

**Development of a high-speed ultrasonic tomography system for  
measurements of rising bubbles in a horizontal cross-section**

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1 Development of a high-speed ultrasonic tomography system for measurements of  
2 rising bubbles in a horizontal cross-section

3

4 Abstract

5 The present study deals with high-speed ultrasonic tomography (UT) as a powerful tool to characterize  
6 the behavior of multiphase flows. A major goal of the work is to improve the temporal resolution for  
7 the detection of transit flow structures and time-dependent phenomena such as the incidence of rising  
8 gas bubbles. A special transducer with a wide divergence angle of  $110^\circ$  and a vertical height of the  
9 measurement volume of approx. 4 mm was developed and tested. The system thus enables the  
10 acquisition of cross-sectional images at a frame rate of up to 1,000 frames/s. Scatter noise was eliminated  
11 using a time series filtering method. This UT system was applied to a chain of gas bubbles rising in a  
12 cylindrical container with an internal diameter of 50 mm. The measurement system provides qualitative  
13 observations of the turbulent dynamics of bubbly flows including bubble-bubble interactions, such as  
14 the coalescence of individual bubbles.

15

16 Keywords: full-matrix capture, reflection mode, time-series filtering, pseudo three-dimensional image,  
17 bubble column, large divergence-angle transducer

## 1 1. Introduction

2           Two-phase flows are widely used in many industrial applications. Knowing how gas bubbles  
3 move and interact in a liquid is an extremely important prerequisite for developing suitable strategies  
4 for efficient and safe industrial processes and for achieving optimal product quality. As the bubble  
5 motion strongly depends on the shape and the size of the bubble and/or the distance between two  
6 neighboring bubbles, the evaluation of the instantaneous gas distribution, the frequency of passing  
7 bubbles and the measurement of bubble size, shape and velocity provide important and valuable  
8 information for a better understanding of the dynamics of two-phase flows. To this end, numerous  
9 studies have already been carried out on bubble movement for single bubbles and bubble plumes [1, 2].  
10 Sanada et al. [3] reported that trajectories of bubbles released continuously at the injector depend on  
11 the detachment frequency. . The dispersion of the bubble position increases with increasing frequency,  
12 since the distance between successive bubbles decreases and the ascending bubble is influenced to a  
13 greater extent by the wake of the leading bubble. . Detailed knowledge about bubble-bubble interactions  
14 or the effects occurring in the turbulent wakes of the bubbles is important for interpreting the differences  
15 in behavior between a single bubble and bubble plumes [4].

16           Further investigations are required for two-phase flows particularly in opaque fluids such as

1 liquid metals. So far, only few data exist for this, as optical measurement methods cannot be used here  
2 due to the non-transparency. Previous experimental studies were performed [5-7] using X-ray and  
3 neutron radiographies for flow visualization. However, the size of the flow channel is limited depending  
4 on the radiation attenuation by the working fluid, hence, investigations in gallium alloys have been  
5 conducted in rectangular channels with thicknesses of less than 20 mm.

6 Various tomography techniques based on different physical principles, such as X-ray or  
7 neutron radiation [8, 9], electrical conductivity or capacitance [10], and ultrasonic transmission or  
8 reflection [11, 12], have been developed. Applicability, efficiency and resolution of these techniques  
9 varies depending on the properties of the fluids to be investigated. Ultrasonic techniques represent a  
10 highly effective tool in the process industry [13] as they can be applied to opaque fluids and are easy to  
11 use. The propagation of ultrasonic waves in solids and liquids are affected by reflection, diffraction,  
12 scattering, and transmission. The resulting effects can be exploited for measurement purposes.  
13 Reflection and diffraction methods rely on echo intensity detection and the time-of-flight (TOF)  
14 measurements of pulses and are applied for non-destructive testing within materials. The transmission  
15 technique is widely used in flow meters for calculating the volumetric flow rate from the TOF between

1 two sensors. Changes in the signal attenuation and the wave frequency are also analyzed. A suitable  
2 arrangement of a multitude of sensors combined with appropriate data evaluation is the basis of  
3 ultrasonic tomography (UT), which can be employed to obtain two-dimensional (2D) or three-  
4 dimensional (3D) information regarding the characteristic structure of two-phase flows [14, 15]. The  
5 transmission-mode tomography relies on measuring changes in the properties of transmitted ultrasonic  
6 pulses, such as the signal intensity and the TOF between the transducers placed on the circumference of  
7 the measuring domain. Rahiman et al. [16] developed a system using fan-shaped transducers and  
8 demonstrated its capability by succeeding to identify the two-phase flow regime. The basic principle of  
9 reflection-mode tomography was developed based on the amplitude-mode (A-mode) ultrasonic array  
10 technique [17, 18]. This involves the coherent summation of the echo signals received at each transducer  
11 and is generally referred to as acoustic back projection. Langener et al. [19] developed a system to  
12 measure the cross-sectional void distribution in two-phase flows using the reflection method. Thirty-  
13 two transducers with a divergence angle of  $100^\circ$  were set on the circumference of a pipe with an inner  
14 diameter of 53 mm. The bubble movement was successfully detected at 62.5 frames/s. Langener et al.  
15 [20] developed a ray-tracing method that enabled the evaluation of multiple scattering events, which

1 often produce artifacts in two-phase flow measurements.

2           Ultrasonic field distribution is an important parameter which has to be taken into account for  
3 ensuring satisfying results in UT measurements. Increasing the divergence angle of the transmitters  
4 increases the measuring domain. Schlaberg et al. [21] developed large divergence-angle transducers for  
5 reflection-mode applications. They designed a transducer with a divergence angle of  $70^\circ$  and achieved  
6 a reconstruction rate of 100 frames/s, using 36 transducers on a 100 mm pipe measurement target. The  
7 authors also developed an imaging technique using a fan-shaped beam profile [22]. Appropriate  
8 transducers for UT systems have also been investigated by Gai et al. [23]. Xu and Xu [24] developed a  
9 UT system based on both the transmission and the TOF method to monitor bubbly flows. They used six  
10 half-cylindrical transducers with a divergence angle of  $180^\circ$  for the pulse emission and reception, along  
11 with 36 additional rectangular transducers for pulse reception. It was shown that bubble rising motion  
12 could be detected monitored with a time resolution of 4.8 ms in a circular vessel with an inner diameter  
13 of 187 mm. The same measuring system was tested also for flow regime identification in a horizontal  
14 pipe [25]. Li et al. [26] analyzed the effect of the divergence angle of an ultrasonic transducer on the  
15 signal amplitude in transmission-mode tomography. Although the side-lobe signal amplitude is typically

1 not high compared to that of the main lobe, they utilized the weaker signal amplitude in the side lobe  
2 region and showed that wider divergence angles yielded better reconstructed images of the phantom  
3 outlines.

4 High-speed tomography is useful for obtaining 3D information on bubble movement. Cross-  
5 sectional images of the gas-liquid interfaces are reconstructed using the corresponding echo signals  
6 received at the transducers. The scanning time for the cross-sectional information determines the  
7 temporal resolution of the image. The improvement of the temporal resolution is one of the relevant  
8 topics under consideration for high-speed UT. The measuring principle consists of emitting an ultrasonic  
9 pulse from a single transducer while the resulting echo signals are received by an arrangement of  
10 multiple sensors. The pulse emission interval selected should be longer than the TOF for each sensor.  
11 Cross-sectional information is obtained by repeating pulse emission and reception at all transducers.  
12 Thus, the reduction of the number of transducers is a key parameter for improving the temporal  
13 resolution. For achieving a reconstructed image with only a small number of transducers, Li and Hoyle  
14 [27] proposed the application of spectral analysis. Yang et al. [22] showed that the divergence angle is  
15 an important parameter for reducing the number of transducers. Tan et al. [28] developed a tomography

1 system to measure two-phase flow using both the transmission- and reflection-mode methods. It  
2 comprises 16 ultrasonic transducers and can successfully obtain cross-sectional images at up to 625  
3 frames/s. Rahiman et al. [29] developed a 3D reconstruction method for bubble movement. They used  
4 32 transducers with a divergence angle of  $95^\circ$  and captured cross-sectional images at 59.7 frames/s. It  
5 was shown that the bubble shape and 3D interactions could be detected. However, the temporal  
6 resolution of 16.75 ms was insufficient for measuring bubble movements, causing a distinct measuring  
7 uncertainty with respect to the positions of the interface.

