

# Photon Strength Functions at the low-energy tail of GDR

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**(Problems with)  
Photon Strength Functions  
at the low-energy tail of GDR  
(from experimentalists point of view)**

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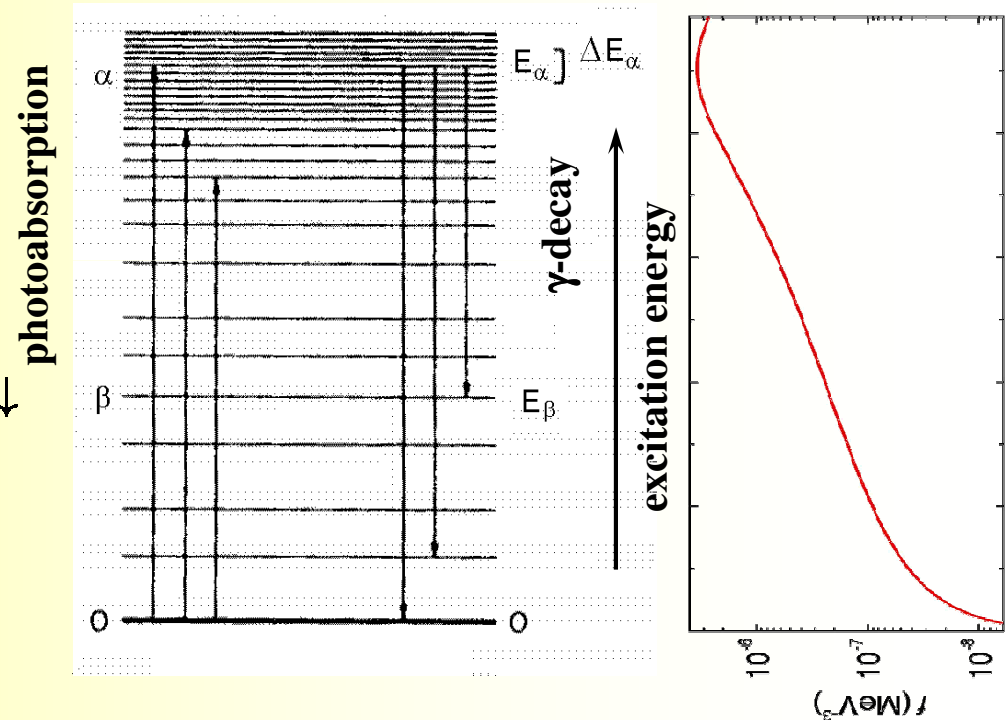
# Photon Strength Functions

- PSFs describe the (average) energy distribution of photon emission from “highly-excited” states or cross section for photon absorption (detailed balance principle)

$$\bar{\Gamma}_{\alpha\gamma\beta}^{(XL)} = \frac{1}{(\pi\hbar c)^2} \frac{E_\gamma^2}{2L+1} \frac{\bar{\sigma}_{\text{tot}}^{(XL)}(\beta \rightarrow \alpha)}{\rho(E_\alpha, J_\alpha, \pi_\alpha)}$$

$$\begin{aligned} \bar{\Gamma}_{\alpha\gamma\beta}^{(XL)} &= \frac{f^{(XL)} E_\gamma^{2L+1}}{\rho(E_\alpha, J_\alpha, \pi_\alpha)} \\ &= \frac{8\pi(L+1)}{L[(2L+1)!!]^2} \left( \frac{E_\gamma}{\hbar c} \right)^{2L+1} B(XL) \downarrow \end{aligned}$$

$$f^{(XL)} = \frac{1}{(\pi\hbar c)^2} \frac{\bar{\sigma}_{\text{tot}}^{(XL)}(\beta \rightarrow \alpha)}{(2L+1)E_\gamma^{2L-1}}$$

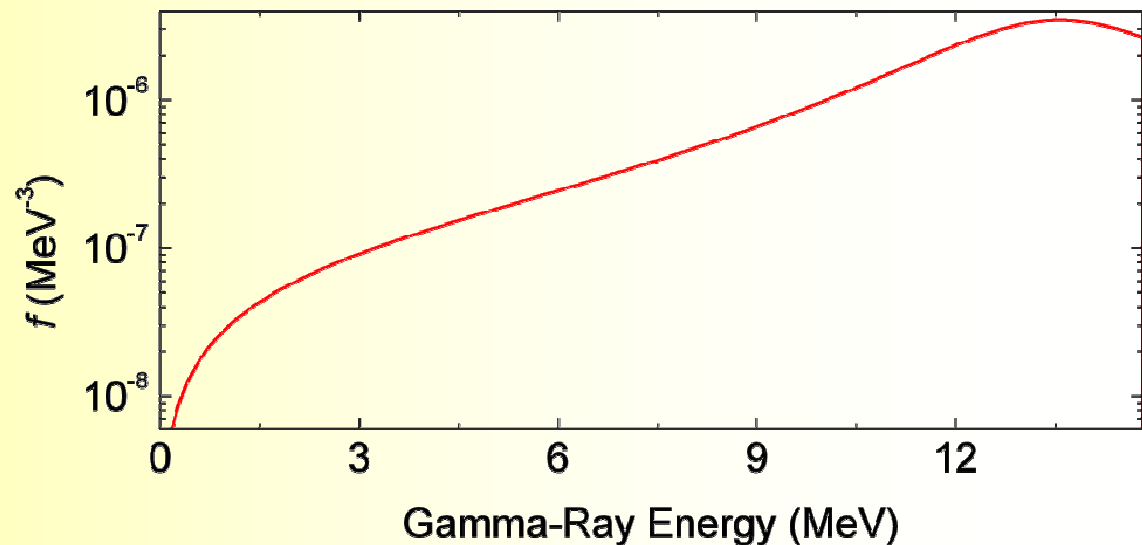


- Individual intensities fluctuate (according to Porter-Thomas distribution)  
see also talk of Paul Koehler

# Photon Strength Functions

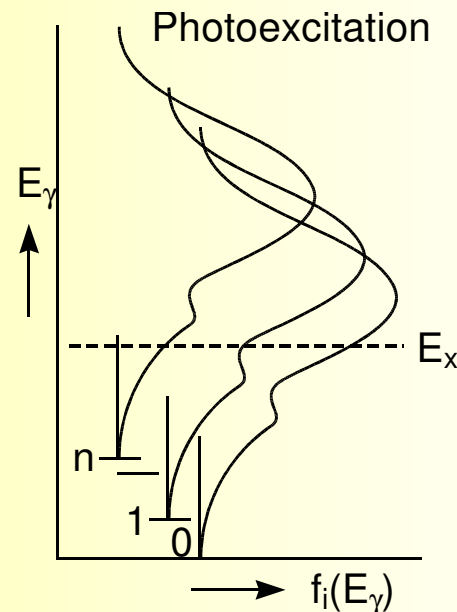
Quantities which PSFs can depend on:

- type of transitions (E1, M1, E2, ...) ✓
- gamma-ray energy ✓
- microscopic properties of the level (energy,  $J^\pi$ ) ?  
⇒ Brink hypothesis

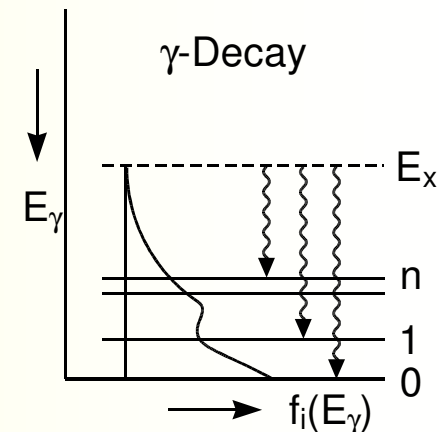


# Brink hypothesis

- The energy dependence of the photoeffect is independent of the detailed structure of the initial state  
⇒ dependence on  $\gamma$ -ray but not on excitation energy ( $T$ ),  $J^\pi, \dots$
- validity of the hypothesis?
- at least approximately - from  $(n, \gamma)$  reaction, hot nuclei, Oslo method
- some signs for temperature dependence

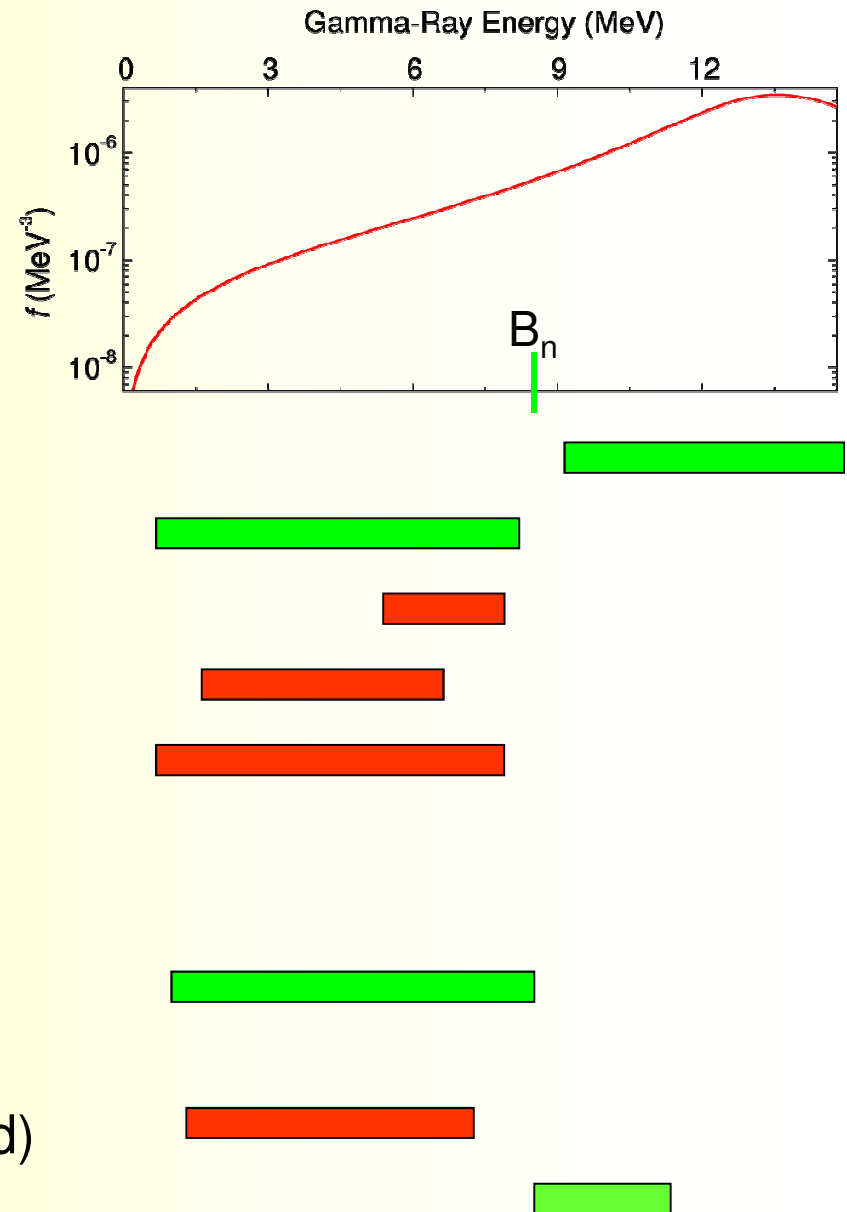


$$f_0(E_\gamma) = f_1(E_\gamma) = f_n(E_\gamma) = f(E_\gamma)$$

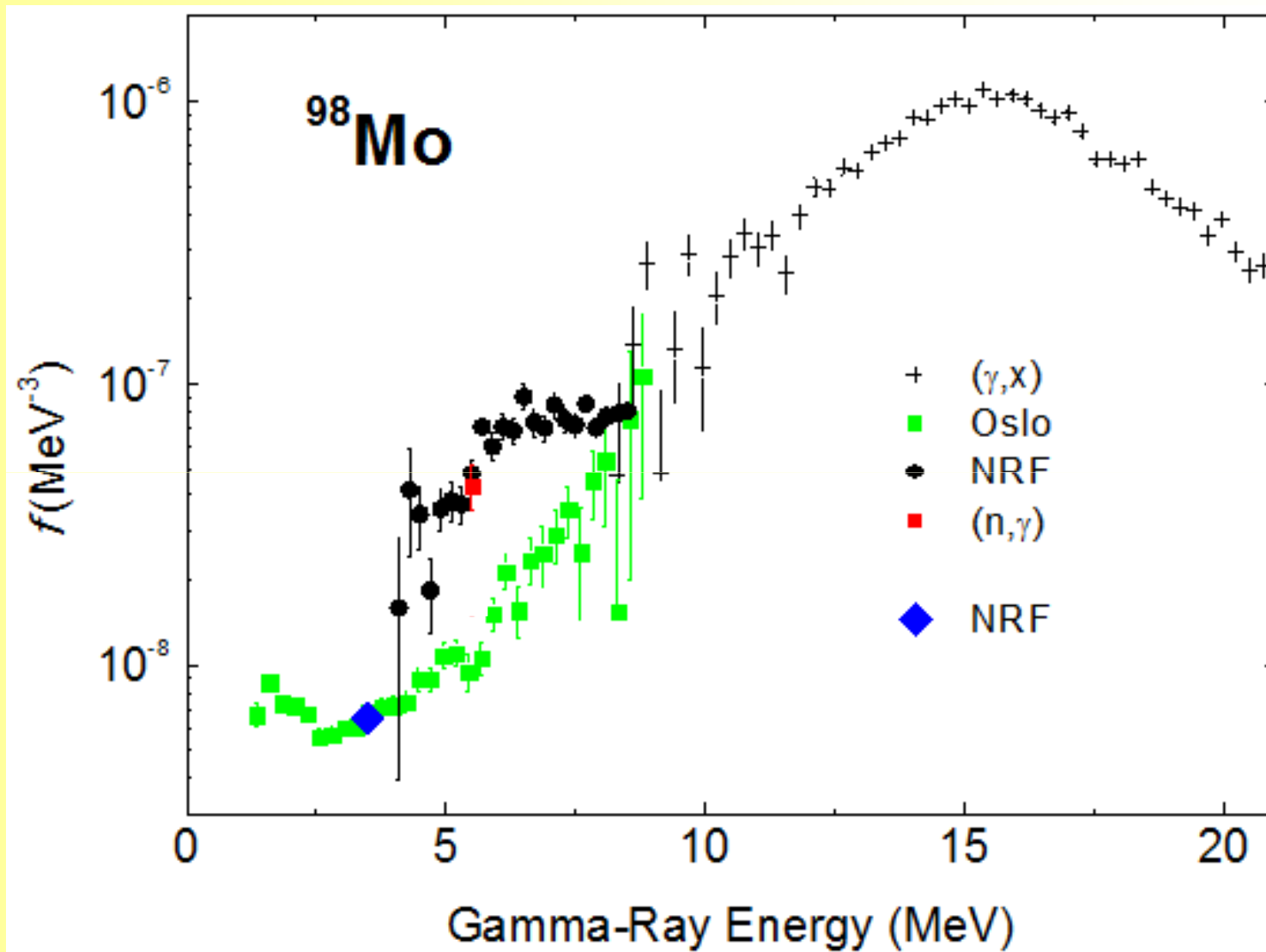


# Where could we learn about PSFs from?

- photoexcitation techniques
  - $(\gamma, \text{particle})$
  - NRF experiments
- primaries from  $(n, \gamma)$  reaction
- two-step cascades spectra -  $(n, \gamma)$
- spectrum fitting method
  - single spectra
  - coincidence spectra
- inelastic scattering of charged particles  $(e, e')$ ,  $(p, p')$ , ...
- sequential extraction (Oslo,  $^3\text{He}$ -induced)
- RA beams – Coulomb dissociation
- ...



