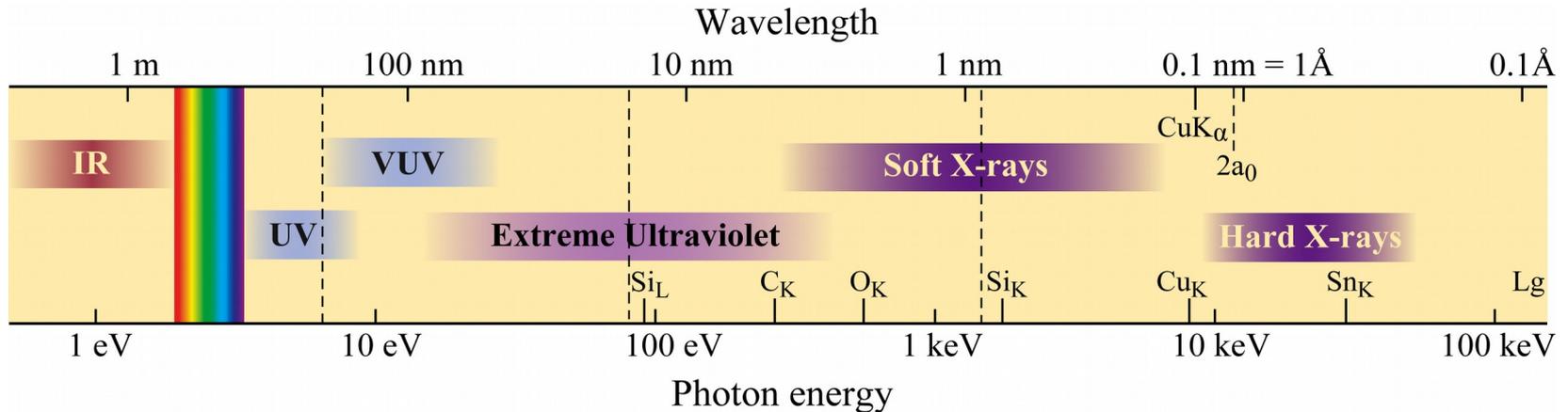




Introduction to Synchrotron Radiation

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The short wavelength region of the electromagnetic spectrum



- Elemental and chemical sensitivity
- Penetrate visibly opaque objects
- See smaller features
- Write smaller patterns

Ch 01 F01 Feb2017 LG.ai

$$\hbar\omega \cdot \lambda = hc = 1239.842 \text{ eV nm}$$

$$n = 1 - \delta + i\beta \quad \delta, \beta \ll 1$$

Broadly tunable radiation is needed to probe the primary (n = 1 & n = 2) resonances of the elements



Periodic Table of the Elements

| Group IA | | | | | | | | | | | | | | | | | | | | | | VIII |
|---------------------------------------|---------------------------------------|--|--|---------------------------------------|---|---------------------------------------|---------------------------------------|---|---|--|--|---------------------------------------|--|--|--|---|--|--|--|--|--|------------------------------------|
| 1 | 2 | | | | | | | | | | | | | | | | | | | | | 10 |
| 1.0079 1 H Hydrogen | | | | | | | | | | | | | | | | | | | | | | 4.003 1 He Helium |
| 6.941 3 Li Lithium | 9.012 4 Be Beryllium | | | | | | | | | | | | | | | | | | | | | 20.180 10 Ne Neon |
| 22.990 11 Na Sodium | 24.31 12 Mg Magnesium | | | | | | | | | | | | | | | | | | | | | 39.948 18 Ar Argon |
| 39.098 19 K Potassium | 40.08 20 Ca Calcium | 44.96 21 Sc Scandium | 47.88 22 Ti Titanium | 50.94 23 V Vanadium | 52.00 24 Cr Chromium | 54.94 25 Mn Manganese | 55.85 26 Fe Iron | 58.93 27 Co Cobalt | 58.69 28 Ni Nickel | 63.55 29 Cu Copper | 65.39 30 Zn Zinc | 69.72 31 Ga Gallium | 72.61 32 Ge Germanium | 74.92 33 As Arsenic | 78.96 34 Se Selenium | 79.904 35 Br Bromine | 83.80 36 Kr Krypton | | | | | |
| 85.47 37 Rb Rubidium | 87.62 38 Sr Strontium | 88.91 39 Y Yttrium | 91.22 40 Zr Zirconium | 92.91 41 Nb Niobium | 95.94 42 Mo Molybdenum | 98 43 Tc Technetium | 101.1 44 Ru Ruthenium | 102.91 45 Rh Rhodium | 106.4 46 Pd Palladium | 107.87 47 Ag Silver | 112.41 48 Cd Cadmium | 114.82 49 In Indium | 118.71 50 Sn Tin | 121.76 51 Sb Antimony | 127.60 52 Te Tellurium | 126.90 53 I Iodine | 131.29 54 Xe Xenon | | | | | |
| 132.91 55 Cs Cesium | 137.33 56 Ba Barium | 138.91 57 La Lanthanum | 178.49 72 Hf Hafnium | 180.95 73 Ta Tantalum | 183.85 74 W Tungsten | 186.21 75 Re Rhenium | 190.2 76 Os Osmium | 192.2 77 Ir Iridium | 195.08 78 Pt Platinum | 197.0 79 Au Gold | 200.59 80 Hg Mercury | 204.38 81 Tl Thallium | 207.2 82 Pb Lead | 208.98 83 Bi Bismuth | (209) 84 Po Polonium | (210) 85 At Astatine | (222) 86 Rn Radon | | | | | |
| (223) 87 Fr Francium | (226) 88 Ra Radium | (227) 89 Ac Actinium | (267) 104 Rf Rutherfordium | (268) 105 Db Dubnium | (271) 106 Sg Seaborgium | (272) 107 Bh Bohrium | (270) 108 Hs Hassium | (276) 109 Mt Meitnerium | (281) 110 Ds Darmstadtium | (280) 111 Rg Roentgenium | (285) 112 Cn Copernicium | (286) 113 Nh Nihonium | (289) 114 Fl Flerovium | (289) 115 Mc Moscovium | (293) 116 Lv Livermorium | (294) 117 Ts Tennessine | (294) 118 Og Oganesson | | | | | |

Key

- Atomic number
- Atomic weight
- Density (g/cm³)
- Concentration (10²²atoms/cm³)
- Nearest neighbor (Å)
- Name
- Oxidation states (Bold most stable)
- Solid
- Gas
- Liquid
- Synthetically prepared
- Symbol
- Electron configuration

Example: **14** 28.09 **Si**
[Ne]3s²3p²
Silicon

References: International Tables for X-ray Crystallography (Reidel, London, 1983) (Ref. 33) and J.R. De Laeter and K.G. Heumann (Ref. 34, 1991); NIST Sept. 2014).

Lanthanide series

| | | | | | | | | | | | | | |
|--|--|---|---|---|--|---|--|---|---|--|---|---|--|
| 58 140.12 3.4 6.77 2.91 3.65 [Xe]4f ¹ 5d ¹ 6s ² Ce Cerium | 59 140.91 3.4 6.78 2.90 3.64 [Xe]4f ³ 6s ² Pr Praseodymium | 60 144.24 3 7.00 2.92 3.63 [Xe]4f ⁴ 6s ² Nd Neodymium | (145) 61 7.54 3.02 3.59 [Xe]4f ⁶ 6s ² Pm Promethium | 150.36 3.2 7.02 2.08 3.97 [Xe]4f ⁶ 6s ² Sm Samarium | 152.0 3.2 5.25 2.08 3.97 [Xe]4f ⁷ 6s ² Eu Europium | 157.25 3 7.87 3.01 3.58 [Xe]4f ⁷ 5d ¹ 6s ² Gd Gadolinium | 158.93 3.4 8.27 3.13 3.53 [Xe]4f ⁷ 6s ² Tb Terbium | 162.50 3 8.80 3.16 3.51 [Xe]4f ⁹ 6s ² Dy Dysprosium | 164.93 3 9.04 3.26 3.47 [Xe]4f ¹⁰ 6s ² Ho Holmium | 167.26 3 9.33 3.26 3.45 [Xe]4f ¹² 6s ² Er Erbium | 168.93 3.2 9.33 2.42 3.88 [Xe]4f ¹³ 6s ² Tm Thulium | 173.04 3.2 6.97 2.42 3.43 [Xe]4f ¹⁴ 6s ² Yb Ytterbium | 174.97 3 9.84 3.39 3.43 [Xe]4f ¹⁴ 5d ¹ 6s ² Lu Lutetium |
|--|--|---|---|---|--|---|--|---|---|--|---|---|--|

Actinide series

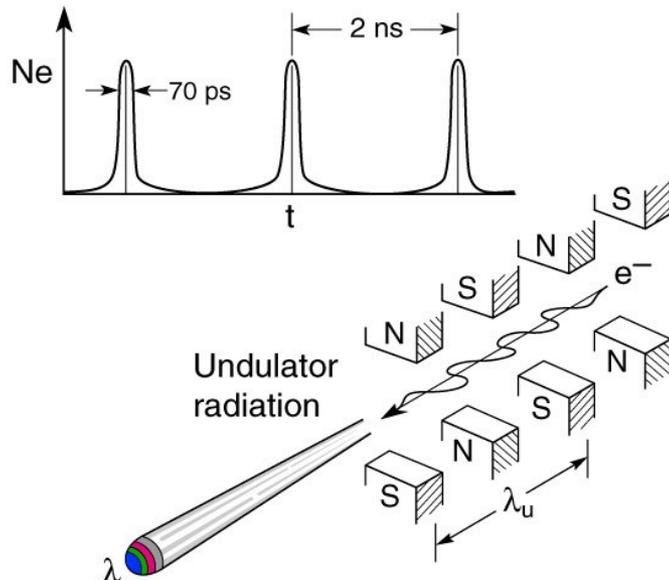
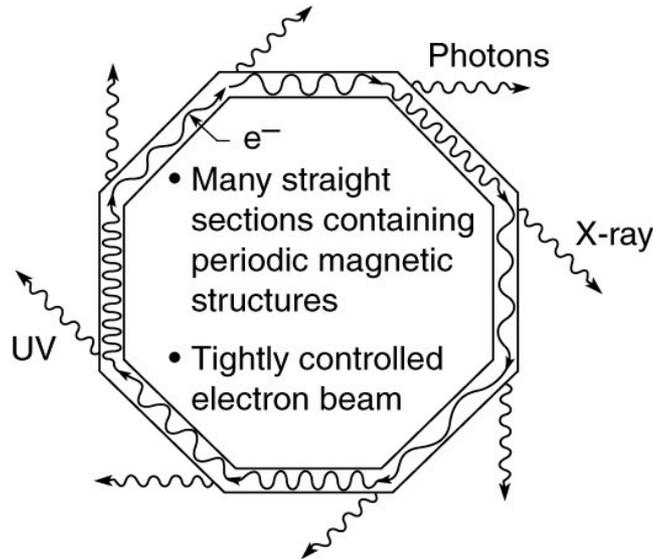
| | | | | | | | | | | | | | |
|---|--|--|--|--|--|---|--|---|---|--|--|---|---|
| 90 232.04 4 11.7 3.04 3.60 [Rn]6d ² 7s ² Th Thorium | 91 231.04 5.4 15.4 4.01 3.21 [Rn]5f ¹ 6d ¹ 7s ² Pa Protactinium | 92 238.03 6.5,4,3 19.1 4.82 2.75 [Rn]5f ³ 6d ¹ 7s ² U Uranium | (237) 93 20.5 4.82 5.20 [Rn]5f ⁴ 6d ¹ 7s ² Np Neptunium | (244) 94 19.8 4.89 [Rn]5f ⁶ 7s ² Pu Plutonium | (243) 95 11.9 2.94 3.61 [Rn]5f ⁷ 7s ² Am Americium | (247) 96 [Rn]5f ⁷ 6d ¹ 7s ² Cm Curium | (247) 97 [Rn]5f ⁷ 7s ² Bk Berkelium | (285) 98 [Rn]5f ¹⁰ 7s ² Cf Californium | (252) 99 [Rn]5f ¹¹ 7s ² Es Einsteinium | (257) 100 [Rn]5f ¹² 7s ² Fm Fermium | (258) 101 [Rn]5f ¹³ 7s ² Md Mendelevium | (259) 102 [Rn]5f ¹⁴ 7s ² No Nobelium | (262) 103 [Rn]5f ¹⁴ 6d ¹ 7s ² Lr Lawrencium |
|---|--|--|--|--|--|---|--|---|---|--|--|---|---|

Electron binding energies, in electron volts (eV), for the elements in their natural forms

| Element | K 1s | L ₁ 2s | L ₂ 2p _{1/2} | L ₃ 2p _{3/2} | M ₁ 3s | M ₂ 3p _{1/2} | M ₃ 3p _{3/2} | M ₄ 3d _{3/2} | M ₅ 3d _{5/2} | N ₁ 4s | N ₂ 4p _{1/2} | N ₃ 4p _{3/2} |
|---------|---------------------|---------------------|----------------------------------|----------------------------------|--------------------|----------------------------------|----------------------------------|----------------------------------|----------------------------------|-------------------|----------------------------------|----------------------------------|
| 1 H | 13.6 | | | | | | | | | | | |
| 2 He | 24.6 ^b | | | | | | | | | | | |
| 3 Li | 54.7 ^b | | | | | | | | | | | |
| 4 Be | 111.5 ^b | | | | | | | | | | | |
| 5 B | 188 ^b | | | | | | | | | | | |
| 6 C | 284.2 ^b | | | | | | | | | | | |
| 7 N | 409.9 ^b | 37.3 ^b | | | | | | | | | | |
| 8 O | 543.1 ^b | 41.6 ^b | | | | | | | | | | |
| 9 F | 696.7 ^b | | | | | | | | | | | |
| 10 Ne | 870.2 ^b | 48.5 ^b | 21.7 ^b | 21.6 ^b | | | | | | | | |
| 11 Na | 1070.8 ^c | 63.5 ^c | 30.4 ^c | 30.5 ^c | | | | | | | | |
| 12 Mg | 1303.0 ^c | 88.6 ^b | 49.6 ^c | 49.2 ^c | | | | | | | | |
| 13 Al | 1559.6 | 117.8 ^b | 72.9 ^b | 72.5 ^b | | | | | | | | |
| 14 Si | 1838.9 | 149.7 ^b | 99.8 ^b | 99.2 ^b | | | | | | | | |
| 15 P | 2145.5 | 189 ^b | 136 ^b | 135 ^b | | | | | | | | |
| 16 S | 2472 | 230.9 ^b | 163.6 ^b | 162.5 ^b | | | | | | | | |
| 17 Cl | 2822.4 | 270.2 ^b | 202 ^b | 200 ^b | | | | | | | | |
| 18 Ar | 3205.9 ^b | 326.3 ^b | 250.6 ^b | 248.4 ^b | 29.3 ^b | 15.9 ^b | 15.7 ^b | | | | | |
| 19 K | 3608.4 ^b | 378.6 ^b | 297.3 ^b | 294.6 ^b | 34.8 ^b | 18.3 ^b | 18.3 ^b | | | | | |
| 20 Ca | 4038.5 ^b | 438.4 ^c | 349.7 ^c | 346.2 ^c | 44.3 ^c | 25.4 ^c | 25.4 ^c | | | | | |
| 21 Sc | 4492.8 | 498.0 ^b | 403.6 ^b | 398.7 ^b | 51.1 ^b | 28.3 ^b | 28.3 ^b | | | | | |
| 22 Ti | 4966.4 | 560.9 ^c | 461.2 ^c | 453.8 ^c | 58.7 ^c | 32.6 ^c | 32.6 ^c | | | | | |
| 23 V | 5465.1 | 626.7 ^c | 519.8 ^c | 512.1 ^c | 66.3 ^c | 37.2 ^c | 37.2 ^c | | | | | |
| 24 Cr | 5989.2 | 695.7 ^c | 583.8 ^c | 574.1 ^c | 74.1 ^c | 42.2 ^c | 42.2 ^c | | | | | |
| 25 Mn | 6539.0 | 769.1 ^c | 649.9 ^c | 638.7 ^c | 82.3 ^c | 47.2 ^c | 47.2 ^c | | | | | |
| 26 Fe | 7112.0 | 844.6 ^c | 719.9 ^c | 706.8 ^c | 91.3 ^c | 52.7 ^c | 52.7 ^c | | | | | |
| 27 Co | 7708.9 | 925.1 ^c | 793.3 ^c | 778.1 ^c | 101.0 ^c | 58.9 ^c | 58.9 ^c | | | | | |
| 28 Ni | 8332.8 | 1008.6 ^c | 870.0 ^c | 852.7 ^c | 110.8 ^c | 68.0 ^c | 66.2 ^c | | | | | |
| 29 Cu | 8978.9 | 1096.7 ^c | 952.3 ^c | 932.5 ^c | 122.5 ^c | 77.3 ^c | 75.1 ^c | | | | | |
| 30 Zn | 9658.6 | 1196.2 ^b | 1044.9 ^b | 1021.8 ^b | 139.8 ^b | 91.4 ^b | 88.6 ^b | 10.2 ^b | 10.1 ^b | | | |
| 31 Ga | 10367.1 | 1299.0 ^b | 1143.2 ^c | 1116.4 ^c | 159.5 ^c | 103.5 ^c | 103.5 ^c | 18.7 ^c | 18.7 ^c | | | |
| 32 Ge | 11103.1 | 1414.6 ^b | 1248.1 ^b | 1217.0 ^b | 180.1 ^b | 124.9 ^b | 120.8 ^b | 29.0 ^b | 29.0 ^b | | | |
| 33 As | 11866.7 | 1527.0 ^b | 1359.1 ^b | 1323.6 ^b | 204.7 ^b | 146.2 ^b | 141.2 ^b | 41.7 ^b | 41.7 ^b | | | |
| 34 Se | 12657.8 | 1652.0 ^b | 1474.3 ^b | 1433.9 ^b | 229.6 ^b | 166.5 ^b | 160.7 ^b | 55.5 ^b | 54.6 ^b | | | |
| 35 Br | 13473.7 | 1782.0 ^b | 1596.0 ^b | 1549.9 ^b | 257 ^b | 189 ^b | 182 ^b | 70 ^b | 69 ^b | | | |
| 36 Kr | 14325.6 | 1921.0 | 1730.9 ^b | 1678.4 ^b | 292.8 ^b | 222.2 ^b | 214.4 ^b | 95.0 ^b | 93.8 ^b | 27.5 ^b | 14.1 ^b | 14.1 ^b |
| 37 Rb | 15199.7 | 2065.1 | 1863.9 | 1804.4 | 326.7 ^b | 248.7 ^b | 239.1 ^b | 113.0 ^b | 112 ^b | 30.5 ^b | 16.3 ^b | 15.3 ^b |
| 38 Sr | 16104.6 | 2216.3 | 2006.8 | 1939.6 | 358.7 ^c | 280.3 ^c | 270.0 ^c | 136.0 ^c | 134.2 ^c | 38.9 ^c | 20.3 ^c | 20.3 ^c |
| 39 Y | 17038.4 | 2372.5 | 2155.5 | 2080.0 | 392.0 ^b | 310.6 ^b | 298.8 ^b | 157.7 ^c | 155.8 ^c | 43.8 ^b | 24.4 ^b | 23.1 ^b |
| 40 Zr | 17997.6 | 2531.6 | 2306.7 | 2222.3 | 430.3 ^c | 343.5 ^c | 329.8 ^c | 181.1 ^c | 178.8 ^c | 50.6 ^c | 28.5 ^c | 27.7 ^c |
| 41 Nb | 18985.6 | 2697.7 | 2464.7 | 2370.5 | 466.6 ^c | 376.1 ^c | 360.6 ^c | 205.0 ^c | 202.3 ^c | 56.4 ^c | 32.6 ^c | 30.8 ^c |
| 42 Mo | 19999.5 | 2865.5 | 2625.1 | 2520.2 | 506.3 ^c | 411.6 ^c | 394.0 ^c | 231.1 ^c | 227.9 ^c | 63.2 ^c | 37.6 ^c | 35.5 ^c |
| 43 Tc | 21044.0 | 3042.5 | 2793.2 | 2676.9 | 544 ^b | 445 ^b | 425 ^b | 257 ^b | 253 ^b | 68 ^b | 39 ^c | 39 ^b |
| 44 Ru | 22117.2 | 3224.0 | 2966.9 | 2837.9 | 586.2 ^c | 483.5 ^c | 461.4 ^c | 284.2 ^c | 280.0 ^c | 75.0 ^c | 46.5 ^c | 43.2 ^c |
| 45 Rh | 23219.9 | 3411.9 | 3146.1 | 3003.8 | 628.1 ^c | 521.3 ^c | 496.5 ^c | 311.9 ^c | 307.2 ^c | 81.4 ^b | 50.5 ^c | 47.3 ^c |
| 46 Pd | 24350.3 | 3604.3 | 3330.3 | 3173.3 | 671.6 ^c | 559.9 ^c | 532.3 ^c | 340.5 ^c | 335.2 ^c | 87.6 ^b | 55.7 ^c | 50.9 ^c |
| 47 Ag | 25514.0 | 3805.8 | 3523.7 | 3351.1 | 719.0 ^c | 603.8 ^c | 573.0 ^c | 374.0 ^c | 368.0 ^c | 97.0 ^c | 63.7 ^c | 58.3 ^c |