8           The objective of this study is the development of a high-speed UT system for evaluating bubble  
9 position and bubble shape of continuously released bubbles in a circular pipe. A large divergence-angle  
10 transducer with a half-cylindrical shape was developed to generate a fan-shaped beam. The measuring  
11 system was tested by studying stationary rods, moving spheres and rising bubbles in a column with an  
12 inner diameter of 50 mm. The developed system generates pseudo-3D images at very high frame rates.  
13 Shapes of the bubbles are reconstructed from the time-series data using a time-filtering method. The  
14 results presented here demonstrate the applicability of the measuring system for reconstructing the  
15 behavior of bubble chains in a horizontal cross-sectional area.

16

17 2. Experimental setup

1            Fig. 1 shows a schematic of the test section. The test section was made of an acrylic resin pipe  
2            with an inner diameter of 50 mm and a total height of 240 mm. The transducers were set at a vertical  
3            position that was 140 mm from the bottom. The container was filled with water up to a height of 210 mm.  
4            Argon gas was injected through a needle with an inner diameter of 1 mm. The argon flow rate was  
5            controlled using a mass flow controller (model: 1179BX52CM1BV, MKS Instruments Deutschland  
6            GmbH), covering a flow range of up to 500 sccm (standard cubic centimeter per minute, volumetric  
7            flow rate at 0 °C under 1 atm) and with an accuracy of  $\pm 1.0\%$  (related to full scale). Eight transducers  
8            whose properties are described in the section 4 were fixed equidistantly on the circumference of the pipe  
9            every 45° using O-rings. The fan-shaped piezoelectric elements protruded approximately 3 mm from  
10           the inner wall of the container. To accurately determine the sensor position, the TOF between each pair  
11           of sensors is measured before beginning the experiments for the container filled with water. Based on  
12           the relative distance between the sensors, the sensor positions were calculated under the assumption that  
13           the sensor installation angles were accurate. Synchronized measurements were performed using a high-  
14           speed camera (model: FASTCAM-1024PCI model 100K, Photron Ltd.) along with the UT to evaluate  
15           the reconstructed results.

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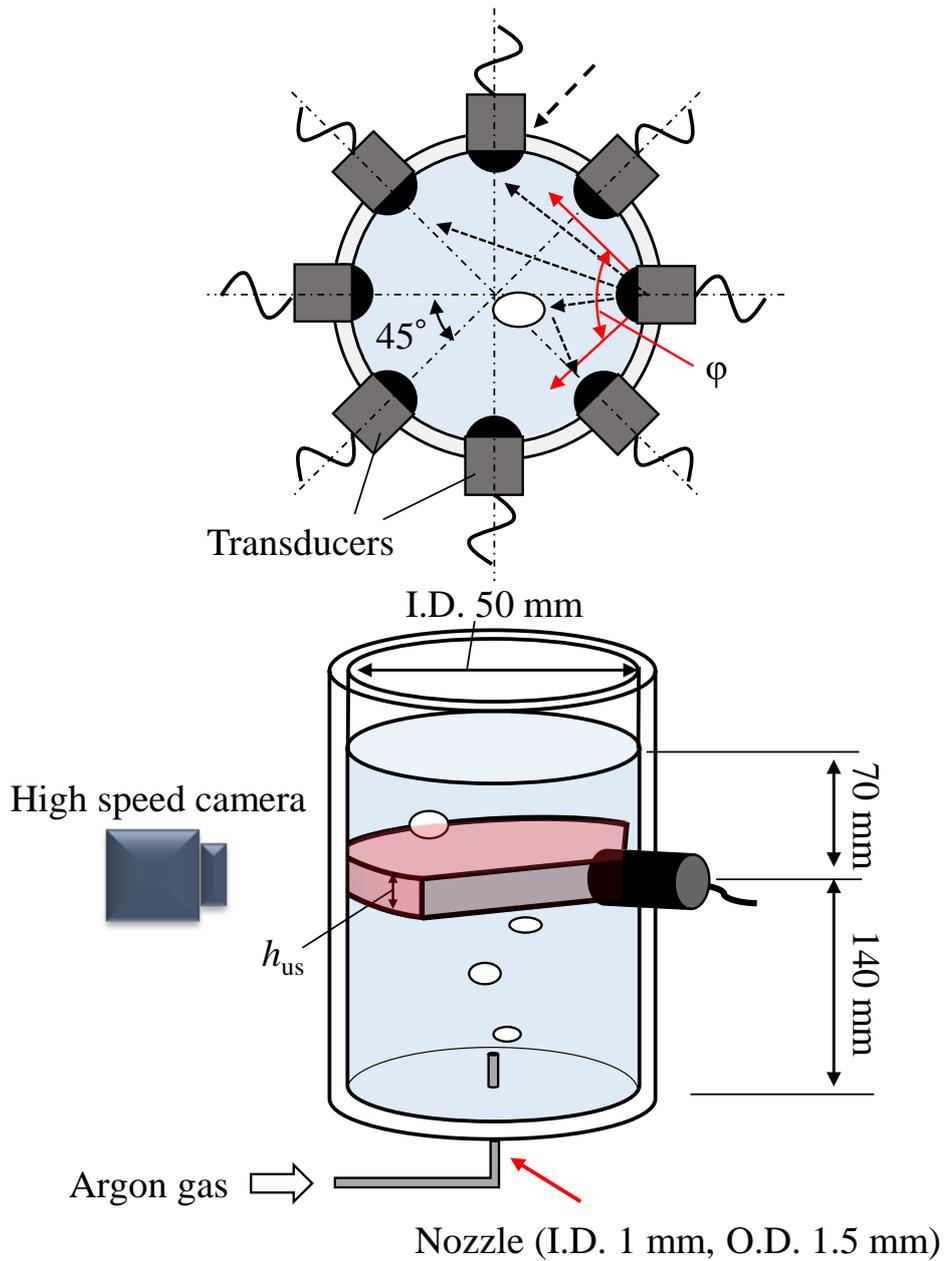


Fig. 1 Schematic representation of the test section and sensing area for reflection-mode tomography using a large divergence-angle transducer with the divergence angle  $\phi$  and the lateral dimension  $h_{us}$ .

1

2

3 3. Selection of essential system parameters

4 For designing the measuring system, three important system parameters have to be considered

1 regarding the choice of the transducers and the related ultrasonic characteristics: the number of  
2 transducers,  $N_{\text{tdx}}$ ; the ultrasonic divergence angle,  $\varphi$ ; and the lateral dimension of the ultrasonic,  $h_{\text{us}}$  as  
3 shown in Fig. 1. In general, a larger number of sensors  $N_{\text{tdx}}$  yields a better image quality of the  
4 reconstructed two-phase flow structures in the cross-sectional image [22]. On the other hand,  $N_{\text{tdx}}$  also  
5 directly affects the temporal resolution of the measurement,  $\Delta t$ , as follows:

$$\Delta t = T_p \times N_{\text{tdx}} \quad (1)$$

6 where  $T_p$  is the time offset for serial actuation of the transducers. The ultrasound signal is emitted from  
7 a single transducer, and the echo signal is received at a number of transducers. The minimum  $T_p$  should  
8 be set taking into account the distance between the transducer and the object to be measured and the  
9 speed of sound in that medium.  $\Delta t$  should be as short as possible to prevent motion blur of the moving  
10 objects in the reconstructed image. From this perspective, a compromise between acceptable  
11 reconstructed image quality and optimal temporal resolution must be found when choosing  $N_{\text{tdx}}$ .  
12 Reducing  $N_{\text{tdx}}$  effectively reduces  $\Delta t$ , but also leads to an incomplete target outline and/or noisy cross-  
13 sectional images. A lowering of  $N_{\text{tdx}}$  can be partially compensated by a simultaneous increase of the  
14 divergence angle  $\varphi$  [22]. The lateral dimension of the ultrasonic beam,  $h_{\text{us}}$ , determines the measuring

1 volume and, hence the image resolution. It should be spatially constant to form a uniform measurement  
2 volume. If  $h_{us}$  is much larger than the target objects, it may be difficult to distinguish between individual  
3 objects at the same cross-sectional position if several objects occur simultaneously within the  
4 measurement volume. This is an essential argument for choosing a smaller value of  $h_{us}$  for reflection  
5 mode tomography. However, the application of a transducer with a small  $h_{us}$  relative to the moving  
6 distance of the target objects during  $\Delta t$  is problematic, since in this case the movement of the target  
7 objects to be detected within the measurement plane during the time span  $\Delta t$  can no longer be neglected.  
8 A suitable combination of both parameters must therefore be selected, taking into account the velocity  
9 and size of the target objects.

