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The thermocapillary effect on gas bubbles growing on electrodes of different sizes

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Abstract

Recently, the strongly inhomogeneous current density occurring near a microelectrode was identified as driving a thermocapillary electrolyte flow near gas bubbles growing during electrolysis [1]. The present paper is investigating this effect in more detail under various operating conditions. Furthermore, by simplified modeling, the question is answered of whether this effect is also of importance at large planar electrodes. The direction of the thermocapillary force on the bubble is found to change from retarding to advancing the bubble release when the size of the electrode is increased. Conclusions are drawn on how the thermocapillary effect at planar electrodes depends on the electrode coverage and the bubble departure size, also considering industrially relevant values of the current density.

Keywords: hydrogen evolution, electrolysis, thermocapillarity, Marangoni force, microelectrode, macroelectrode

1. Introduction

Interfaces between media of different phases are ubiquitous in nature and play an important role in many physico-chemical systems. If liquids are involved, capillary effects often influence the system behavior [2]. The surface tension for a given liquid-gas pair is known to depend on physical properties of the interface, namely the temperature, chemical composition and electric potential in the presence of interfacial charge [3]. Thus, interfacial gradients of these physical properties cause the surface tension to vary along the interface. As a result, due to unbalanced forces at the interface, fluid elements there experience a net shear stress and move towards interface regions of higher interfacial tension. The resulting capillary flow is commonly called Marangoni flow [4]. This Marangoni effect is known to occur in many systems of scientific and technological importance. For example, thermo-capillarity is the mechanism which drives the well-known Bénard cells ([5–7] and references therein), a phenomenon occurring in many engineering heat transfer applications. In liquid-liquid extraction processes, soluto-capillary flows may significantly change the mass transfer rate

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21 [8]. Furthermore, Marangoni flow exists at sessile evaporating droplets due to the interfacial temperature
22 gradient caused by a nonuniform rate of evaporation [9]. This influences the well-known coffee-ring-like
23 structures [10], and may thus affect patterned deposition [11] and particle self-assembly [12].

24 In 1959, Young et al. [13] demonstrated the profound effect which Marangoni flow can have on air bubbles
25 in liquids by applying a positive temperature gradient in the direction of gravity to suspend them against
26 buoyancy. The temperature gradient induced a surface tension gradient along the bubble interface and
27 thus exerted a thermocapillary stress on the interface, which caused the bubble to experience a force against
28 buoyancy. At a sufficiently steep temperature gradient, the thermocapillary force can be as large as buoyancy.
29 Later, with the advent of space research, bubble actuation in micro-gravity by means of thermocapillarity
30 attracted much interest [14, 15]. Experiments conducted in the space shuttle in orbit showed that by applying
31 a temperature gradient of the order of 1 K/mm, a bubble migration speed of ~ 1 mm/s could be achieved
32 for a bubble of millimeter size [16]. McGrew et al. [17] speculated that Marangoni convection might have a
33 significant contribution to heat transfer in nucleate boiling, as the observed flow structure around a pendant
34 air bubble heated from above was found to be similar to that of a vapor bubble during boiling. Later, in
35 nucleate boiling experiments conducted under microgravity conditions, the heat transfer rate obtained by
36 Straub was similar to that obtained under normal gravity conditions [18], which lent further credence to the
37 importance of Marangoni flow around the bubbles. Further experiments and numerical simulations [19–21]
38 established the significant importance of thermocapillarity-driven flow in the subcooled boiling regime and
39 showed that the resulting Marangoni force acting on the bubble slowed down their detachment from the
40 boiling surface [22].

41 It has long been hypothesised that the Marangoni effect also influences the dynamics of bubbles grown
42 electrochemically on electrodes [23, 24]. Definitive experimental evidence of the Marangoni effect was first
43 provided by Yang et al. [25], who performed a detailed investigation of the interfacial flow around hydrogen
44 bubbles grown on a Platinum microelectrode. Then, by simultaneously measuring the electrolyte velocity
45 and temperature and correlating the results with the numerical solution obtained when considering only ther-
46 mocapillarity, Massing et al. [1] were able to show that the Marangoni flow observed is primarily attributed
47 to the thermocapillary effect caused by the temperature gradient along the bubble interface. Interestingly,
48 for strong local boiling at microheaters, the thermocapillary flow found near the gas bubble qualitatively
49 matches the flow structure near the electrogenerated gas bubble at a microelectrode [1], though due to strong
50 laser heating the maximum flow velocity is about 10 times higher [26].

51 As gas bubbles are generated in many electrochemical processes such as plating, refining of metal or
52 the chloralkali process [27–29], a better understanding of the dynamics of electrogenerated bubbles and
53 associated thermo-fluidic phenomena is of great technological and scientific interest. This is particularly
54 relevant for H_2 production through water electrolysis, as the bubble evolution rate directly influences both
55 the system throughput and the process efficiency [30], which may be of increasing importance for next-

56 generation green energy storage and mobility applications [31–33].

57 As bubbles attached to the electrode surface disturb a homogeneous surface reaction rate, reduce the
58 active reaction area and increase the electrical resistance of the cell, the speedy removal of generated bubbles
59 from the electrode surface is highly desirable with respect to both deposit quality and electrical efficiency.
60 The instant of bubble departure and the departing diameter is determined by the equilibrium of forces acting
61 on the bubble [34]. However, the often-used Fritz equation [35] does not provide an accurate prediction of
62 the departure diameter [36]. For the special case of oxygen bubbles grown photocatalytically on TiO₂
63 nanorods where a temperature gradient is caused by light irradiation, Chen et al. have recently shown that
64 the inclusion of both thermocapillary and solutal Marangoni forces in the force balance of the bubble could
65 considerably improve the estimate of the bubble departure [37]. However, beside the aforementioned study
66 by Massing et al. [1], where a retarding influence of the thermocapillary effect on the bubble departure was
67 found, no systematic study has been carried out for electrogenerated bubbles.

68 For studying bubble evolution during electrolysis, microscale electrodes have been widely used, as the
69 nucleation area is limited, and single bubble growth can be more easily observed compared to the spatially
70 random nucleation occurring at large planar electrodes [38–41]. The recent work which was the first to
71 confirm the existence of thermocapillary flow around electrogenerated bubbles [1] was also carried out at
72 microelectrodes. However, there remains a need for more detailed investigations of this phenomenon. In
73 particular, the question has not yet been addressed of whether this effect is also of importance at the larger
74 electrodes, which are more relevant to industrial applications. Therefore, in this study we perform detailed
75 numerical simulations and analyses of the thermocapillary effect at electrogenerated bubbles on electrodes
76 of varying size. Different operating conditions are investigated, and the important qualitative differences
77 found between microelectrodes and macroelectrodes will be emphasized.

78 2. Simulation setup

79 *Microelectrode.* To study the thermocapillary effect around a hydrogen bubble at a microelectrode of vary-
80 ing size, our simulation setup closely follows the methodology used by Massing et al. [1]. A cylindrical
81 electrochemical cell with a radius $R_c = 5$ mm and a height $R_h = 5$ mm is considered. It is filled with an
82 aqueous solution of 1 M H₂SO₄. The computational domain is sketched in Figure 1a. At the bottom of
83 the cell, a bubble with a radius $R_b = 560$ μ m sits on a Pt microelectrode (radius R_e), which works as the
84 cathode. The contact angle between the bubble and electrode is $\theta_c = 4.2^\circ$ [1]. It should be noted here that
85 the bubble radius is much smaller than the size of the cell. The Pt microelectrode is embedded in a glass
86 bottom. The top of the cell is completely covered by a counter-electrode made of platinum. The electrodes
87 and the glass bottom have a height of 5 mm each. The inclusion of the glass bottom and both electrode
88 domains is important for an accurate calculation of the temperature field in the electrolyte due to non-zero