www.cxro.lbl.gov

Synchrotron radiation



Bending Magnet:

$$\hbar\omega_c = \frac{3e\hbar B\gamma^2}{2m} \quad (5.7)$$

Wiggler:

$$\hbar\omega_c = \frac{3e\hbar B\gamma^2}{2m} \quad (5.80)$$

$$n_c = \frac{3K}{4} \left(1 + \frac{K^2}{2}\right) \quad (5.82)$$

$$P_T = \frac{\pi e K^2 \gamma^2 I N}{3\epsilon_0 \lambda_u} \quad (5.85)$$

Undulator:

$$\lambda = \frac{\lambda_u}{2\gamma^2} \left(1 + \frac{K^2}{2} + \gamma^2\theta^2\right) \quad (5.28)$$

$$K = \frac{eB_0\lambda_u}{2\pi mc} \quad (5.18)$$

$$\theta_{\text{cen}} = \frac{1}{\gamma^* \sqrt{N}} \quad (5.15)$$

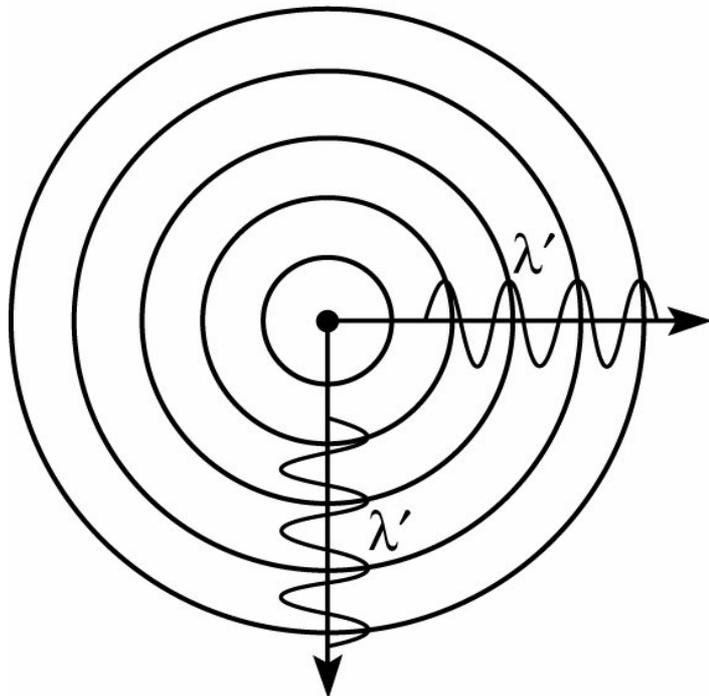
$$\left. \frac{\Delta\lambda}{\lambda} \right|_{\text{cen}} = \frac{1}{N} \quad (5.14)$$

$$\bar{P}_{\text{cen}} = \frac{\pi e \gamma^2 I}{\epsilon_0 \lambda_u} \frac{K^2}{\left(1 + \frac{K^2}{2}\right)^2} [JJ]^2 \quad (5.41)$$

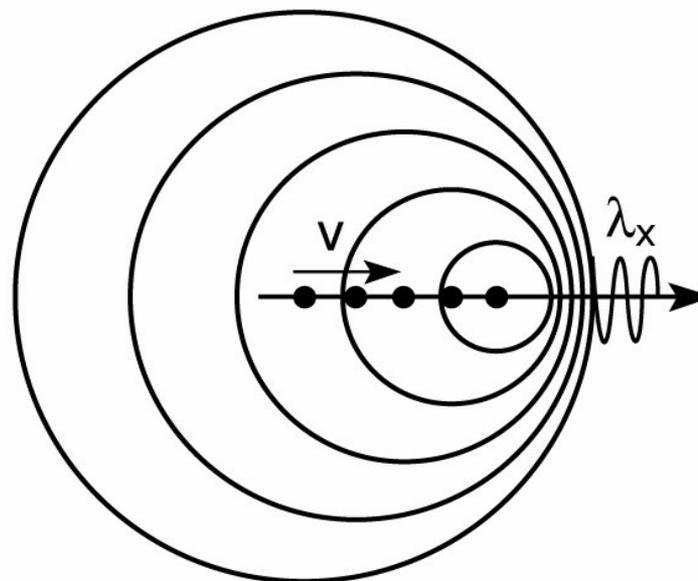
Synchrotron radiation from relativistic electrons



$v \ll c$



$v \lesssim c$



Note: Angle-dependent doppler shift

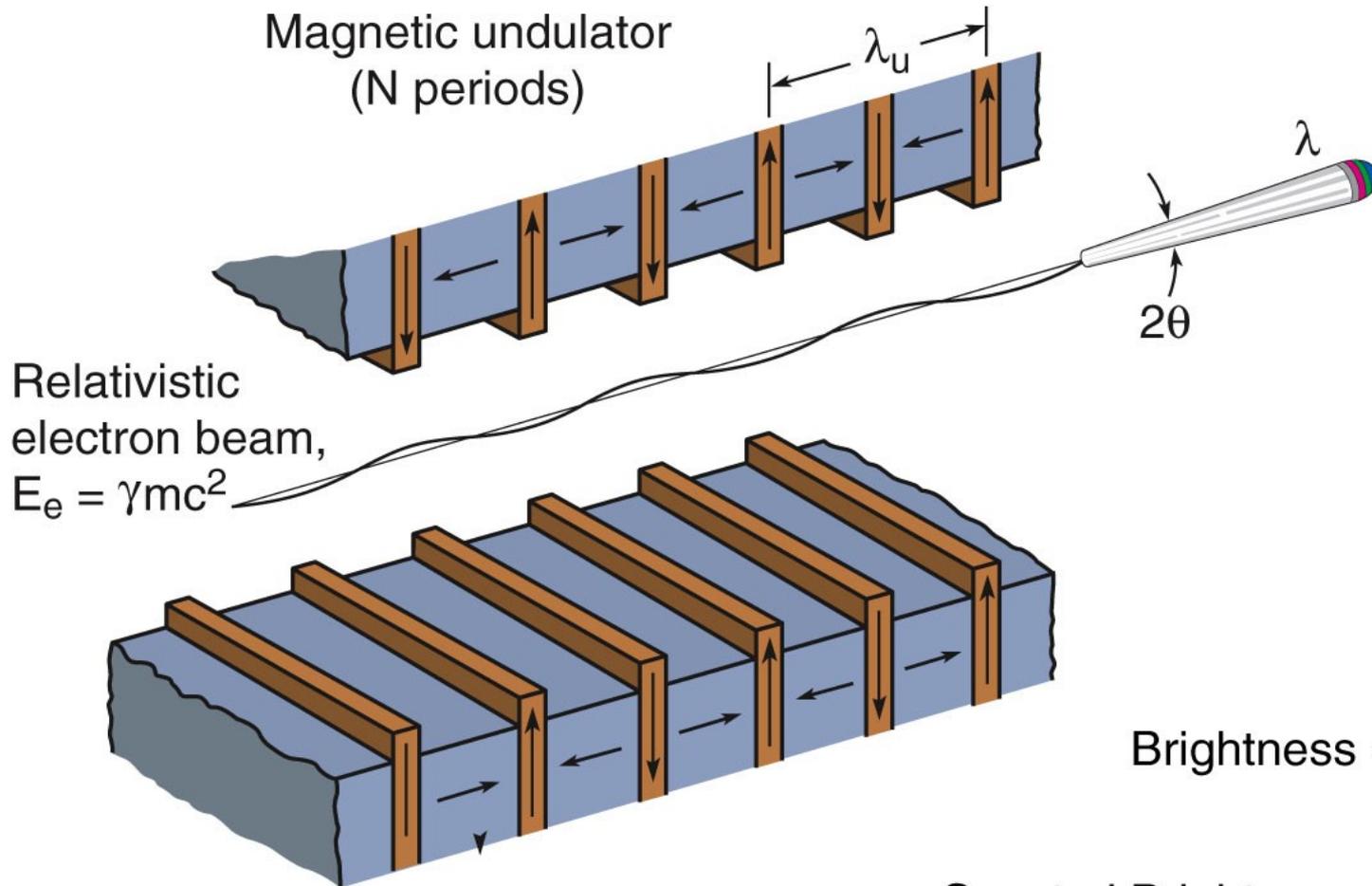
$$\lambda = \lambda' \left(1 - \frac{v}{c} \cos\theta\right)$$

$$\lambda = \lambda' \gamma \left(1 - \frac{v}{c} \cos\theta\right)$$

$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$$

Following John Madey

Undulator radiation from a small electron beam radiating into a narrow forward cone is very bright



$$\lambda \approx \frac{\lambda_u}{2\gamma^2}$$

$$\theta_{\text{cen}} \approx \frac{1}{\gamma \sqrt{N}}$$

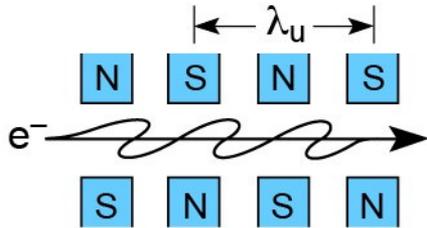
$$\left[\frac{\Delta\lambda}{\lambda} \right]_{\text{cen}} = \frac{1}{N}$$

$$\text{Brightness} = \frac{\text{photon flux}}{(\Delta A) (\Delta\Omega)}$$

$$\text{Spectral Brightness} = \frac{\text{photon flux}}{(\Delta A) (\Delta\Omega) (\Delta\lambda/\lambda)}$$

Undulator radiation

Laboratory Frame of Reference

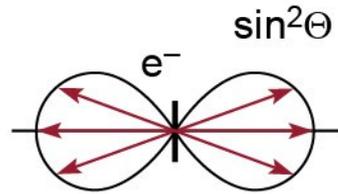


$$E = \gamma mc^2$$

$$\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$$

$N = \#$ periods

Frame of Moving e^-



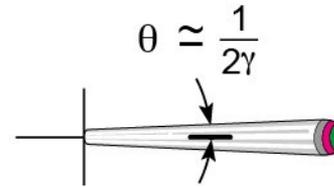
e^- radiates at the Lorentz contracted wavelength:

$$\lambda' = \frac{\lambda_u}{\gamma}$$

Bandwidth:

$$\frac{\lambda'}{\Delta\lambda'} \simeq N$$

Frame of Observer



Doppler shortened wavelength on axis:

$$\lambda = \lambda' \gamma (1 - \beta \cos \theta)$$

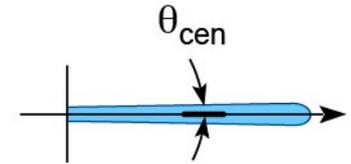
$$\lambda = \frac{\lambda_u}{2\gamma^2} (1 + \gamma^2 \theta^2)$$

Accounting for transverse motion due to the periodic magnetic field:

$$\lambda = \frac{\lambda_u}{2\gamma^2} \left(1 + \frac{K^2}{2} + \gamma^2 \theta^2 \right)$$

where $K = eB_0\lambda_u/2\pi mc$

Following Monochromator



$$\text{For } \frac{\Delta\lambda}{\lambda} \simeq \frac{1}{N}$$

$$\theta_{\text{cen}} \simeq \frac{1}{\gamma \sqrt{N}}$$

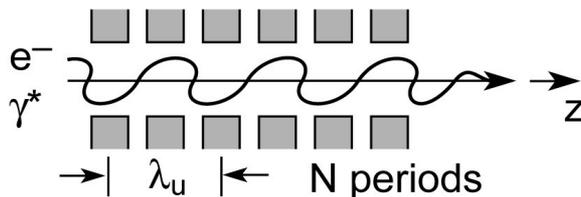
typically

$$\theta_{\text{cen}} \simeq 10\text{-}30 \mu\text{rad}$$

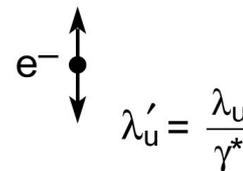
Calculating Power in the Central Radiation Cone: Using the well known “dipole radiation” formula by transforming to the frame of reference moving with the electrons



x, z, t laboratory frame of reference



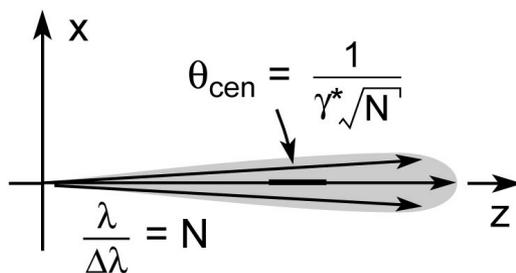
x', z', t' frame of reference moving with the average velocity of the electron



Lorentz transformation

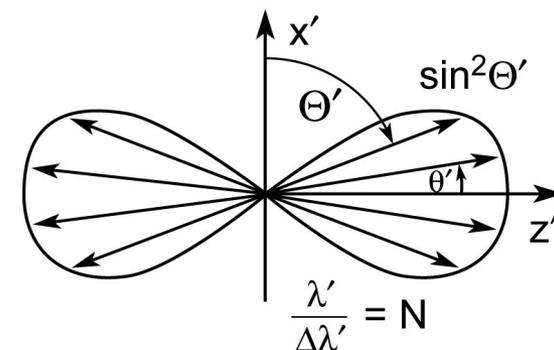
Determine x, z, t motion:

$$\frac{d\mathbf{p}}{dt} = -e (\mathbf{E} + \mathbf{v} \times \mathbf{B})$$



Dipole radiation:

$$\frac{dP'}{d\Omega'} = \frac{e^2 a'^2 \sin^2 \Theta'}{16\pi^2 \epsilon_0 c^3}$$



Lorentz transformation

$$\bar{P}_{\text{cen}} = \frac{\pi e \gamma^2 I}{\epsilon_0 \lambda_u} \frac{K^2}{(1 + K^2/2)^2}$$

$$\frac{dP'}{d\Omega'} = \frac{e^2 c \gamma^2}{4\epsilon_0 \lambda_u^2} \frac{K^2}{(1 + K^2/2)^2} (1 - \sin^2 \theta' \cos^2 \phi') \cos^2 \omega'_u t'$$

Power in the central radiation cone

$$\lambda_x = \frac{\lambda_u}{2\gamma^2} \left(1 + \frac{K^2}{2} + \gamma^2 \theta^2\right)$$