10           The value of the TOF must be at least approx.  $67 \mu s$  in the pipe with an inner diameter of 50  
11 mm, as this is the time span for a round trip of the ultrasonic pulse given a sound velocity of 1,500 m/s  
12 at 25 °C. In order to adequately take into account possible multiple reflections in the pipe, a value of the  
13 time offset  $T_p$  of more than  $100 \mu s$  was specified. The typical size of the measurement targets, *i.e.*,  
14 bubbles, was of the order of several mm. For a water column at rest, bubble velocities less than 0.5 m/s  
15 can be expected. The use of 8 sensors and the choice of  $T_p = 125 \mu s$  results in a temporal resolution of

1  $\Delta t = 1$  ms. If the bubble velocity is assumed to be 0.5 m/s, the bubbles move a distance of 0.5 mm during  
2 the measurement. If  $h_{\text{us}}$  is much smaller than the bubble size, bubble detection may be difficult because  
3 the deformation of the interface can produce interfering instantaneous reflections. Therefore,  $h_{\text{us}}$  has to  
4 be of the same order of magnitude as the target size.

5           The detection of the liquid–gas interface position relies on the reflection of the emitted pulse  
6 at the interface which produces the echo signal which is received at the receivers. The echo signal from  
7 the bubble interface is propagating in different directions and can be obtained at the multiple transducers  
8 set on the circumference of the pipe. This information obtained at different receiving transducers is used  
9 to identify the bubble shape. Therefore, the area cross-section of the pipe covered by all of the installed  
10 transducers should be as large as possible to deliver sufficient data for the image reconstruction. Fig. 2  
11 displays fractions of the area covered by eight transducers for different divergence angles  $\varphi$ . If the  
12 fraction is 1 at a position in the measurement area, ultrasonic pulses may reach the position of all  
13 transducers when there is no obstacle to the ultrasound propagation along the beam path. The figure also  
14 shows that a divergence angle of approximately  $120^\circ$  is appropriate for the measurement.

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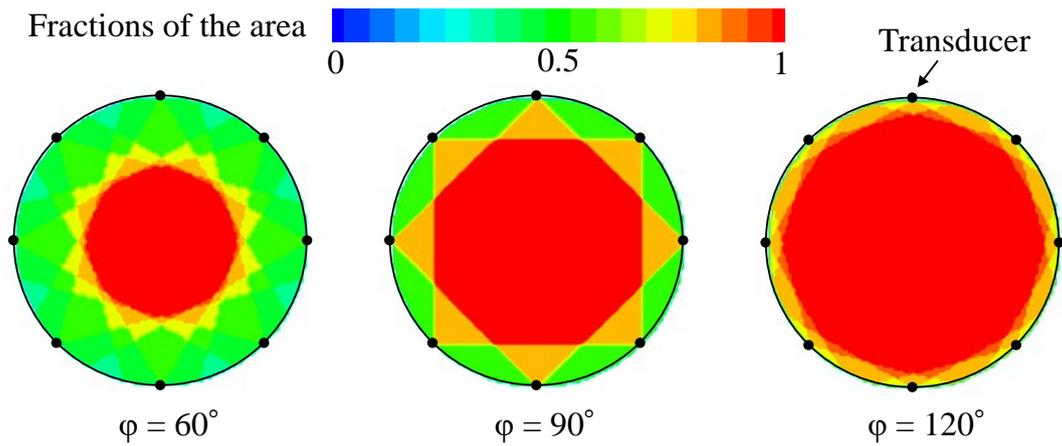


Fig. 2 Relationship between the coverage fractions of the area and the divergence angle,  $\varphi$ .

1

2 4. Ultrasonic transducer

3 Based on these considerations, a large divergence-angle ultrasonic transducer was developed,

4 as shown in Fig. 3. The transducer contains a piezoelectric element with a circular arc. The radius and

5 the arc angle are 5 mm and  $120^\circ$ , respectively. The height of the element is 5 mm and the resonant

6 frequency  $f_0$  is 5 MHz.

7

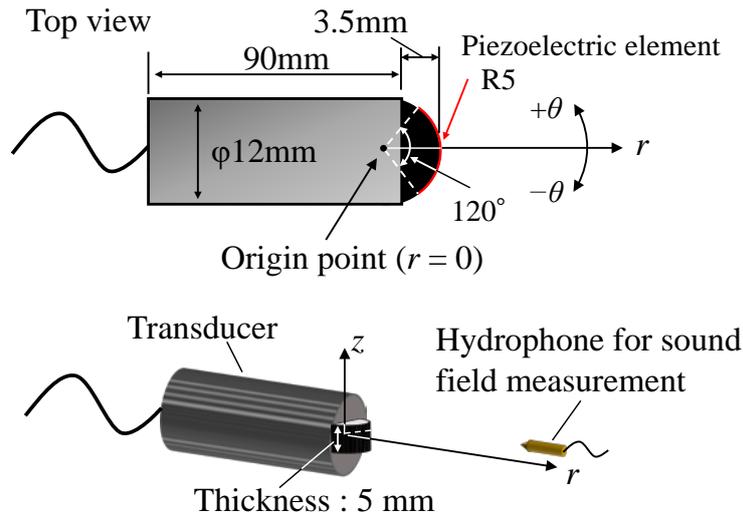


Fig. 3 Details of the large divergence-angle transducer with coordinate axes.

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The ultrasound field distribution of the transducer is investigated. We use a coordinate system

3

of the cylindrical coordinates  $r$ ,  $\theta$  and  $z$  which origin is set at the 5 mm behind the transducer surface, as

4

indicated in Fig. 3. The origin point is considered as the representative position of the transducer. A

5

needle hydrophone (model: HNC-0400, Onda Corp.) with an effective diameter of 0.4 mm was used for

6

the pulse reception. The ultrasonic transducer and the hydrophone were set in a box filled with water.

7

The ultrasonic transducer was connected to a pulser/receiver to emit ultrasonic pulses. The hydrophone

8

was connected to a digitizer (NI-5114, National Instruments Corp.) to record the signal. The hydrophone

9

was rotated around the point of origin so that the tip of the needle pointed towards the transducer. For

10

various positions of the hydrophone, the peak-to-peak signal amplitude,  $V_{pp}$ , was obtained from the

1 recorded signal at each position.

2 Fig. 4 shows the change in the sound pressure associated with varying  $\theta$  at  $r = 55$  mm.  $\bar{V}_{pp}$   
3 represents the peak-to-peak value of the sound pressure  $V_{pp}$  normalized to the maximum amplitude  
4 detected in the measurements. The profiles in Fig. 4 confirm that the sound pressure is almost constant  
5 between  $\theta = \pm 55^\circ$ . For values at  $\theta = \pm 65^\circ$ , the sound pressure decreases steeply. Fig. 5 shows the 2D  
6 sound pressure distribution at  $\theta = 0^\circ$ . The surface of the transducer is at  $r = 5$  mm. The ultrasound  
7 pressure gradually decreases with increasing distance from the transducer. However, the sound pressure  
8 is high in a range of  $\pm 2$  mm in  $z$ -direction, and no divergence and no large side-lobes of the ultrasonic  
9 field distribution are found. The results indicate that the developed transducer has an effective  
10 divergence angle of  $110^\circ$ , and the effective lateral dimension  $h_{us}$  is almost constant at 4 mm. It is  
11 confirmed that the large divergence-angle transducer would be suitable for use in reflection-mode  
12 tomography.