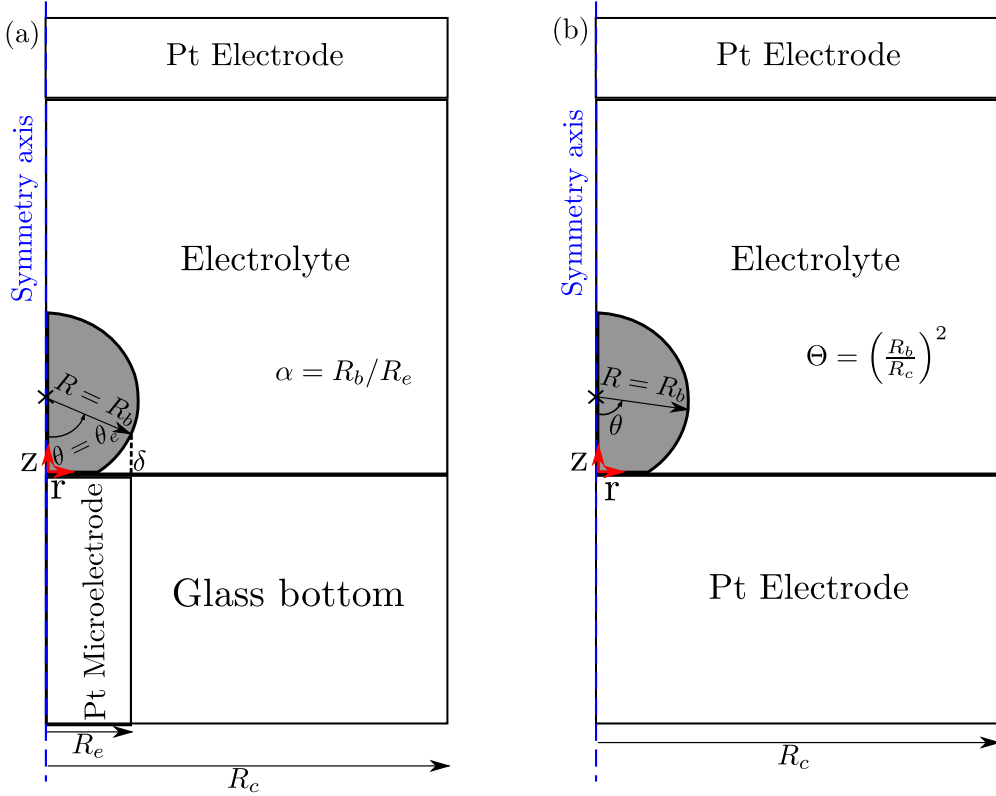


Figure 1: Computational domain (not to scale). a) microelectrode, b) macroelectrode.

89 and non-uniform heat flux through these domains.

90 We follow Massing et al. [1] and consider a bubble of fixed size to resemble a late stage of the bubble
 91 growth cycle. As shown in Figure 1, we utilize the rotational symmetry of the cell and hence perform
 92 axisymmetrical simulations. The leftmost edge in Figure 1 is the axis of symmetry. The following equations
 93 to be solved describe the spatial and temporal distribution of the electric potential (ϕ), velocity (\mathbf{u}) and
 94 temperature (T) in the electrolyte:

$$\nabla^2 \phi = 0 \quad (1)$$

$$\nabla \cdot \mathbf{u} = 0 \quad (2)$$

$$\rho \left(\frac{\partial \mathbf{u}}{\partial t} + (\mathbf{u} \cdot \nabla) \mathbf{u} \right) = -\nabla p + \mu \nabla^2 \mathbf{u} \quad (3)$$

$$\rho C_p \left(\frac{\partial T}{\partial t} + (\mathbf{u} \cdot \nabla) T \right) = k \nabla^2 T + \frac{|\mathbf{j}|^2}{\sigma} \quad (4)$$

98 Here, the primary current density $\mathbf{j} = -\sigma \nabla \phi$ is obtained by solving Eq. (1), where σ denotes the electrical
 99 conductivity of the electrolyte, which is assumed to be constant. The electrolyte velocity is obtained by
 100 solving the incompressible Navier-Stokes equation (3) complemented by the incompressibility constraint (2),

101 where p , ρ and μ denote the pressure field and the material properties of density and viscosity. Thermal
102 and solutal buoyancy effects may safely be neglected, as discussed in [1]. The electrolyte temperature is
103 obtained by solving Equation (4), where C_p and k denote the material properties of the specific heat capacity
104 and thermal conductivity. The latter term denotes Joule heating due to electric current passing through the
105 electrolyte. It should be noted here that this term may be neglected in the electrodes, where the electrical
106 conductivity σ is several orders of magnitude larger than in the electrolyte. Therefore, in all other domains
107 (both electrodes, glass bottom and gas bubble), only heat diffusion is solved:

$$\rho C_p \frac{\partial T}{\partial t} = k \nabla^2 T \quad (5)$$

108 Here, convective heat transport in the gas bubble may safely be neglected, as discussed in [1].

109 The boundary conditions applied to these equations are as follows: for Equation (1), the electrode
110 surfaces exposed to electrolyte are kept at a fixed potential, i.e. $\phi = 0$ for the working electrode and $\phi = \phi_0$
111 for the counter electrode. The outer boundary at R_c is electrically insulating, i.e. $\frac{\partial \phi}{\partial \mathbf{n}} = 0$, where \mathbf{n} is the
112 normal unit vector. For Equation (3), a shear stress balance is applied at the electrolyte–bubble interface,
113 i.e. $\tau_H = \tau_M$, where the hydrodynamic shear stress is given by $\tau_H = \mu \left(\nabla \mathbf{u} + (\nabla \mathbf{u})^T \right) \cdot \mathbf{n}$, and the thermal
114 Marangoni stress is given by

$$\tau_M = \frac{\partial \gamma}{\partial T} \cdot \nabla_s T \quad (6)$$

115 Here, γ denotes the interfacial tension, which is assumed to depend on the temperature only, and
116 $\nabla_s \equiv \nabla - (\nabla \cdot \mathbf{n}) \mathbf{n}$ denotes the gradient along the surface of the interface. As the temperature field is
117 solved in all domains by Eqns. (4) and (5), boundary conditions are required only at the outermost surfaces.
118 The top and the bottom of the computational domain are kept at an ambient temperature $T_{amb} = 20^\circ \text{C}$,
119 while at the outer surface at R_c far from the bubble an adiabatic condition $\frac{\partial T}{\partial \mathbf{n}} = 0$ is applied. Finally, at the
120 symmetry axis at $r = 0$, a zero radial gradient condition is applied on all variables, i.e. $\frac{\partial}{\partial r}(\phi, \mathbf{u}, T) = 0$. The
121 temperature coefficient of the surface tension at the gas-liquid interface is taken to be $\partial \gamma / \partial T = -1.6 \cdot 10^{-4}$
122 N/m·K [1]. The value of the surface tension γ does not appear directly in our model as the bubble is
123 assumed to be of fixed shape and size. All other material properties are assumed to be constant over the
124 electric potential and temperature range solved for and are shown in Tables 1 and 2.

125 All equations are solved using the FEM-based simulation software COMSOL 5.4. The initial conditions
126 applied are zero potential, electrolyte at rest and ambient temperature. As discussed extensively in [1],
127 a time integration period of one second was chosen at which nearly stationary and realistic values of the
128 temperature and velocity distribution and the resulting Marangoni force may be expected. To study the
129 effect of the size of the working microelectrode, R_e is varied while R_b is kept constant. We introduce a

Electrolyte	$\mu = 10^{-3} \text{ Pa}\cdot\text{s}$
	$\sigma = 40 \text{ S/m}$
	$\rho = 10^3 \text{ kg/m}^3$
	$C_p = 4.182 \text{ kJ/kg}\cdot\text{K}$
	$k = 0.58 \text{ W/m}\cdot\text{K}$

Table 1: Material properties of the electrolyte for Equations 3 and 4

Material	$\rho(\text{kg/m}^3)$	$C_p(\text{kJ/kg}\cdot\text{K})$	$k(\text{W/m}\cdot\text{K})$
Platinum	21450	0.13	72
Glass	2201	1.052	1.38
Hydrogen	0.09	14.32	0.186

Table 2: Material properties for Equation 5

130 non-dimensional length parameter as the ratio of the bubble radius and the microelectrode radius,

$$\alpha = \frac{R_b}{R_e} \quad (7)$$

131 As we are here primarily interested in studying how the increasing size of the microelectrode affects the
 132 behavior in the vicinity of the gas bubble, unless otherwise mentioned, the radius of the microelectrode is
 133 varied from $50 \mu\text{m}$ to $400 \mu\text{m}$ such that $R_e < R_b$, i.e. $\alpha > 1$.

