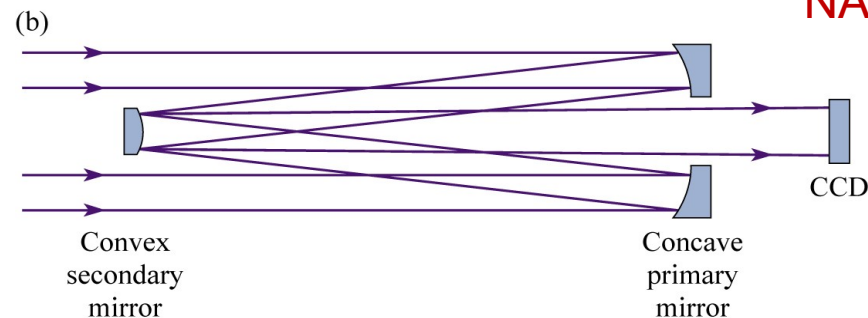
Lockheed/NASA Atmospheric Imaging Assembly (AIA) telescope, part of the geo-synchronous **Solar Dynamics Observatory (SDO)**.

Multilayer coatings provided by R. Soufli, LLNL and D.L. Windt, Reflective X-ray Optics. J.R. Lemen, *Solar Physics* **275**, 14 (2012)



NASA/SDO

Multilayer coated
Cassegrain telescope
Mo/Si, 17.1 nm,



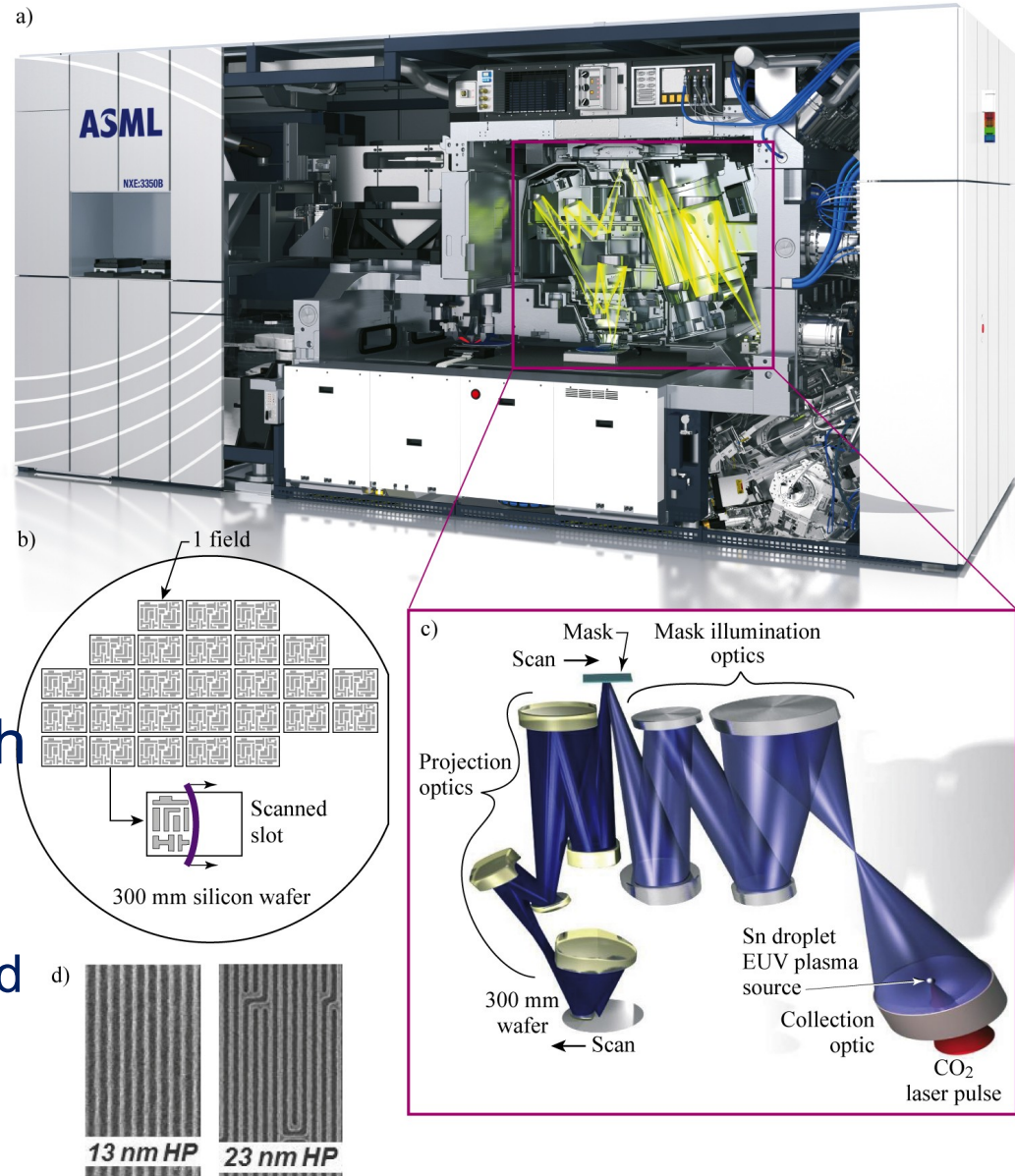
Moore's Law is not dead, saved by Extreme Ultraviolet (EUV) Lithography using these same multilayer mirrors



Step and scan system,
Mo/Si coated reflective
optics at 13.5 nm
wavelength, CO₂ laser
irradiated 30 μ m Sn
microspheres.