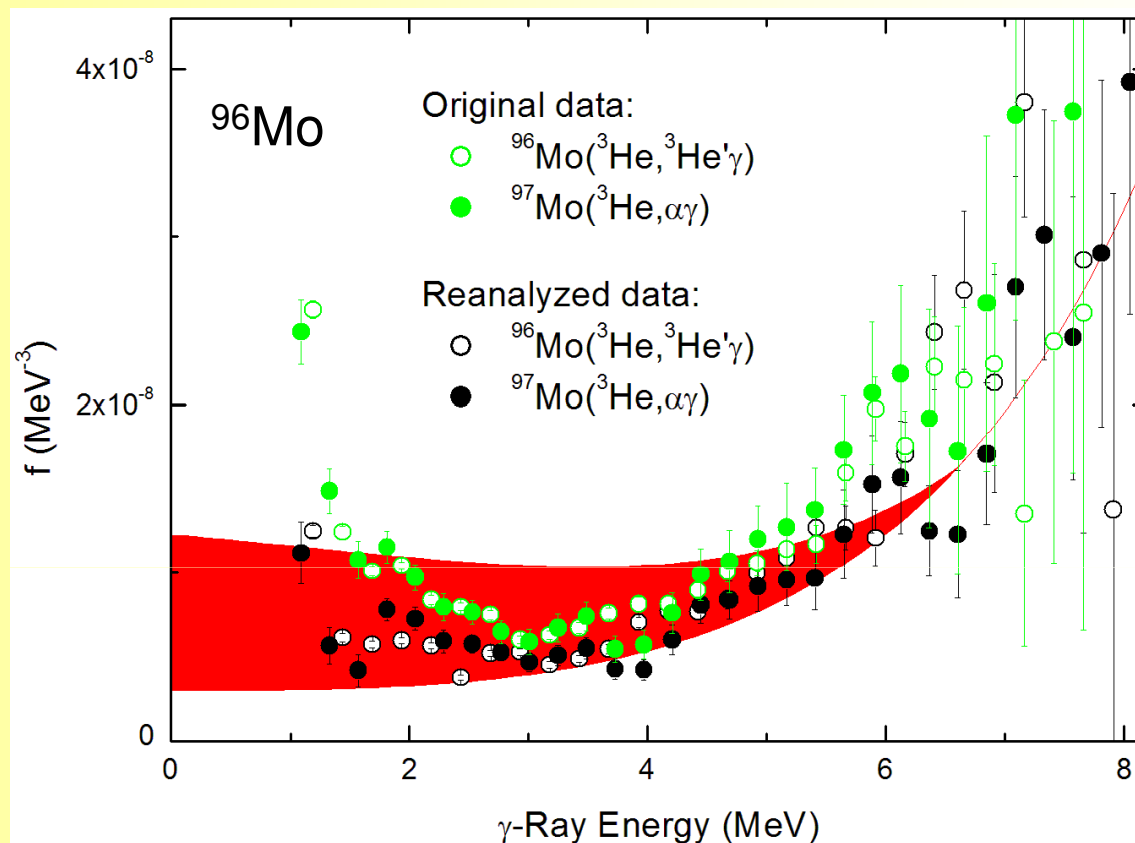
# Are results consistent?



G. Rusev et al., PRC77, 064321 (2008)

Dresden workshop, Aug 30, 2010

# Are results consistent?



PSF (T-dependent) which is consistent spectra from (n, $\gamma$ ) experiments - TSC and multistep spectra from DANCE experiment – simulations performed with the DICEBOX code

Krticka et al., PRC 77 054319 (2008), Sheets et al., PRC 79 024301 (2009)



# Why are there different results?

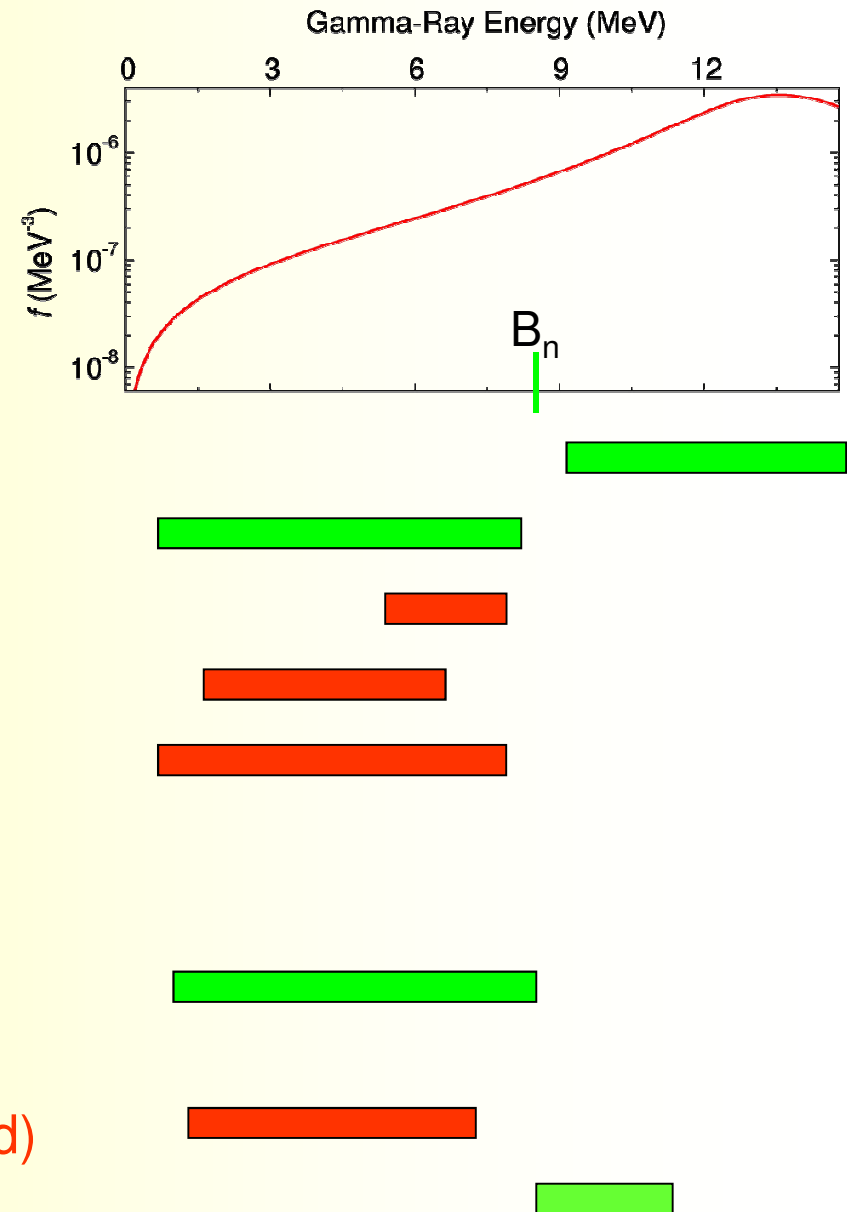
- Concept of photon strength function and/or Brink hypothesis is not valid
- Quantities deduced from different experiments are not the same
- The same quantities are deduced but interpretation is not correct

# Why are there different results?

- Concept of photon strength function and/or Brink hypothesis is not valid
- Quantities deduced from different experiments are not the same
- The same quantities are deduced but interpretation is not correct
  - The methods are usually “not direct”
  - Measured spectra must be often deconvoluted and interpreted
  - Spectra often comes from an interplay of PSF and level density
  - Additional information, often about level density, is required to produce final results

# Where could we learn about PSFs from?

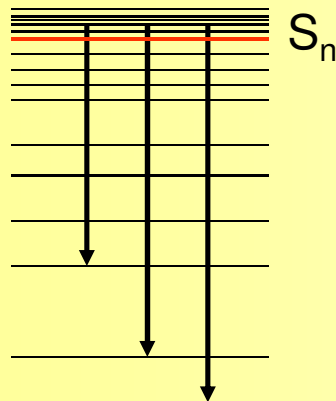
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# (n,γ) reactions – part 1

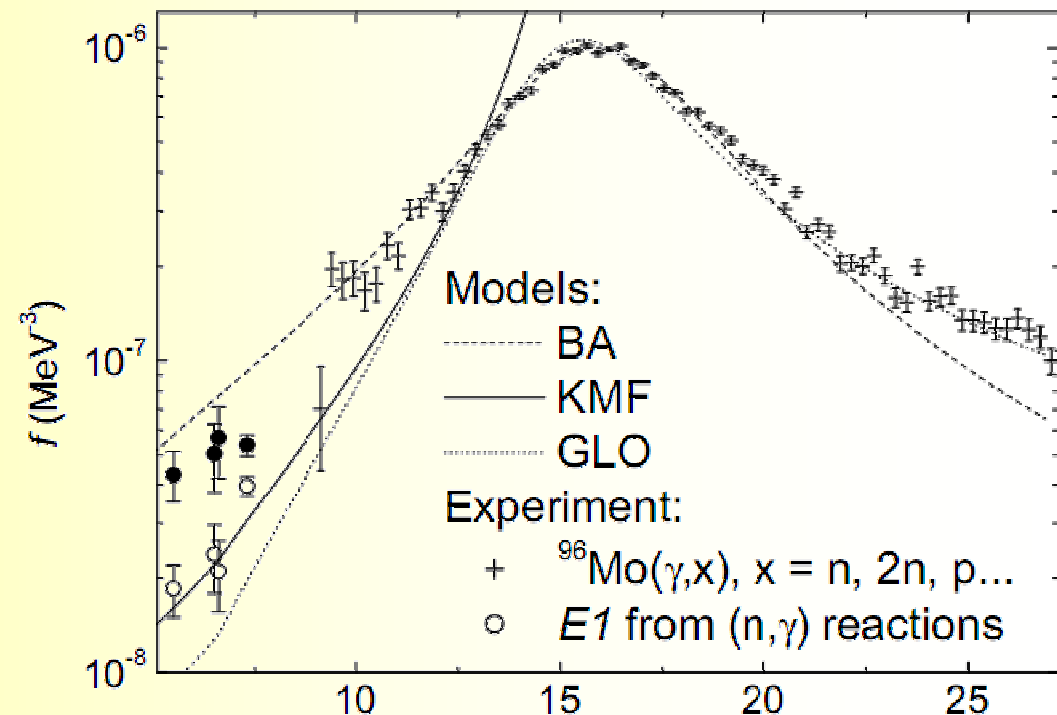
- PSF from intensities of primary transitions (Kopecky values in RIPL)

$$\bar{\Gamma}_{\alpha\gamma\beta}^{(XL)} = \frac{f^{(XL)} E_{\gamma}^{2L+1}}{\rho(E_{\alpha}, J_{\alpha}, \pi_{\alpha})}$$



- Values from RIPL must be taken with care

Nucleus	$XL$	$E_{\gamma}$ (MeV)	original (Kopecky) $\langle D \rangle$ (eV)	$f_{XL} \times 10^{-8}$ (MeV $^{-3}$ )	recalculated (RIPL) $\langle D \rangle$ (eV)	$f_{XL} \times 10^{-8}$ (MeV $^{-3}$ )
$^{93}\text{Mo}$	$E1$	6.6	1000	5.67(147)	2700(500)	2.10(54)
	$M1$	6.2		1.46(42)		0.54(16)
$^{95}\text{Mo}$	$E1$	7.3	975	5.38(41)	1320(180)	3.97(30)
$^{98}\text{Mo}$	$E1$	5.5	429	4.32(81)	1000(200)	1.85(35)
	$M1$	5.5		0.59(18)		0.25(7)
$^{94}\text{Nb}$	$E1$	6.5	37.8	5.04(124)	80(10)	2.38(59)
	$M1$	6.5		1.20(44)		0.57(21)



# (n,γ) reactions – part 2

Data from “spectrum fitting method”, TSC spectra,...

– decay simulated using the DICEBOX code (see also talk of Jiri Kroll)

- Try and error method
  - agreement of simulated spectra with experiment is checked
  - “standard” PSFs are usually tested
- There is a sensitivity to energy dependence of PSFs and sometimes (TSC spectra) to ratios of PSFs of different types (E1, M1, E2)
- There is **no** sensitivity to absolute values of PSFs in simulation of decay
- The only “absolute” quantity in simulations of decay is the total radiation width

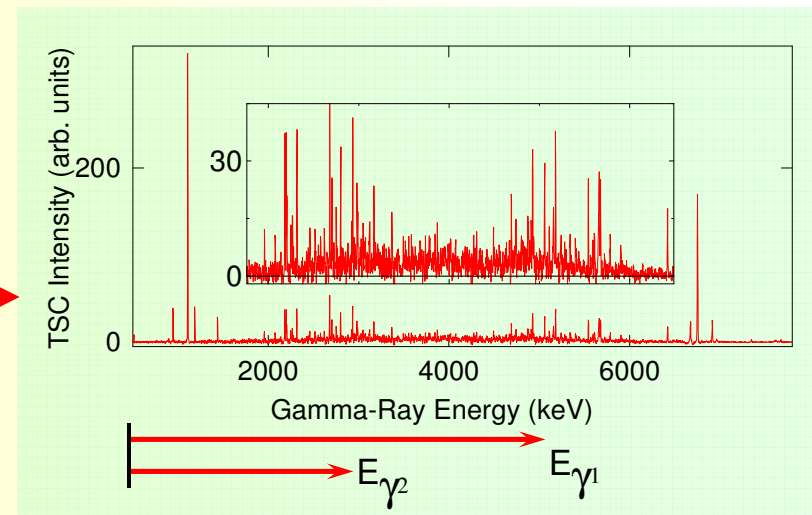
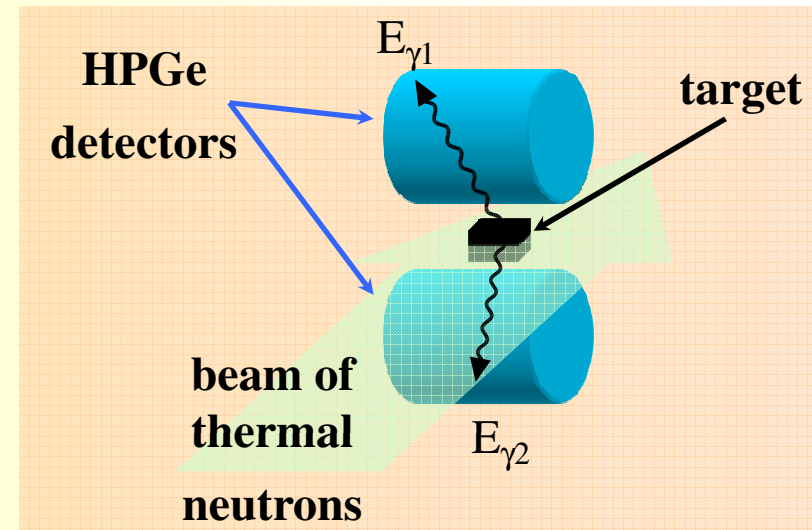
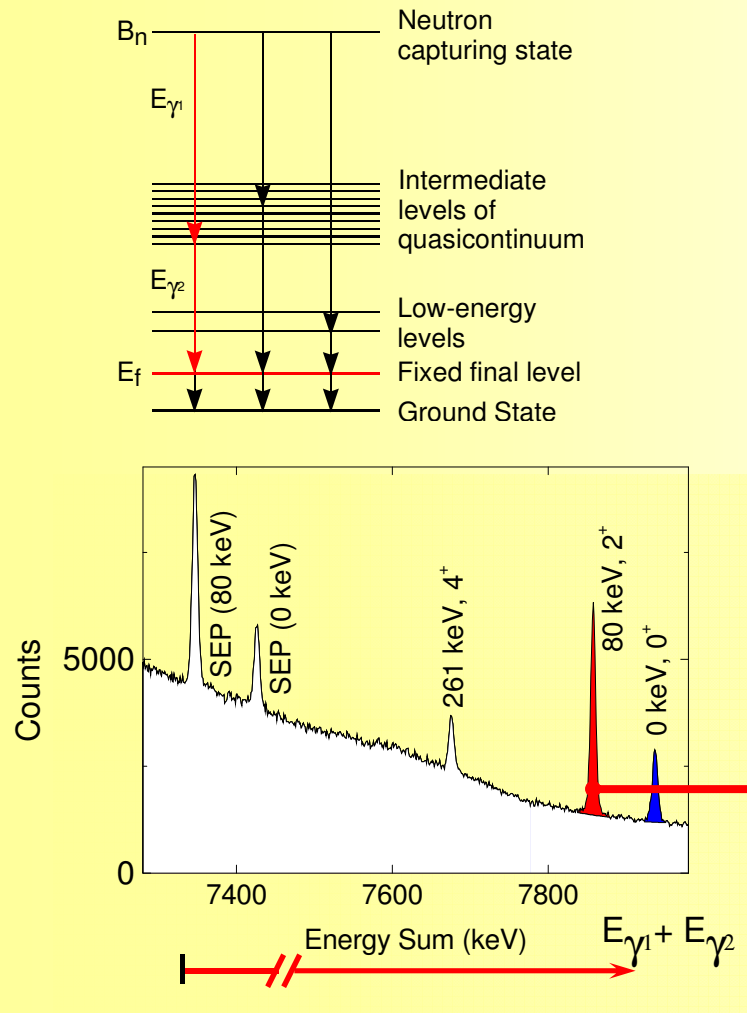
$$\Gamma_{\lambda\gamma} = \sum_f \Gamma_{\lambda\gamma f} \approx \sum_{XL} \int_0^{B_n} \frac{\rho(B_n - E_\gamma, J_f)}{\rho(B_n, J_{B_n})} f^{(XL)} E_\gamma^{2L+1} dE_\gamma$$

