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(NH₄)₂IrCl₆ and K₂IrCl₆**

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Antiferromagnetic resonance in the cubic iridium hexahalides $(\text{NH}_4)_2\text{IrCl}_6$ and K_2IrCl_6 L. Bhaskaran ^{1,*}, A. N. Ponomaryov,^{1,†} J. Wosnitzer,^{1,2} N. Khan,³ A. A. Tsirlin ³,
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We report on high-field electron spin resonance studies of two iridium hexahalide compounds $(\text{NH}_4)_2\text{IrCl}_6$ and K_2IrCl_6 . In the paramagnetic state, our measurements reveal isotropic g factors $g = 1.79(1)$ for the Ir^{4+} ions, in agreement with their cubic symmetries. Most importantly, in the magnetically ordered state, we observe two magnon modes with zero-field gaps of 11.3 and 14.2 K for $(\text{NH}_4)_2\text{IrCl}_6$ and K_2IrCl_6 , respectively. Based on that and using linear spin-wave theory, we estimate the nearest-neighbor exchange couplings and anisotropic Kitaev interactions $J_1/k_B = 10.3$ K, $K/k_B = 0.7$ K for $(\text{NH}_4)_2\text{IrCl}_6$, and $J_1/k_B = 13.8$ K, $K/k_B = 0.9$ K for K_2IrCl_6 , revealing the nearest-neighbor Heisenberg coupling as the leading interaction term, with only a weak Kitaev anisotropy.

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Transition-metal compounds with partly filled $4d$ and $5d$ orbitals have recently attracted enormous attention as promising candidates for realizing novel magnetic phenomena, emerging from the interplay between crystal-field effects and spin-orbit interactions [1–3]. In particular, honeycomb magnets with $j_{\text{eff}} = \frac{1}{2}$ moments and bond-anisotropic Kitaev interactions have come under extensive scrutiny due to the possible realization of quantum spin liquid states, characterized by unusual spin dynamics with fractionalized Majorana fermions and flux excitations [4–8].

While the majority of experimental and theoretical studies remains focused on honeycomb materials as the most promising platform for the Kitaev interaction [9–11], there is also a significant interest in detecting anisotropic exchange terms (including the Kitaev interaction) in Ir^{4+} compounds with structures distinct from the honeycomb geometry [12–17]. However, most of the nonhoneycomb iridates studied over the last decade still evade detailed spectroscopic characterization with an unambiguous experimental determination of their interaction parameters. In particular, the absence of large single crystals as well as the notoriously strong neutron absorption by Ir atoms (which is of crucial importance for inelastic neutron scattering studies) and the insufficient energy resolution (in case of resonant inelastic x-ray scattering, RIXS) have often hindered the experimental access to relevant magnetic excitations.

Here we focus on two compounds from the family of Ir^{4+} antiferrofluorites [18–21], $(\text{NH}_4)_2\text{IrCl}_6$ and K_2IrCl_6 , that have been recently revisited by crystallographic and thermodynamic studies [22–24]. These compounds feature Ir^{4+} ions arranged on a face-centered cubic (fcc) lattice with four sublattices [Fig. 1(a)] and distinct long-range superexchange pathways mediated by the covalently bonded halogen ions [Fig. 1(b)]. The presence of possible frustration in fcc lattices is interesting in its own right as it shows an intricate competition of magnetic ground states, even in the absence of Kitaev or any other exchange anisotropy [25–27]. In contrast to many other iridates, these compounds are available as relatively large single crystals amenable to laboratory spectroscopic probes, featuring a cubic symmetry of the molecule that not only ensures the spin-orbit-coupled $j_{\text{eff}} = \frac{1}{2}$ state of the Ir^{4+} ions, but also restricts the number of relevant interaction parameters.