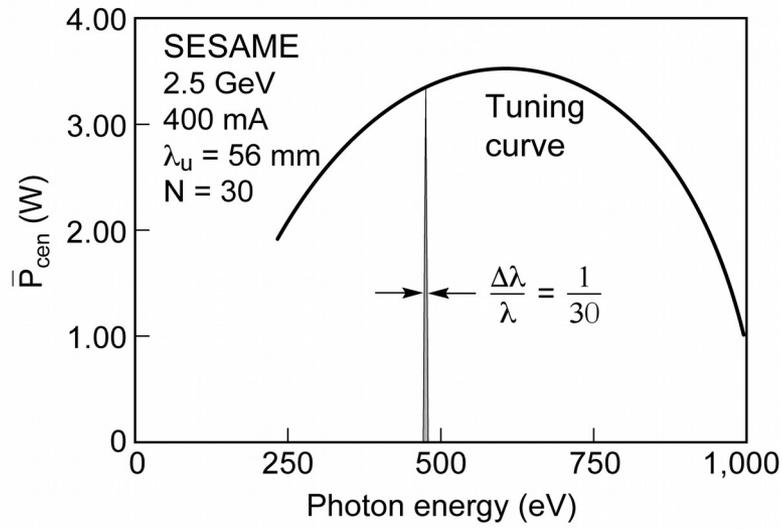
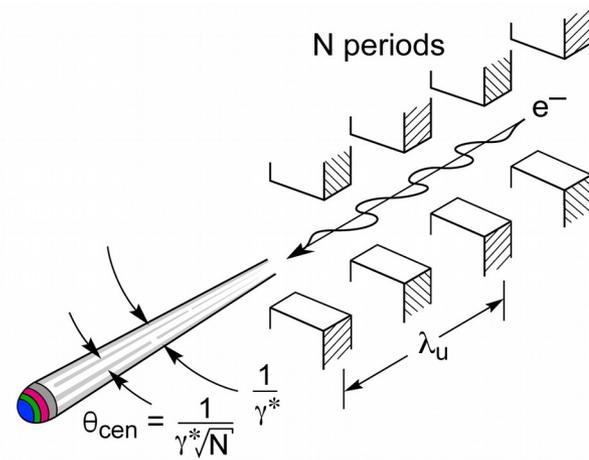
$$\bar{P}_{\text{cen}} = \frac{\pi e \gamma^2 I}{\epsilon_0 \lambda_u} \frac{K^2}{\left(1 + \frac{K^2}{2}\right)^2} [\text{JJ}]^2$$

$$\theta_{\text{cen}} = \frac{1}{\gamma^* \sqrt{N}}$$

$$\left(\frac{\Delta\lambda}{\lambda}\right)_{\text{cen}} = \frac{1}{N}$$

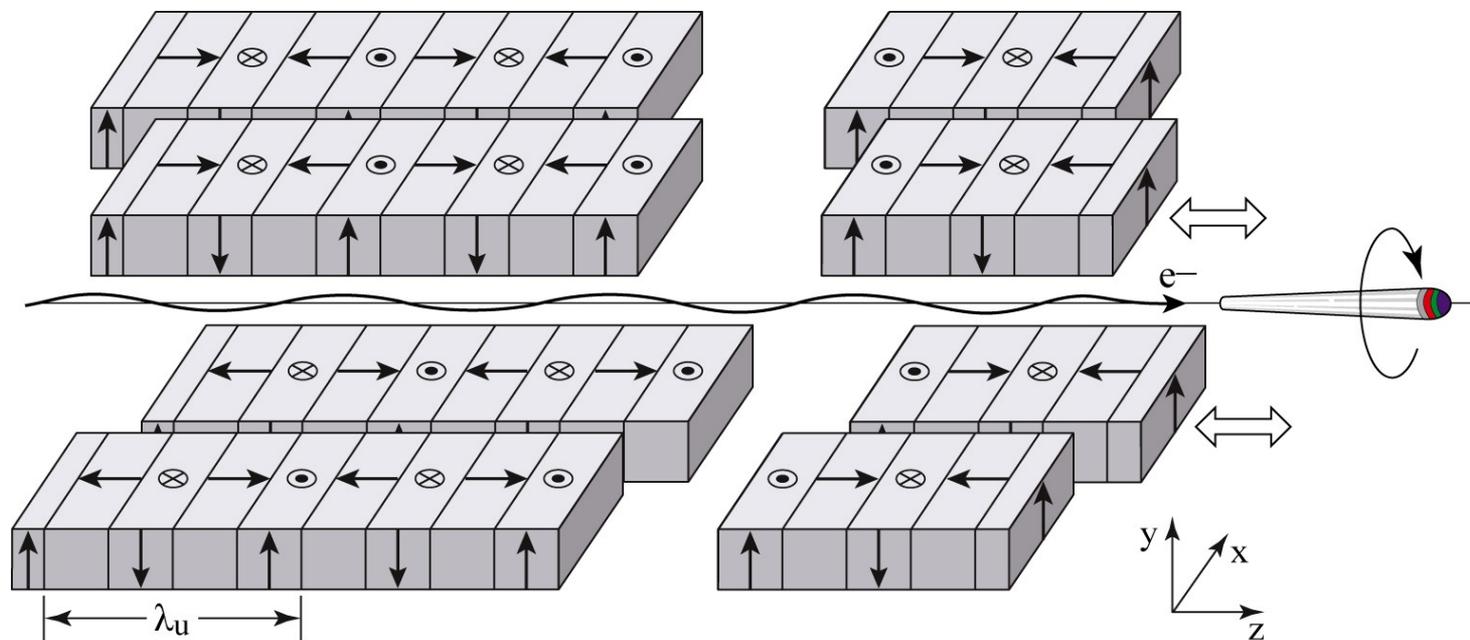
$$K = \frac{eB_0 \lambda_u}{2\pi m_0 c}$$

$$\gamma^* = \gamma / \sqrt{1 + \frac{K^2}{2}}$$



PowerCentralCone_SESAMe.ai

APPLE II Elliptically Polarizing Undulator (EPU)

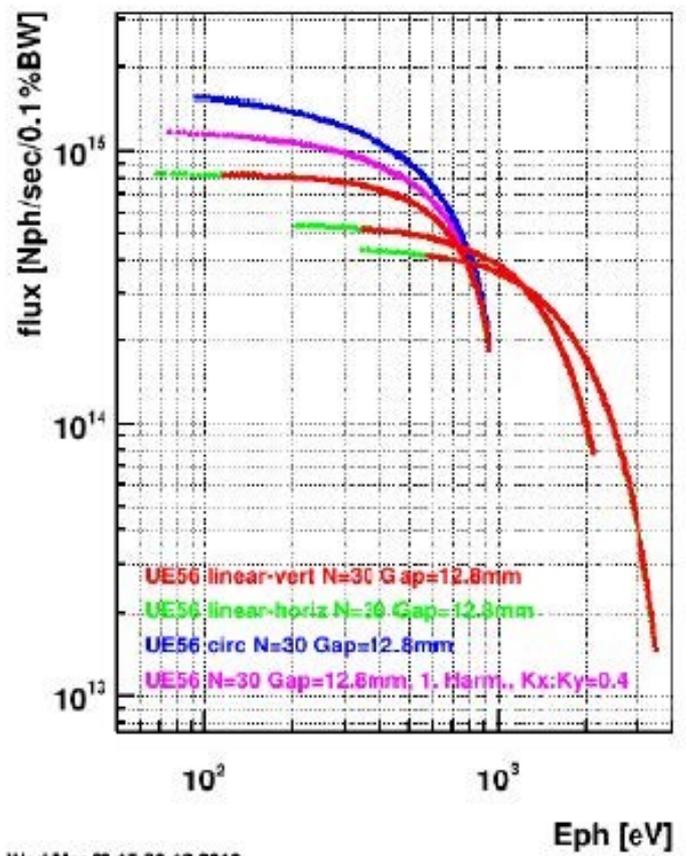




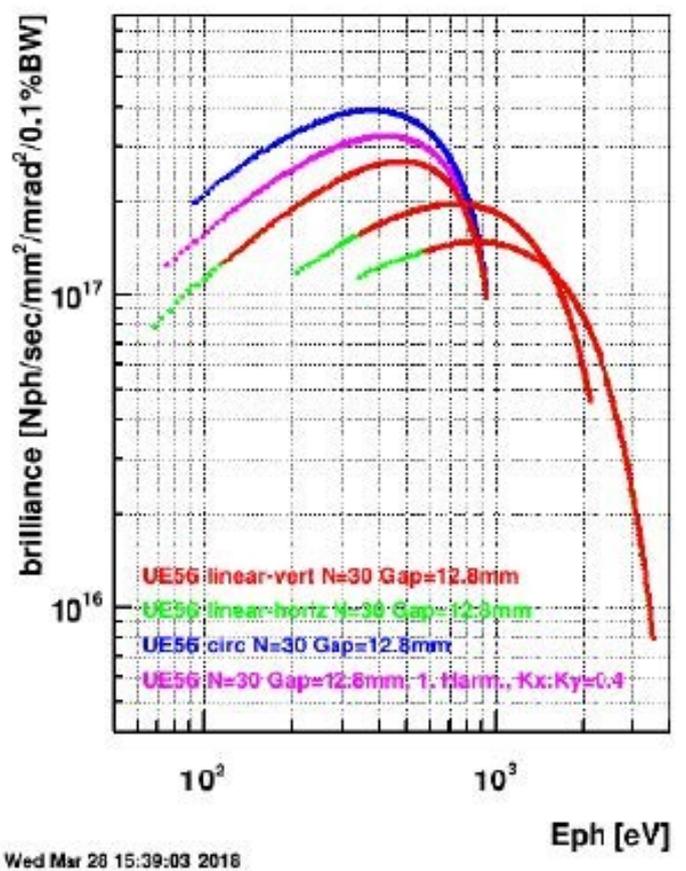
Add Si, C, Fe to both



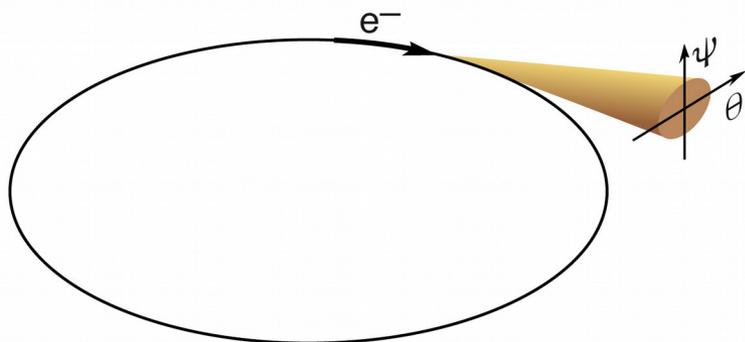
Flux, 2.5 GeV, 400 mA



Brilliance, 2.5 GeV, 400 mA



Bending magnet radiation covers a broad region of the spectrum, including the primary absorption edges of most elements



$$E_c = \hbar\omega_c = \frac{3e\hbar\gamma^2}{2m} \quad (5.7a)$$

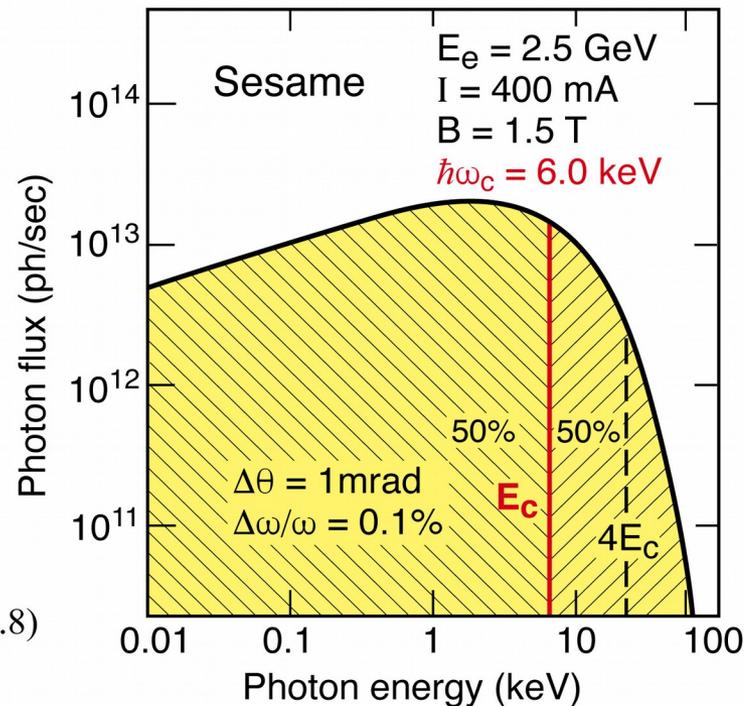
$$E_c[\text{keV}] = 0.6650E_e^2[\text{GeV}]B[\text{T}] \quad (5.7b)$$

$$F_{1\text{mrad}, 0.1\% \text{BW}} = 2.46 \times 10^{13} E_e[\text{GeV}]I[\text{A}]G_1(E/E_c) \text{ ph/sec} \quad (5.8)$$

where $G_1(1) = 0.6514$

- Advantages:
- covers broad spectral range
 - least expensive
 - most accessible

- Disadvantages:
- not as bright as an undulator

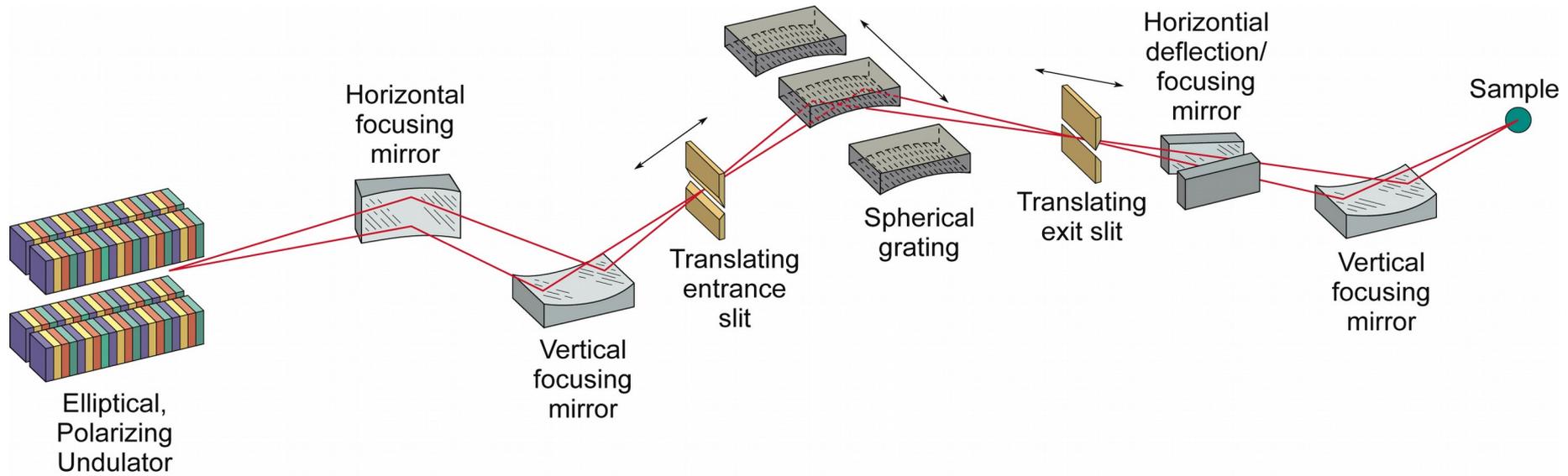


$$E_c = 6 \text{ keV}$$

$$4E_c = 24 \text{ keV}$$

Ch05_F07_Sesame.ai

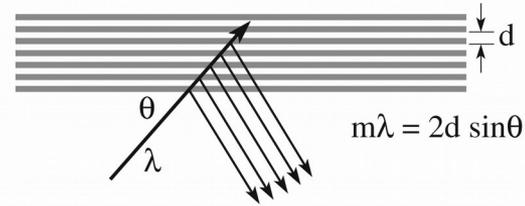
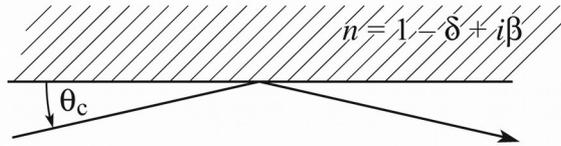
A typical beamline: A monochromator plus glancing incidence optics deliver radiation to the sample



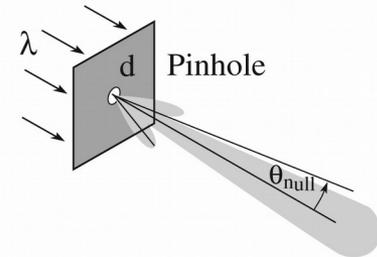
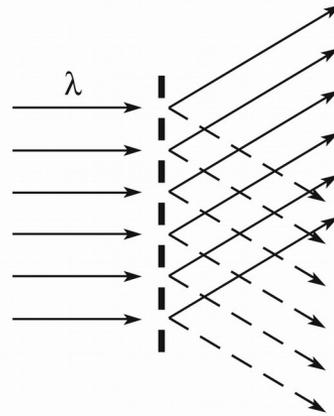
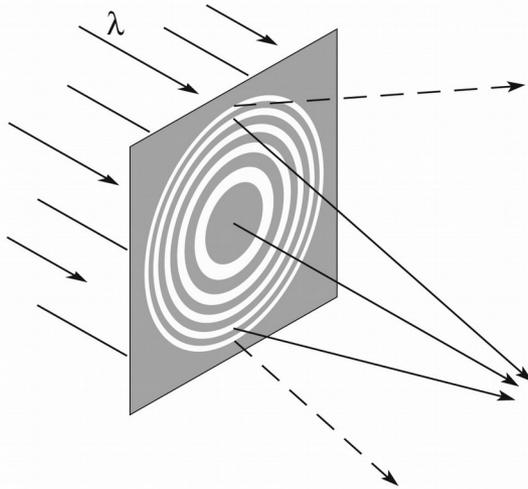
Available Optical Techniques for Soft X-Rays and EUV