- Often photoabsorption data are matched above  $S_n$  and comparison of PSF from primaries is done

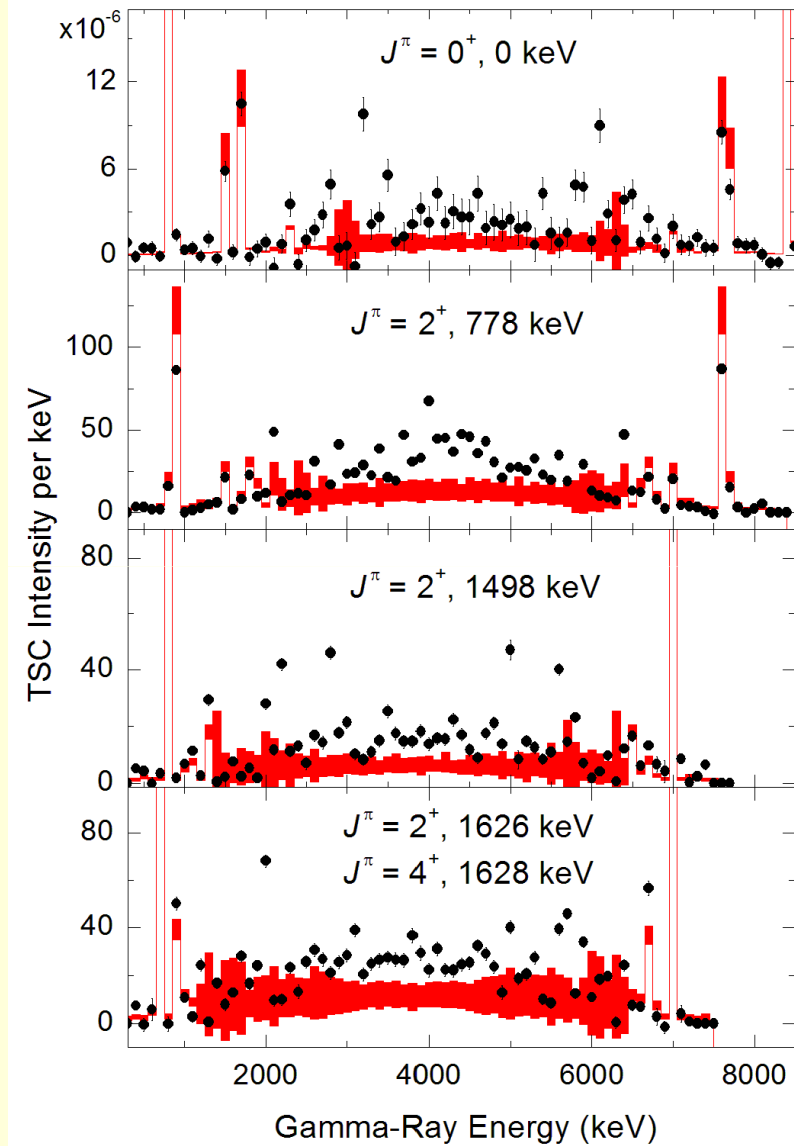
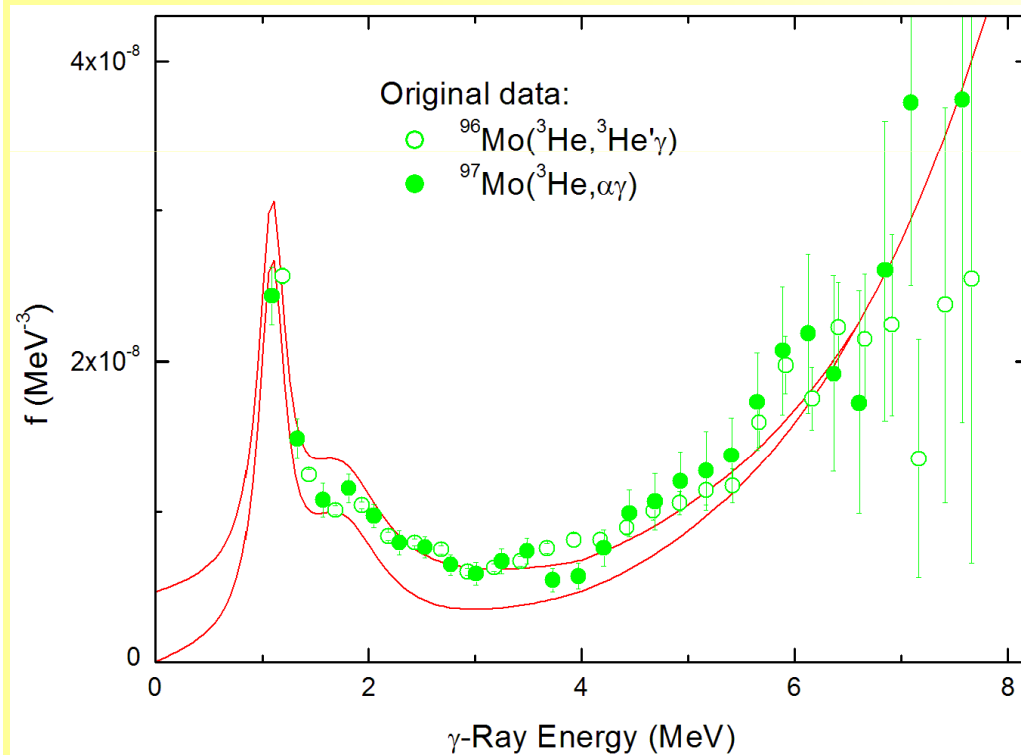
# TSC spektra

(see also talk of Jiri Kroll)

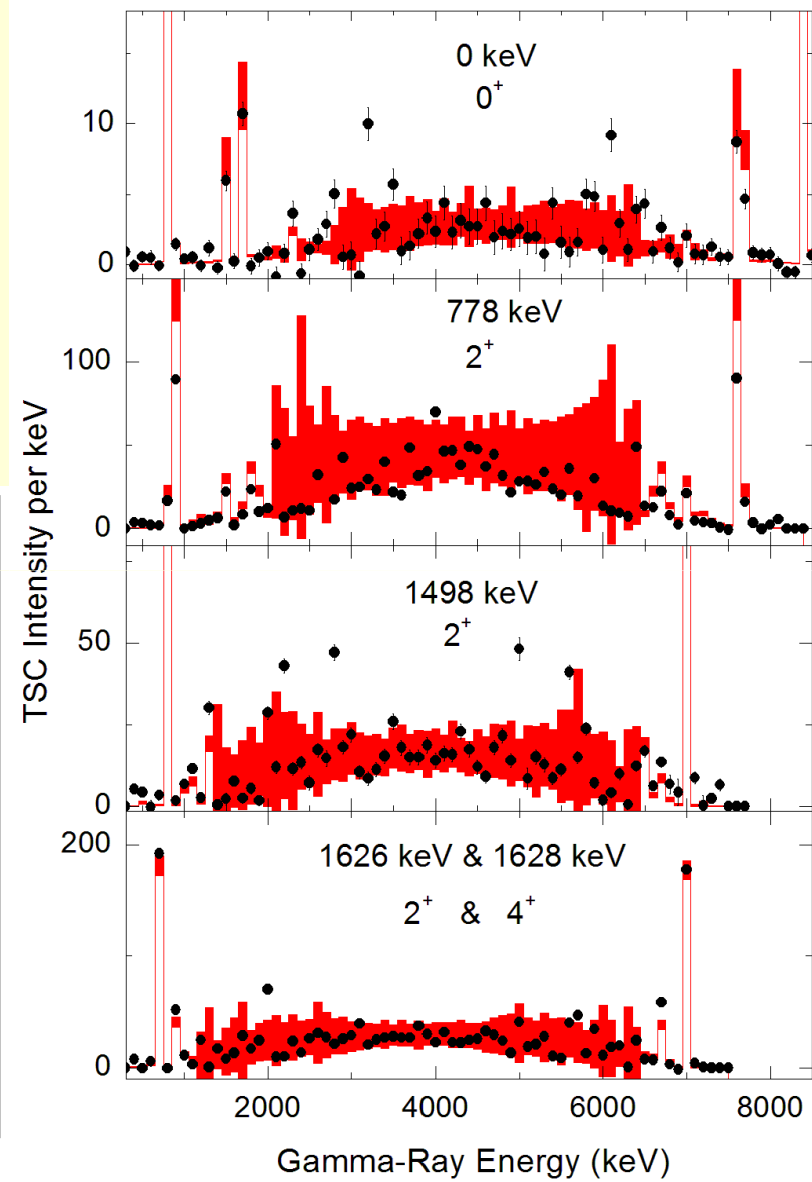
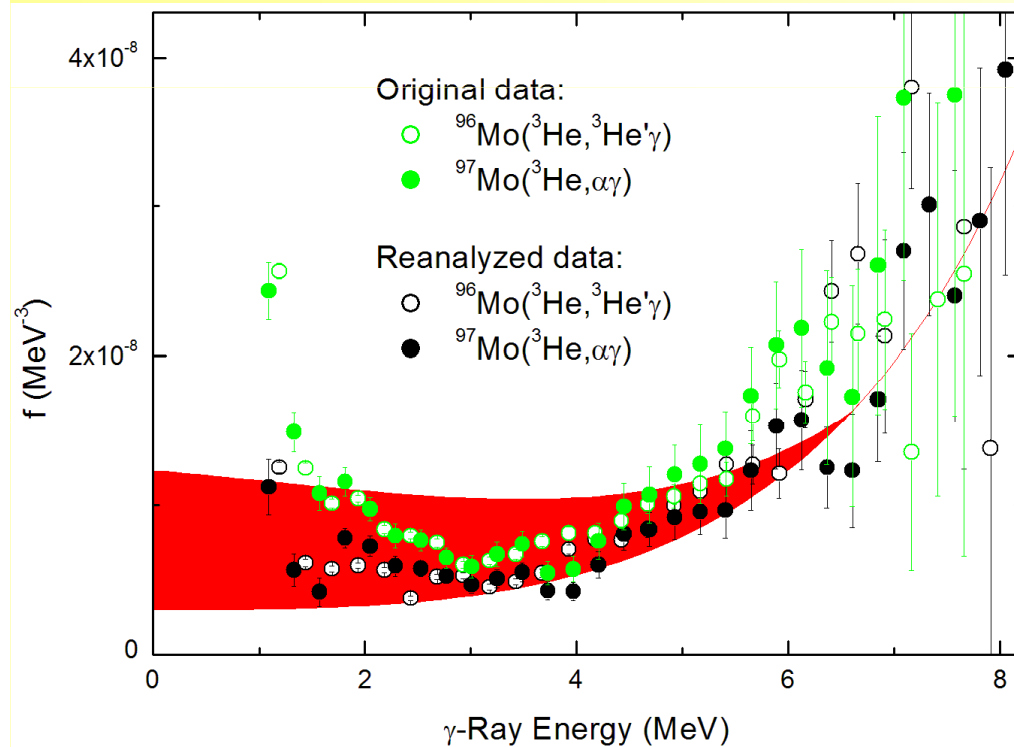
capture of thermal neutrons



# TSC spectra in $^{96}\text{Mo}$

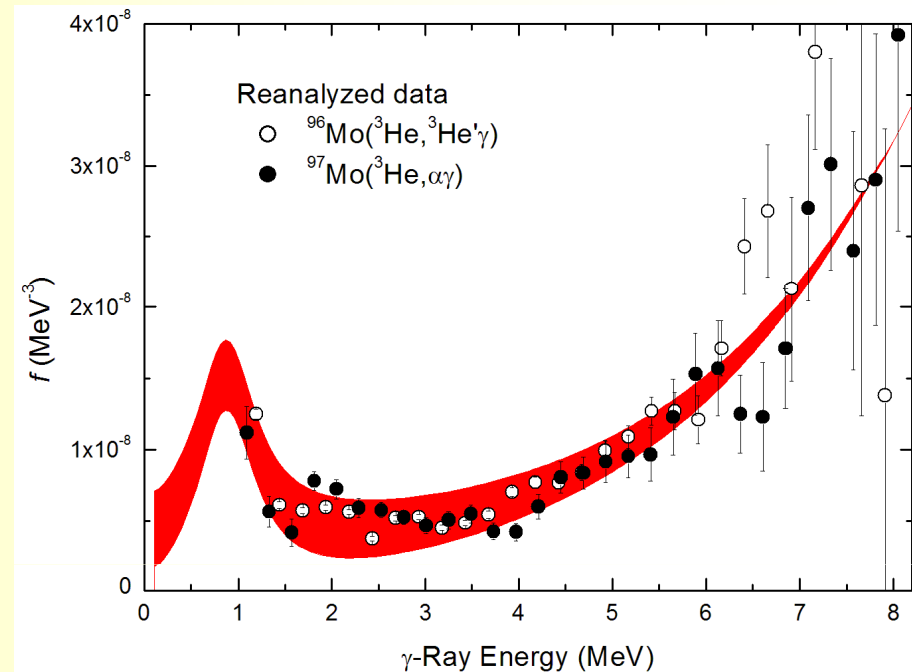
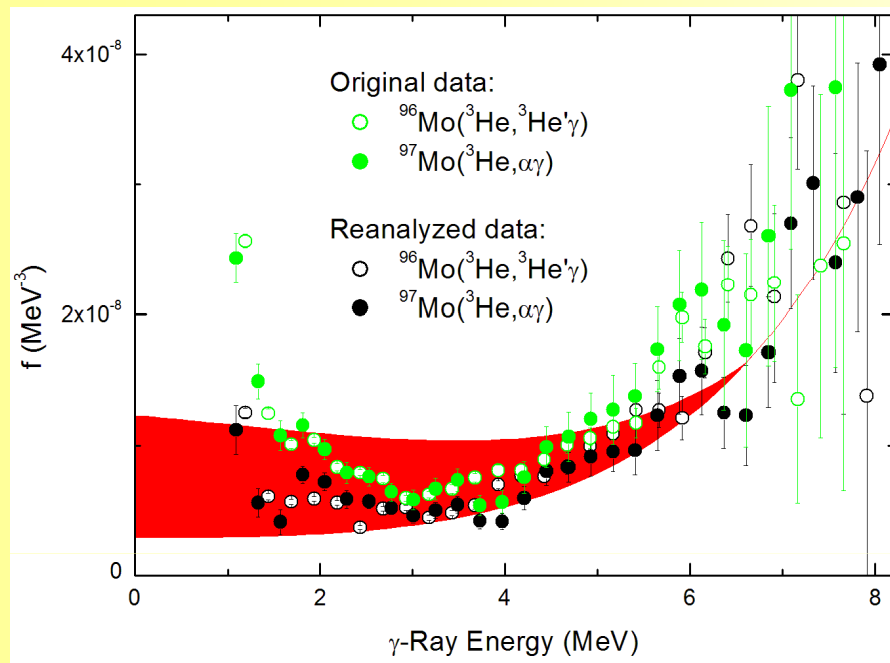