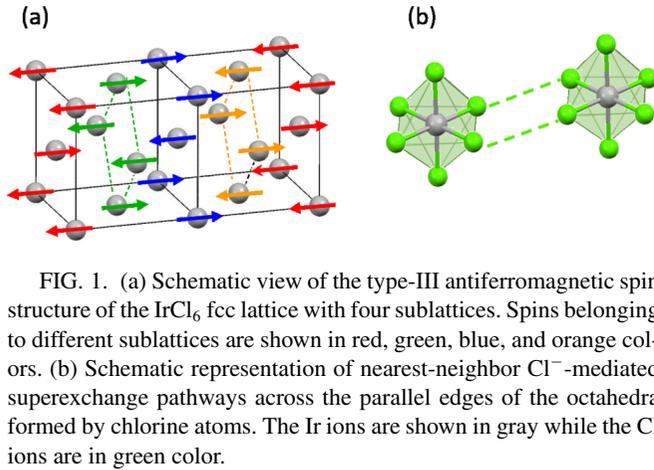
In the following we present electron spin resonance (ESR) studies of $(\text{NH}_4)_2\text{IrCl}_6$ and K_2IrCl_6 , revealing the presence of two gapped magnon modes in each of the compounds. Employing linear spin-wave-theory calculations, we estimate the spin-Hamiltonian parameters and, consequently, establish the main interaction terms.

Single crystals of $(\text{NH}_4)_2\text{IrCl}_6$ and K_2IrCl_6 were grown from solutions prepared by dissolving commercially available powders (Alfa Aesar) in deionized water and keeping the solutions at 60°C for several days. The resulting crystals had well-defined hexagonal (111) faces and sizes of $\sim 2\text{--}3$ mm³. Magnetization measurements revealed magnetic ordering transitions at 2.15 K for $(\text{NH}_4)_2\text{IrCl}_6$ and 3.1 K for K_2IrCl_6 , in agreement with previous studies [20,22,23,28].

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High-field electron spin resonance (ESR) measurements were performed employing a transmission-type ESR spectrometer (similar to that described in Ref. [29]), in magnetic fields up to 16 T. Measurements were done in the frequency range of 60–400 GHz, using a set of VDI microwave-chain radiation sources (product of Virginia Diodes, Inc., USA). An InSb hot-electron bolometer (QMC Instruments Ltd., UK) was used to record the spectra. We measured single crystals in the Faraday configuration with magnetic field $H \parallel [111]$ and in the Voigt configuration with $H \perp [111]$. For the powder samples we confined the specimens by a binding agent such as high vacuum grease. The powders were obtained by crushing single crystals to ensure consistency between single-crystal and powder measurements. The stable free-radical molecule DPPH (2,2-diphenyl-1-picrylhydrazyl) was used as a frequency-field marker.

ESR is traditionally recognized as a powerful tool to probe crystal-field effects in solids. A very sensitive test of the presence of noncubic distortions in covalently bound $[\text{IrCl}_6]^{2-}$ complexes is provided by a g -factor anisotropy [18]. In Fig. 2 we show powder and single-crystal spectra obtained for $(\text{NH}_4)_2\text{IrCl}_6$ (a) and K_2IrCl_6 (b) at a temperature of 50 K. Both powder spectra were fit using a Lorentzian function with $g = 1.79(1)$, and linewidths of 0.93 and 1.23 T for $(\text{NH}_4)_2\text{IrCl}_6$ and K_2IrCl_6 , respectively. These parameters perfectly agree with the simulation results for the single crystals along both $H \parallel [111]$ and $H \perp [111]$, revealing isotropic paramagnetic g factors, and thus evidencing the cubic symmetry for both compounds. The reduction of the g factor from the free-spin value ($g = 2$) can be attributed to the covalent nature of the Ir and Cl bonds [30,31]. Large covalency of the Ir^{4+} halides was indeed confirmed by recent RIXS studies [24], detecting also minor deviations from the $j_{\text{eff}} = \frac{1}{2}$ state [23], despite the absence of any macroscopic symmetry lowering [22].

Upon cooling, the ESR spectra for $H \parallel [111]$ exhibit significant broadening, evidencing enhancement of magnetic correlations, with the maximum in the vicinity of T_N (Figs. 3 and 4). On further decreasing the temperature, the ESR linewidth rapidly decreases, revealing the onset of long-range ordering below T_N . This transition into the ordered state also results in a pronounced low-temperature shift of the ESR field positions.