134 *Macroelectrode.* To study the thermocapillary effect on a large, flat electrode where multiple gas bubbles
 135 are growing simultaneously, we take a simplified approach as follows: we first zoom into a small part of the
 136 electrode in order to focus only on a single bubble. A cylindrical domain around this bubble is considered,
 137 where the radial extension R_c of the domain is half the distance to the next neighboring bubble. We
 138 assume that the cell with large electrodes is essentially composed of this periodically repeating domain.
 139 Though there are time shifts between the evolution cycles of neighboring bubbles, our simplified approach
 140 therefore assumes that all bubbles develop synchronously and also ignores possible coalescence phenomena
 141 of neighboring bubbles during growth. A further approximation consists in neglecting azimuthal variations
 142 of potential, temperature and velocity which might arise from the finite number of neighboring bubbles
 143 sitting at unknown azimuthal positions. This approach treats neighboring effects in an approximate manner
 144 averaged over the azimuthal direction and allows the problem to be simulated axisymmetrically. We can
 145 therefore make use of the axisymmetric computational domain shown in Figure 1b, which is similar to the
 146 one used previously for the microelectrode shown in Figure 1a, and which only needs minor modifications:
 147 at the bottom of the cell, the outer glass part is removed, and the electrode is now enlarged over the full
 148 radial extent of the cell R_c . At the outer radial boundary, the conditions of electrical insulation for the

149 potential and an adiabatic condition for the temperature remain unchanged, but in the case of the velocity,
 150 vertical slip is applied. The governing equations to be solved for remain as before. In order to quantify the
 151 ratio between the bubble size and the size of the cell, we introduce

$$\Theta = \left(\frac{R_b}{R_c} \right)^2 \quad (8)$$

152 In the framework of our approach, this ratio describes the bubble coverage of the electrode which is defined
 153 as the ratio of the bubble area projected on the electrode and the electrode surface area. We can later simply
 154 change the bubble coverage of the electrode (which is known to depend on e.g. the mean current density),
 155 for example by varying the radial extension of the cell while retaining a fixed bubble size.

156 3. Results and Discussion

157 3.1. Microelectrode

158 3.1.1. General overview

159 It is evident from Equation 4 that the electrolyte is heated because of the electric current passing through
 160 the cell. This causes a temperature gradient along the bubble interface which gives rise to Marangoni
 161 flow. Therefore, the current distribution near the interface strongly influences the temperature and flow
 162 distribution in the electrolyte. Figure 2(a) shows numerically obtained current lines near the interface for
 163 $\alpha = 11.2$. As the gas bubble is electrically insulating, current must pass around it to converge at the
 164 microelectrode. Therefore, as the entire cell current must squeeze through a narrow wedge-like region at
 165 the bubble foot, the local current density there is very high. In addition, the presence of the bubble makes
 166 the outer region of the electrode more accessible to the electric current. This causes an inhomogeneous
 167 distribution of the current density over the electrode surface wetted by the electrolyte, as shown in Figure 2(b)
 168 for different microelectrode sizes. Here, the cell voltage was kept constant at $\phi_0 = 4.5$ V, and the radial
 169 position on the microelectrode is presented normalized by the electrode radius, i.e. $r^* = r/R_e$. As the
 170 current density is shown on a logarithmic scale, it clearly can be seen that it varies quite strongly over the
 171 radial electrode position and is largest at the electrode periphery. The smaller the microelectrode becomes,
 172 the stronger the radial variation of the current density and also its maximum value at the electrode periphery.

173 As the rate of heat generation scales with the current density squared ($|\mathbf{j}|^2$), the electrolyte experiences
 174 strong heating near the periphery of the electrode. Figure 3 shows a zoomed view of the distribution of the
 175 temperature rise ($\Delta T = T - T_{amb}$) in the vicinity of the outer electrode edge for $R_e = 200 \mu\text{m}$ ($\alpha = 2.8$). It
 176 can be seen that the temperature maximum occurs just above the microelectrode periphery at $r^* = 1$. As
 177 the surface tension of the bubble interface decreases with increasing temperature, the electrolyte is pulled
 178 towards colder parts of the interface, thus establishing an interfacial flow away from the point of maximum
 179 temperature. As this bidirectional interfacial flow must be replenished from the bulk, a double-vortex

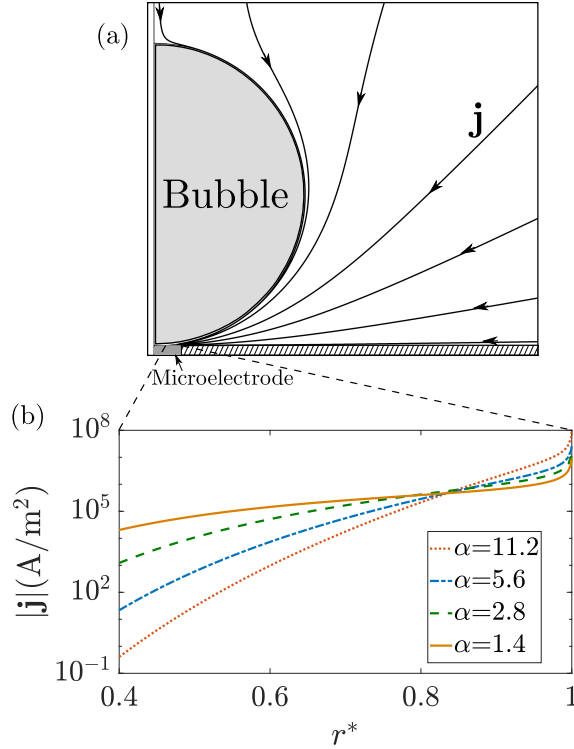


Figure 2: (a) Current lines near the bubble interface as obtained from a simulation for $\phi_0 = 4.5$ V and $\alpha = 11.2$. (b) Distribution of the magnitude of the current density ($|j|$) on microelectrodes of different size versus the radial position on the wetted part of the electrode normalized with the electrode radius ($r^* = r/R_e$). $\phi_0 = 4.5$ V. $|j|$ is shown in log scale.

180 structure is created, as shown for the first time in Figure 3. As will be elaborated in the following, this
 181 double-vortex structure is a characteristic feature of the thermocapillary flow driven at the interface of an
 182 electrogenerated bubble. In the case of microelectrodes, for geometric reasons, the temperature hotspot
 183 appears above the electrode periphery, thus confining the left vortex, and the thermocapillary effect is
 184 dominated by the large right vortex. The small size of the left vortex explains, why it was not observed
 185 during earlier work at microelectrodes [1].

186 3.1.2. Interfacial temperature and velocity profile

187 We now discuss the interfacial temperature and velocity profiles at electrodes of different sizes R_e while
 188 the cell voltage is kept constant at $\phi_0 = 4.5$ V. It is to be noted here that, at constant voltage, the electrical
 189 resistance of the cell decreases and hence the cell current increases when the microelectrode is enlarged. The
 190 obtained profiles of the temperature increment ΔT and tangential velocity ($u_t = \mathbf{u} \cdot \mathbf{t}$) along the bubble
 191 interface are shown in Figure 4, with the definition of the angular position θ based on Figure 1. Starting
 192 from the point of contact between the bubble and electrode ($\theta_c = 4.2^\circ$), an initial temperature increment
 193 is seen in all cases. The smaller the microelectrode is, i.e. the larger α is, the steeper the increase in

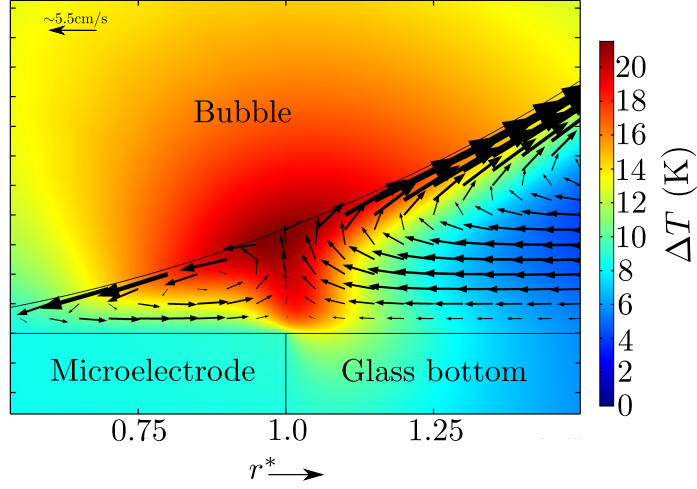


Figure 3: Color contours of the temperature distribution ($\Delta T = T - T_{amb}$) and related electrolyte flow pattern (black: velocity vectors) near the temperature hotspot for a microelectrode of $R_e = 200 \mu\text{m}$ ($\alpha = 2.8$) at potential $\phi_0 = 4.5 \text{ V}$. The radial coordinate is $r^* = r/R_e$.