# TSC spectra in $^{96}\text{Mo}$





# TSC spectra in $^{96}\text{Mo}$



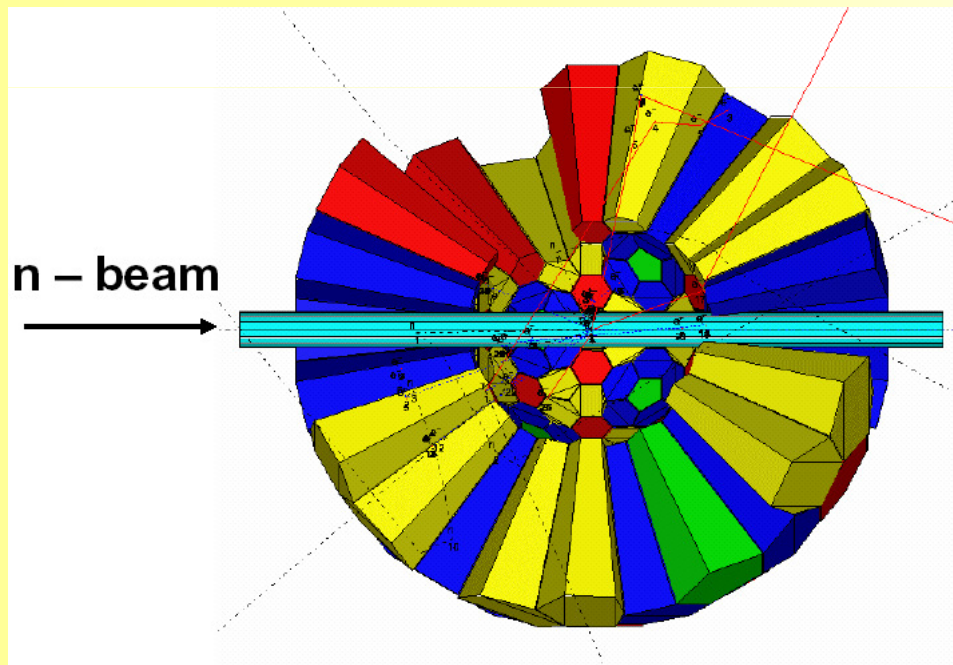
Pictures with comparison similar but correct statistical analysis excludes also this model at 99.8 % confidence level

[Krticka et al., PRC 77 054319 \(2008\)](#)

$\Rightarrow$  the enhancement is very weak if any analysis of data from DANCE confirm this

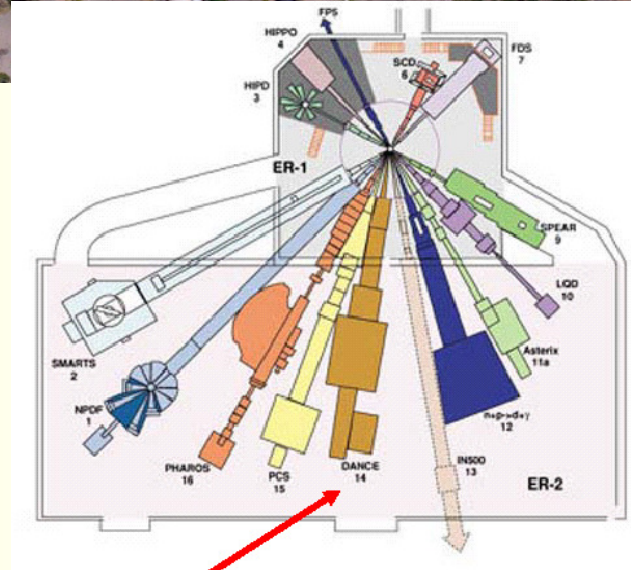
# DANCE @ LANSCE

- Moderated W target gives “white” neutron spectrum,  $\sim 14$  n’s/proton
- DANCE is on a 20 m flight path /  $\sim 1$  cm @ beam after collimation
- repetition rate 20 Hz
- pulse width  $\approx 125$  ns
- DANCE consists of 160 BaF<sub>2</sub> crystals

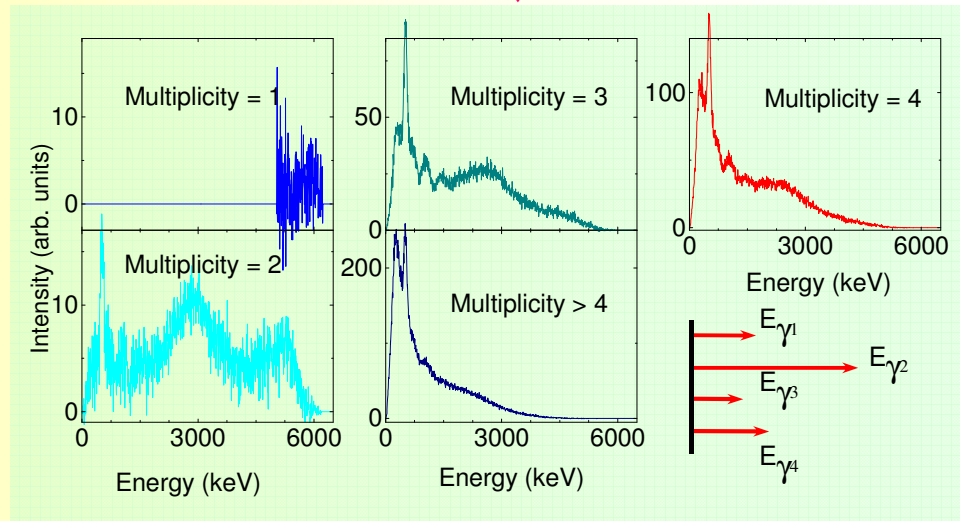
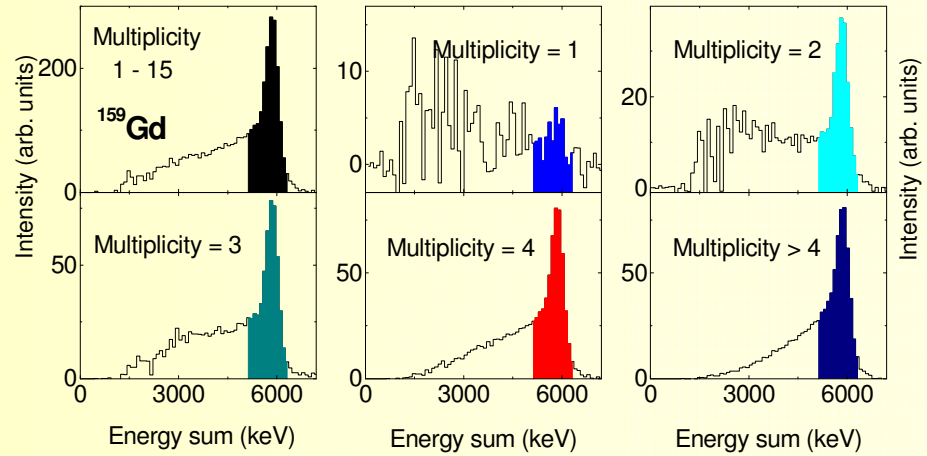
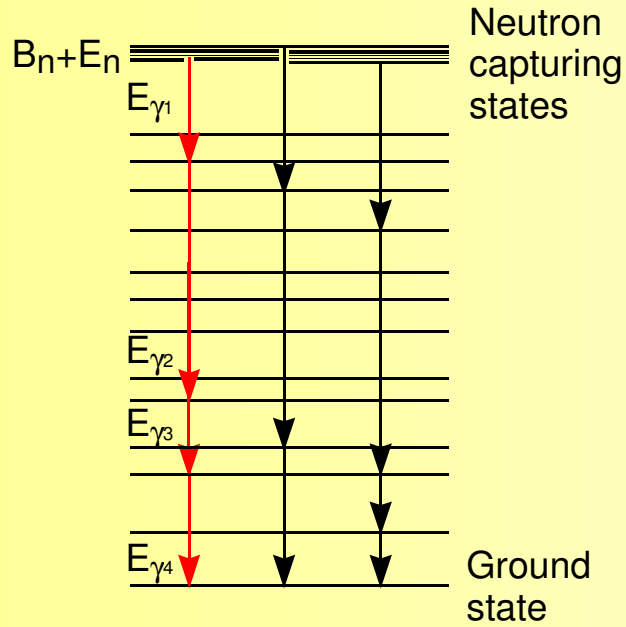