Bending magnet and
undulator radiation used for
critical early research at both
the ALS and BESSY II.

Courtesy of V. Banine (ASML) and
W. Kaiser (Zeiss)



EUV lithography: High volume manufacturing (HVM) of computer chips and smart phone chip began in 2019



9 October 2018

TSMC's second-generation 7 nm manufacturing technology will use extreme ultraviolet lithography. Apple's new iPhone 11 uses TSMC chips patterned by EUV lithography

VB VentureBeat

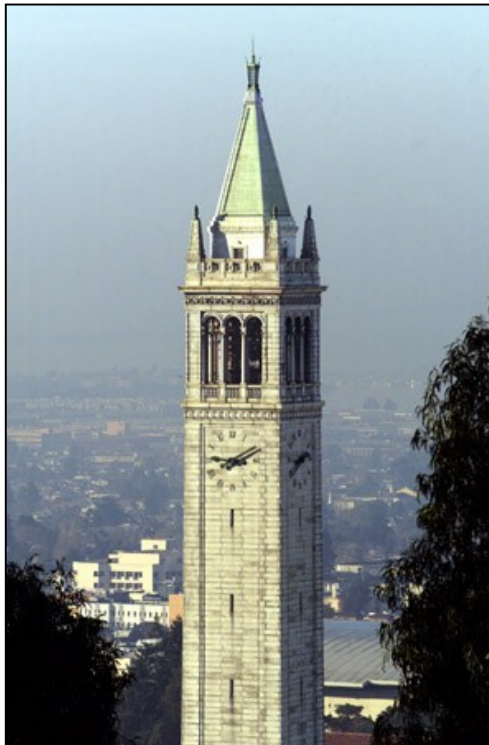
18 October

2018

Samsung begins making 7LPP chips, commercializing 7nm EUV lithography

7nm EUV lithography In a significant milestone for the semiconductor industry, Samsung today announced that it is now manufacturing 7LPP chips: processors based on extreme ultraviolet lithography (EUV) and a 7-nanometer manufacturing process. Beyond this specific accomplishment, the company notes that it is providing customers a clear path to future 3-nanometer chips.

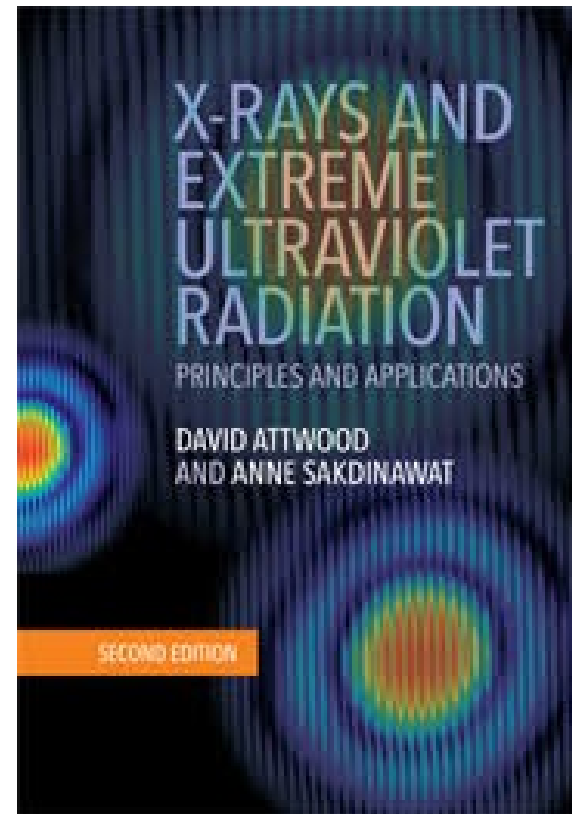
Further reading, 2021 online lectures, slides that you can use



UC Berkeley 2021 lectures online:

[https://www.youtube.com/playlist?](https://www.youtube.com/playlist?list=PL2wgq6z751n6EieNsPAx_b8elkmLS41GT)

[list=PL2wgq6z751n6EieNsPAx_b8elkmLS41GT](https://www.youtube.com/playlist?list=PL2wgq6z751n6EieNsPAx_b8elkmLS41GT)



Cambridge University Press

www.cambridge.org/xrayeuv

For slides, errata and HWs click
'Resources'