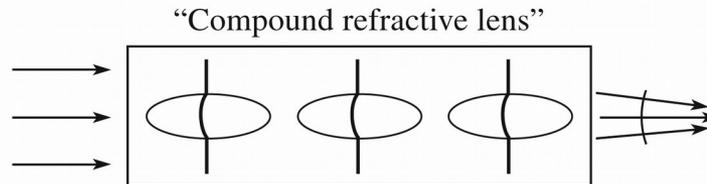
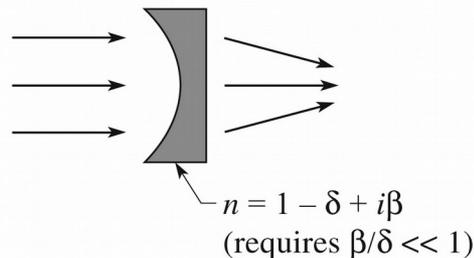
- Reflection (glancing incidence or multilayer coatings)



- Diffraction (zone plates, gratings, pinholes)



- Refraction (only for hard x-rays, > 20 keV)



A. Snigerev et al., *Nature* **384**, 49 (7Nov.1996)

B. Lengeler et al., *J. Appl. Phys.* **84**, 5855 (1Dec.1998)



Refractive index at x-ray wavelengths

Based on a simple, semi-classical oscillator in the presence of an electric field $E = E_0 \cos \omega t$

$$n(\omega) = 1 - \frac{1}{2} \frac{e^2 n_a}{\hbar_0 m} \sum_s \frac{g_s}{(\omega^2 - \omega_s^2) + i\gamma\omega} \quad (3.8)$$

Expressed in terms of atomic scattering factors:

$$n(\omega) = 1 - \frac{n_a r_e \lambda^2}{2\pi} \left[f_1^0(\omega) - i f_2^0(\omega) \right] \quad (3.9)$$

which we can write simply as

$$n(\omega) = 1 - \delta + i\beta \quad (3.12)$$

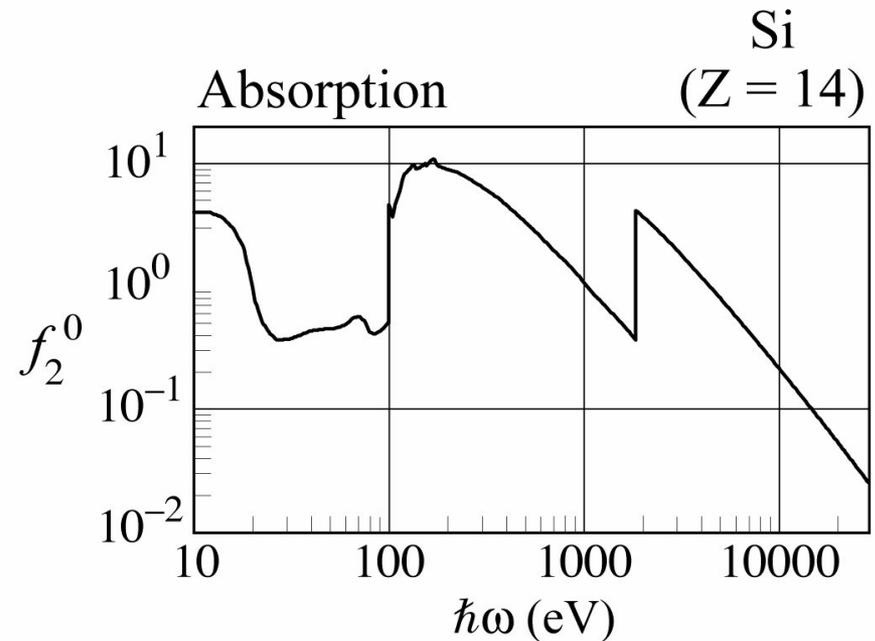
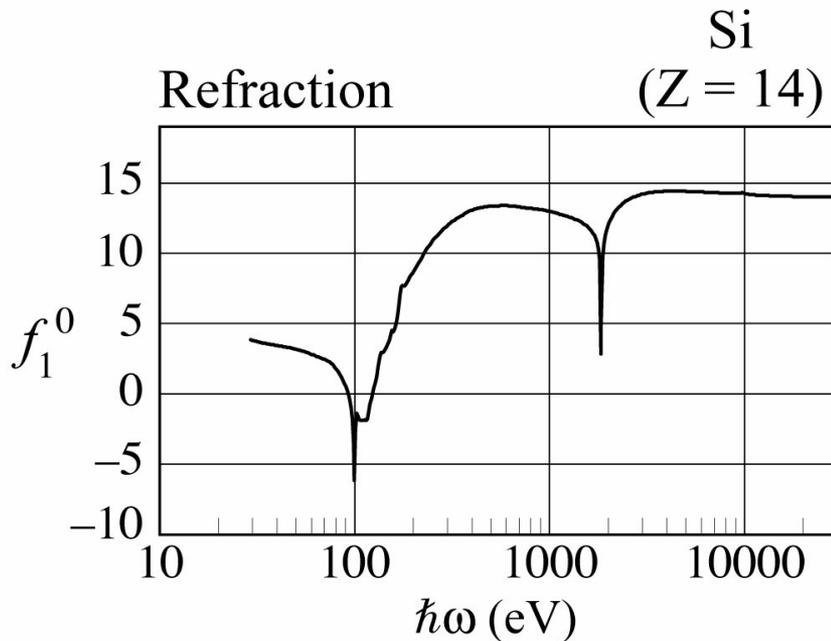


Refractive index at nanometer wavelengths

Refractive Index

$$n = 1 - \delta + i\beta = 1 - \frac{n_a r_e \lambda^2}{2\pi} (f_1^0 - if_2^0)$$

Atomic scattering factors



www.cxro.LBL.gov/optical_constants

ScattngRefracIndex_June2009.ai

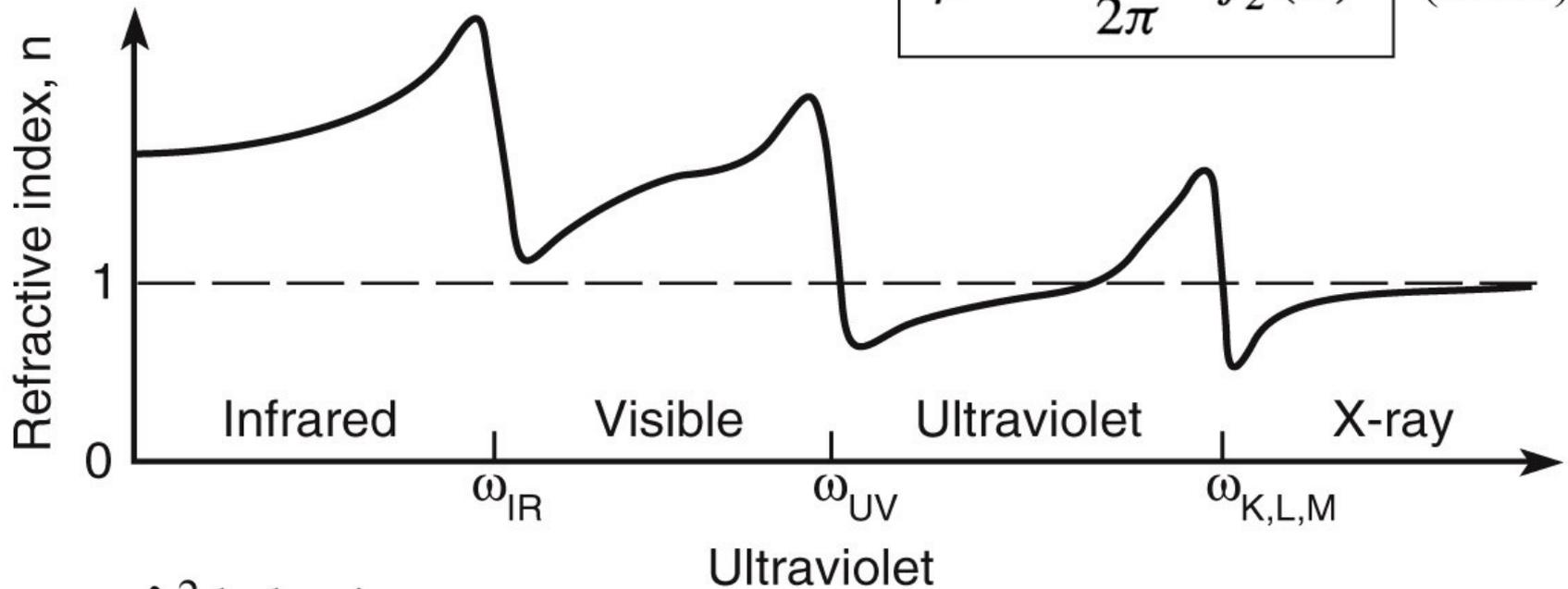
Refractive index from the IR to x-ray spectral region



$$n(\omega) = 1 - \delta + i\beta \quad (3.12)$$

$$\delta = \frac{n_a r_e \lambda^2}{2\pi} f_1^0(\omega) \quad (3.13a)$$

$$\beta = \frac{n_a r_e \lambda^2}{2\pi} f_2^0(\omega) \quad (3.13b)$$



- λ^2 behavior
- δ & $\beta \ll 1$
- δ -crossover



Normal incidence reflection of x-rays is very small

$$R_s = \frac{|\cos \phi - \sqrt{n^2 - \sin^2 \phi}|^2}{|\cos \phi + \sqrt{n^2 - \sin^2 \phi}|^2} \quad (3.49)$$

at $\phi = 0$:

$$R_{s,\perp} = \frac{|1 - n|^2}{|1 + n|^2} = \frac{(1 - n)(1 - n^*)}{(1 + n)(1 + n^*)}$$

For $n = 1 - \delta + i\beta$

$$R_{s,\perp} = \frac{(\delta - i\beta)(\delta + i\beta)}{(2 - \delta + i\beta)(2 - \delta - i\beta)} = \frac{\delta^2 + \beta^2}{(2 - \delta)^2 + \beta^2}$$

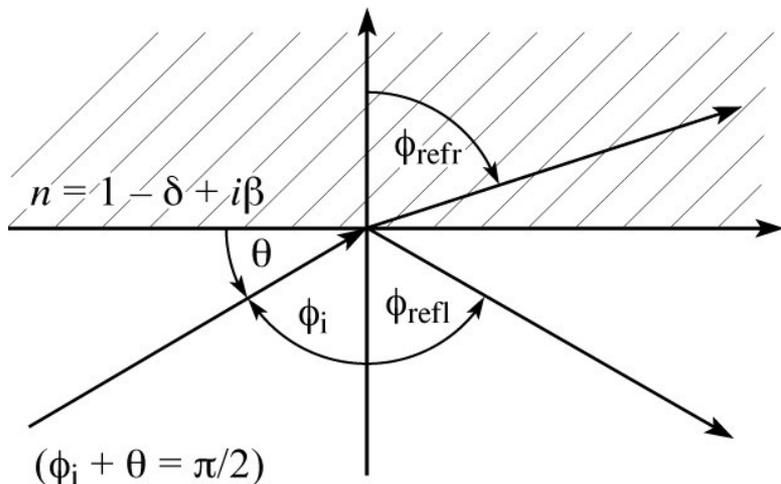
Reflectivity for x-ray and EUV radiation at normal incidence ($\phi = 0$):

$$R_{s,\perp} \simeq \frac{\delta^2 + \beta^2}{4} \quad (3.50)$$

Example: Nickel @ 300 eV (4.13 nm)

| | | | |
|--------------------|--------------------|---|--|
| $f_1^\circ = 17.8$ | $f_2^\circ = 7.70$ | } | $R_\perp = 4.58 \times 10^{-5}$ [@ 300 eV] |
| $\delta = 0.0124$ | $\beta = 0.00538$ | | |
| | | | |

Glancing Incidence Optics



Snell's Law: $\text{Sin } \phi_{\text{refr.}} = \frac{\text{Sin } \phi_i}{n}$

Total external Reflection:

$$\phi_{\text{refr.}} \rightarrow \frac{\pi}{2} \text{ as } \phi_i \rightarrow \phi_{\text{critical}}$$

$$\text{Snell's Law: } 1 = \frac{\text{Sin } \phi_c}{1 - \delta}$$

$$\text{Sin}(90^\circ - \theta_c) = 1 - \delta$$

$$\text{Cos } \theta_c = 1 - \delta$$

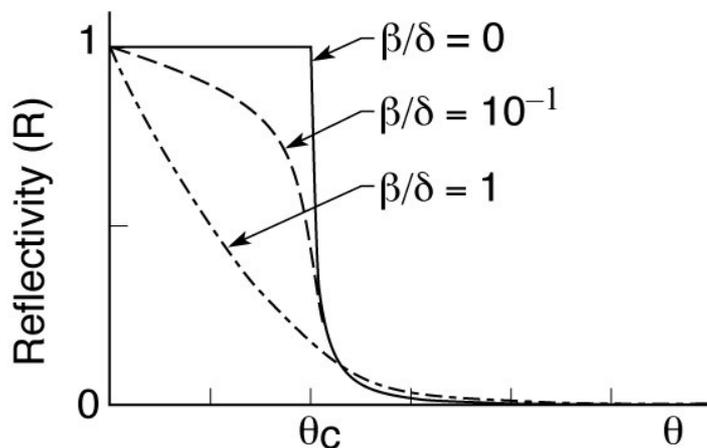
$$1 - \frac{\theta_c^2}{2} = 1 - \delta$$

$$\theta_c = \sqrt{2\delta}$$

For gold at 1 keV

$$\delta = 2.1 \times 10^{-3}$$

$$\theta_c = 3.7^\circ$$



(www.cxro.LBL.gov ;
 “X-ray properties of the elements”
 “X-ray interaction with matter”)