see also talk of John Ullmann

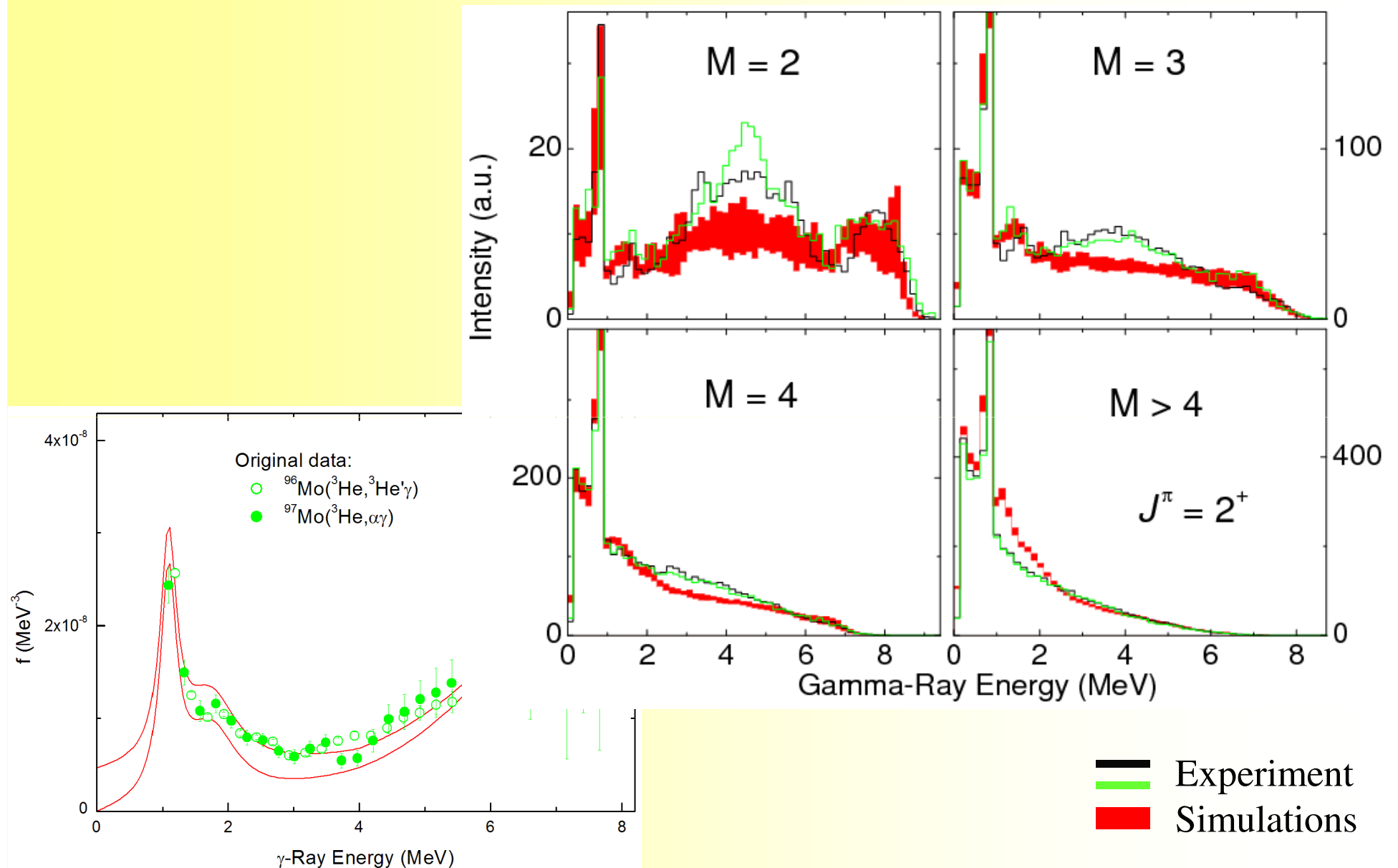
Dresden workshop, Aug 30, 2010



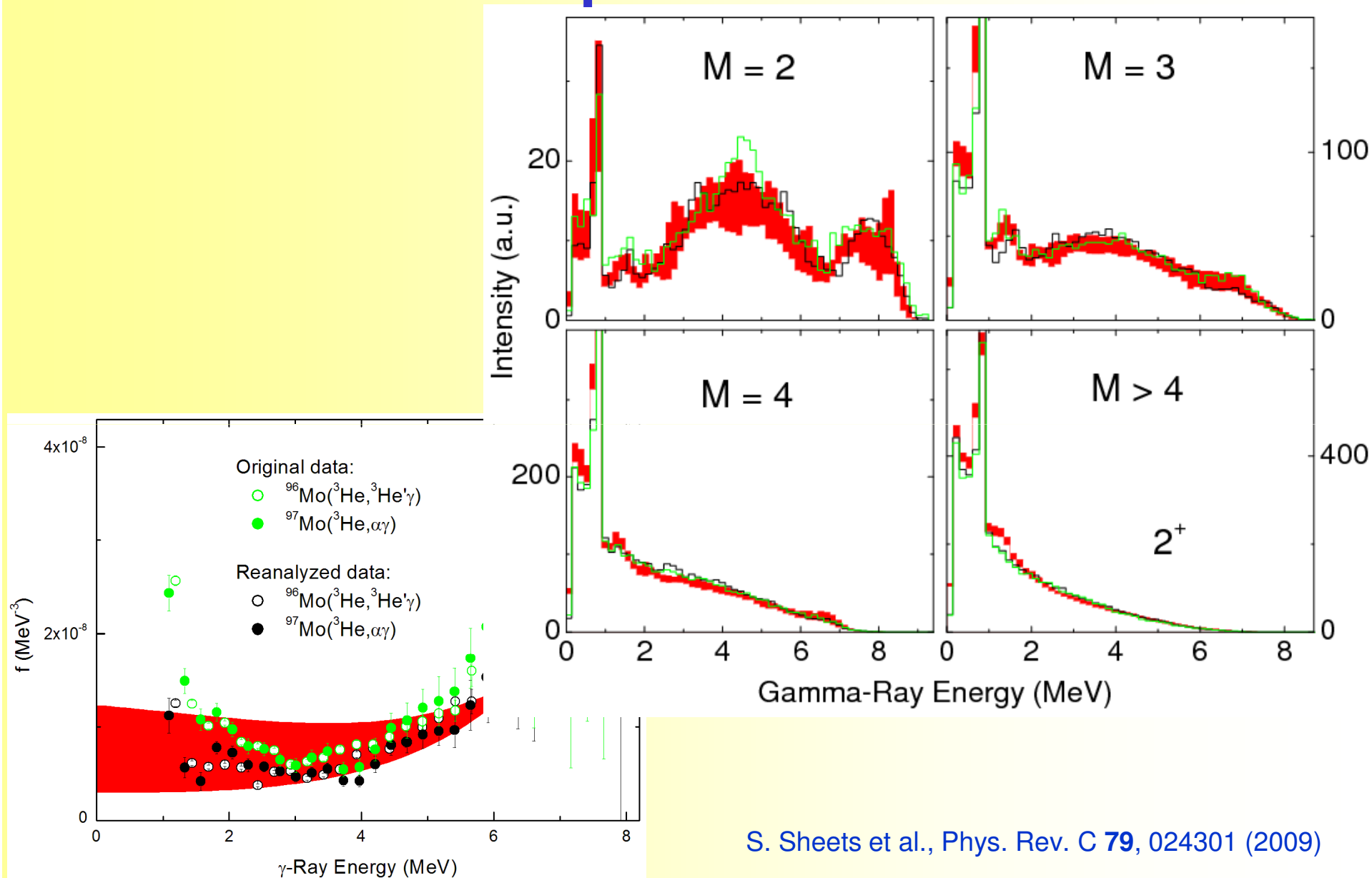
# What can be checked?



# MSC spectra in $^{96}\text{Mo}$



# MSC spectra in $^{96}\text{Mo}$



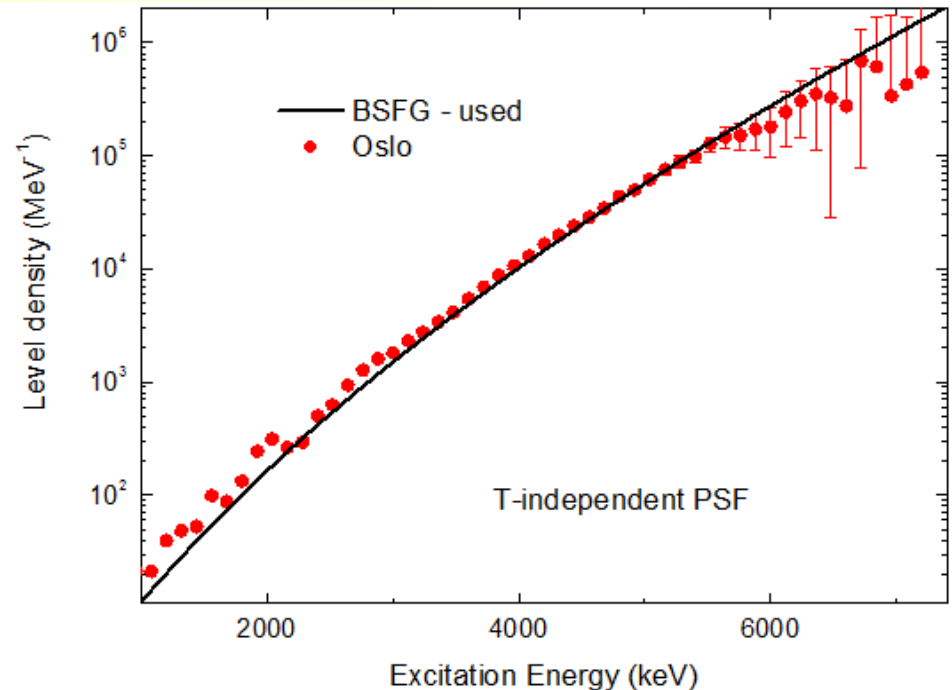
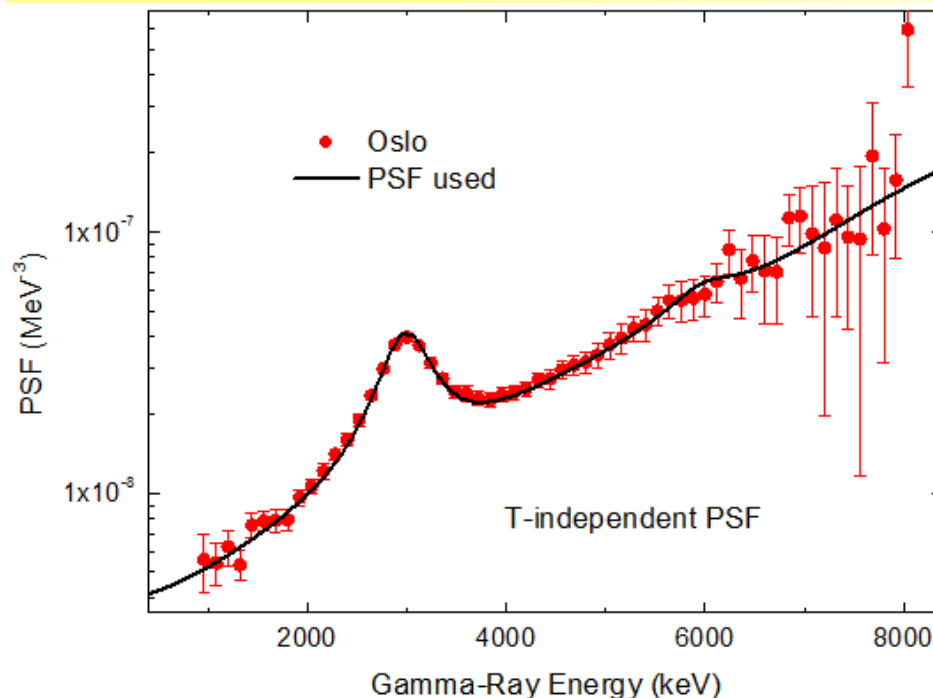
S. Sheets et al., Phys. Rev. C **79**, 024301 (2009)



# Oslo method

(see also talk of Ann-Cecilie Larsen)

- Spectra of primaries are extracted from measured spectra (unfolding of detector response)
- Iterative procedure applied to spectra of primaries - two functions can be obtained
  - one dependent only on excitation energy (level density)
  - the other one only on gamma-ray energy (PSF)



# Oslo method

- Spectra of primaries are extracted from measured spectra (unfolding of detector response)
- Iterative procedure applied to spectra of primaries - two functions can be obtained
  - one dependent only on excitation energy (level density)
  - the other one only on gamma-ray energy (PSF)
- The procedure works very well but there are **no unique results** – infinite number of solutions connected via relations

$$f(E_\gamma) = N_f e^{-\alpha E_\gamma} \tilde{f}(E_\gamma)$$

$$\rho(E_{\text{exc}}) = N_\rho e^{\alpha E_{\text{exc}}} \tilde{\rho}(E_{\text{exc}})$$

- What does happen if the PSF depends on excitation energy?  
Not discussed here ...

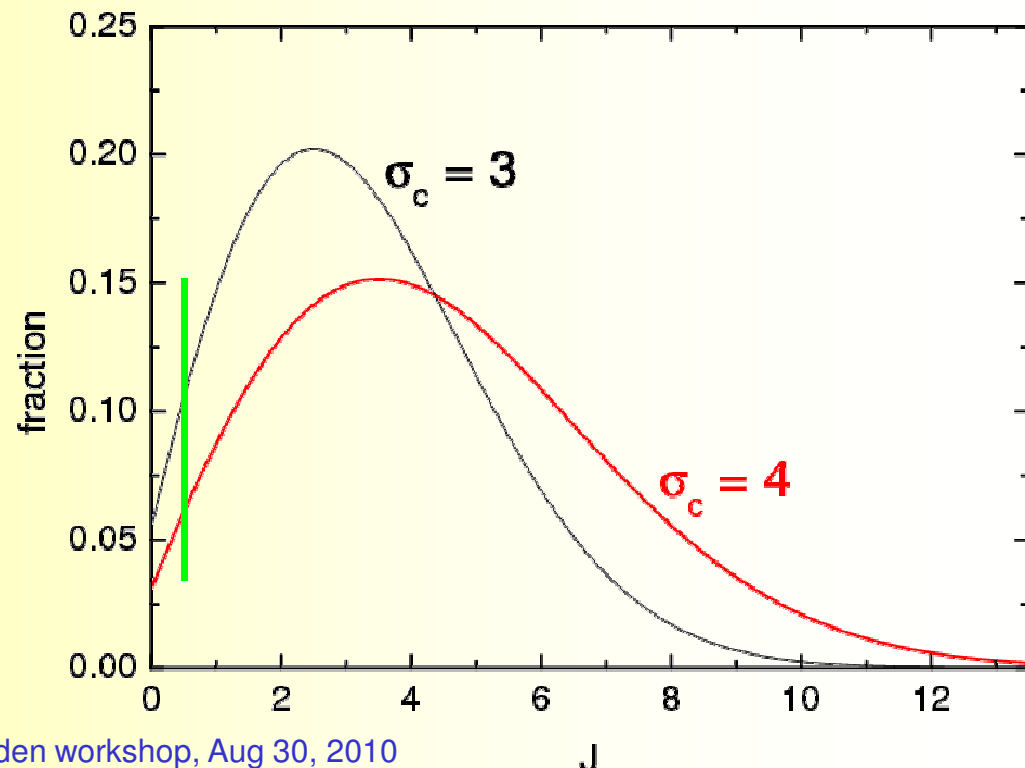
# Oslo method

- Slope (coef  $\alpha$ ) and absolute value of level density are fixed using levels near the ground state and neutron resonances
- **Problem** – spin dependence of level density, especially in the resonance region

$$\rho(J) = \frac{2J+1}{2\sigma_c^2} \exp\left(-\frac{(J+1/2)^2}{2\sigma_c^2}\right)$$

$$f(E_\gamma) = N_f e^{-\alpha E_\gamma} \tilde{f}(E_\gamma)$$

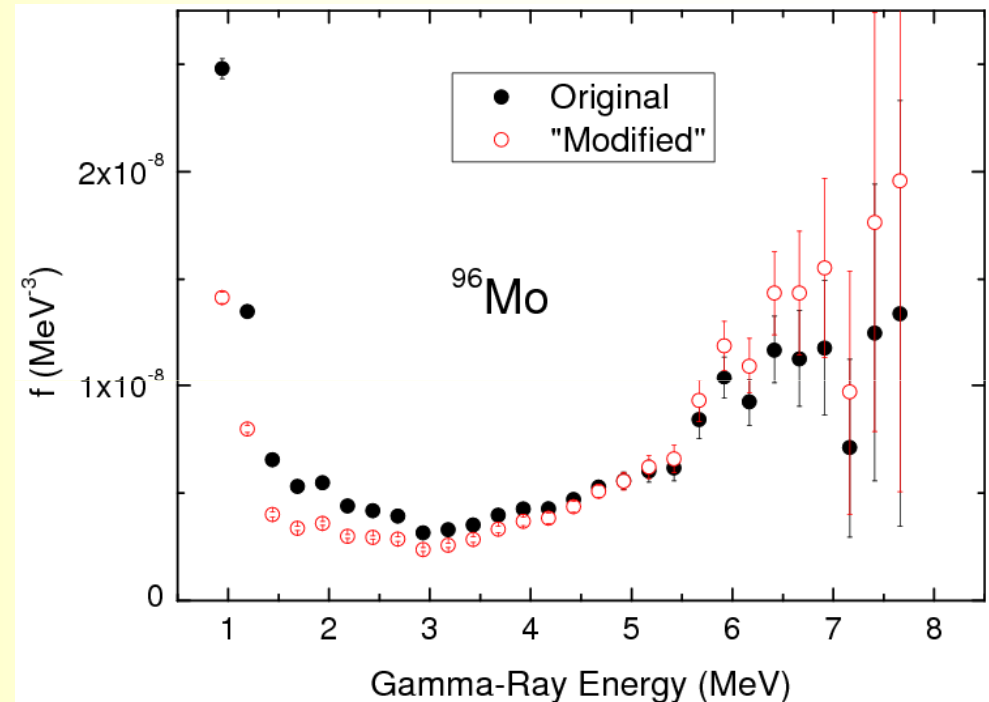
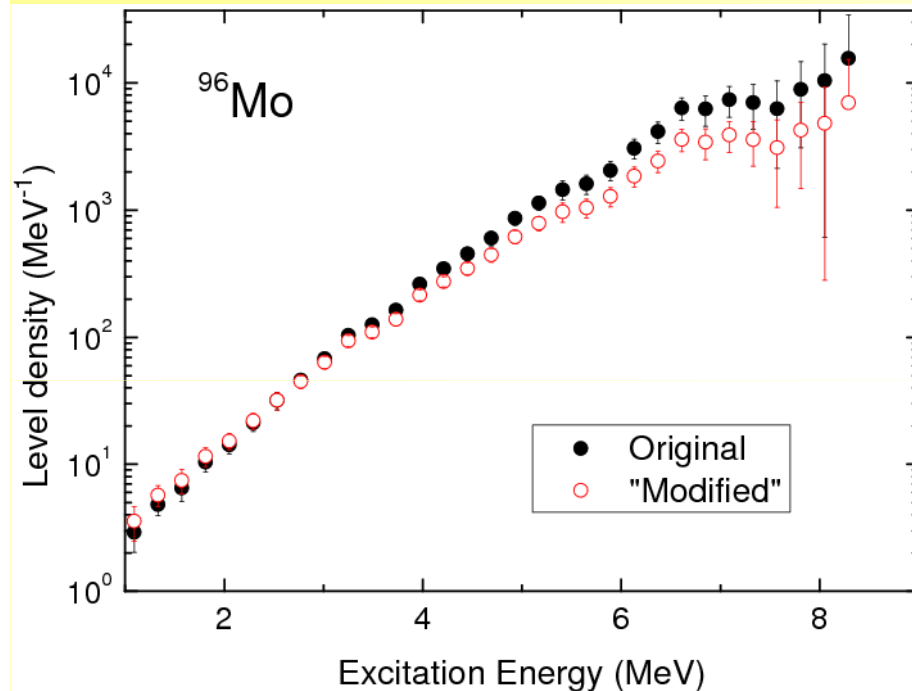
$$\rho(E_{\text{exc}}) = N_\rho e^{\alpha E_{\text{exc}}} \tilde{\rho}(E_{\text{exc}})$$





# Oslo method

- This might lead to very different value of coef  $\alpha$  and shape of PSF



- Additional problem with absolute value (normalization) of PSF
  - usually done with help of total radiation width