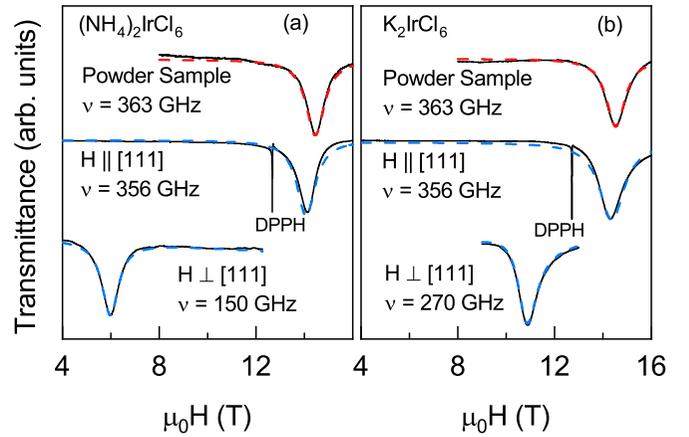


FIG. 2. Normalized ESR spectra measured in single-crystalline ($H \parallel [111]$ and $H \perp [111]$) and powder samples of (a) $(\text{NH}_4)_2\text{IrCl}_6$ and (b) K_2IrCl_6 at 50 K. The spectra are offset for clarity. Lorentzian fits to the powder sample are shown by the dashed red lines, while simulation of the single-crystal spectra are shown by the dashed blue lines.

Two antiferromagnetic resonance (AFMR) modes A_1 and A_2 were observed in the magnetically ordered state (Figs. 5 and 7). Selected AFMR spectra measured at 1.5 K with magnetic field applied along the $[111]$ direction are shown in Fig. 6 for $(\text{NH}_4)_2\text{IrCl}_6$ and in the inset of Fig. 7 for K_2IrCl_6 .

The frequency-field dependencies of the modes A_1 and A_2 can be described using the equation

$$h\nu = \Delta \pm g_{\text{eff}}\mu_B B, \quad (1)$$

where h is the Planck constant, ν represents the excitation frequency, g_{eff} is the effective g factor, and μ_B is the Bohr magneton. From this linear fit we obtain the zero-field magnon gaps $\Delta = 235 \pm 10$ and 295 ± 10 GHz (which correspond to 11.3 and 14.2 K; $g_{\text{eff}} = 0.8$) for $(\text{NH}_4)_2\text{IrCl}_6$ and K_2IrCl_6 , respectively. For both materials, mode A_1 shows a linear increase in the resonance-field position, while some deviation from the linear dependence was observed for mode A_2 in high

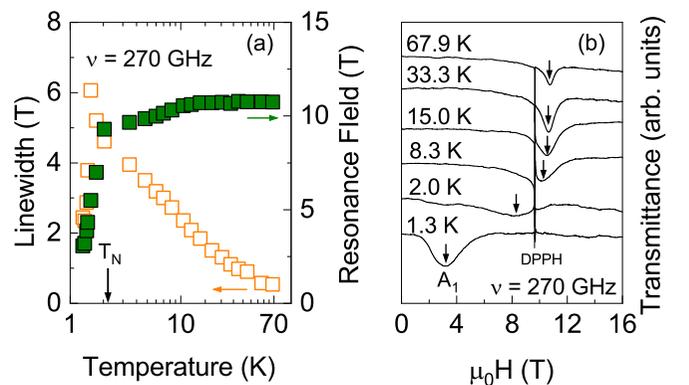


FIG. 3. (a) Temperature dependence of the resonance field (closed squares) and linewidth (open squares) measured in $(\text{NH}_4)_2\text{IrCl}_6$ at 270 GHz. (b) Examples of normalized ESR spectra recorded at 270 GHz and different temperatures. The spectra are offset for clarity. Magnetic field is applied along the $[111]$ direction.