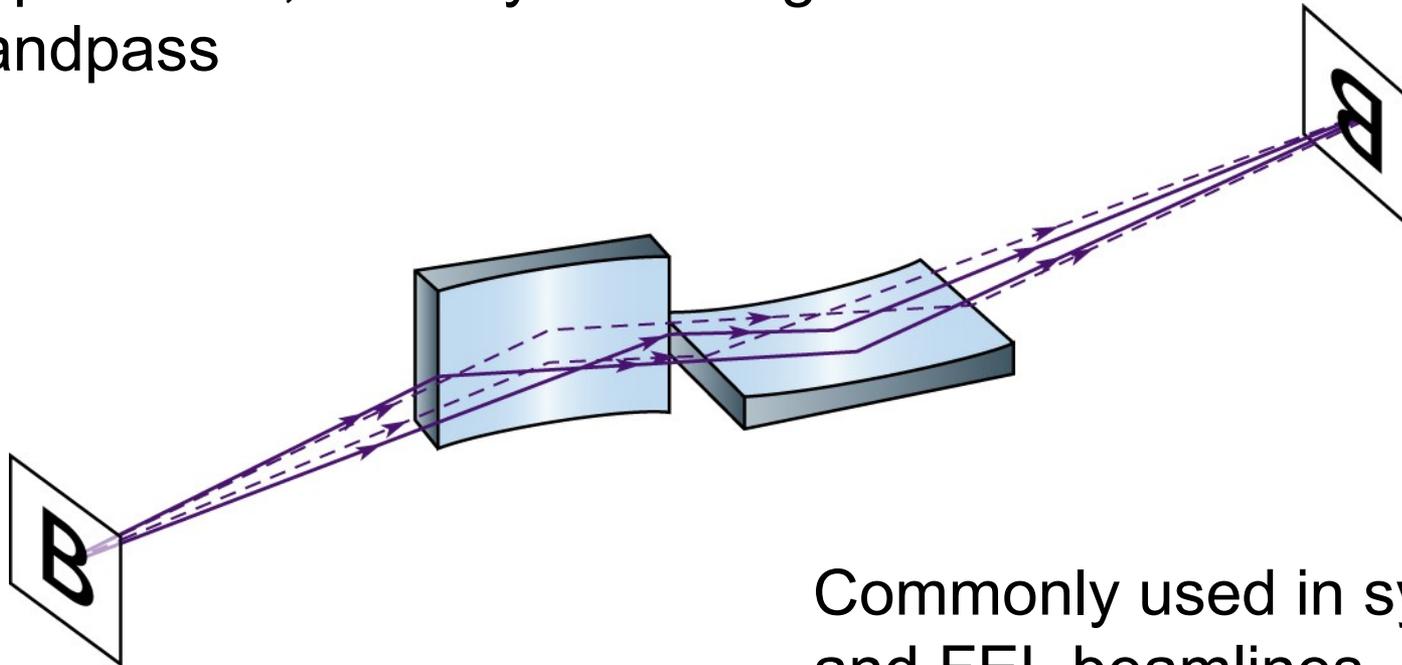
Kirkpatrick-Baez Mirror Pair



Orthogonal mirrors cancel astigmatism

Elliptical surfaces for point to point imaging

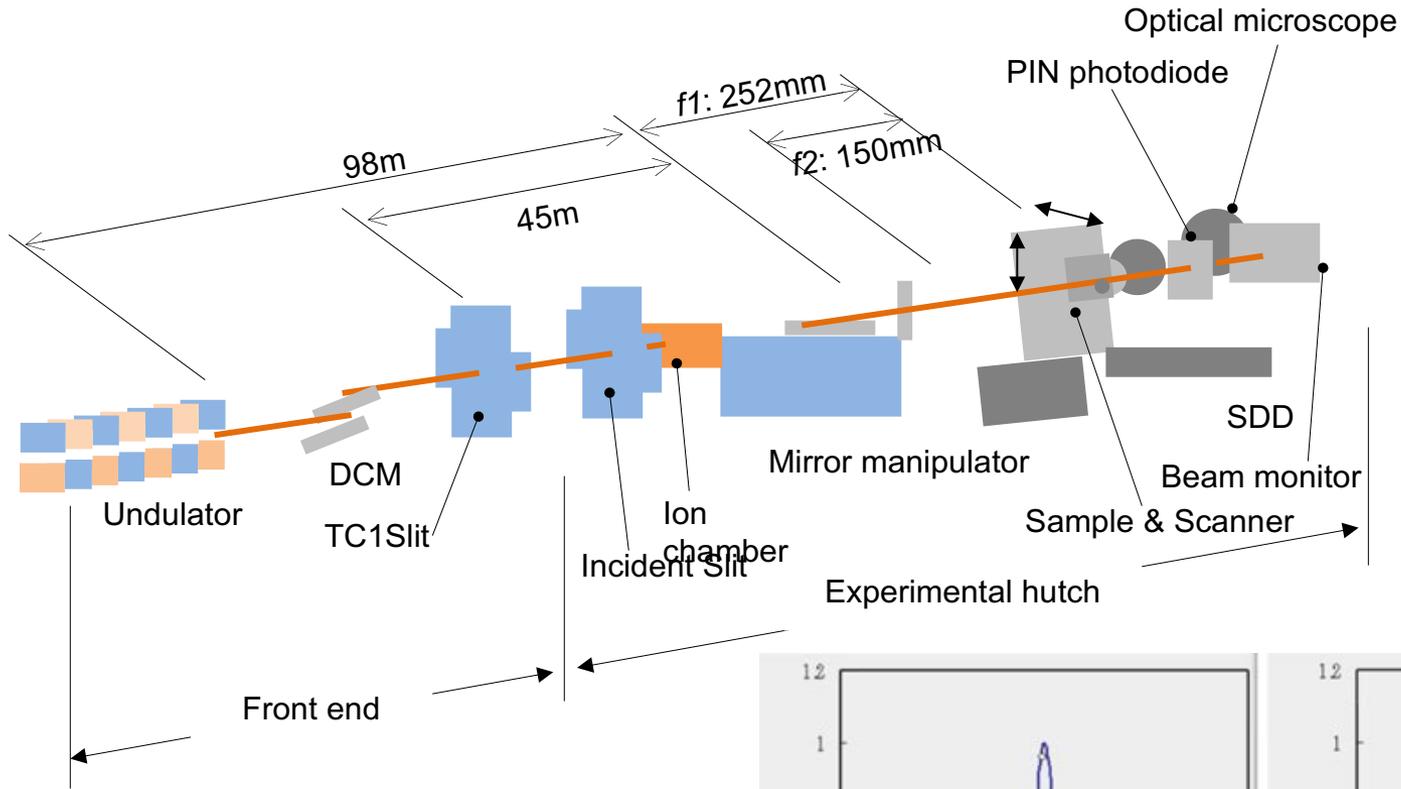
Glancing incidence coatings for broad band applications, multilayer coatings for fixed bandpass



Commonly used in synchrotron and FEL beamlines, and in plasma diagnostics

Courtesy of J. Underwood, LBNL

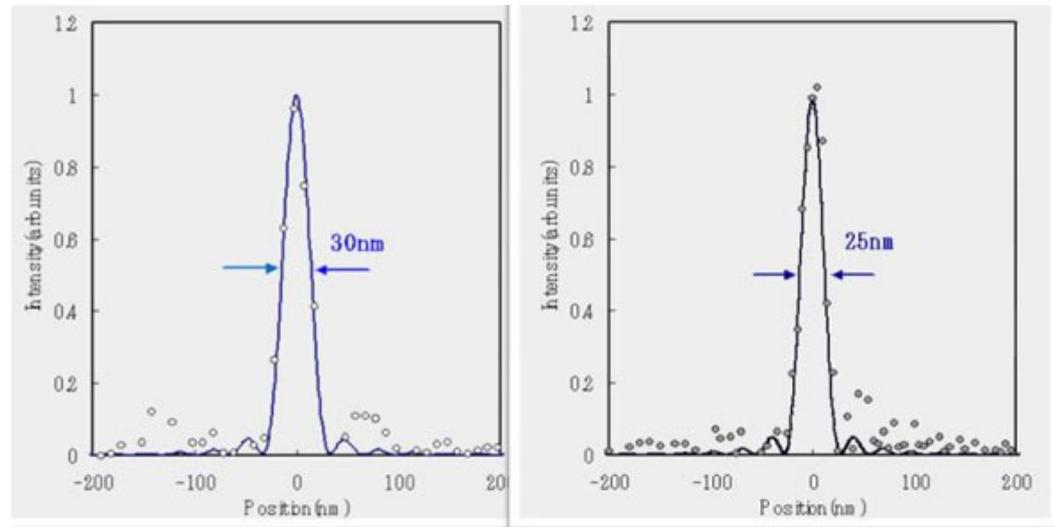
X-ray microprobe at SPring-8



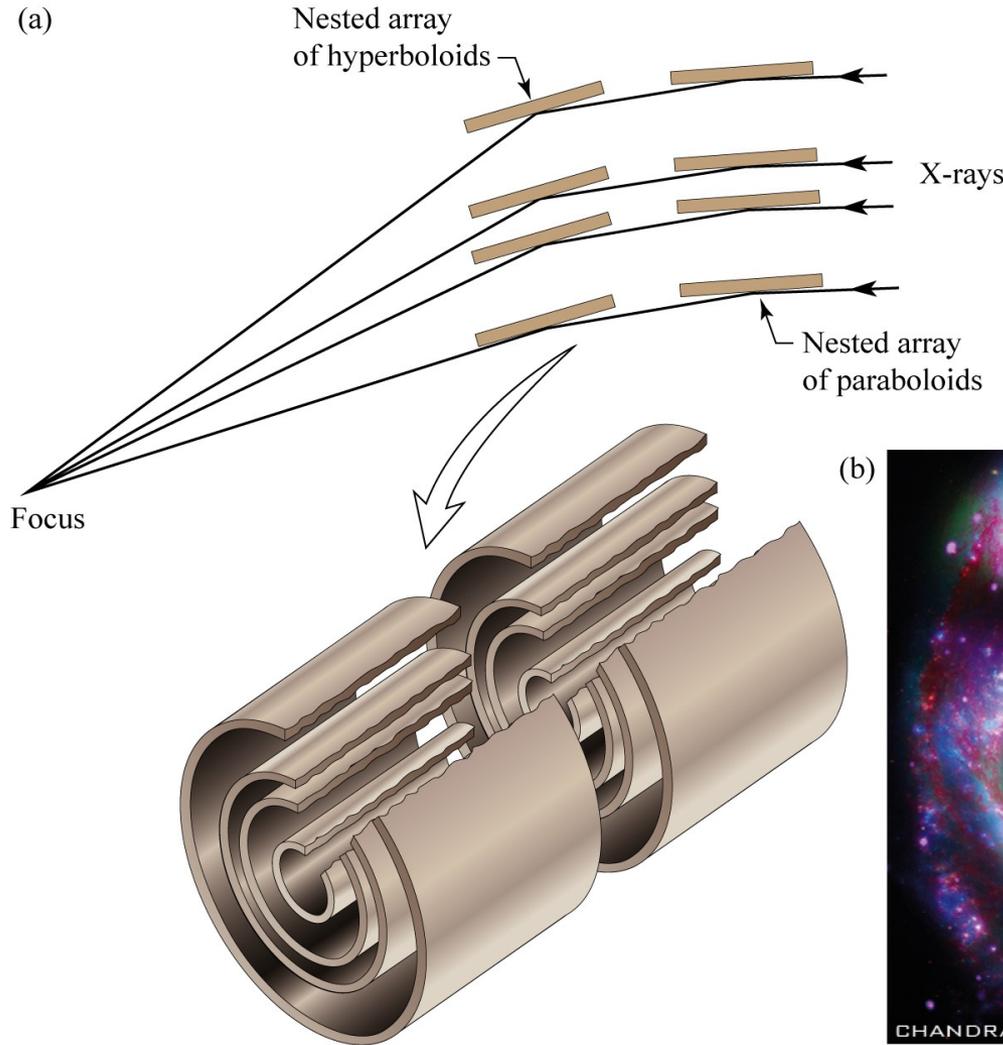
**Now focused
to 7 nm**

S. Matsuyama et al.,
Rev. Sci. Instrum.
77, 103102 (2006)

Courtesy of Professor Kazuto Yamauchi,
Osaka University and Spring-8



Nested pairs of Wolter type 1 reflective x-ray optics for the orbiting Chandra X-ray Observatory



Composite view of the M51 "Whirlpool Galaxy"

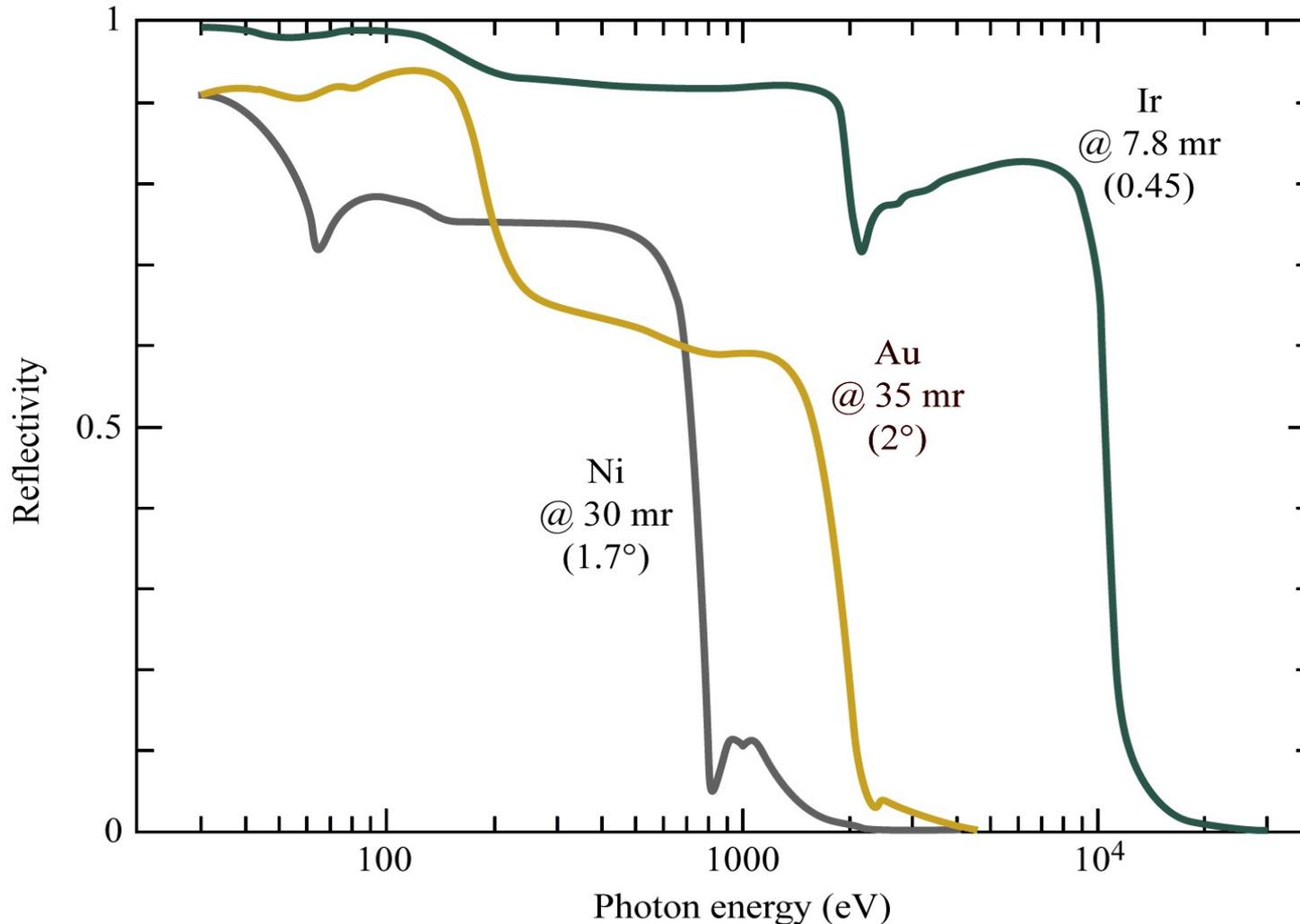


Courtesy of D. Schwartz (Harvard-Smithsonian Center for Astrophysics) and NASA

Single surface mirrors for x-ray astronomy

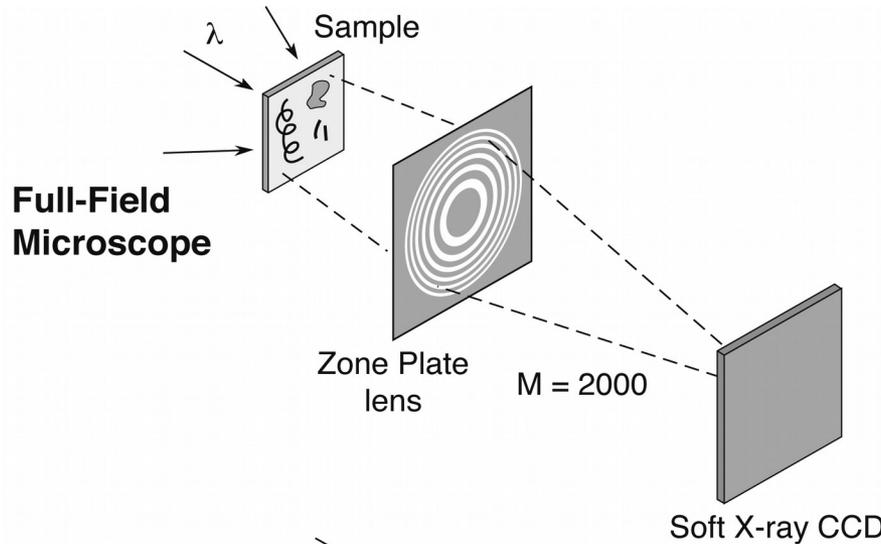


Sharp cutoffs at 700 eV, 2 keV and 10 keV

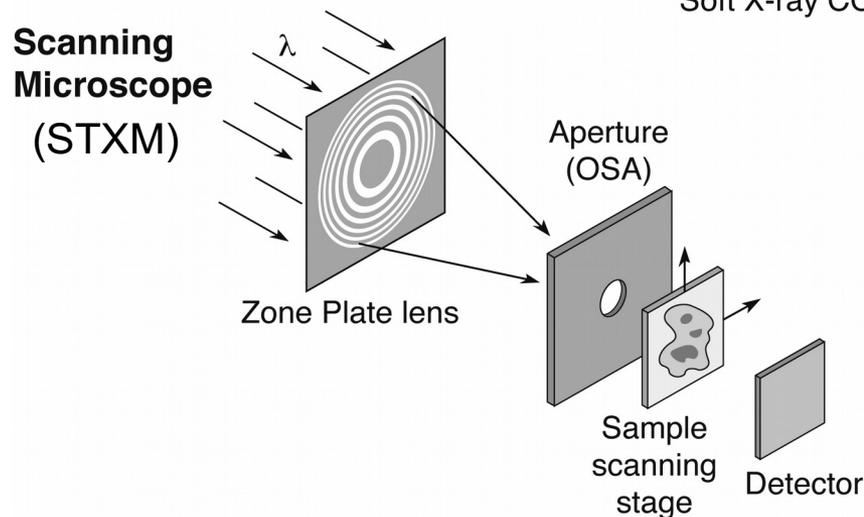


Courtesy of R. Soufli, LLNL, and E. Gullikson, LBL; www.cxro.LBL.gov/ical_constants

Two common zone plate x-ray microscopes



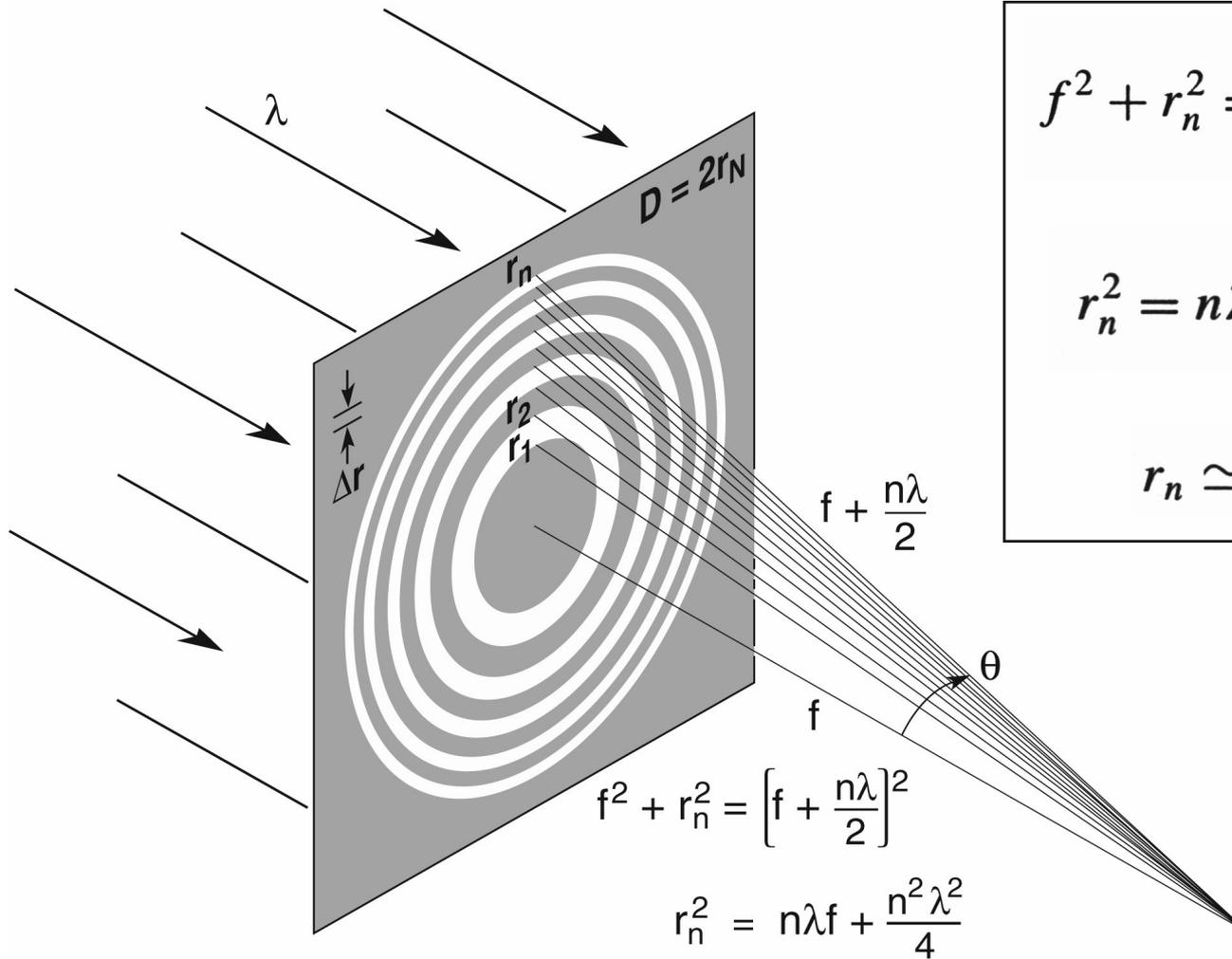
- 10–20 nm spatial resolution
- High spectral resolution
- Seconds exposure time
- Bending magnet, or undulator
- Higher radiation dose
- Flexible sample environment (wet, cryo, labeled magnetic fields, electric fields, cement, ...)



