

## Problem sheet 6

Plasma Physics course  
TU Dresden  
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### Question 1:

In the limit of  $T_i \ll T_e$  the ion-acoustic wave has the dispersion relation:

$$\omega(k) = \frac{\omega_{pi} \lambda_{De} k}{(1 + k^2 \lambda_{De}^2)^{1/2}}$$

- Derive an expression for the phase velocity  $v_\phi(k)$  and the group velocity  $v_g(k)$  as a function of the wave number  $k$ .
- Discuss the result with respect to “acoustic behavior” at  $k\lambda_{De} \ll 1$ .

### Question 2:

The ionospheric F-layer has a plasma density of  $n = 10^{12} \text{ m}^{-3}$  and consist of mainly  $\text{O}^+$  ions.

- What is the Alfvén speed at a typical magnetic field of  $B = 3 \times 10^{-5} \text{ T}$ ?
- Compare this result with the ion sound speed at a temperature  $T_e = T_i = 3000 \text{ K}$ .