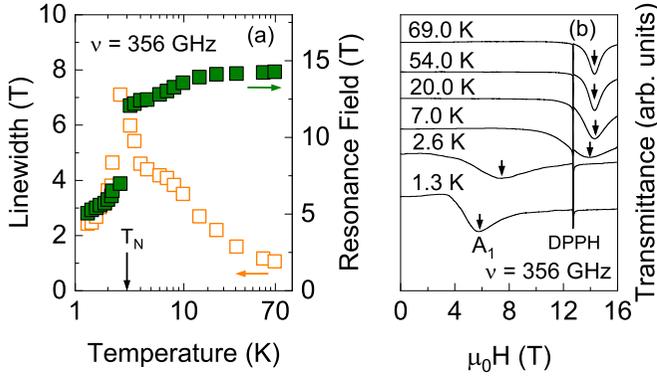


FIG. 4. (a) Temperature dependence of the resonance field (solid squares) and linewidth (open squares) measured in K_2IrCl_6 at 356 GHz. (b) Examples of normalized ESR spectra recorded at 356 GHz and different temperatures. The spectra are offset for clarity. Magnetic field is applied along the [111] direction.

fields. Noticeably, the mode A_2 disappears above ~ 6 T. This field corresponds to a field-induced transition reported for K_2IrCl_6 [32], whereas in $(\text{NH}_4)_2\text{IrCl}_6$ the changes in applied field appear to be limited to a domain repopulation wherein the number of domains with magnetic moments oriented perpendicular to the applied field increases [33].

A general form of spin-spin interactions in magnetic systems with an fcc crystal structure was discussed by several authors [13,22,34,35]. Apart from the Heisenberg exchange, it includes symmetry-allowed anisotropic terms typical for materials with strong spin-orbit coupling. According to an *ab initio* calculation [22] two strongest spin-spin interactions in $(\text{NH}_4)_2\text{IrCl}_6$ and K_2IrCl_6 are the Heisenberg exchange $J_1 > 0$ and the Kitaev interaction $K > 0$ for the nearest-neighbor (nn) pairs of Ir ions. In addition, a weak next-nearest-neighbor (nnn) exchange $J_2 > 0$ is necessary to explain the experimentally observed type-III antiferromagnetic order [36]. Accordingly, we consider the following Hamiltonian for effective $S = 1/2$ moments of iridium ions:

$$\hat{\mathcal{H}} = \sum_{(ij)}^{\text{nn}} (J_1 \mathbf{S}_i \cdot \mathbf{S}_j + K S_i^\gamma S_j^\gamma) + J_2 \sum_{(ij)}^{\text{nnn}} \mathbf{S}_i \cdot \mathbf{S}_j, \quad (2)$$

where \mathbf{S}_i and \mathbf{S}_j are spin-1/2 operators at site i and j , respectively. In the anisotropic Kitaev term, γ is one of the cubic axes (x, y, z) that is orthogonal to a given bond.

The Heisenberg fcc antiferromagnet with only the nearest-neighbor interactions has highly degenerate classical ground states [37]. A small positive next-nearest-neighbor exchange J_2 lifts this degeneracy in favor of the type-III magnetic structure described by the propagation vector $\mathbf{Q} = (2\pi/a, \pi/a, 0)$ [38] [note that $\mathbf{Q}' = (0, \pi/a, 2\pi/a) = -\mathbf{Q} + \mathbf{G}$, where \mathbf{G} is a reciprocal lattice vector]. In addition, the anisotropy $K > 0$ locks magnetic moments in the $(0,1,0)$ direction:

$$\mathbf{S}_i = \sqrt{2} S \hat{\mathbf{y}} \cos(\mathbf{Q} \cdot \mathbf{r}_i \pm \pi/4). \quad (3)$$

Together with two other equivalent \mathbf{Q} , obtained by permutation of $Q_{x,y,z}$, there are in total six domains for the type-III collinear structure.