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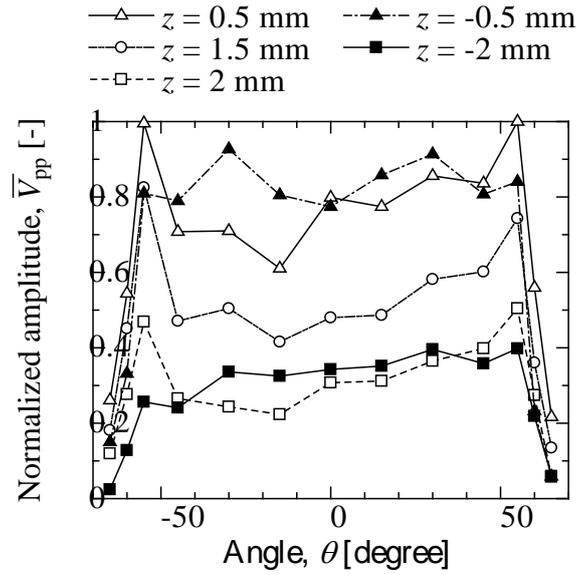


Fig. 4 Variation of normalized amplitudes of the sound pressure as a function of  $\theta$  at  $r = 55$  mm.

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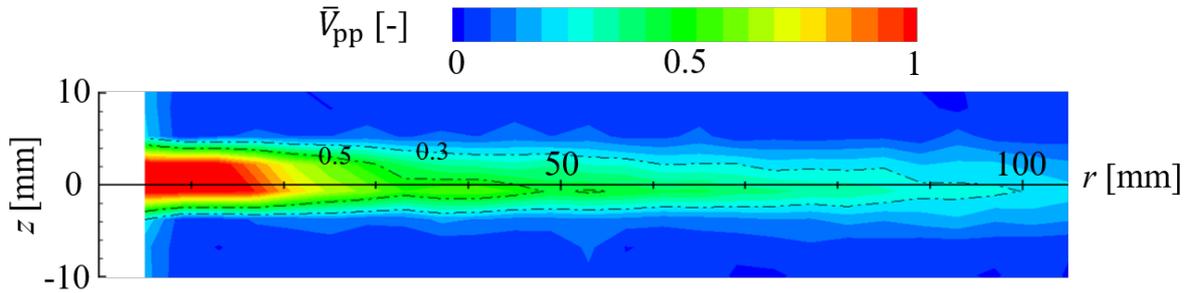


Fig. 5 Two-dimensional ultrasonic field distribution at  $\theta = 0^\circ$ .

3

4

5 5. Methodology

6 5.1 Reflection-mode tomography

7 This reflection-mode tomography relies on the intensity back projection of the pulse-echo

8 signals [17]. The first transducer emits a pulse, while the echo signals are received by all the transducers,

1 including the transmitter. In the course of the measurement, the active role of the transmitter alternates  
2 between the transducers, switching in sequence after each pulse emission, so that ultrasonic pulses are  
3 emanated from all transducers. This technique is known as full-matrix capture [30].

4 The signal intensity,  $V_p(\tau)$ , is calculated as the maximum amplitude of the received waveform  
5 at a transducer,  $V(\tau)$ , in the range  $\tau \pm \frac{T_0}{2}$ , where  $\tau$  is the TOF of the pulses and  $T_0$  is a period of the burst  
6 ultrasonic signals. It is necessary to remove all signals emitted by other sensors and propagating directly  
7 to the receivers, caused by multiple ultrasonic reflections in the measurement area and originating from  
8 echoes at the wall or the other sensors. To identify the echo signals from the liquid–gas interface, the  
9 difference in amplitude between the measured data and calibration data,  $V_{p,0}$ , is calculated to reduce  
10 these artifacts as follows:

$$V_{p,Cal}(\tau) = V_p(\tau) - V_{p,0}(\tau) \quad (2)$$

11  $V_{p,0}$  is the signal amplitude without bubble reflection, which is considered to be the base condition and  
12 is measured at the pipe filled with water.  $V_{p,Cal}(\tau)$  is calculated for each transmitter- $i$  and receiver- $j$   
13 pair and is referred to as  $V_{p,Cal_{i,j}}(\tau)$ .

14 Based on the transducer locations and the TOF,  $V_{p,Cal_{i,j}}(\tau)$  are linearly back-projected to

1 obtain the intensity distribution,  $I_{i,j}(x, y)$ . When a number of transducers,  $N_{tdx}$ , is used for the  
 2 measurement,  $N_{tdx} \times N_{tdx}$  echo signals are obtained. The final intensity distribution  $I(x, y)$  can be  
 3 expressed as follows:

$$I(x, y) = \sum_{i=1}^{N_{tdx}} \sum_{j=1}^{N_{tdx}} I_{i,j}(x, y) \quad (3)$$

4  $I(x, y)$  becomes large at positions where the reflection intensity is high, such as at the liquid–gas interface.  
 5 The higher intensity appears as an elliptical arc with focal points at the transmitter and receiver positions  
 6 in the cross-section. By overlapping the elliptic arcs calculated from the multiple echo signals in each  
 7 transducer, the shape of the bubble interface can be recognized as the higher intensity region. The elliptic  
 8 arcs appear at the bubble interface and at places where no bubbles exist. Therefore,  $I(x, y)$  can include  
 9 various artifacts. A weight distribution function,  $F(x, y)$ , is newly proposed to suppress the number of  
 10 artifacts. Fig. 6 shows a schematic of the calculation procedure for  $F(x, y)$ . The purpose of introducing  
 11  $F(x, y)$  is to eliminate the liquid-phase region from the bubble reconstruction region. If  $V_{p,Cal}(\tau)$  is  
 12 sufficiently high, the large amplitude of the signal can be considered as originating from the liquid–gas  
 13 interface. Here,  $\tau_{1,i,j}$  is defined at the earliest  $\tau$  when  $V_{p,i,j}(\tau)$  exceeds a  $V_{p,0}(\tau) \times 1.1$ . In this case,  
 14 the gas phase may be present in the region where the TOF between the transmitter, gas–liquid interface  
 15 and receiver is larger than  $\tau_{1,i,j}$ . Therefore,  $F_{i,j}(x, y)$  can be expressed as follows:

$$F_{i,j}(x, y) = \begin{cases} 1 & ((R_1 + R_2)/c \geq \tau_{1,i,j}) \\ 0 & (\text{otherwise}) \end{cases} \quad (4)$$

16 By adding  $F_{i,j}(x, y)$  for all transducers,  $F(x, y)$  can be obtained as follows:

$$F(x, y) = \sum_{i=1}^{N_{tdx}} \sum_{j=1}^{N_{tdx}} F_{i,j}(x, y) \quad (5)$$

- 1 To reduce the artifacts, a threshold,  $F_{th}$ , is applied to  $F(x, y)$ . If  $F(x, y)$  is lower than  $F_{th}$ , 0 is substituted
- 2 for  $F(x, y)$ . Ultimately, the cross-sectional intensity distribution  $I_R(x, y)$  can be calculated as follows:

$$I_R(x, y) = I(x, y) \times F(x, y) \quad (6)$$

- 3 The reconstructed 2D image is calculated when  $I_R(x, y)$  exceeds its threshold value of  $I_{Rth}$ , which
- 4 removes the artifacts with low signal intensities.