# Oslo method

Spin dependence of level density may be much more complicated than that given by closed-form expression

$$\rho(J) = \frac{2J+1}{2\sigma_c^2} \exp\left(-\frac{(J+1/2)^2}{2\sigma_c^2}\right)$$

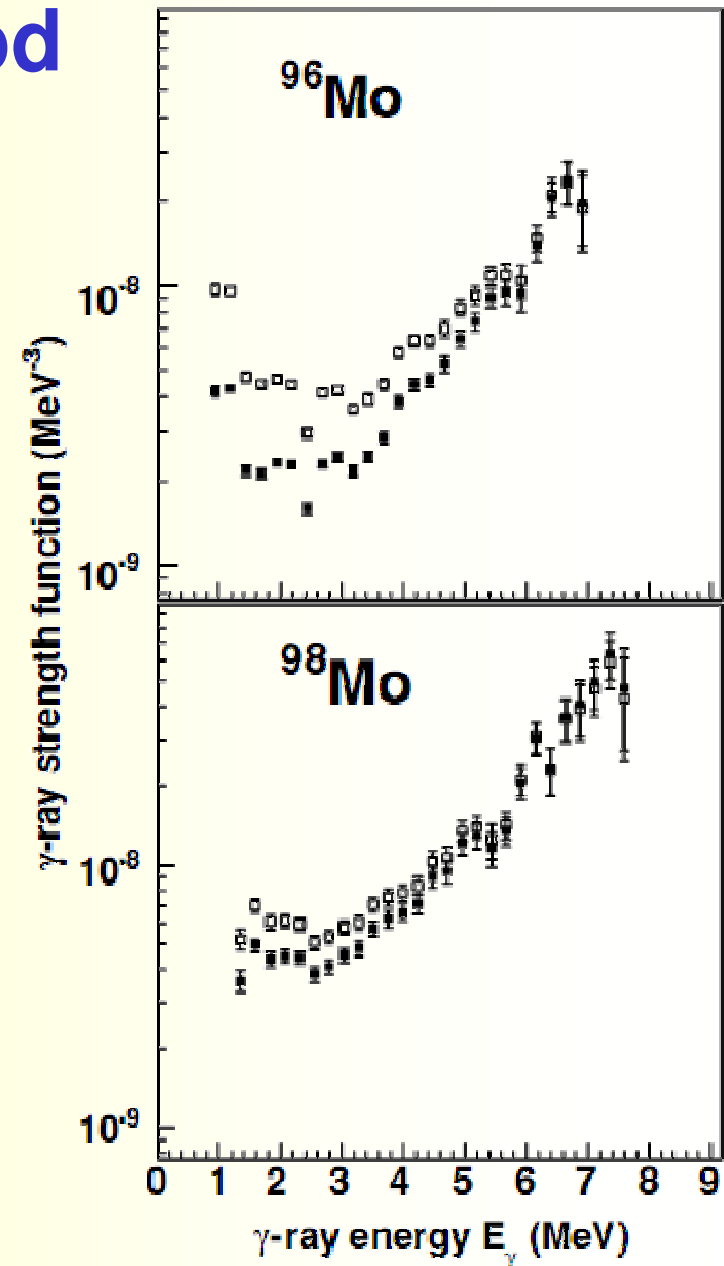
A published example:

Recalculation of RSF based on calculated level density from

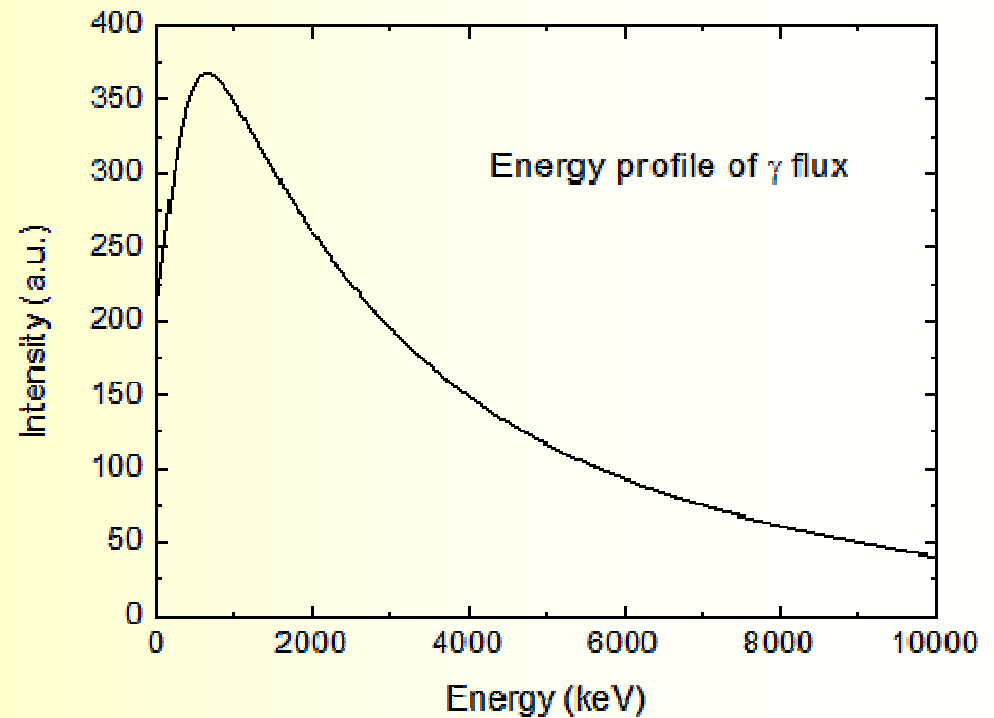
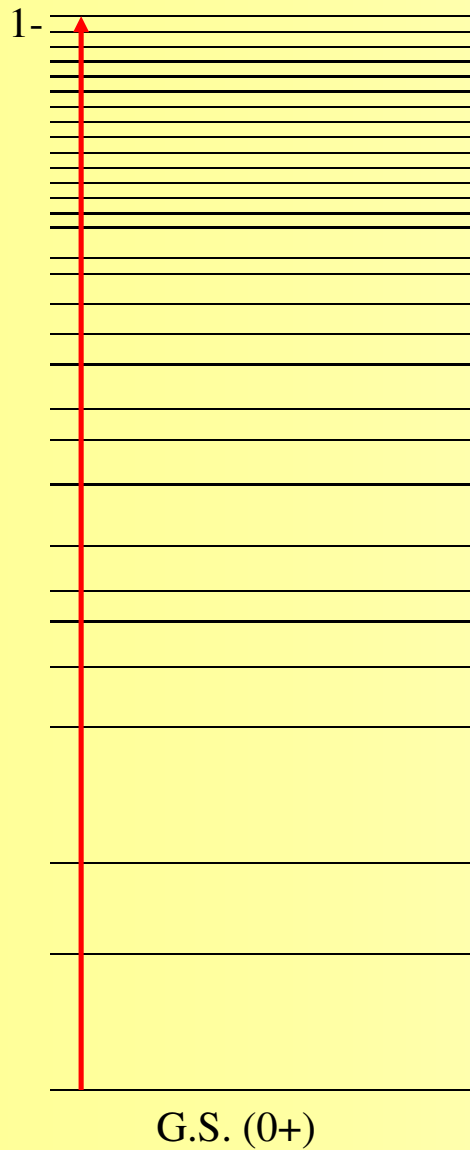
Goriely, Hilaire, and Koning, Phys.Rev.C 78, 064307(2008)

were published recently in

Larsen and Goriely, PRC 82 014318 (2010)

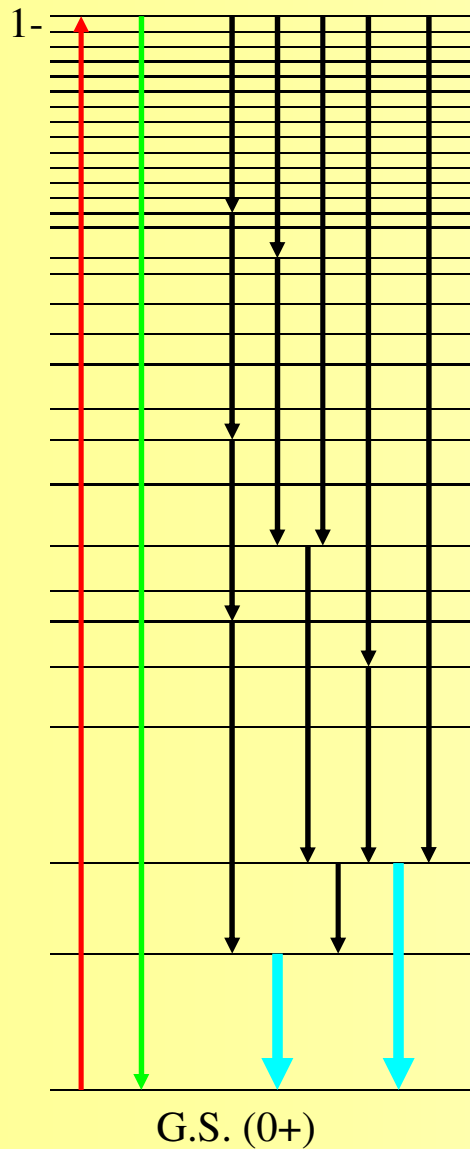


# NRF with beam from “bremsstrahlung”



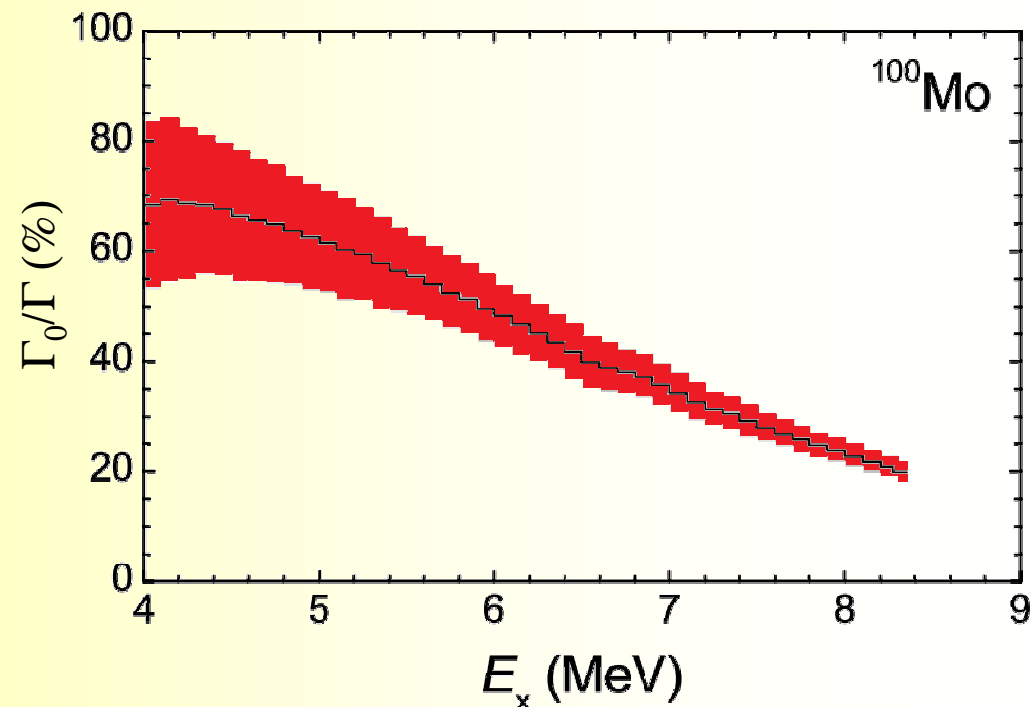
(see also talks of members of Rossendorf group)

# NRF with beam from “bremsstrahlung”



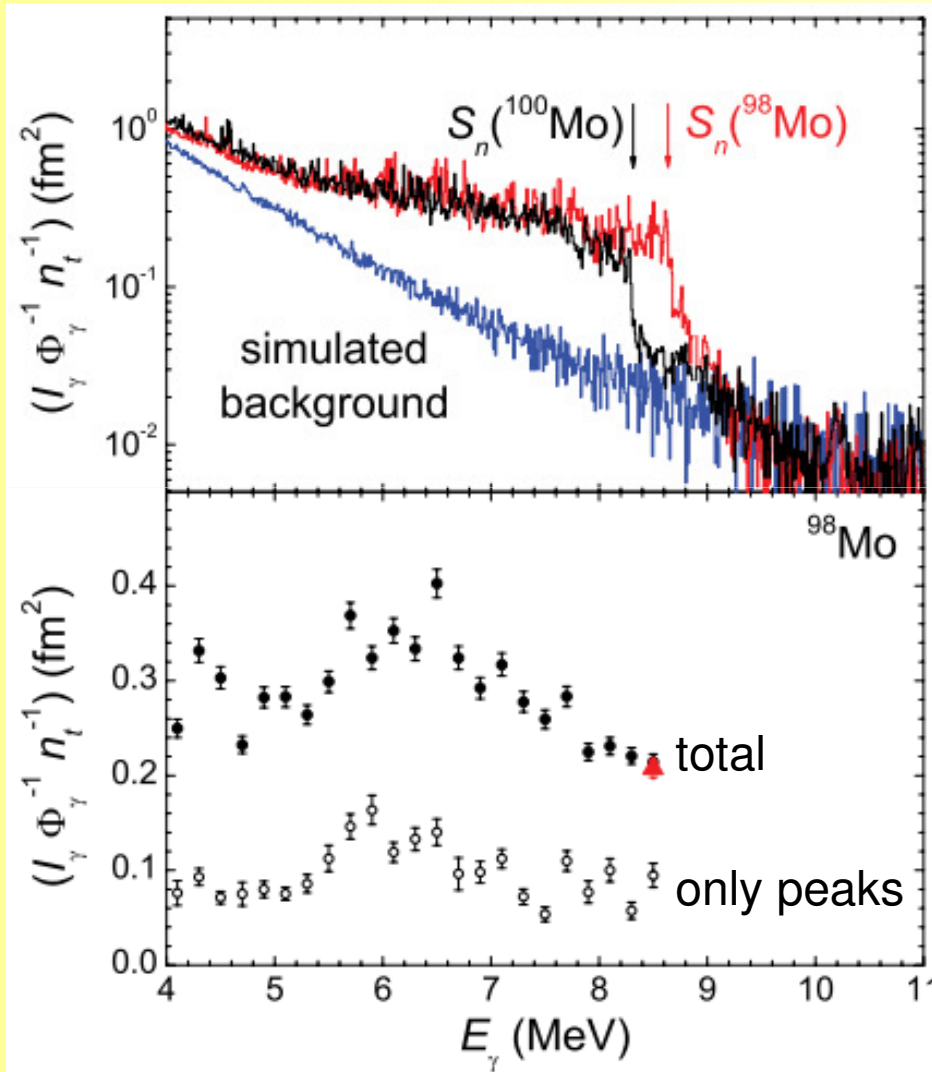
Many transitions to excited states –  
correction for them is needed

$$I_s = \int_0^\infty \sigma_{\gamma f}(E) dE = \frac{2J_R + 1}{2J_0 + 1} \left( \frac{\pi \hbar c}{E_R} \right)^2 \Gamma_0 \frac{\Gamma_f}{\Gamma}$$