- 10–20 nm spatial resolution
- Least radiation dose
- High spectral resolution
- Requires spatially coherent radiation
- Minutes exposure time
- Flexible sample environment
- Photoemission, fluorescence imaging

Ch09_F21_Feb2017.ai

A Fresnel zone plate lens



$$f^2 + r_n^2 = \left(f + \frac{n\lambda}{2} \right)^2 \quad (9.8)$$

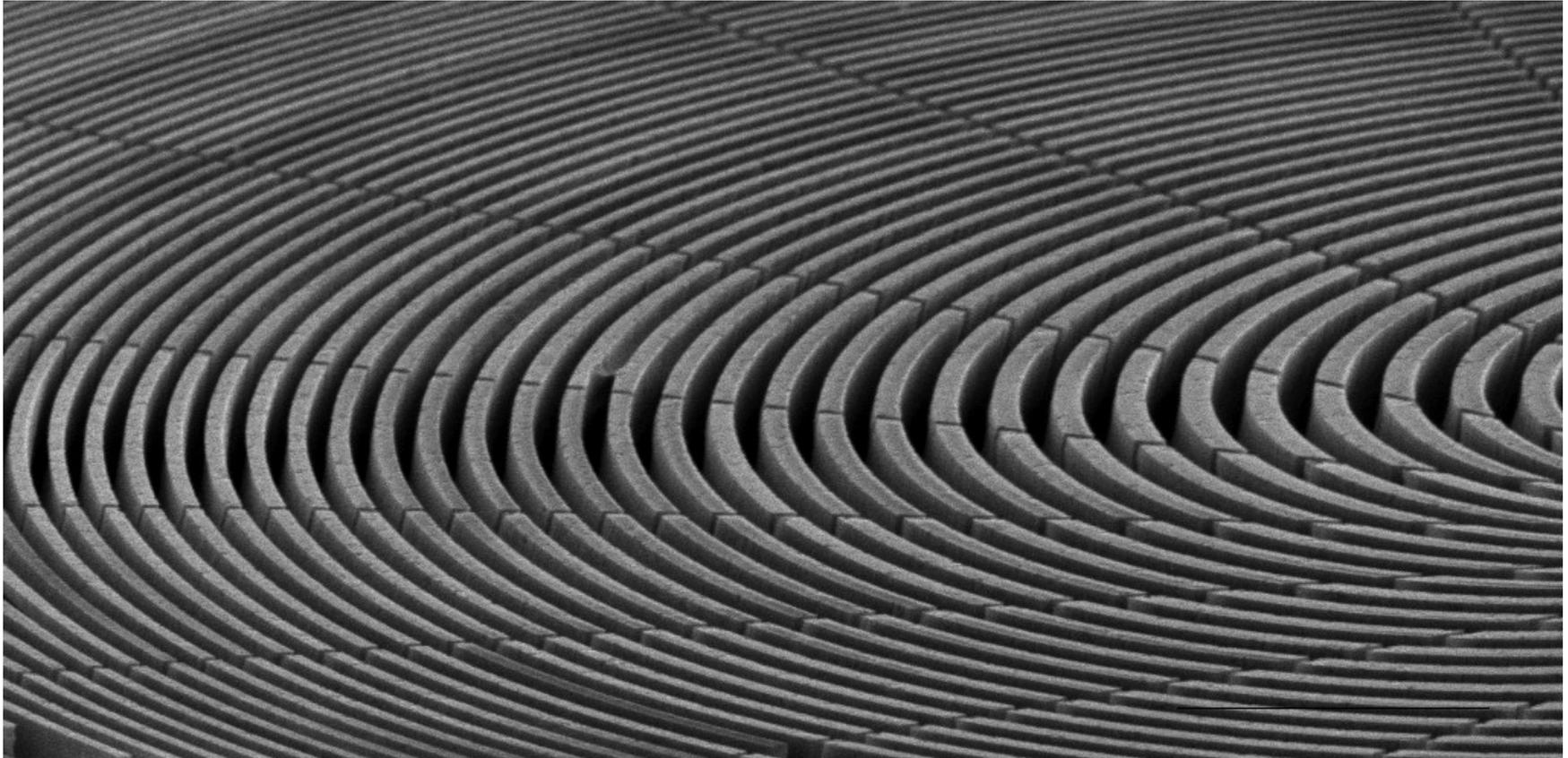
$$r_n^2 = n\lambda f + \frac{n^2 \lambda^2}{4} \quad (9.9)$$

$$r_n \simeq \sqrt{n\lambda f} \quad (9.10)$$

HW: Note right triangles. Use Pythagorean Theorem to derive zone plate equations above.



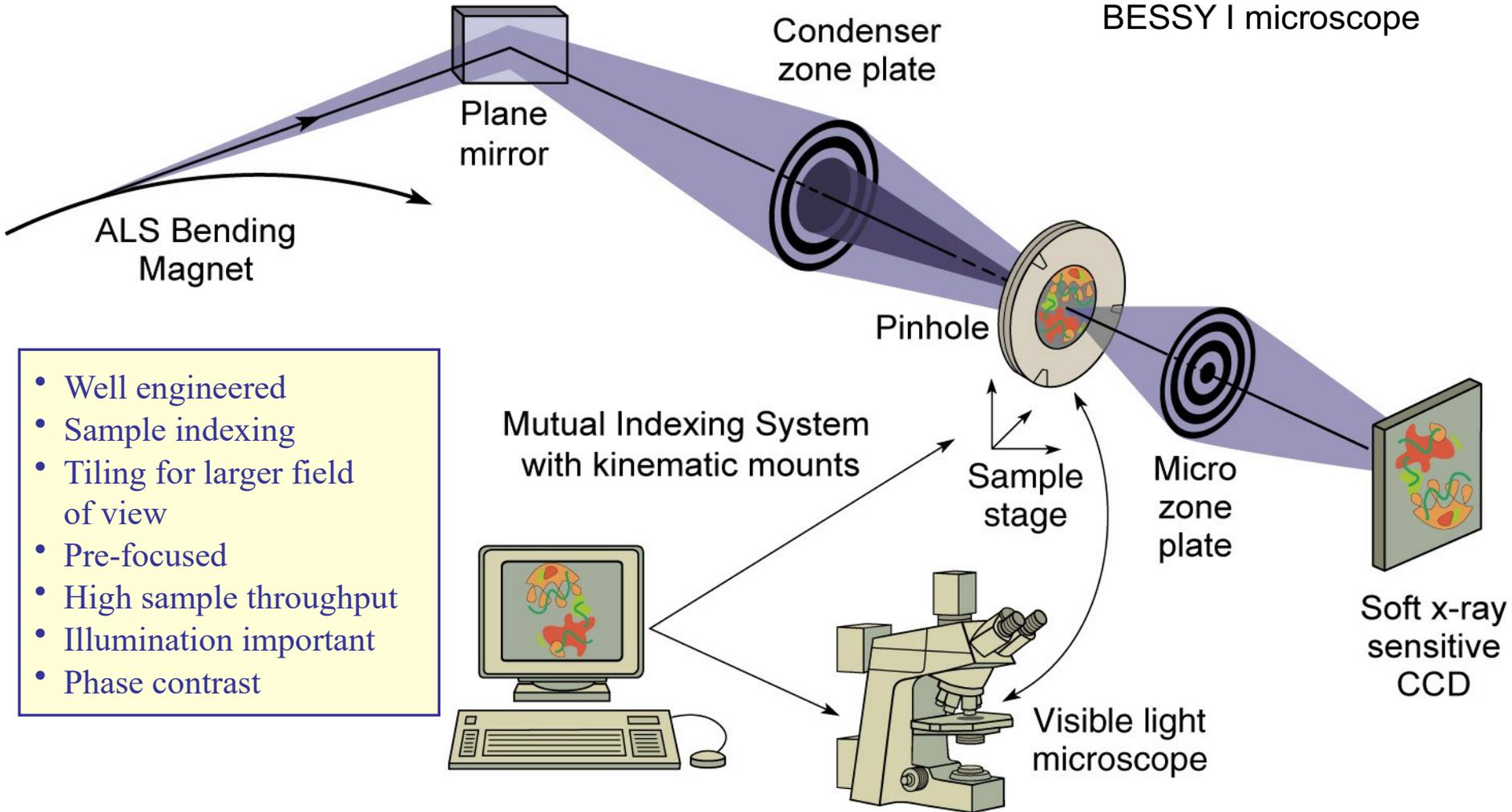
X-ray Fresnel zone plate lens can be used for imaging at high spatial resolution



Courtesy of A. Sakdinawat and Chieh Chang (SLAC/ Stanford)

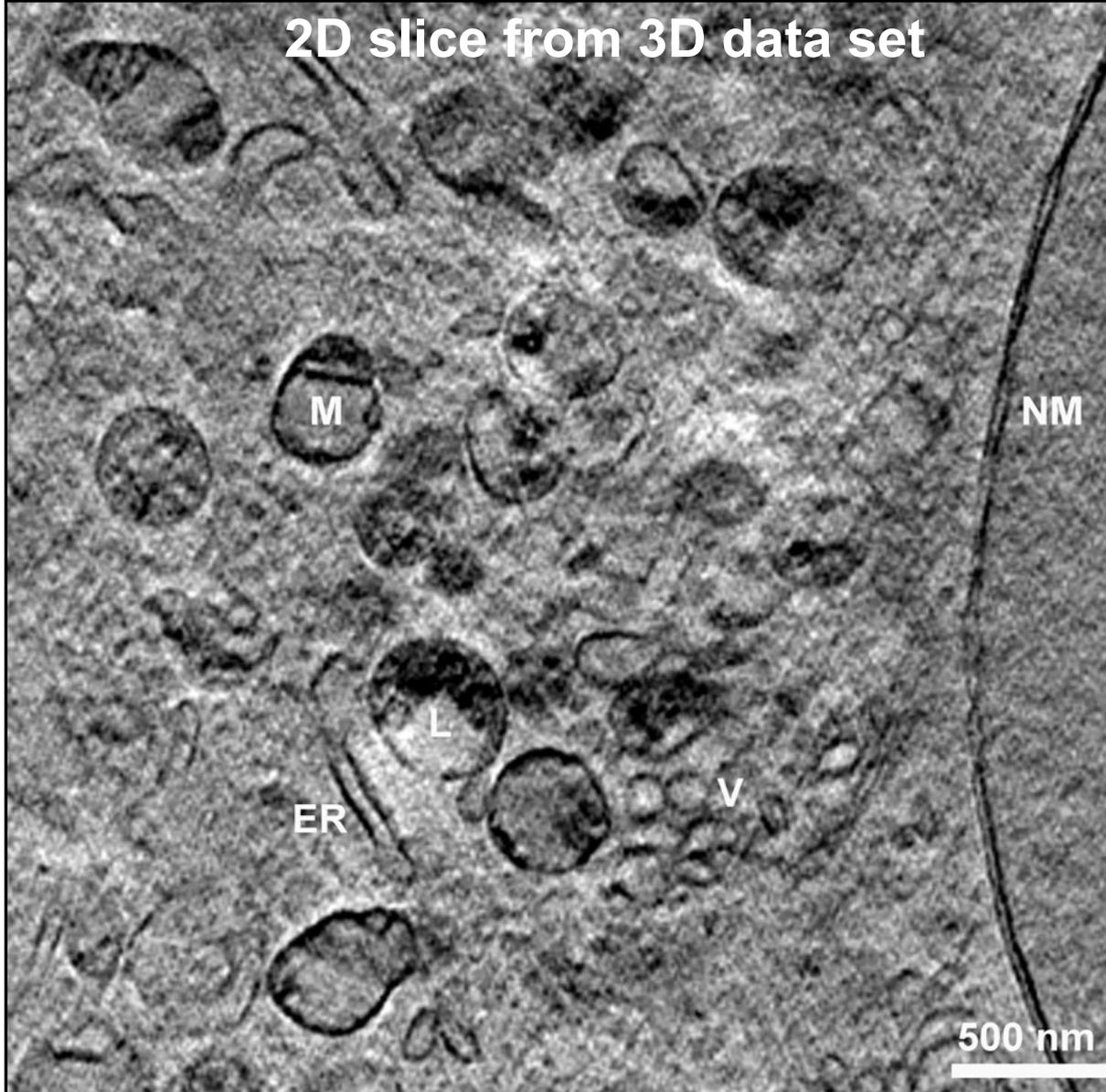
High resolution zone plate microscopy

A near clone of the BESSY I microscope



- Well engineered
- Sample indexing
- Tiling for larger field of view
- Pre-focused
- High sample throughput
- Illumination important
- Phase contrast

2D slice from 3D data set

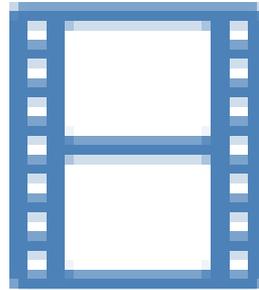
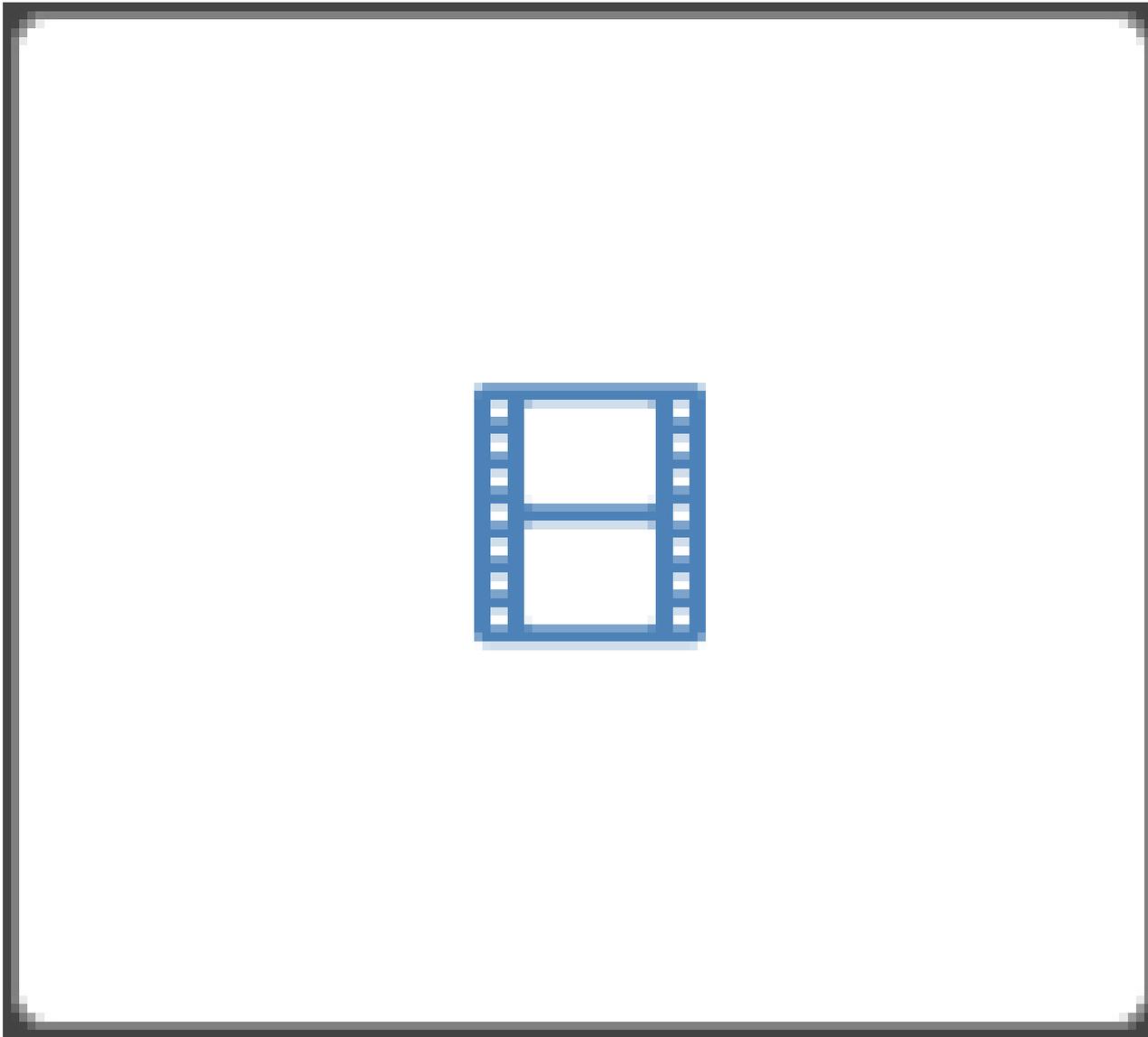