5

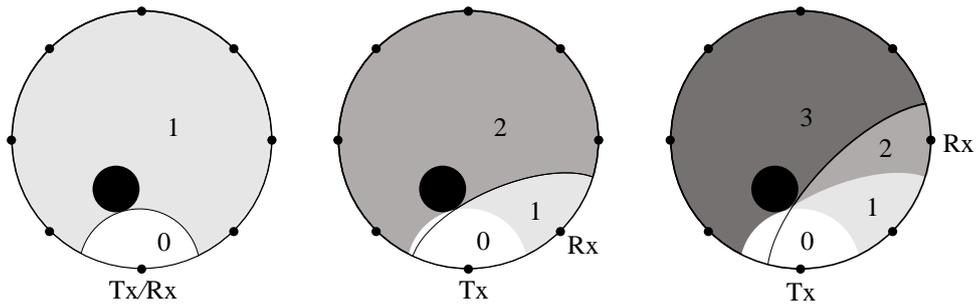


Fig. 6 Calculation of the weight distribution function,  $F(x, y)$ .

6

7

## 8 5.2 Design of the measuring system

9 A schematic of the measurement system is shown in Fig. 7. Eight transducers are used for the

10 measurements. The ultrasonic transducers are connected to a pulser/receiver (model: JPR-10C-8CH-KB,

11 Japan Probe Co. Ltd., Japan) containing eight channels for the emission of pulses and the reception of

1 signals. A digital I/O board (model: PXIe-6535, National Instruments Corporation, USA) is connected  
 2 to the external triggers on each channel to control the pulse emission interval. Echo-signals are recorded  
 3 using a high-speed digitizer (model: PXIe-5105, National Instruments Corporation, USA) with a  
 4 sampling rate of 30 MS/s (mega-samples per second). One-cycle 5 MHz burst are emitted as the  
 5 ultrasonic pulses. With this system, a full-matrix capture is possible with a minimum  $T_p$  of 5  $\mu$ s.

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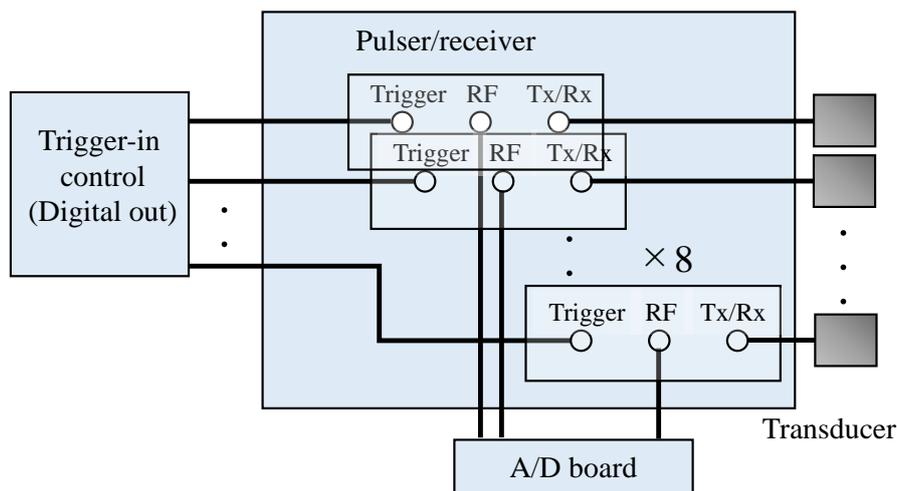


Fig. 7 Schematic of measurement system for reflection-mode tomography.

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8 Taking the TOF and the reverberation within the measurement area in the 50 mm pipe into  
 9 consideration,  $T_p$  was set to 0.125 ms, resulting in  $\Delta t = 1$  ms. With increasing measurement distance,  
 10  $T_p$  should increase owing to the growing TOF. All waveforms are stored in the high-speed digitizer's  
 11 on-board memory during the measurements. After the recording process has been completed, all  
 12 waveforms are transferred to a PC, where the post-processing reconstruction is performed. Under these

1 conditions, the maximum frame rate that could be achieved for the cross-sectional image is 1,000  
2 frames/s. The measurement interval for each cross-sectional measurement is set to 1 ms considering the  
3 bubble rising velocity and the on-board memory capacity. Therefore, 488 cross-sectional images are  
4 obtained during one measurement at 500 frames/s, which corresponds to 0.974 s for each measurement.

5 The experiments were carried out at room temperature (21–22 °C). The speed of sound in  
6 water is in the range of 1486–1489 m/s at this temperature. For a frequency  $f_0 = 5$  MHz, the wavelength  
7  $\lambda_0$  is 0.30 mm in water. The measurement area of  $50 \times 50$  mm<sup>2</sup> was divided into  $100 \times 100$  sections for  
8 reconstruction resulting in a spatial resolution of  $0.5 \times 0.5$  mm<sup>2</sup>.

9

10

## 11 6. Results and discussion

### 12 6.1 Detection of stationary rods

13 To evaluate the applicability of the system and the developed algorithm, stainless-steel rods  
14 with a diameter of 6 mm were used as a phantom for reconstructing an image. The rod length was  
15 sufficiently long in comparison with  $h_{us}$ .

16 Fig. 8 shows the results obtained from different test cases involving one, two, and three rods.  
17  $\bar{I}(x, y)$ ,  $\bar{F}(x, y)$ , and  $\bar{I}_R(x, y)$  are the respective values normalized to their corresponding maximum  
18 values. Due to the normalizations, the constant threshold values in  $\bar{F}_{th}$  and  $\bar{I}_{Rth}$  can be used for  
19  $\bar{F}_{th}(x, y)$  and  $\bar{I}_{Rth}(x, y)$ . In this case,  $\bar{F}_{th} = 0.9$  and  $\bar{I}_{Rth} = 0.2$  are determined by evaluating the  
20 reconstructed image of the rods. The black circles in Fig. 8(c) represent the real locations of the rod

1 surfaces. The rod locations are qualitatively derived from  $\bar{I}(x, y)$ . However, higher intensities are found  
2 in addition to the rod surface in  $\bar{I}(x, y)$  in the cases of 2- and 3-rod. It proves impossible to obtain the  
3 rod position from  $\bar{I}(x, y)$  alone, except for the single rod. As the number of rods increase, the average  
4 value of  $\bar{F}(x, y)$  increases. However,  $\bar{I}_R(x, y)$  can be used to reconstruct the rod locations in the 2-  
5 rod case. In the 3-rod case, artifacts appear between the rods. Because the difference in  $\bar{F}(x, y)$   
6 becomes small in terms of cross-sectional area with an increasing number of rods, artifact elimination  
7 is difficult using  $\bar{F}_{th}$ . Because  $N_{idx}$  is limited, the difficulty associated with the detection of a target  
8 behind other objects makes reconstruction of the image difficult. Two rods are clearly identified,  
9 whereas the detection becomes difficult in the case of three rods.