194 temperature becomes. At the same time, the angle θ_m at which the maximum temperature increase ΔT_m
 195 is observed reduces. This behavior can qualitatively be understood from the discussion on the temperature
 196 hotspot in the section above: this was found to be located approximately above $r^* = 1$. Therefore, when the
 197 microelectrode grows in size, θ_m also increases. A more detailed discussion on θ_m is given in Section 3.1.3.
 198 Moving further along the interface away from θ_m , ΔT gradually decreases towards the bubble north pole at
 199 $\theta = 180^\circ$. This general trend in the interfacial temperature profile is seen for all cathode sizes investigated.

200 It is also to be noted here that the variation of ΔT_m with α is not monotonic. This is because increasing
 201 R_e while keeping ϕ_0 constant increases the cell current. Thus the total heat generation in the cell increases,
 202 which tends to increase the peak interfacial temperature. As the electrode gets bigger, more heat is carried
 203 away by the Pt microelectrode. Greater heat advection from the hotspot by the electrolyte (cf. Figure 4(b))
 204 also contributes similarly. These effects tend to reduce ΔT_m . As a result of the combined action of greater
 205 heat generation and higher heat transfer, ΔT_m varies non-monotonically with R_e and thus α . Hence we can
 206 see from Figure 4(a) that ΔT_m first increases and then decreases to an almost constant value with a larger
 207 electrode i.e. smaller α .

208 The non-uniform interfacial temperature profile causes thermocapillary stress as shown in Equation 6.
 209 Because of the stress balance at the interface, $\tau_M = \tau_H \sim \frac{\partial u_t}{\partial \theta}$, where u_t denotes the tangential velocity
 210 at the interface, a Marangoni flow is driven, as already mentioned in Section 3.1.1. The interfacial flow
 211 profiles for different microelectrode sizes are shown in Figure 4(b) and can be understood by applying the
 212 following sequence of reasoning: According to Equation 6, when the negative temperature coefficient of the
 213 surface tension of the electrolyte mentioned in Section 2 is taken into account, positive or negative slopes

214 of the temperature profile cause negative or positive thermocapillary stress, respectively. Hence, because of
 215 the stress balance, the tangential velocity of the Marangoni flow becomes negative or positive, respectively.
 216 Consequently, as the flow is purely driven by thermocapillarity, the temperature hotspot separates a region
 217 of negative tangential velocity at small angles from a region of positive tangential velocity at larger angles.
 218 At the temperature hotspot θ_m itself, the tangential velocity must vanish, i.e. $u_t = 0$. In Figure 4 and later
 219 also in Figure 5, an example of this is emphasized for the case $\alpha = 5.6$ by a vertical black line. The two
 220 regions of velocity of opposite sign are the interfacial parts of the two counter-rotating vortices already seen
 221 in Figure 3. As the microelectrode increases in size, the region of negative velocity also increases, yielding
 222 a larger vortex above the microelectrode. At the same time, the extremum positions of maximum negative
 223 and positive interfacial velocity are both shifted towards larger angles. During this process, the maximum
 224 negative velocity decreases monotonically in amplitude, with the initially growing maximum velocity later
 225 seeming to level out near a value of about 15 cm/s for $\alpha \sim 1$. However, the total kinetic energy at the
 226 interface reaches a maximum at the largest microelectrode size, a straightforward example of the above
 227 argument of maximum heat generation at smallest α .

228 The interfacial temperature distribution at the bubble is determined by the interplay between the gener-
 229 ation of heat and the diffusion and advection of heat. For the case of a constant cell voltage (ϕ_0) considered
 230 above, all these quantities vary with varying electrode size (α). In order to partly decouple these effects, in
 231 the following we study the case of a constant electric cell power which mainly (apart from kinetic losses)
 232 determines the generation of heat by Joule dissipation. The total electric power of the cell is given by
 233 $P = \phi_0 I_c$, where I_c is the cell current, which in the simulations was determined by integrating the normal
 234 current density over the counter-electrode surface ($I_c = \int j_n dA$). In the following, the electrical power is
 235 kept constant at $P = 13.4$ mW and α is varied. This power value chosen is the same as the constant cell
 236 voltage case at $\alpha = 11.2$, i.e. for the smallest electrode. Hence, the constant cell potential and constant
 237 cell power cases are identical for $\alpha = 11.2$. This way, a major remaining factor determining $\Delta T(\theta)$ along
 238 the bubble interface is the heat carried by the Pt microelectrode, which increases with decreasing α . The
 239 simulation results are shown in Figure 5. The interfacial temperature profile still maintains the character-
 240 istics seen in Figure 4(a). However, because the heat generation is kept constant and the heat carried away
 241 from the electrolyte increases along with the electrode size, ΔT_m decreases monotonically with decreasing
 242 α , as seen in Figure 5(a). Accordingly, the extrema of maximum negative and positive interfacial velocity
 243 eventually decrease monotonically with decreasing α , as seen in Figure 5(b). The same holds for the total
 244 kinetic energy at the interface.

245 3.1.3. Position of the temperature hotspot

246 As mentioned in Section 3.1.2, the reversal of the direction of interfacial flow coincides with the location
 247 of the temperature maximum ΔT_m at the angular position θ_m . It can be further seen in Figure 3 that

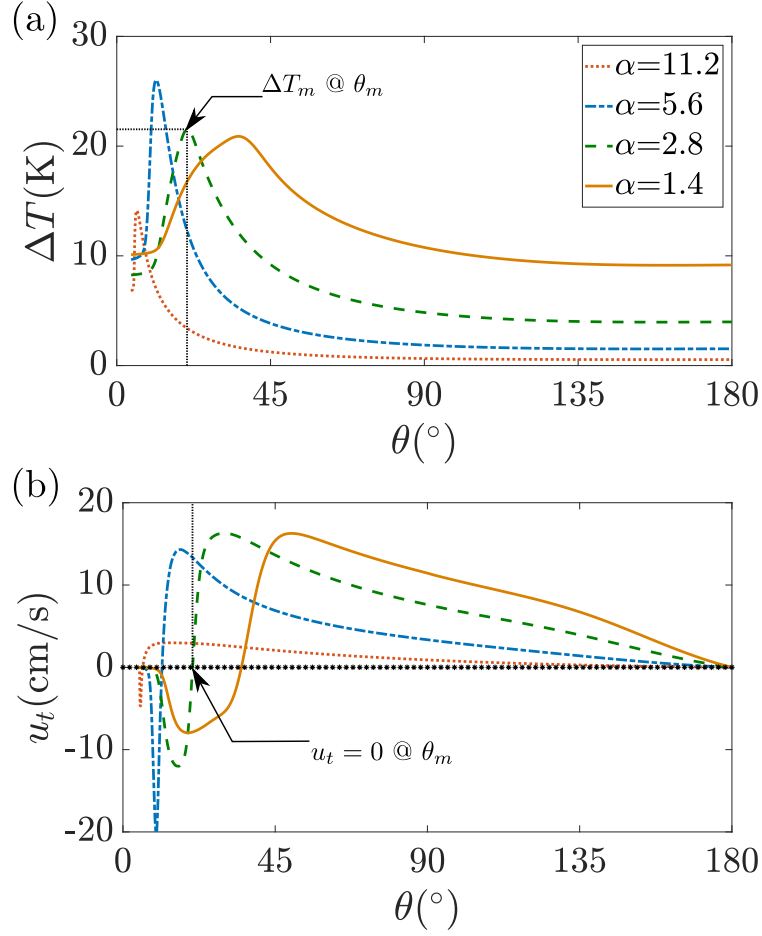


Figure 4: Constant cell voltage case: interfacial temperature (a) and tangential velocity (b) profile as a function of angular position for different electrode sizes expressed by $\alpha = R_b/R_e$