510 eV (2.43 nm)
 $\Delta r = 25$ nm,
 1° intervals, $\pm 60^\circ$
36 nm nuclear
double membrane.
Exposure ~ 5 minutes

Endoplasmic Reticulum
(ER)
Mitochondria (M)
Nuclear Membrane (NM)
Lysosomes (L)
Vesicles (V)
Nuclear pores (NP)

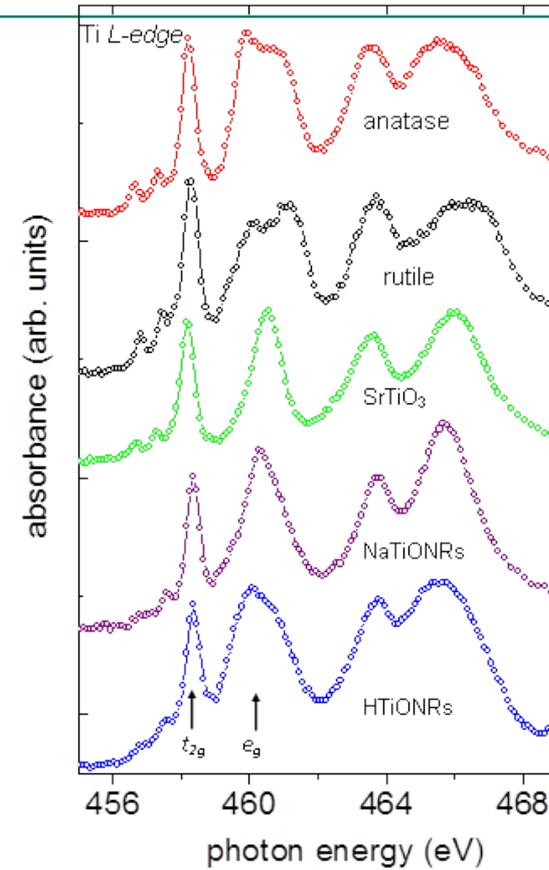
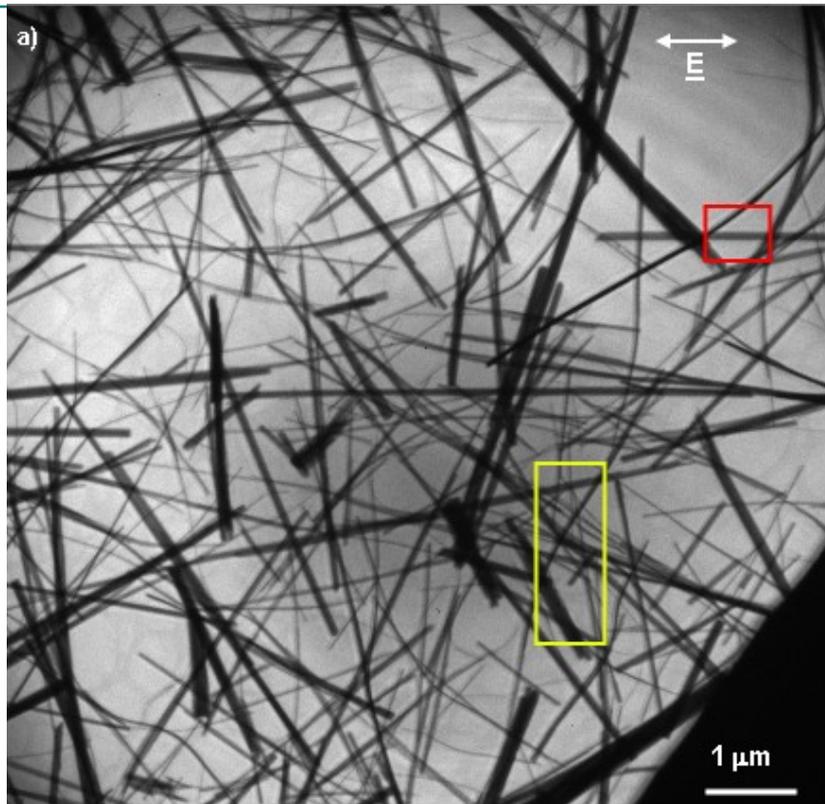
Courtesy of Gerd Schneider,
BESSYII and James McNally,
NIH.
Nature Methods 7, 985 (2010).

X-ray computed tomography of a single biological cell

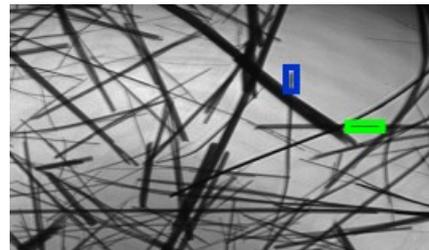
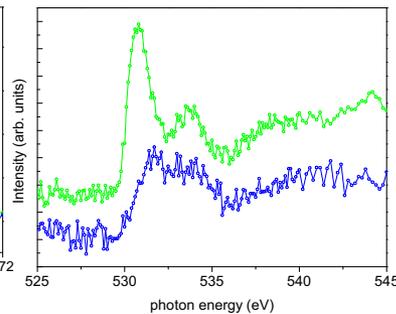
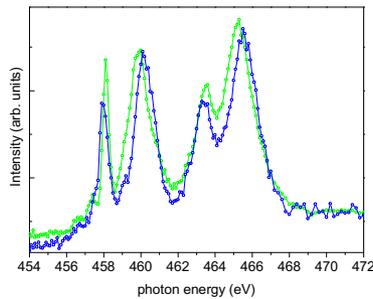


Courtesy of Gerd Schneider, BESSYII and James McNally, NIH.

Nano-spectroscopy of sodium titanate nanoribbons



In collaboration with:
C. Bittencourt,
U. Antwerp, Belgium

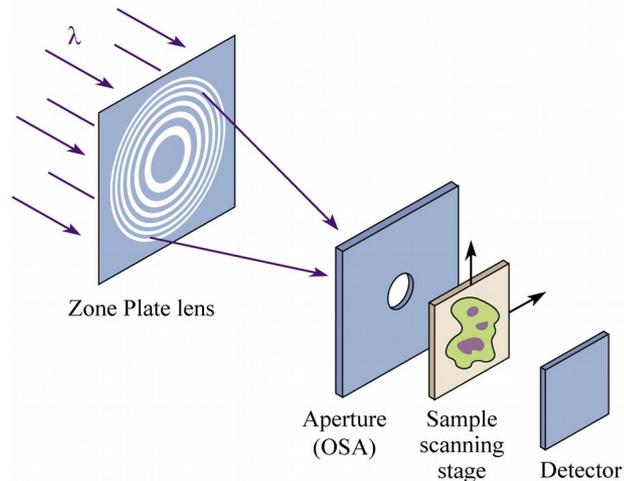


P. Guttman et al., *Nature Photonics*
(Dec. 2011).

Scanning Transmission X-ray Microscope (STXM)

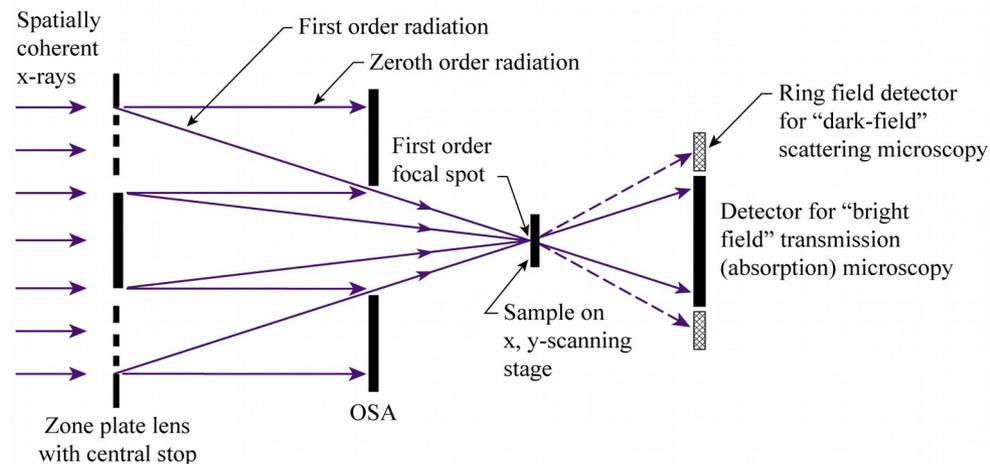


(a) Scanning Transmission X-ray Microscope



Especially useful for spectromicroscopy of radiation sensitive samples

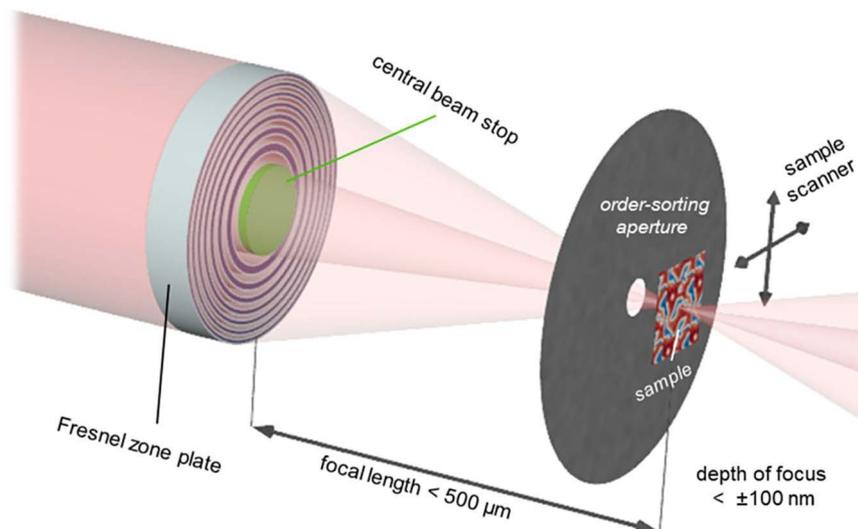
(b)



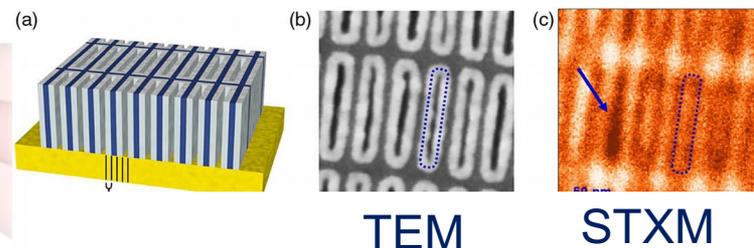
Soft x-ray microscopy with 7 nm resolution



Scanning Transmission X-ray Microscope (STXM)
PSI, Swiss Light Source

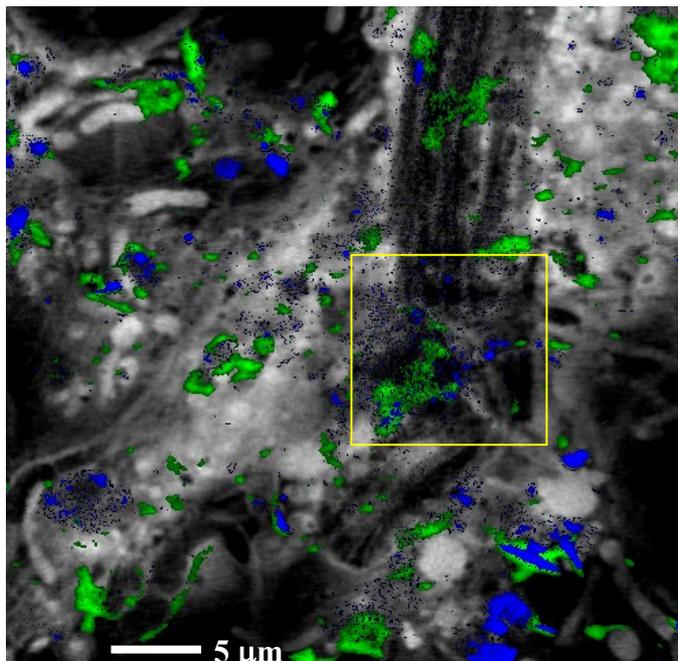


Magnetic nanostructure



B. Rosner,* S. Finizio, F. Koch, F. Doring, V.A. Guzenko, M. Langer, E. Kirk, B. Watts, M. Meyer, J. Lorona Ornelas, A. Spath, S. Stanescu, S. Swaraj, R. Belkhou, T. Ishikawa, T.F. Keller, B. Gross, M. Poggio, R.H. Fink, J. Raabe, A. Kleibert, AND Christian David **Optica** 7, 1602 (November 2020).

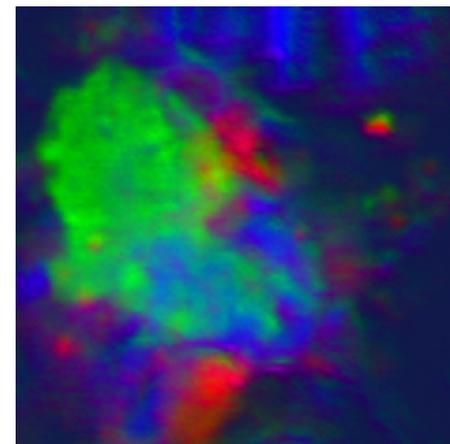
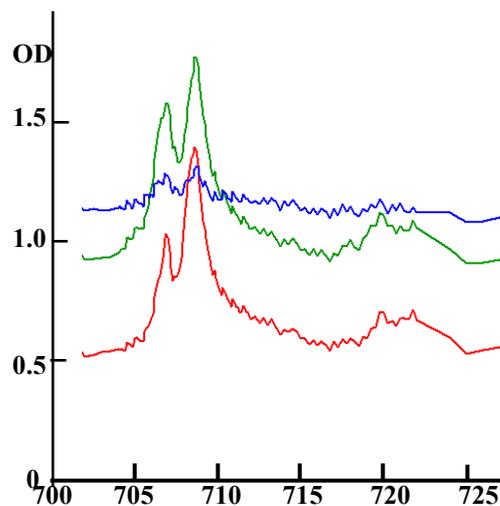
PSI, ETH, Erlangen-Nurnberg, Soleil, DESY. U. Hamburg, U. Basel



Protein (gray), Ca, K

RESULTS

- Ni, Fe, Mn, Ca, K, O, C elemental map, (there was no sign of Cr.)
- Different oxidation states for Fe and Ni



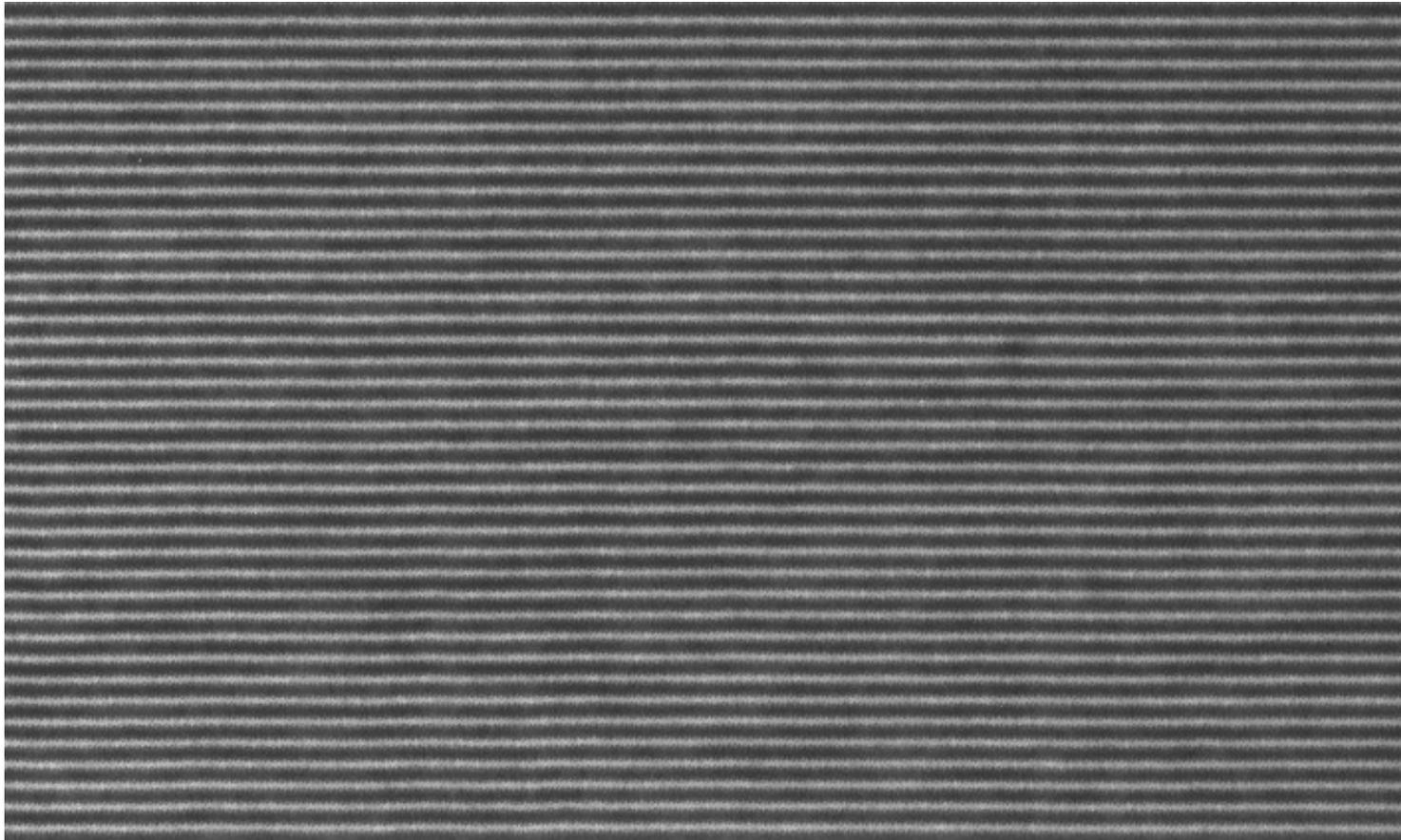
Different oxidation states (minerals) found for Fe & Ni