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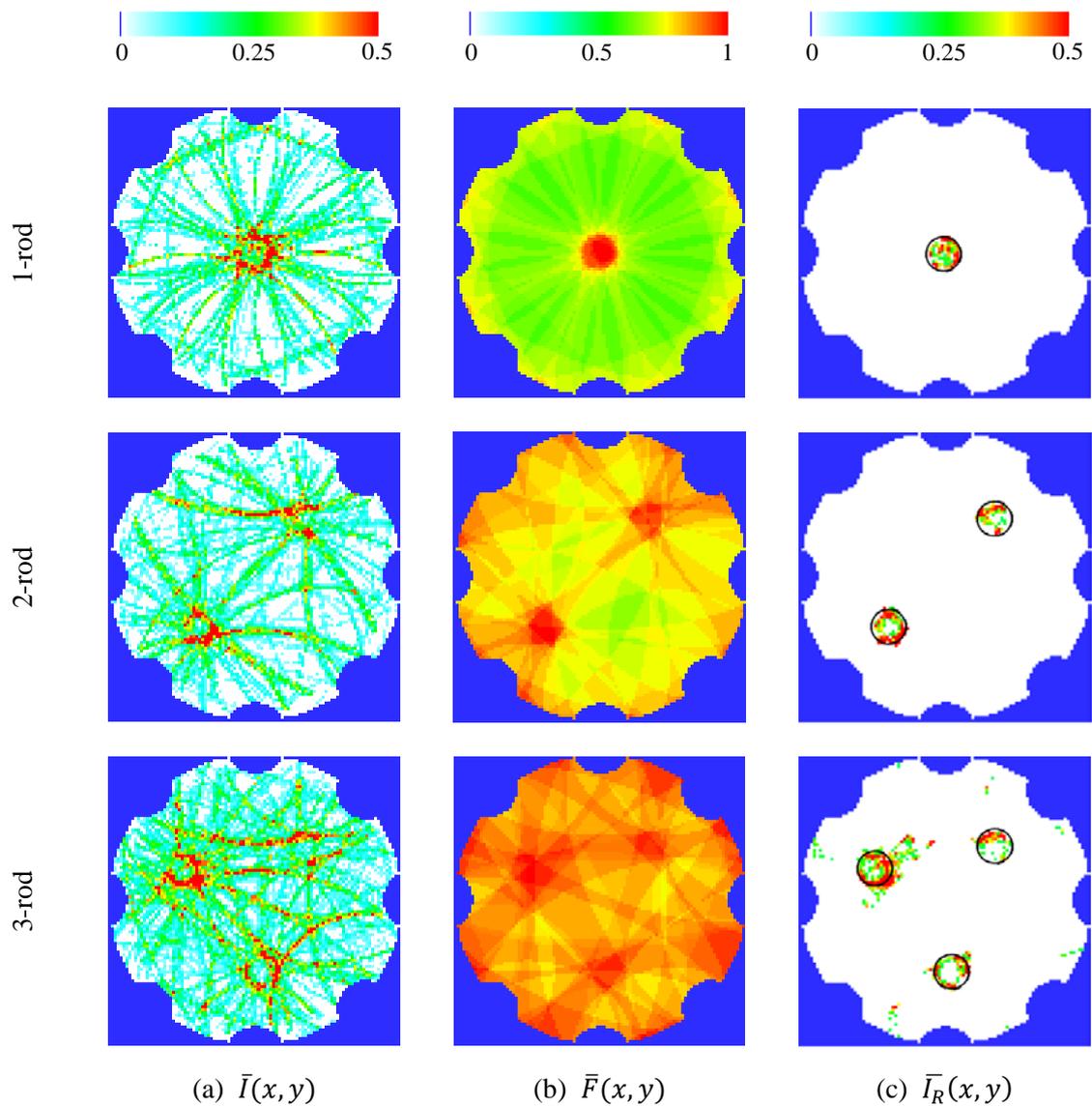


Fig. 8 Reconstruction results of  $\bar{I}(x, y)$ ,  $\bar{F}(x, y)$  and  $\bar{I}_R(x, y)$  for stationary rods.

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### 3 6.2 Detection of moving spheres

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Reconstruction tests were also performed using moving targets. In these experiments, a

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stainless-steel sphere with a diameter of 6 mm was employed, along with four different sizes of acrylic

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spheres with diameters ranging between 2.4 and 8.0 mm. Each sphere was dropped into the water from

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the top of the container.

1 Fig. 9 shows the reconstructed image of the moving stainless-steel sphere. The contour  
2 represents  $I_R$  normalized to the maximum value in the time-series of the reconstructed image. Typically,  
3 the maximum intensity appears when a sphere crosses the measurement volume. Therefore,  $\bar{I}_R(x, y)$   
4 becomes small if there is no reflector in the measurement volume, which makes it easier to eliminate  
5 the artifacts using  $\bar{I}_{R_{th}}$ . The outer shape of the sphere is clearly confirmed. The black circle represents  
6 the estimated shape. The average diameter of the sphere calculated from the reconstructed image is  
7 6.5 mm. Although the diameter is overestimated, the difference is almost identical to the spatial  
8 resolution. Displaying a pseudo 3D image of a continuously moving object is useful for easy recognition  
9 of the target. Here, the method used by Rahiman et al. [29] is applied. Fig. 10 shows the reconstruction  
10 of the pseudo 3D image of the stainless-steel sphere. In this experiment, the sphere's shape is identified  
11 in four consecutive frames. Because the tomography is performed at a frame rate of 500 frames/s, a  
12 tomography image can be plotted on the time axis every 2 ms. The color of the image frames is lineally  
13 interpolated. The resultant iso-intensity surface is shown in Fig. 10(b). As in the case of the stationary  
14 rods, threshold values of  $\bar{F}_{th} = 0.9$  and  $\bar{I}_{R_{th}} = 0.2$  are used. Average dropping velocity of the sphere  
15 at the measurement position is determined to be 0.70 m/s using the high-speed camera. The time step  
16 between the four images is 6 ms. Therefore, the equivalent moving distance of the stainless-steel sphere,  
17 *i.e.* average velocity  $\times$  detection time, becomes 4.2 mm. This distance is shorter than the sphere diameter  
18 of 6 mm.

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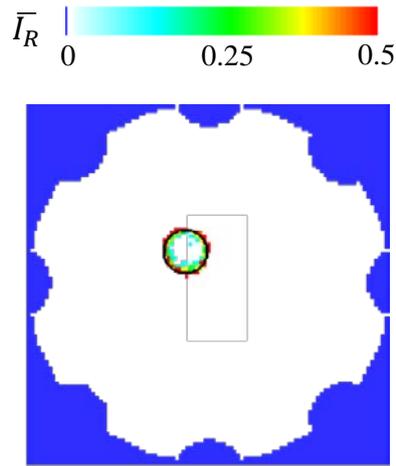


Fig. 9 A temporal reconstructed image of the moving stainless-steel sphere

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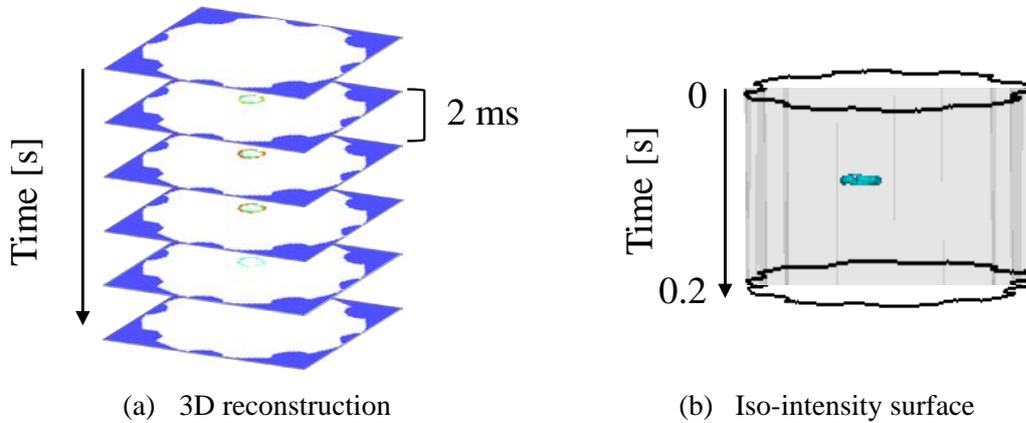


Fig. 10 Pseudo 3D image of the moving stainless-steel sphere.