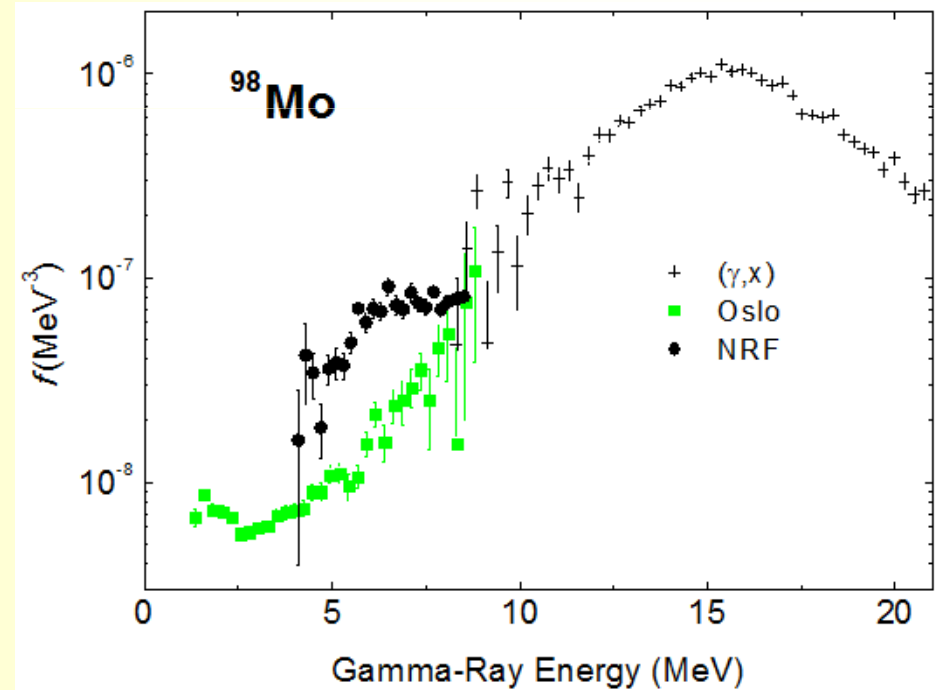


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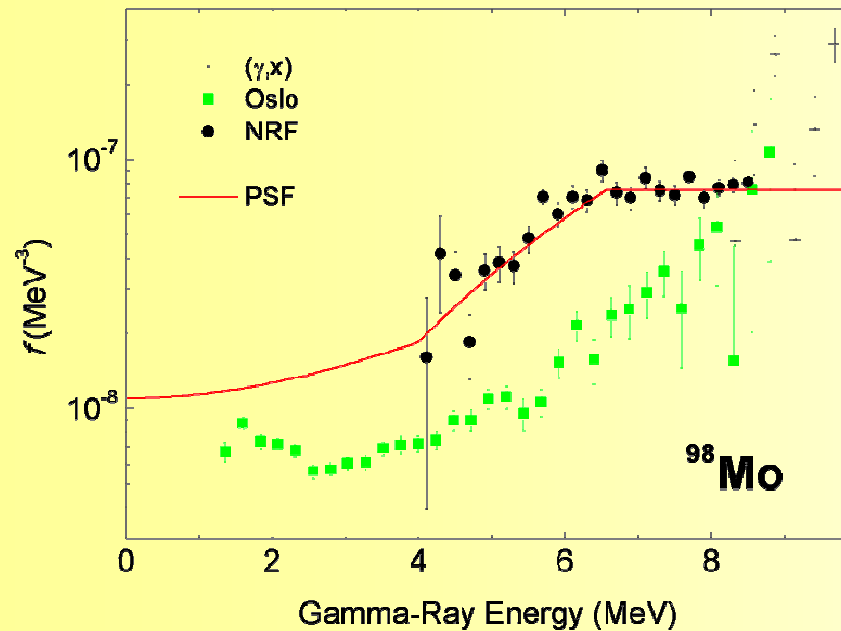
- An “iterative” procedure is applied and PSF to the GS is obtained



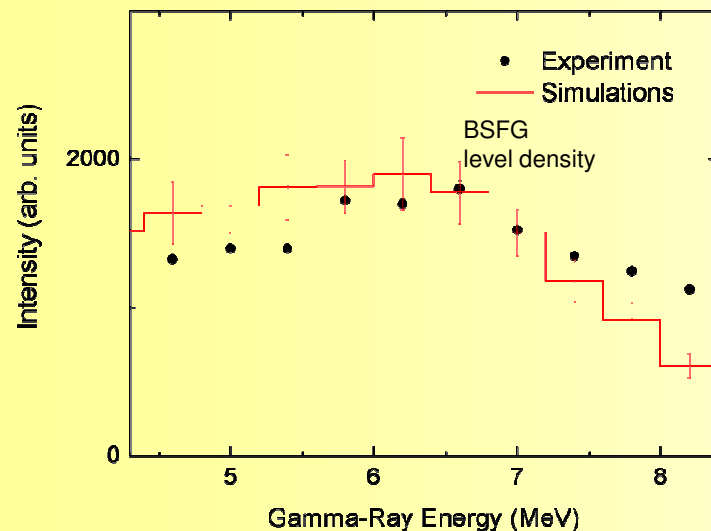
G. Rusev et al., PRC77, 064321 (2008)



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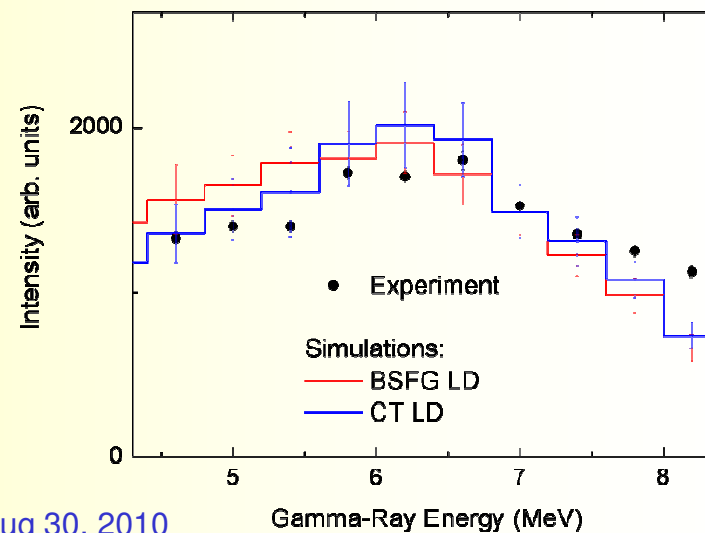
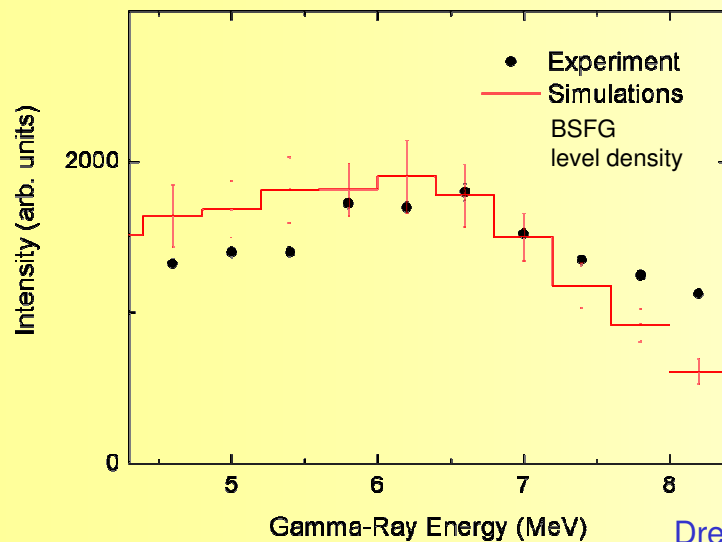
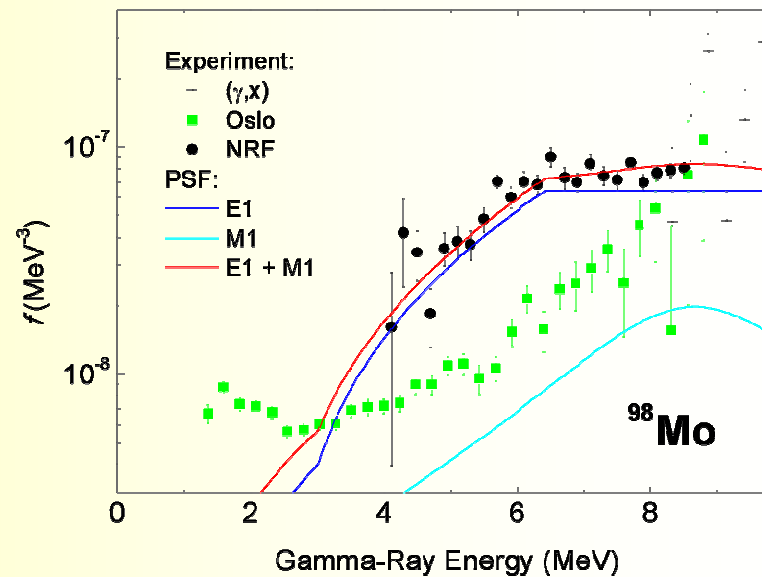
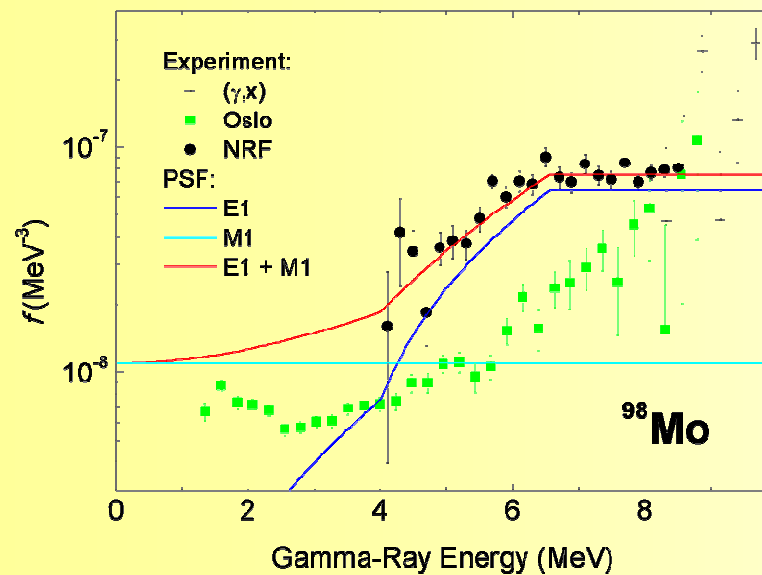
- Simulations of gamma decay with DICEBOX code can produce spectra comparable to measured ones.



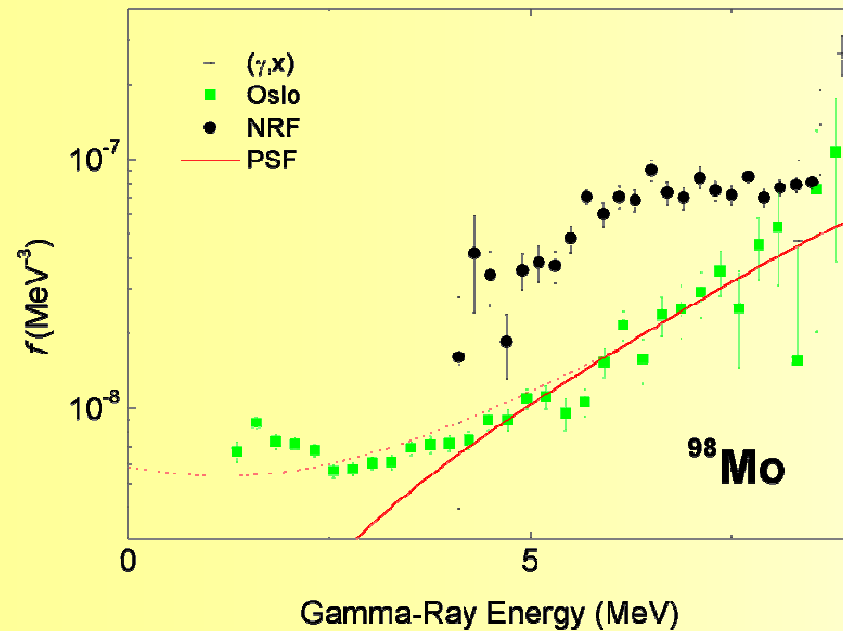
- The PSF reproducing NRF data seems not to reproduce the spectrum

The results are preliminary

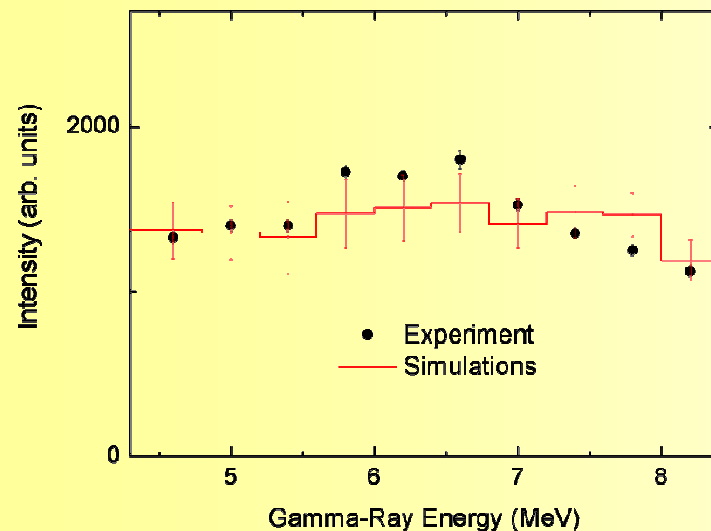
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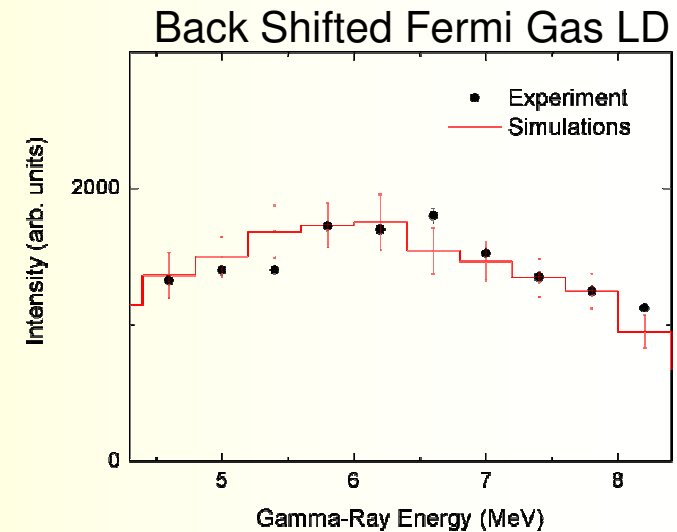
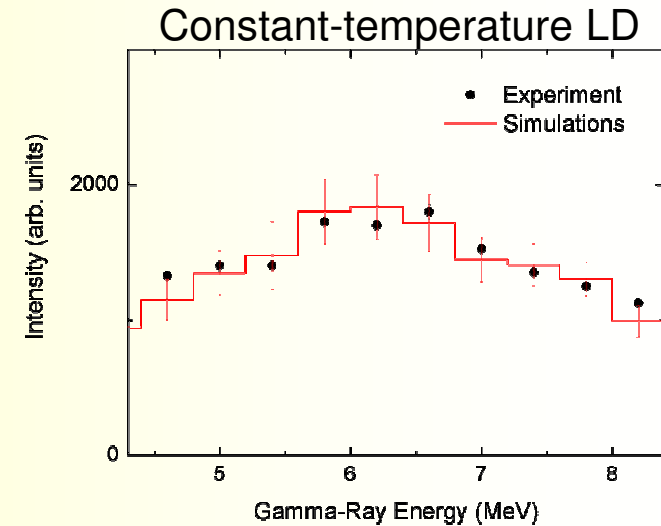
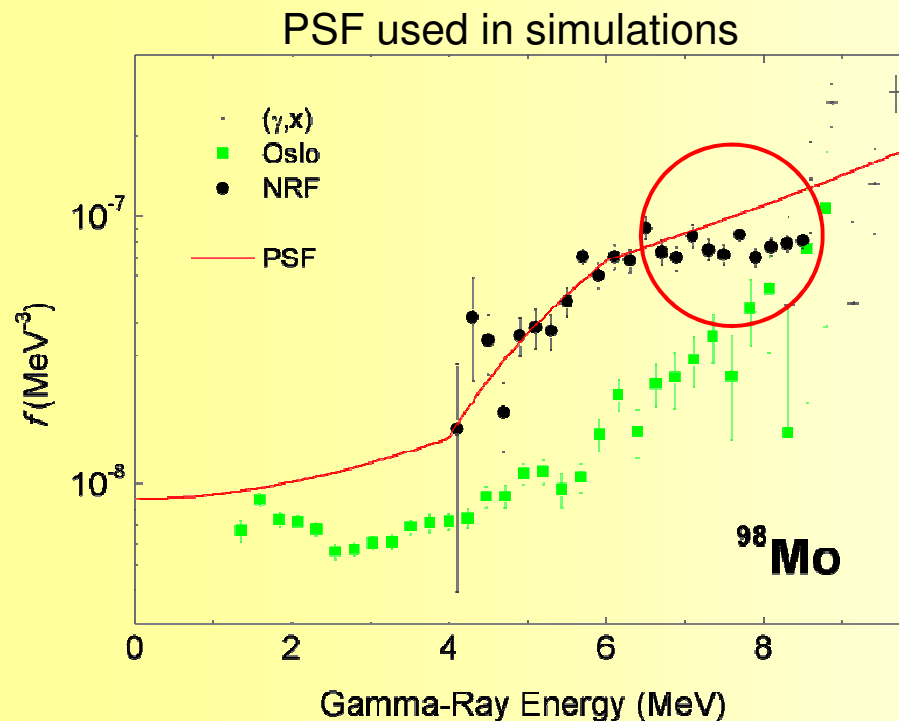
- Spectra cannot be reproduced also using PSF from Oslo measurement