Courtesy of Tohru Araki, Adam Hitchcock (McMaster University) and Tolek Tyliczszak, LBNL; Sample from: John Lawrence, George Swerhone (NWRI-Saskatoon) and Gary Leppard (NWRI-CCIW)

A High Quality Mo/Si Multilayer Mirror can Achieve 70% Normal Incidence Reflectivity in the EUV



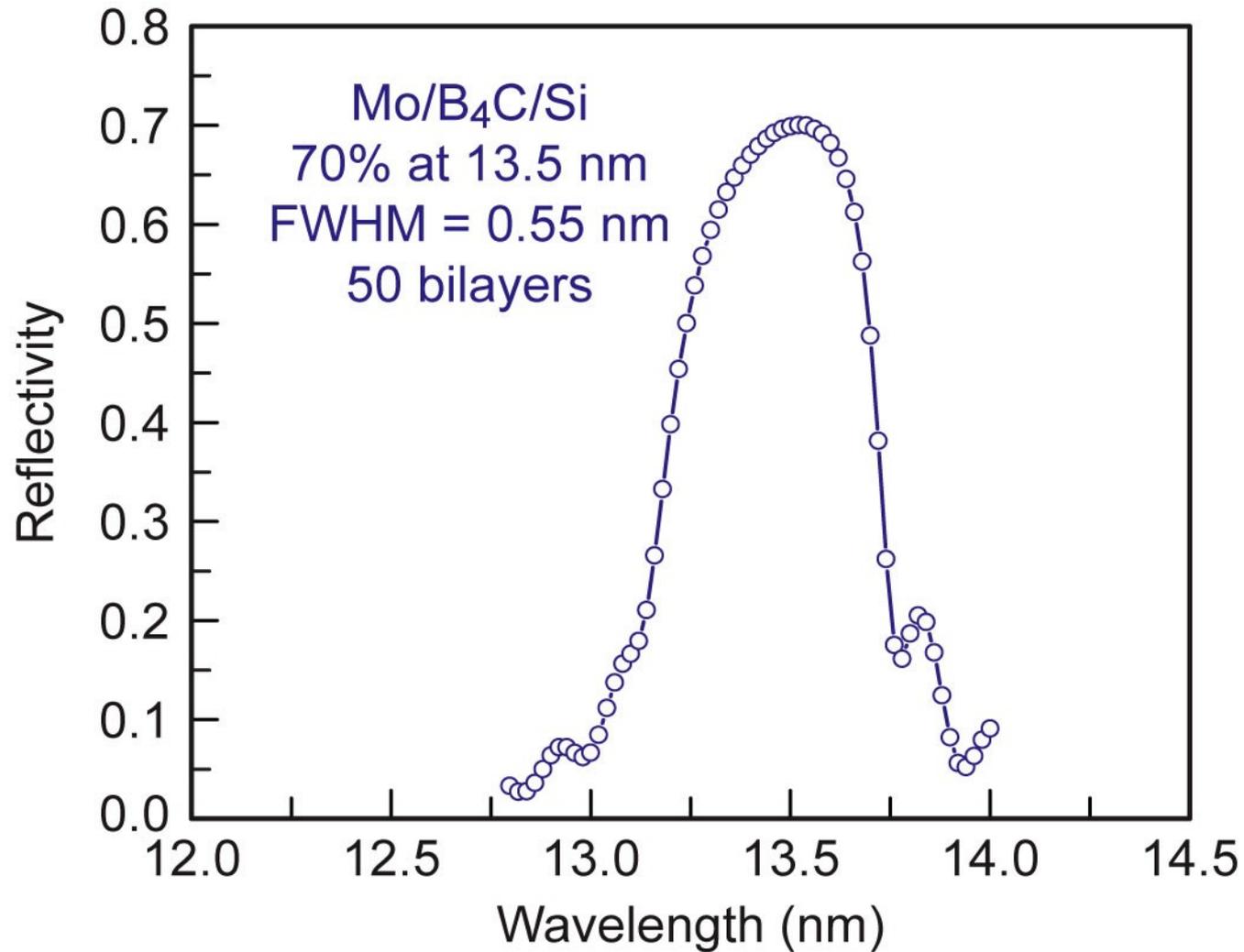
Small reflections at many interfaces add in phase at the Bragg angle.
In the EUV δ and β are relatively large (λ dependence)



$N = 40$
 $d = 6.7$
 $\lambda = 13.5 \text{ nm}$
(92.5 eV)

Courtesy of Saa Bajt (CFEL/DESY)

Multilayer mirrors have achieved a reflectivity of 70% in the extreme ultraviolet (EUV) ... an unusual result



Courtesy of Saša Bajt (LLNL)

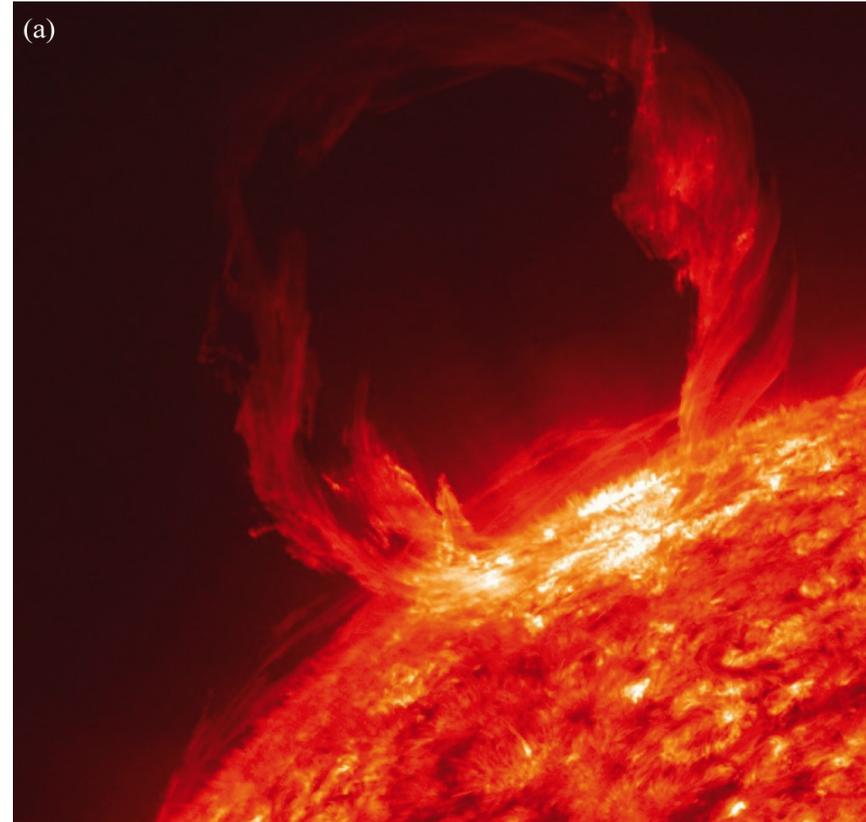
Ch04_ReflectCurv70.ai

EUV Image obtained with Mo/Si coated optics: coronal loop of magnetized plasma at the sun's surface



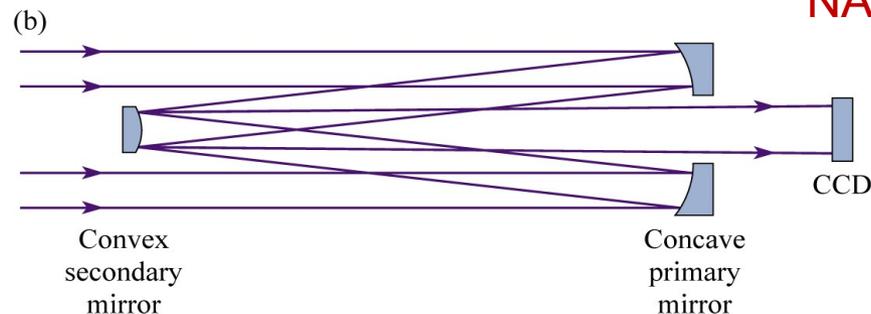
Lockheed/NASA Atmospheric Imaging Assembly (AIA) telescope, part of the geosynchronous **Solar Dynamics Observatory (SDO)**.

Multilayer coatings provided by R. Soufli, LLNL and D.L. Windt, Reflective X-ray Optics. J.R. Lemen, *Solar Physics* **275**, 14 (2012)



NASA/SDO

Multilayer coated
Cassegrain telescope
Mo/Si, 17.1 nm,



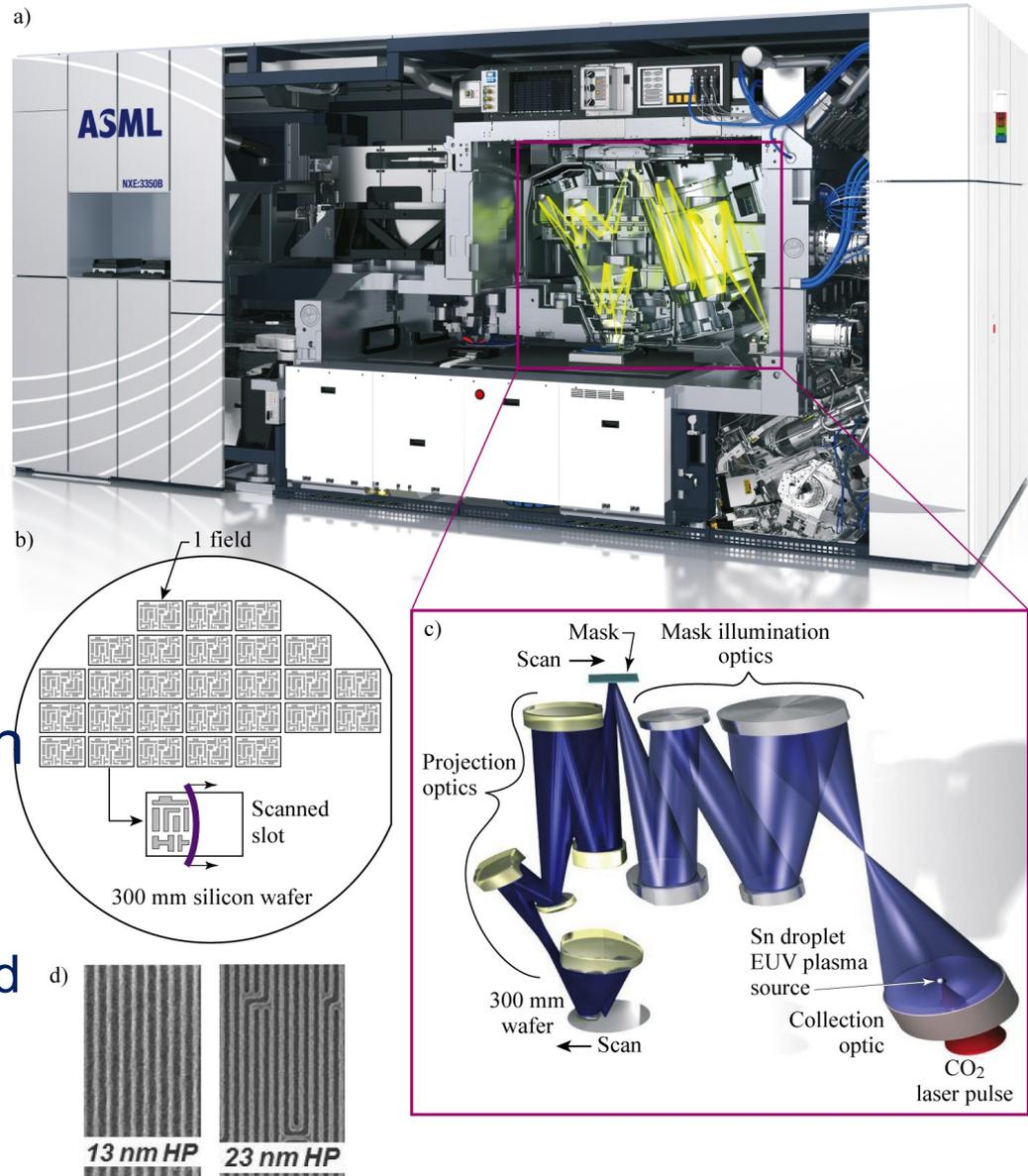
Moore's Law is not dead, saved by Extreme Ultraviolet (EUV) Lithography using these same multilayer mirrors



Step and scan system, Mo/Si coated reflective optics at 13.5 nm wavelength, CO₂ laser irradiated 30 μm Sn microspheres.

Bending magnet and undulator radiation used for critical early research at both the ALS and BESSY II.

Courtesy of V. Banine (ASML) and W. Kaiser (Zeiss)



EUV lithography: High volume manufacturing (HVM) of computer chips and smart phone chip began in 2019



ANANDTECH

9 October 2018

TSMC's second-generation 7 nm manufacturing technology will use extreme ultraviolet lithography. Apple's new iPhone 11 uses TSMC chips patterned by EUV lithography

VB VentureBeat

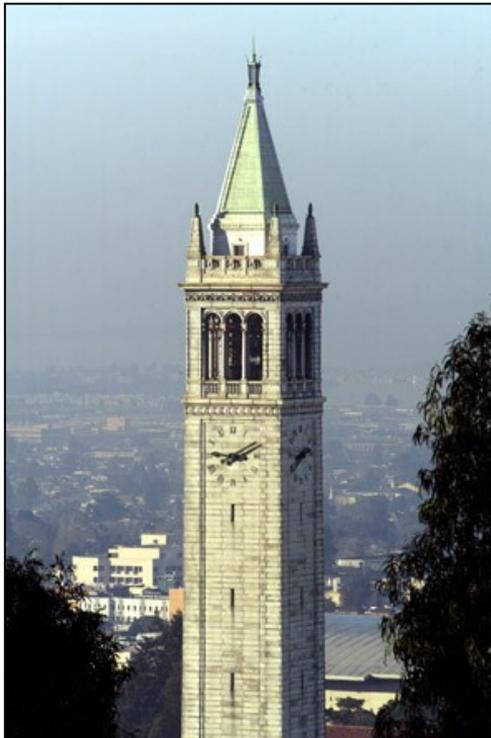
18 October

2018

Samsung begins making 7LPP chips, commercializing 7nm EUV lithography

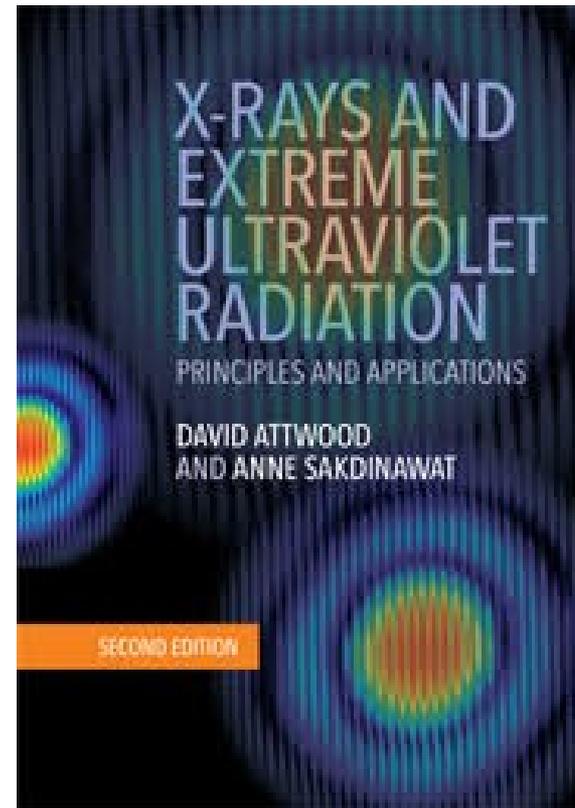
7nm EUV lithography In a significant milestone for the semiconductor industry, Samsung today [announced](#) that it is now manufacturing 7LPP chips: processors based on extreme ultraviolet lithography (EUV) and a 7-nanometer manufacturing process. Beyond this specific accomplishment, the company notes that it is providing customers a clear path to future 3-nanometer chips.

Further reading, 2021 online lectures, slides that you can use



UC Berkeley 2021 lectures online:

[https://www.youtube.com/playlist?
list=PL2wgq6z751n6ELeNsPAx_b8elkmLS41G
T](https://www.youtube.com/playlist?list=PL2wgq6z751n6ELeNsPAx_b8elkmLS41GT)



Cambridge University Press
www.cambridge.org/xrayeuv
For slides, errata and HWs click
'Resources'