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Fig. 11 shows the results for the acrylic spheres of varying diameter. When only one target is present in the measurement volume, the image can be correctly reconstructed for any diameter of the target. However, it is difficult to confirm a complete circular outline in all the frames. This shows that the interface could not be detected even though target objects are completely inside the measurement volume. The pseudo 3D image results are shown in Fig. 12. Although the measurement accuracy is not high in each frame, the sphere movement can clearly be reconstructed in the pseudo 3D images. The average velocity measured using the high-speed camera, the detection time of the sphere calculated from

1 the number of reconstructed images in which the sphere appears, and the equivalent moving distance  
 2 are summarized in Table 1. It is clear that the equivalent moving distance of the spherical targets is  
 3 shorter than the sphere diameter. As  $h_{us}$  is approximately 4 mm as shown in Fig. 4, it appears that the  
 4 high-intensity ultrasonic reflections only occur at a few points on the sphere. Because almost no  
 5 ultrasonic reflection originates when a sphere enters or leave the measurement volume, it is not easy to  
 6 detect the sphere's surface at these moments. Thus, it is considered that the detection time of the spheres  
 7 changes with  $h_{us}$ . However, the cross-sectional diameter and the position of the bubble can be detected  
 8 when the bubble center is in the measurement volume.

9

Table 1 Relation between the acrylic sphere diameters, velocities and the detection time using the UT.

Sphere diameter	Average velocity	Detection time of the spheres	Equivalent moving distance
2.4 mm	0.051 m/s	38 ms	1.9 mm
4.0 mm	0.070 m/s	34 ms	2.4 mm
6.4 mm	0.087 m/s	30 ms	2.6 mm
7.9 mm	0.097 m/s	32 ms	3.1 mm

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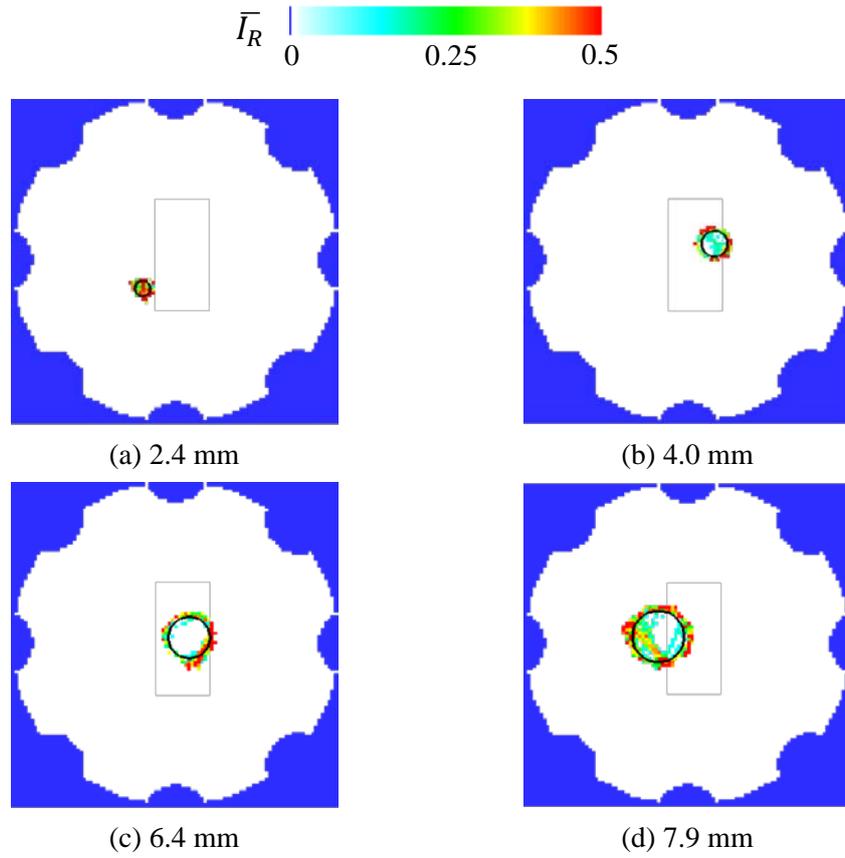


Fig. 11 Reconstructed images of acrylic spheres with different diameters.

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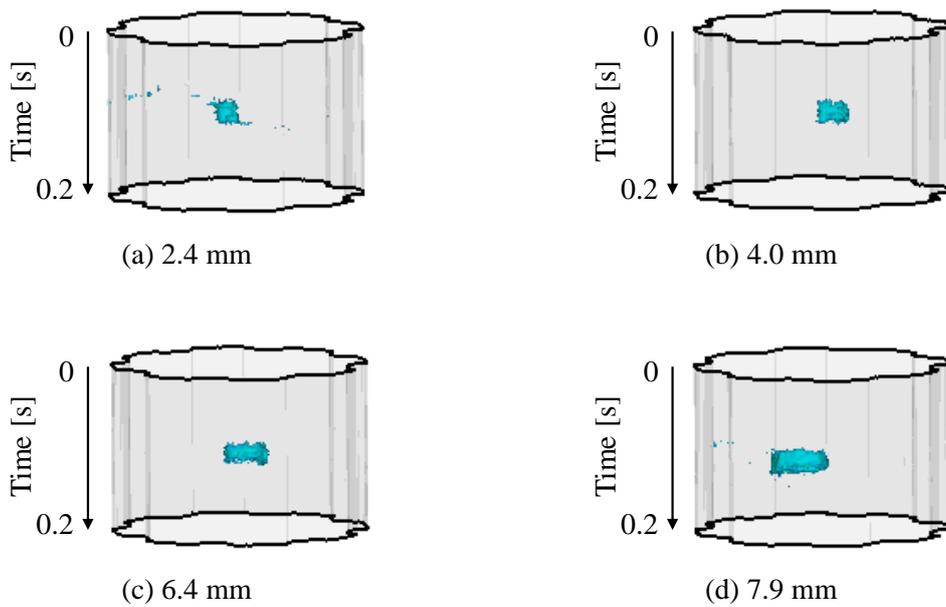


Fig. 12 Pseudo 3D images of acrylic spheres.

### 1 6.3 Bubble chain in a container

2 Argon gas was injected via the bottom nozzle at a flow rate,  $Q$ , of 15, 30, 60, and 120 sccm.  
3 Fig. 13 shows the pseudo 3D image at  $Q = 120$  sccm between 0 and 0.974 sec. The threshold values as  
4 used so far for the stainless-steel rods and the moving spheres,  $\bar{F}_{th} = 0.9$  and  $\bar{I}_{Rth} = 0.2$ , are  
5 maintained here. It can be confirmed that scattering noises are detected over the measurement period.  
6 These noises are mainly due to the liquid–gas interfaces. As the number of bubbles increases, multiple  
7 reflections between bubbles causes noise in the pseudo 3D image.

8 A significant reduction of the scattering noise can be achieved by optimizing the threshold  
9 values  $\bar{F}_{th}$  and  $\bar{I}_{Rth}$ . A time-series filtering method is suggested to facilitate the threshold  
10 determination. Fig. 14 shows a schematic of the filtering process. Because the bubble velocity ranges  
11 between 0.2–0.3 m/s, it can be expected that the echo signals from the bubble appear in more than six  
12 continuous frames. The temporal change in  $\bar{I}_R$  at a particular position is shown schematically in the  
13 Fig. 14. If a bubble moves into this domain,  $\bar{I}_R$  becomes large due to the ultrasonic reflection at the  
14 interface. The average intensity,  $\bar{I}_{ave}$ , and its standard deviation  $\bar{I}_\sigma$  are calculated for each cross-  
15 sectional position  $(x, y)$  from the time-series data to detect the higher intensity of the signal. It is assumed  
16 that the number of frames, where bubbles are detected at the position  $(x, y)$ , is smaller than the total  
17 number of frames. The following equation is used for  $\bar{I}_{th}(x, y)$  instead of using the constant value:

$$\bar{I}_{th}(x, y) = \bar{I}_{ave}(x, y) + 2\bar{I}_\sigma(x, y) \quad (7)$$

18 If  $\bar{I}_R(x, y, t_0)$  is larger than  $\bar{I}_{th}(x, y)$ , the range of  $t$ , where  $\bar{I}_R(x, y, t)$  is larger than  $\bar{I}_{ave}(x, y)$ , should