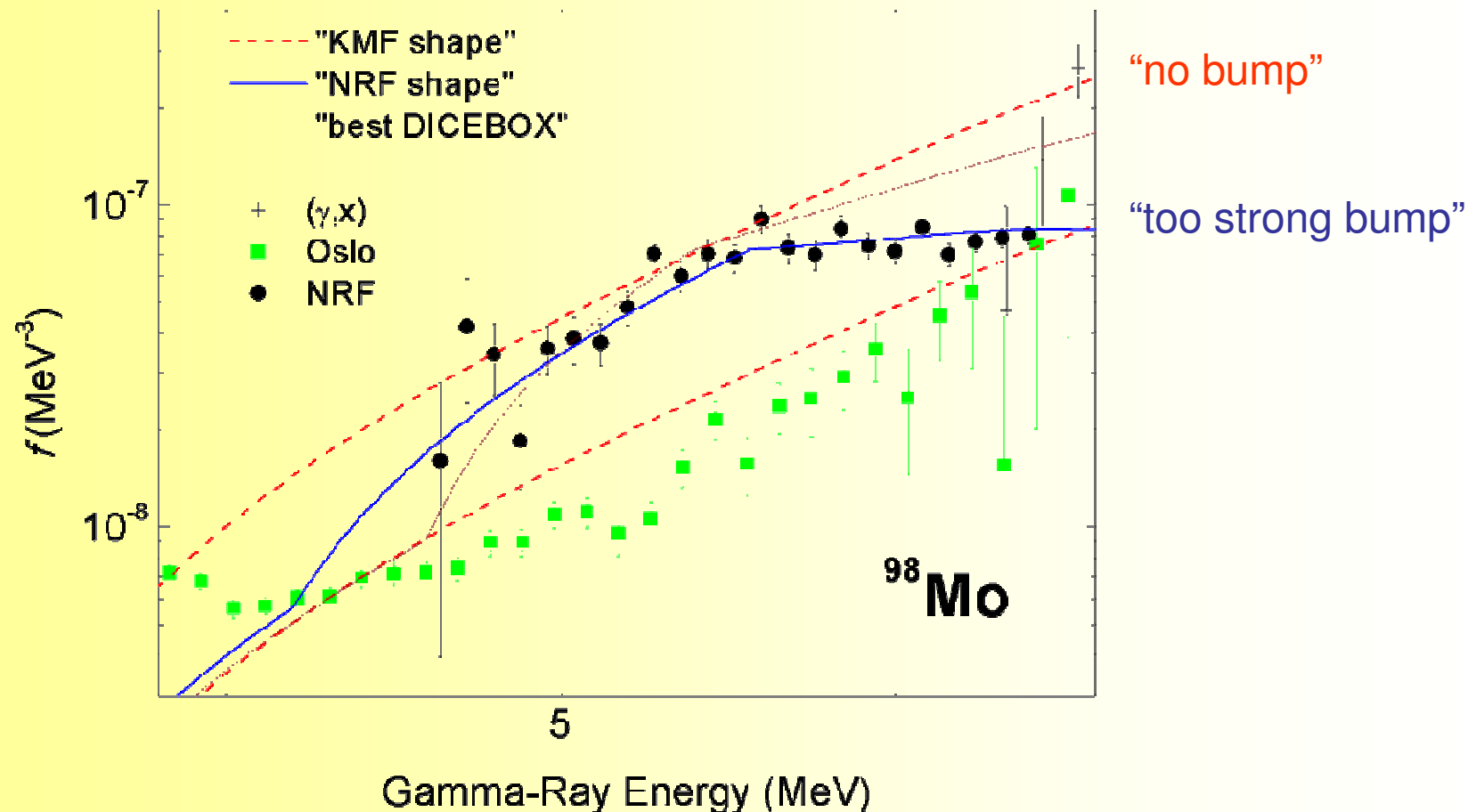


# NRF with beam from “bremsstrahlung”

- Better agreement between experimental data and simulations can be achieved

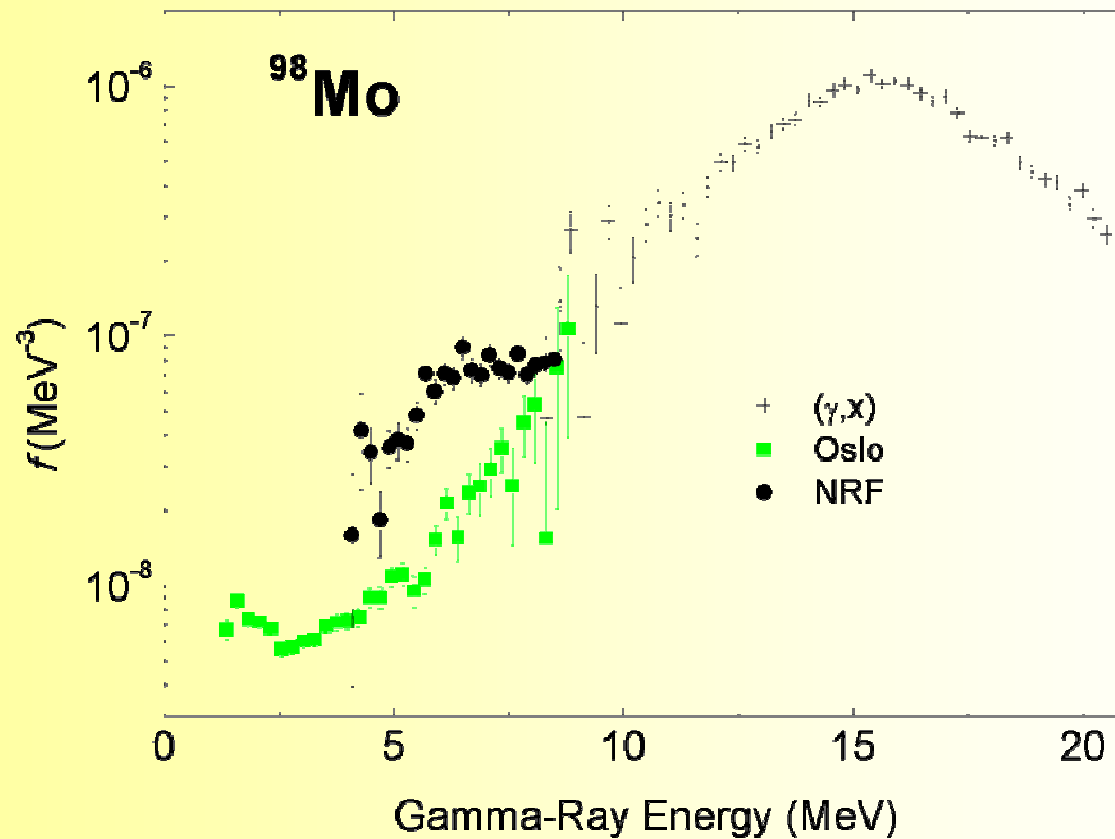


# NRF with beam from “bremsstrahlung”



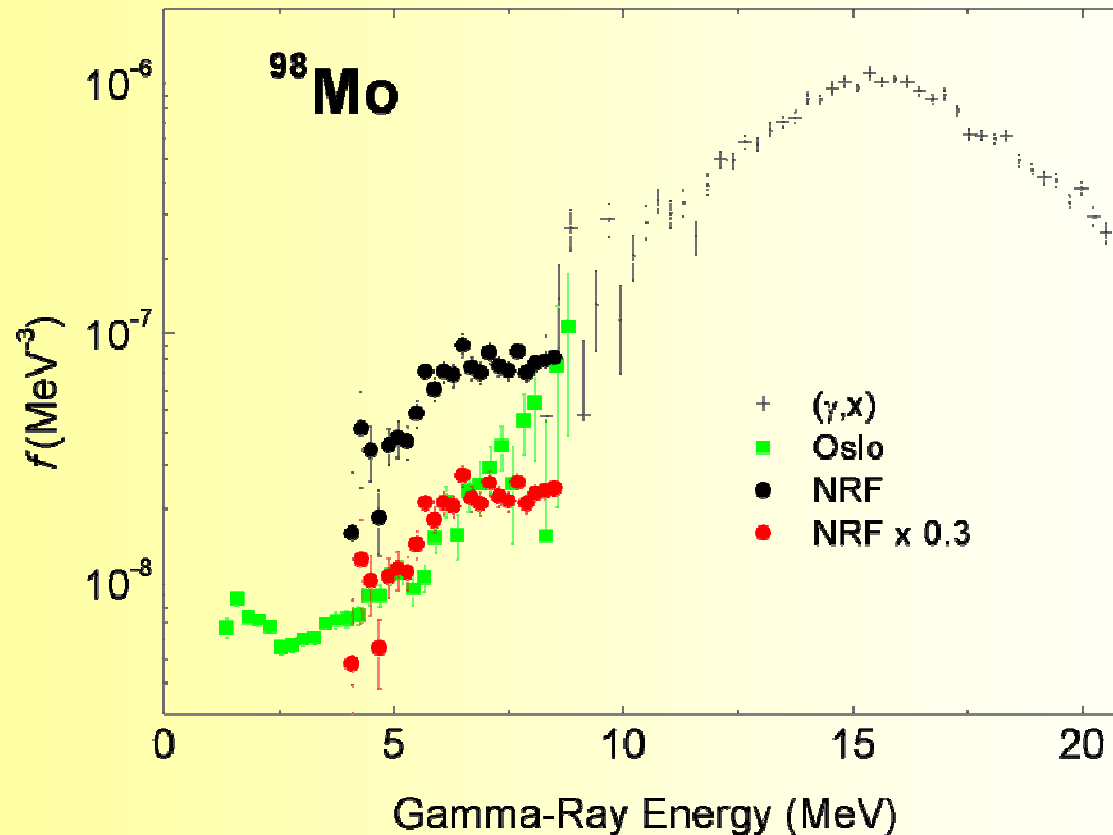
May such a difference occur due to non-validity of Brink hypothesis for the pygmy resonance?

# And a “wild” speculation



Are the data really that different?

# And a “wild” speculation

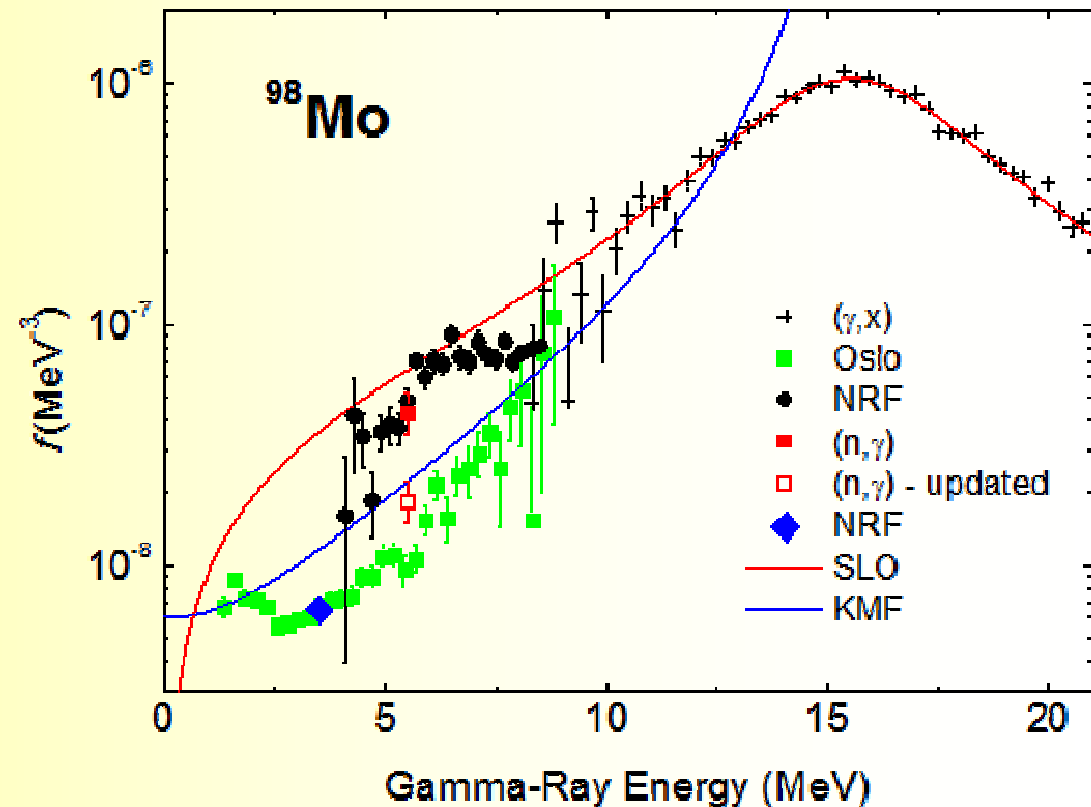


But this would induce other problems

- total radiation width of neutron resonances
- absolute value of PSF near  $S_n$  from ( $\gamma, \gamma'$ )

# Conclusions

- Our understanding of PSF is far from desired
- Each of the discussed methods may be “incorrect”
- Additional information on PSFs and validity of Brink hypothesis is needed



# Invitation

**Compound Nuclear Reactions (CNR\*11)**  
**Prague, September 19-23, 2011**