248 for $\alpha = 2.8$ the position of ΔT_m coincides with the upward projection of the microelectrode's outer edge
 249 ($r^* = 1$) onto the bubble interface, as shown in Figure 1. Therefore, we intend to study ΔT_m closer to see
 250 whether this geometrical interpretation also holds true for other microelectrode sizes. The angular position
 251 of the projection of the microelectrode's outer edge ($r^* = 1$) on the bubble interface is given as

$$\theta_e = \sin^{-1}(R_e/R_b) = \sin^{-1}(1/\alpha). \quad (9)$$

252 Figure 6 displays the angular position of the interfacial temperature maximum θ_m versus the inverse relative
 253 electrode size $\alpha = R_b/R_e$ as obtained from simulations for the cases of constant cell voltage (Figure 4a) and
 254 of constant cell power (Figure 5a) in comparison with the values θ_e obtained from the geometrical approach
 255 by Equation 9. At small relative electrode size, i.e. at large α , the simulation results for both cases perfectly
 256 match with the geometrical relation from Equation 9, which provides a very accurate estimate of the location
 257 of the temperature maximum at the interface. As the microelectrode increases in size, only small differences

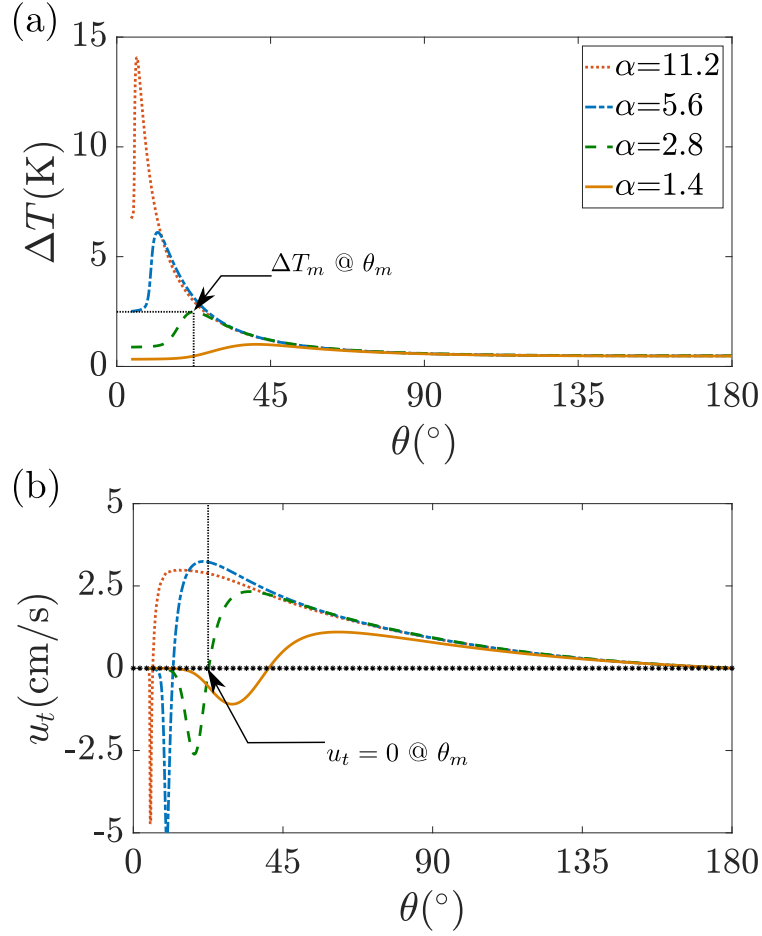


Figure 5: Constant cell electric power ($P = 13.4$ mW) case: interfacial temperature (a) and velocity (b) profile as a function of the angular position for different electrode sizes expressed by $\alpha = R_b/R_e$

258 are seen between the two simulation cases, besides an overall good match being maintained with Equation 9.
 259 Eventually, at $\alpha = 1.2$, both cases seem to deviate from the analytical curve and deliver smaller angular
 260 positions of the temperature hotspot than Equation 9. This is caused by the fact that as the microelectrode
 261 increases in size, as seen from Figure 2, the non-uniformity of the current density, i.e. the ratio of the peak
 262 value at the electrode edge in comparison to the mean value, decreases. Therefore, as α approaches unity,
 263 inner parts of the electrode surface also contribute to the generation of the temperature hotspot, which leads
 264 to the observed slight shift in the position of the temperature maximum towards smaller angular positions.
 265 In summary, the geometrically estimated angular position θ_e of the temperature maximum θ_m based on the
 266 inhomogeneous distribution of the current density at the microelectrode provides a useful estimation of the
 267 position of the temperature maximum θ_m and the resulting interfacial flow characteristics at the bubble
 268 interface at the microelectrode without the need to perform detailed simulations or experimentation. We
 269 would also like to point out here that Equation 9 is only valid for $R_e \leq R_b$, which coincides with the range

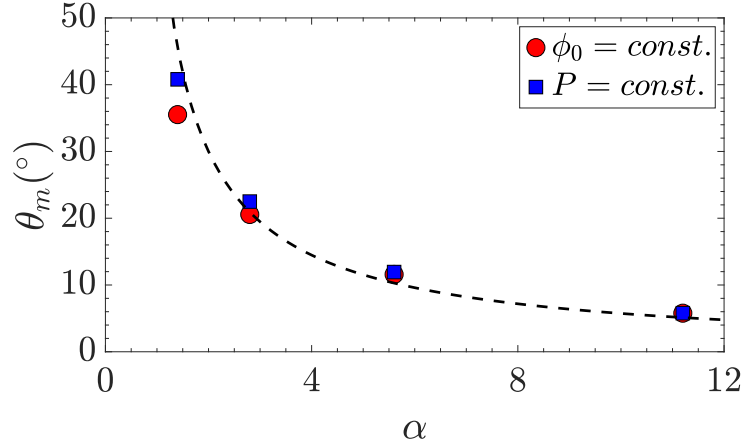


Figure 6: Angular position of the interfacial temperature maximum (θ_m) versus $\alpha = R_b/R_e$ at fixed $R_b = 560 \mu\text{m}$ for the cases of constant cell voltage (red circles) and of constant cell power (blue squares). The dashed curve denotes the geometrical relation from Equation 9.

of studies for the microelectrode case presented here.

3.1.4. Marangoni force

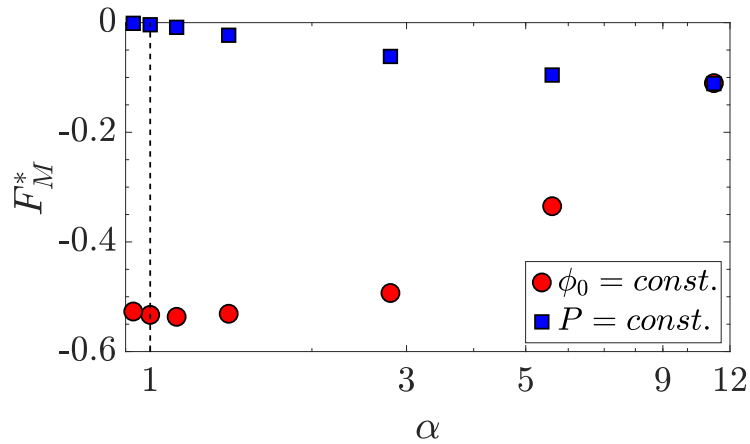


Figure 7: Marangoni force acting on the bubble, shown as normalized by the buoyancy force ($F_M^* = F_M/F_B$), at different values of $\alpha = R_b/R_e$. The x -axis is shown in logarithmic scale to emphasize the behavior at low α . In the case of constant cell voltage, $\phi_0 = 4.5 \text{ V}$. In the case of constant cell power, $P = 13.4 \text{ mW}$.