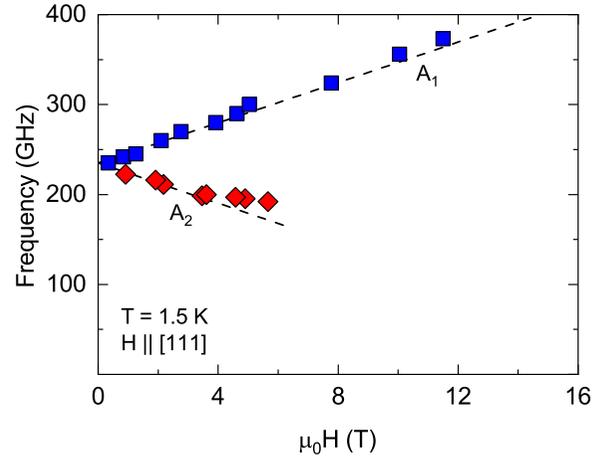


FIG. 5. Frequency-field diagram of ESR excitations in $(\text{NH}_4)_2\text{IrCl}_6$ measured at 1.5 K with magnetic field applied parallel to the [111] direction. The dashed lines represent linear fits using Eq. (1).

Following a recent theoretical study of the excitation spectra in fcc antiferromagnets [26], we have performed linear spin-wave calculations for the Hamiltonian (2) with $J_2, K > 0$. The ESR response corresponds to long wavelength excitations with $\mathbf{k} \rightarrow 0$. Accordingly, the ESR spectrum is formed by two degenerate pairs of gapped magnons with the zero-field excitation energies:

$$\Delta_l = 2\sqrt{KJ_2}, \quad \Delta_u = 2\sqrt{4KJ_1 + 2K^2 + KJ_2}. \quad (4)$$

Note that the size of the low-energy gap Δ_l is determined by both K and J_2 , while the upper gap Δ_u depends mainly on the strength of the Kitaev interaction. Moreover, in the absence of K both gaps vanish, while at $J_2 \rightarrow 0$ they have substantially different magnitudes.

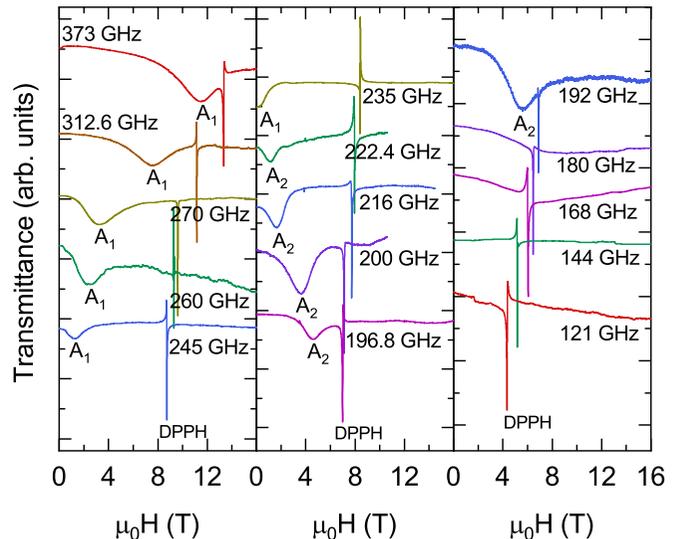


FIG. 6. Examples of normalized ESR spectra for $(\text{NH}_4)_2\text{IrCl}_6$ at different frequencies and $T = 1.5$ K with $H \parallel [111]$. The spectra are offset for clarity.