We now focus on investigating the resulting thermocapillary force on the bubble at different microelectrode sizes. As already mentioned in the introduction, the moment of bubble detachment is determined by the equilibrium of forces acting on the bubble. Therefore, a comprehensive treatment of all the forces acting on a bubble is of importance. A number of different forces may act on the bubble depending on

276 the predominant physical conditions i.e. growth rate, imposed flow condition, orientation relative to gravity,
 277 etc. [34] The relevant static forces acting on an electrogenerated bubble are in general the buoyancy force,
 278 surface tension force, contact pressure force and hydrodynamic force originating from the flow of the elec-
 279 trolyte [42, 43]. Recently it was shown that beside the thermocapillary force [1], an electrostatic force may
 280 also play an important role [44].

281 The thermocapillary force on the bubble is a hydrodynamical force by nature and results from the
 282 interfacial flow around the bubble driven by temperature gradients. In the following, we will denote the
 283 force as the Marangoni force, which can be calculated by integrating the Marangoni shear stress over the
 284 bubble interface (Σ),

$$F_M = - \int_{\Sigma} \tau_M dA. \quad (10)$$

285 Here, dA denotes the related surface differential. Because of the axial symmetry around the bubble, the above
 286 integration results in a force which is acting parallel to the z -axis, i.e. vertically upwards or downwards,
 287 thus influencing the moment of detachment. In the following, we consider the Marangoni force F_M in relation
 288 to the buoyancy force $F_B = gV\Delta\rho$ where g , V and $\Delta\rho$ denote the gravitational acceleration, the bubble
 289 volume and the density difference between the electrolyte and gas, respectively. Thus, we introduce

$$F_M^* = \frac{F_M}{F_B} \quad (11)$$

290 where positive values of F_M^* imply a Marangoni force acting in the direction of buoyancy.

291 Figure 7 shows the dependence of F_M^* on the inverse relative electrode size (α) at a constant cell voltage
 292 and constant cell electric power. Note that the differential local Marangoni force experienced by any part
 293 of the interface is opposite to the direction of local interfacial velocity. According to the velocity profiles
 294 shown in Figure 4(b) and 5(b), the lower part of the bubble ($\theta < \theta_m$) experiences a net Marangoni force in
 295 the upward direction and the upper part of the bubble experiences a net Marangoni force in the downward
 296 direction. As for the microelectrode, the extent of the flow vortex to the left of temperature hotspot is
 297 smaller than that to the right of the temperature hotspot. The integration of Equation 10 gives a net F_M
 298 in the downward direction, hence F_M^* is negative at large α . For the potentiostatic case, as with decreasing
 299 α , the mean current density and thus the heat generation in the electrolyte grows, F_M^* also increases in
 300 magnitude. When decreasing α further, the growing contribution from the left vortex becomes more and
 301 more important, and F_M^* starts to decrease in magnitude near $\alpha \sim 1$. We further see that at $\alpha \sim 1$, due
 302 to very strong heating, the Marangoni force has reached a magnitude of roughly 55% of buoyancy, which
 303 corresponds to a very large mean current density value of 34.8 A/cm².

304 As the electrode size is increased while keeping the total heat generation constant, the temperature
 305 nonuniformity along the interface reduces and the contribution from the two vortices becomes comparable.
 306 Thus, F_M^* decreases with decreasing α , becoming approximately zero at $\alpha \sim 1$.

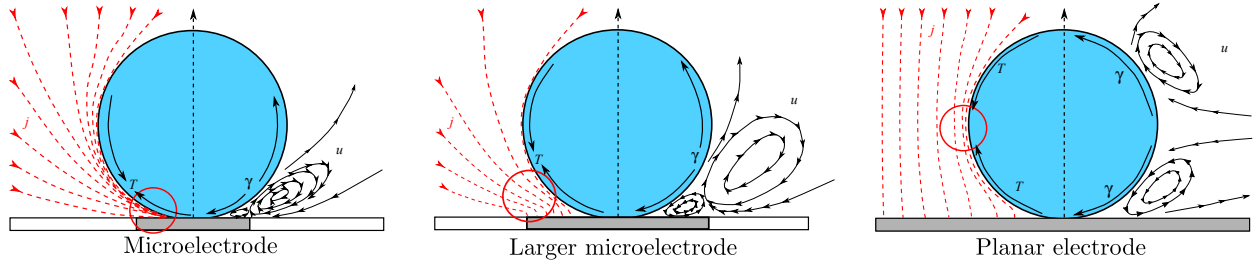


Figure 8: Sketch depicting the qualitative differences in current distribution, position of temperature hotspot (red circle) and resulting thermocapillary flow pattern when the size of the electrode is increased from micro (left) to macro (right). The flow inside the gas bubble and the movement of the interface are not shown.

308 So far we have presented a detailed characterization of the thermocapillary effect on gas bubbles growing
 309 at microelectrodes of different sizes. As larger electrodes are prevalent in industrial processes, an in-depth
 310 understanding of similar phenomena at macroelectrodes is of technological importance. An attempt is made
 311 here to gain an understanding of this kind for the first time. With respect to the modeling, we follow
 312 the simple approach described in detail in Section 2, based on considering single bubble phenomena, and
 313 originating from the previous study of microelectrodes after accounting for differences in length scales and
 314 boundary conditions.

315 Figure 8 schematically displays important qualitative differences of the thermocapillary effect when the size
 316 of the electrode is increased from micro (left) to macro (right) with respect to the bubble size. For the
 317 sake of simplicity, at the macroelectrode only a small part of the electrode is shown, above which a single
 318 bubble evolves. Looking at the distribution of the current density, shown by red dotted lines, important
 319 differences become obvious. At the microelectrode, as discussed before, the current has to squeeze through
 320 a narrow region at the bubble foot, and large current densities occur above the electrode, with a maximum
 321 near its outer edge. In the center of the figure, the intermediate case of a large microelectrode is shown,
 322 where, as discussed before, the temperature hotspot has already moved upward slightly towards a larger
 323 value of θ . At the macroelectrode, however, the situation is changed, as the main geometrical obstacle for
 324 a uniform current flow is now the bubble itself and not the electrode. Here, the current has to pass the
 325 narrower equatorial space between neighboring bubbles. Hence, the maximum of the current density appears
 326 at the bubble's equator. As the position of the temperature hotspot correlates directly with the location of
 327 the maximum current density, the temperature maximum moves from the bubble foot towards the bubble
 328 equator when the size of the electrode is increased from micro to macro.

329 The thermocapillary flow patterns driven at the bubble interface from hot towards cold regions are sketched
 330 in the right half of the subfigures for all three cases. In line with the changing position of the temperature
 331 hotspot, the size and the position of the two counter-rotating vortices driven by thermocapillary stress

332 change accordingly. At the microelectrode, a dominating large vortex brings electrolyte upward along the
 333 interface, and the small vortex above the electrode does not contribute much to the thermocapillary effect.
 334 This small vortex grows in size when the size of the microelectrode is increased and starts contributing to
 335 the Marangoni force on the bubble, as already discussed in the previous section. At the macroelectrode,
 336 eventually, two counter-rotating vortices of almost equal size are therefore expected which advect electrolyte
 337 away from the temperature hotspot at the equator. The ramifications of these qualitative changes are
 338 investigated quantitatively in the following.

339 3.2.1. Temperature and velocity distribution

340 We now study in detail the temperature and velocity distribution near a gas bubble of constant size
 341 ($R_b = 560 \mu\text{m}$) at different values of the bubble coverage Θ of the macroelectrode. In the following, a
 342 potential difference of $\phi_0 = 1 \text{ V}$ is applied between the electrodes. We note that, e.g. for a bubble coverage
 343 of $\Theta = 0.87$, an average current density of 4.9 kA/m^2 is obtained, which is close to typical values of 1–3
 kA/m^2 in related industrial applications [30]. Figure 9(a) shows the temperature distribution in and around

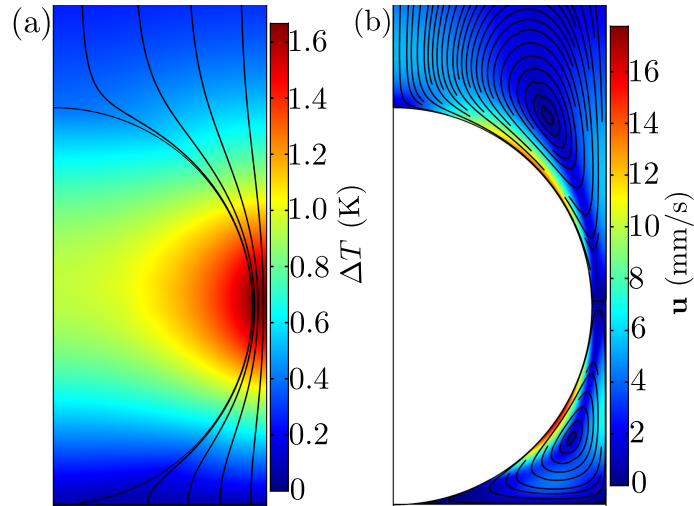


Figure 9: ($\phi_0 = 1 \text{ V}$ and $\Theta = 0.87$) (a) Temperature contours and field lines of the electrical current density. Temperature is maximum at the location of maximum current density near bubble equator. (b) Contours of the electrolyte flow velocity distribution along with velocity streamlines. The electrolyte at the bubble interface flows away from the equator towards both poles.

344
 345 the gas bubble at a bubble coverage of $\Theta = 0.87$. As can be seen from the current lines in the electrolyte, the
 346 electric current must pass around the gas bubble and hence is highly concentrated in the narrow inter-bubble
 347 region near the bubble equator, where the largest current density occurs, in agreement with the expectations
 348 formulated in the previous section. The temperature maximum also occurs at the same spot, as can be seen
 349 from the temperature distribution.

350 Figure 9(b) shows the velocity distribution and the streamlines in the electrolyte. The thermocapillary
 351 flow is driven away from the temperature hotspot, and the electrolyte flows away from the equator towards
 352 either pole. This gives rise to two vortices in the northern and southern hemisphere of the bubble and causes
 353 two interfacial velocity maxima, visible as the red regions in Figure 9(b). It is also to be noted here that the
 354 vortices are not fully symmetric with respect to the equatorial plane. The lower vortex is constrained by
 355 the electrode surface, the bubble interface and the outer boundary of the domain, whereas the upper vortex
 extends upward above the top of the bubble.

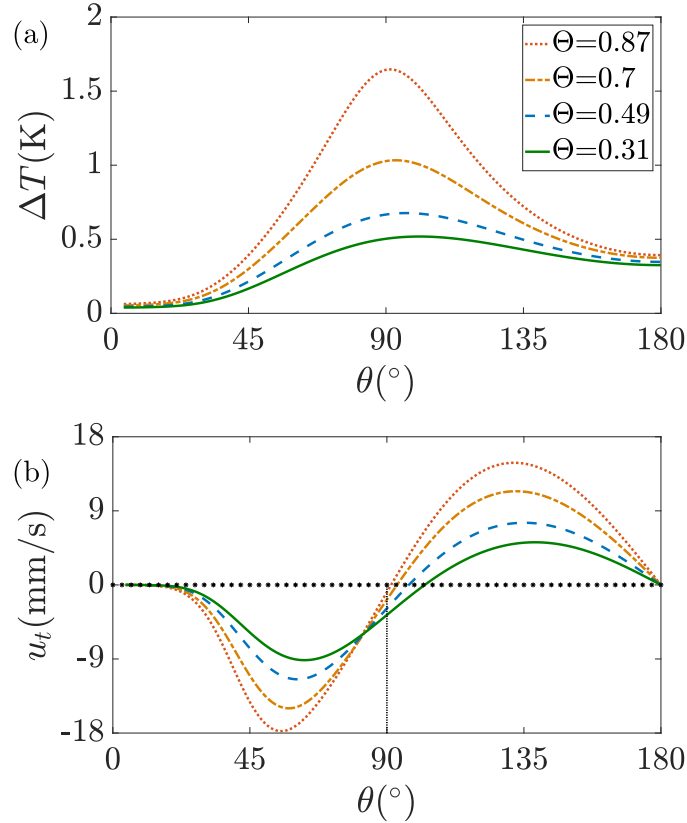


Figure 10: Interfacial (a) temperature and (b) velocity distribution as a function of θ as defined in Figure 1 for different electrode coverage Θ at $\phi_0 = 1$ V. The vertical dashed line marks $\theta = 90^\circ$.

356
 357 Next we study in detail the influence of the bubble coverage on the interfacial temperature and flow
 358 profiles. R_c is varied from 0.6 mm to 1 mm, yielding a range of Θ from 0.87 to 0.31, which, according
 359 to earlier work, provides a realistic range of gas coverage values [45]. Figure 10(a) shows the interfacial
 360 temperature profile as a function of the angular position θ . The occurrence of a temperature maximum
 361 close to the bubble equator ($\theta_m \sim 90^\circ$) is clearly visible in all cases. The temperature maximum also
 362 increases with increasing bubble coverage, as the electric current lines are more densely placed in the inter-
 363 bubble space, causing larger local Joule heating. Figure 10(b) shows the related interfacial velocity profile.

364 Similarly to the microelectrode case discussed in Section 3.1.2, the tangential velocity u_t vanishes at the
365 position of the temperature maximum at θ_m . According to the slopes of opposite sign in the temperature
366 profile left and right of θ_m , interfacial flow in the southern or northern hemisphere is directed downward
367 and upward, respectively, as also shown in Figure 10(b). In this figure, the value of zero tangential velocity
368 $u_t = 0$ and the angular position of the equator $\theta = 90^\circ$ are additionally marked by lines to allow the more
369 accurate identification of the location of the flow reversal (θ_m) in relation to the bubble equator. As can
370 be seen, the temperature hotspot is slightly shifted above the equator at smaller bubble coverage values.
371 Furthermore, it is to be noted that the magnitude of the velocity minimum in the southern hemisphere
372 is larger than the magnitude of the velocity maximum in the northern hemisphere in general. The latter
373 can easily be explained. As the metal electrode at the bottom is a good conductor of heat compared to
374 the electrolyte, the related downward heat flux tends to increase the temperature gradient in the southern
375 hemisphere, leading to a larger velocity magnitude. This larger velocity magnitude also causes enhanced
376 advection of heat at the interface, which leads to a shift in the temperature hotspot above the equator.
377 As increasing the bubble coverage narrows the gap between the bubble equator and domain boundary, the
378 temperature hotspot at the equator increases, and the relative influence of cooling and advection reduces.
379 This is also seen in the two extrema of the velocity profiles, which grow closer to each other in terms of
380 magnitude.

381 3.2.2. Marangoni force on the bubble

382 It is well known from measurements on large planar electrodes that the bubble evolution characteristics
383 depend on the operating current density [45, 46]. At a higher current density, more nucleation sites are
384 activated at the electrode, and thus the bubble coverage increases. Increasing the average current density
385 also reduces the departure diameter and causes early detachment from the electrode surface [47]. In order
386 to discuss the possible influence of thermocapillary effects on these phenomena, we carried out parametric
387 studies to elaborate the influence of varying bubble coverage and bubble size on the Marangoni force under
388 different operating conditions. The results are shown in Figure 11.

389 *Constant bubble radius.* In Figure 11(a) the Marangoni force normalized with the buoyancy force F_M^* (as
390 defined in Section 3.1.4) is shown versus the bubble coverage of the electrode Θ for a gas bubble of fixed
391 size ($R_b = 560 \mu\text{m}$) at a constant cell voltage of $\phi_0 = 1 \text{ V}$. It should be noted first that unlike the case of
392 the microelectrode considered earlier, the Marangoni force is directed upwards, thus advancing the bubble
393 departure. The Marangoni force F_M^* is found to amount to about 2% of the buoyancy force in the range of
394 parameters considered and increases almost linearly with the bubble coverage Θ .