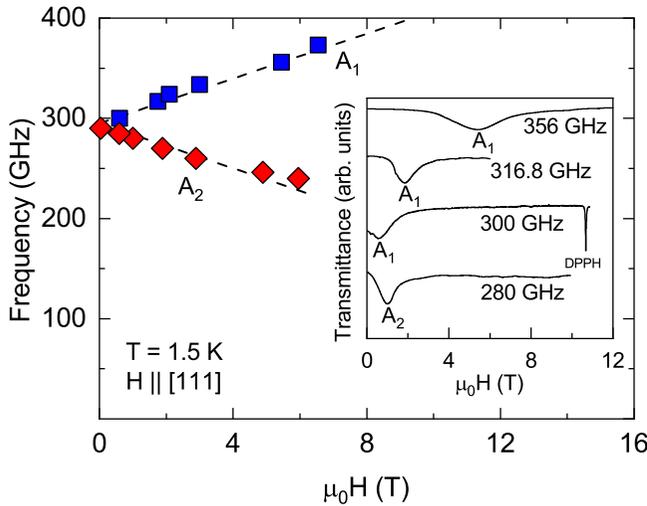


FIG. 7. Frequency-field diagram of ESR excitations in K_2IrCl_6 measured at 1.5 K with magnetic field applied parallel to the [111] direction. The dashed lines represent linear fits using Eq. (1). In the inset, examples of normalized ESR spectra for K_2IrCl_6 at different frequencies and $T = 1.5$ K with $H \parallel [111]$ are shown. The spectra are offset for clarity.

The next-nearest-neighbor isotropic exchange coupling was recently estimated from the *ab initio* calculation as $J_2/k_B \simeq 0.2$ K for both $(\text{NH}_4)_2\text{IrCl}_6$ and K_2IrCl_6 [22,33]. In addition, we use the expression for the Curie-Weiss temperature [39]

$$\theta_{\text{CW}} = 3J_1 + K + \frac{3}{2}J_2. \quad (5)$$

Experimental values for θ_{CW}/k_B are 32 K for $(\text{NH}_4)_2\text{IrCl}_6$ [33] and 42.6 K for K_2IrCl_6 [22]. They are obtained by fits to the magnetic-susceptibility data in the 100–400 K and 150–400 K range, respectively. The corresponding effective moment of $1.73 \mu_B$ confirms that mostly the ground-state $j_{\text{eff}} = \frac{1}{2}$ doublet is occupied in this temperature range. Using Eqs. (4) and (5) we estimate $J_1/k_B = 10.3$ K and $K/k_B = 0.7$ K for $(\text{NH}_4)_2\text{IrCl}_6$, and $J_1/k_B = 13.8$ K and $K/k_B = 0.9$ K for K_2IrCl_6 ($K/J_1 \approx 6\%$ – 7%). The exchange coupling J_1 is stronger for K_2IrCl_6 compared to $(\text{NH}_4)_2\text{IrCl}_6$, due to

the lattice parameter difference ($a = 9.77$ vs 9.87 Å [22,33], respectively), with the respective negative pressure reducing magnetic interactions in $(\text{NH}_4)_2\text{IrCl}_6$. It is worth noting that our experimental value of K is much smaller than the 5 K reported in Ref. [22]. This discrepancy may indicate the importance of Hund's coupling on the Cl ligand, an effect that has been neglected in the superexchange theory used in Ref. [22] and generally leads to a ferromagnetic contribution, which counteracts antiferromagnetic superexchange. Similar effects were previously reported in Cu^{2+} halides [40].

Using the parameters, as obtained above, the size of low-energy gaps was also estimated, yielding $\Delta_l/k_B \approx 1$ K. Our thorough search did not reveal the low-energy AFMR modes (note also that our ESR probe has a cut-off frequency limit of 60–70 GHz that is higher than the expected size of Δ_l). The absence of the low-energy ESR modes, which directly depends on J_2 , may indicate, on the other hand, that the next-nearest-neighbor exchange in these compounds is very small. In such a case the quantum order-by-disorder effect can play a significant role in the Kitaev fcc antiferromagnets [41].

Summarizing, we presented systematic ESR studies of the two iridium hexahalide compounds $(\text{NH}_4)_2\text{IrCl}_6$ and K_2IrCl_6 . In the paramagnetic state, our measurements reveal isotropic g factors $g = 1.79(1)$ for Ir^{4+} ions, confirming their cubic symmetries. By measuring the ESR spectra in the ordered state, we were able to determine the nearest-neighbor Heisenberg exchange J_1 and the Kitaev interaction K for both materials, revealing $K \ll J_1$. The intriguing possibility of the realization of the quantum order-by-disorder effect as well as details of the high-field behavior of magnetic excitations in these frustrated compounds deserves further experimental and theoretical studies.

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