395 As the Marangoni force (F_M) results from the integration of the interfacial temperature gradient along
396 the interface (see Equation 10), the slight asymmetry of the interfacial temperature profile with respect to
397 the equator seen in Figure 10(a) gives rise to a remaining nonzero force F_M . As the temperature gradient

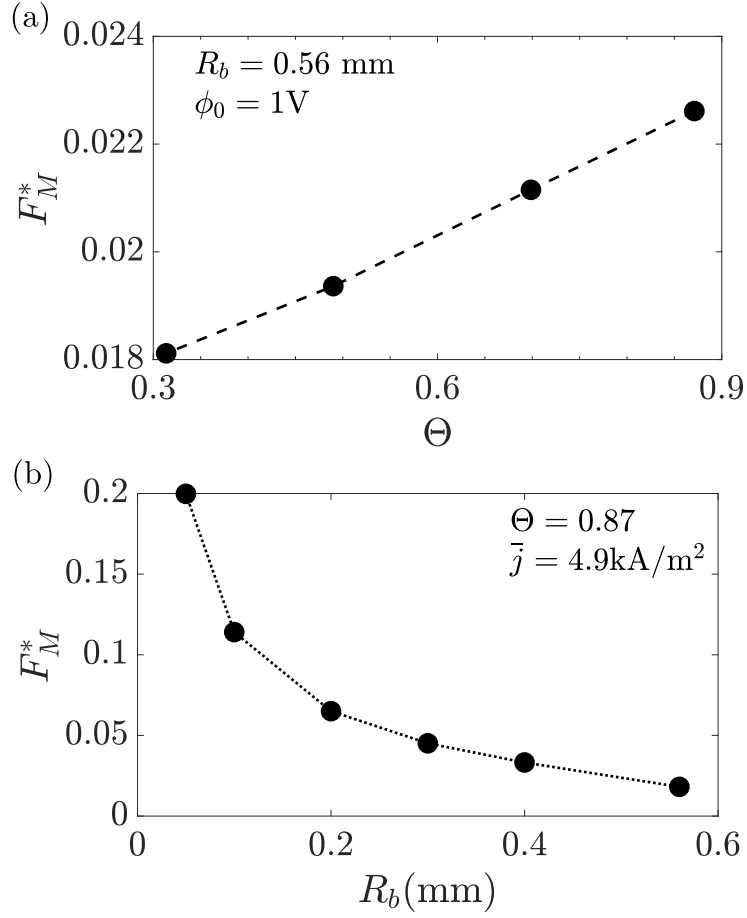


Figure 11: Marangoni force normalized with buoyancy force F_M^* versus (a) bubble coverage Θ at a constant bubble radius $R_b = 560 \mu\text{m}$ and cell voltage $\phi_0 = 1 \text{ V}$ and versus (b) bubble radius R_b at a constant bubble coverage $\Theta = 0.87$ and mean cell current density $\bar{j} = 4.9 \text{ kA/m}^2$.

398 is negative in the region below the equator and larger in magnitude than the positive gradient above the
 399 equator, eventually an upward Marangoni force appears. The almost linear increase in the Marangoni force
 400 as the bubble coverage increases is related to the strong temperature increase of the hotspot near the equator
 401 in conjunction with the heatflux through the electrode, thus retaining a steep temperature profile below the
 402 equator.

403 *Constant bubble coverage.* In order to extend our study to include smaller gas bubble departure sizes,
 404 Figure 11(b) summarizes the Marangoni force F_M^* obtained for different bubble radii R_b at a constant
 405 bubble coverage of $\Theta = 0.87$ and at mean cell current density of $\bar{j} = 4.9 \text{ kA/m}^2$. We would like to point out
 406 here that smaller bubbles have shorter residence times [47]. This was taken into account by adapting the
 407 integration time in the simulations accordingly. The simulation details are summarized in Table 3. Starting

408 out from an integration time of 1 s at $R_b = 560 \mu\text{m}$ in accordance with the constant bubble radius case
 409 considered earlier, the integration time is then linearly decreased along with the bubble size such that for a
 410 bubble of $200 \mu\text{m}$ radius it matches the bubble lifetime of about 0.4 s reported in [48]. Please also note that
 411 for smaller bubbles the contact angle between the bubble and electrode was slightly increased. As can be
 412 seen in Figure 11(b), the Marangoni force F_M^* strongly increases when the size of the bubble reduces. This
 413 behavior is mainly caused by the corresponding variation in the buoyancy force, which scales with the cube
 414 of the bubble size. For a small bubble of $R_b = 50 \mu\text{m}$, the Marangoni force is found to amount to about 20%
 of the buoyancy force.

R_b (μm)	θ_c	Integration Time (s)
50	14.1°	0.15
100	9.9°	0.23
200	7.0°	0.4
300	5.7°	0.57
400	5.0°	0.73
560	4.2°	1.0

Table 3: Bubble radius, contact angle and integration time in the simulation

415

416 4. Conclusions

417 In this study we characterized in detail the thermocapillary flow around electrogenerated bubbles at
 418 electrodes of different sizes, ranging from microelectrodes to large planar electrodes. At microelectrodes, a
 419 detailed analysis of the current density and temperature profiles revealed a clear correlation between the
 420 position of the temperature hotspot at the bubble interface and the upward projection of the outer edge
 421 of the microelectrode. As a result, a double vortex structure of the thermocapillary flow was unveiled
 422 which was overlooked previously [1] because the lower vortex is small at the microelectrodes. This double
 423 vortex structure is also found at larger electrodes. Increasing the electrode size changes the position of the
 424 temperature hotspot, thus increasing the size of the lower vortex and affecting the amplitude and also the
 425 direction of the Marangoni force.

426 At large planar electrodes, multiple bubbles grow simultaneously at random nucleation sites where the
 427 electrical current must pass through the inter-bubble space. The simplified approach we take in order to
 428 gather initial results assumes that the bubbles grow synchronously at a given uniform nucleation density,
 429 meaning that a single bubble can only be considered in the simulations. As a result, the maximum current
 430 density and thus the temperature hotspot are located close to the equatorial inter-bubble region, and a
 431 nearly symmetric double vortex structure is generated near the bubble interface. However, mainly because

432 of the cooling effect of the metal electrode, the interfacial flow of the lower vortex is stronger than that of
433 the upper vortex. Consequently, an upward Marangoni force acts on the bubble, assisting its release, which
434 is the opposite of what is found at the microelectrodes. This clearly helps explain why larger bubbles can
435 be grown on macroelectrodes compared to microelectrodes. At a constant cell voltage, the Marangoni force
436 is found to grow as the bubble coverage of the electrode increases due to higher temperatures occurring in
437 the smaller inter-bubble gaps. For a fixed current density and related large bubble coverage, the force on
438 the bubble is found to get larger when the bubble size is reduced, reaching about 20% of the buoyancy force
439 at $\Theta = 0.87$, $\bar{j} = 4.9$ kA/m².

440 We note here that the quantitative results obtained for the macroelectrode are based on the assumption of
441 uniform bubble distribution, i.e. simultaneous in-phase bubble evolution, and that azimuthal dependencies
442 of quantities originating from neighboring bubbles growing at certain angular positions have so far been
443 neglected. The Marangoni force values obtained for reasonable integration times in our model may further
444 depend on the specific value of the contact angle and neglect more complex aspects such as microbubbles
445 partly covering the cathode. It should also be noted that our results for all electrode sizes naturally depend
446 in quantity on the details of the thermal boundary conditions of the cell. This especially holds true for
447 the metal electrode where the bubble grows, which takes heat out of the electrolyte and thereby shapes the
448 thermocapillary effect. Nevertheless, as this is a common feature, we believe the qualitative findings of the
449 thermocapillary effect are valid in general.

450 In summary, the thermocapillary effect is found to be important for the dynamics of bubbles generated
451 at electrodes under various conditions. A proper inclusion of this effect in future studies may lead to
452 an improved understanding of the instant of the bubble departure and the departure diameter. Finally,
453 appropriate temperature management of the electrodes may be a useful means of improving the efficiency
454 of electrolyzers.

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