1 be defined by the start time  $t_1$  and the end time  $t_2$  ( $t_1 \leq t_0 \leq t_2$ ). In this case,  $\bar{I}_R(x, y, t)$  is considered  
2 to contain bubble associated data only in the range of  $t_1 \leq t \leq t_2$ , while the other data is filtered out.  
3 A sample of the time-series data at the center of the column is shown in Fig. 15(a). A three-period  
4 moving average is applied to  $\bar{I}_R$ . Fig. 15(b) shows the data after the filtering process. Some data points  
5 that are lower than  $\bar{I}_{th}$  but larger than  $\bar{I}_{ave}$  appear. These data are classified as scattering noise. It is  
6 also confirmed that the number of time-series data is limited when  $\bar{I}_R$  is larger than  $\bar{I}_{th}$ . Moreover,  $\bar{I}_R$   
7 gradually increases when a bubble enters the measurement volume and decreases when the bubble leaves.  
8 If the noise has been cancelled using a constant threshold value, liquid–gas interface data at lower  
9 intensity occurring when bubbles enter or leave the measurement volume can be inadvertently  
10 eliminated. However, this filtering method prevents the elimination of these data.  
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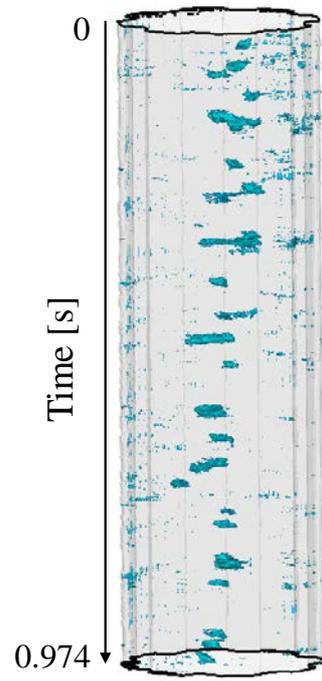


Fig. 13 Pseudo 3D image at  $Q = 120$  sccm without the time-series filtering.

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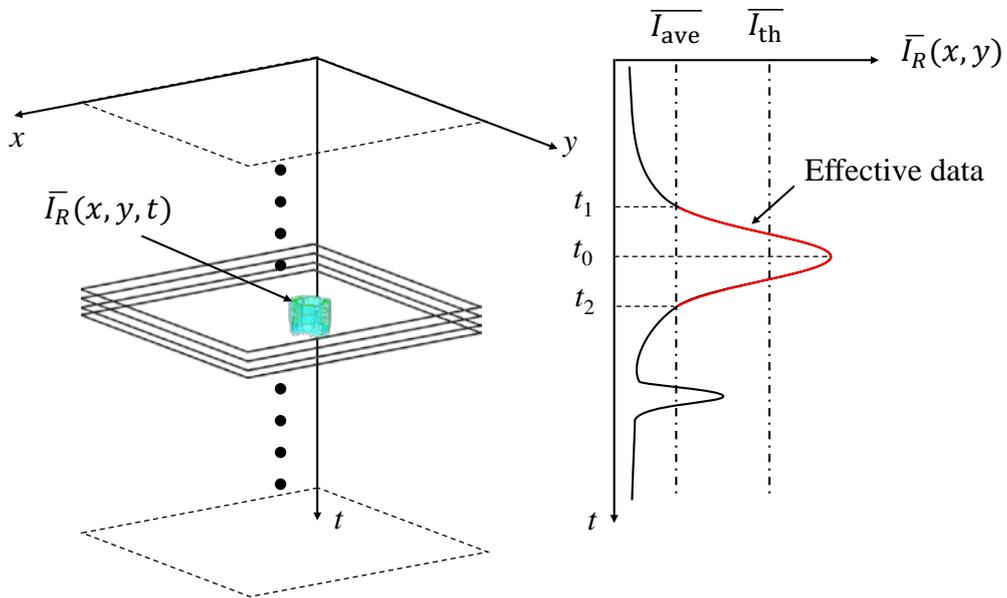
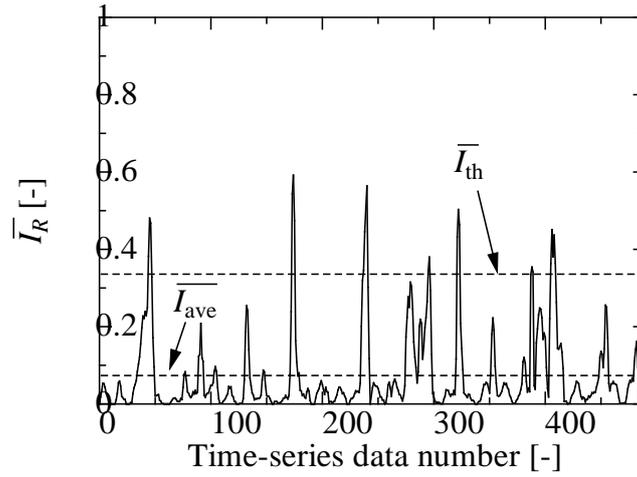
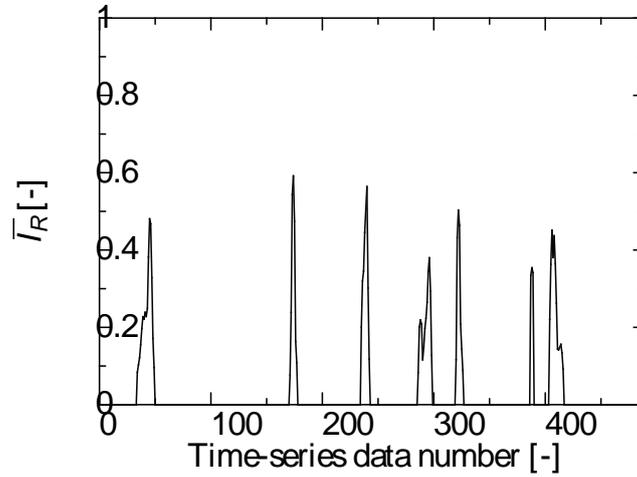


Fig. 14 Schematic of the time-series filtering.

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(a) Non-filtered data



(b) Filtered data

Fig. 15 Applying the time-series filtering to  $\bar{I}_R$ .

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Fig. 16 displays the resultant pseudo 3D images after the time-series filtering along with

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synchronized images obtained by the high-speed camera. The noise level is distinctly reduced, as shown

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for  $Q = 120$  sccm. Since the vertical axes between the pseudo 3D image and the camera image are

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different, the shape of bubbles cannot be compared directly. However, it can be confirmed that the time-

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series filtering prevents the excessive elimination of valid bubble interface data. Because the scattering

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noise is not significant at low flow rates, the time-series filtering is effective particularly for higher flow

1 rate conditions, *i.e.*, 60 and 120 sccm. The frequency of bubble detachment from the injection nozzle  
2 was confirmed to be almost constant at  $Q = 15\text{--}120$  sccm from the visual observation. Based on the  
3 number of bubbles and the flow rate, the volume equivalent bubble diameter is found to be 4.3–4.5 mm  
4 under these conditions.

5           Due to the limited number of transducers, it is difficult to completely reconstruct the outlines  
6 of bubbles in all frames. However, the high frame rate of the UT enables the reconstruction of pseudo  
7 3D images providing valuable information about the bubble motion which also allows for a qualitative  
8 assessment of the bubble distribution in the cross-section. A comparison of the results from the UT and  
9 synchronized images obtained by the high-speed camera demonstrates that the UT can detect  
10 continuously rising bubble movements, such as for  $Q = 15$  and 30 sccm. Further information regarding  
11 the direction of bubble movement or bubble deformation can also be obtained. Owing to the higher  
12 frame rate and the smaller  $h_{us}$ , bubble shape and movement can be clearly determined by UT from the  
13 3D images, even if the shape of the liquid–gas interface changes over time. The distances between the  
14 bubbles become smaller for higher gas flow rates. The images obtained at 120 sccm reveal many  
15 situations where some bubbles come close to each other. When two or three bubbles are present in the  
16 measurement volume, the number of artifacts and the noise level increase. However, the bubble position  
17 and distribution in the cross-section can be qualitatively obtained.

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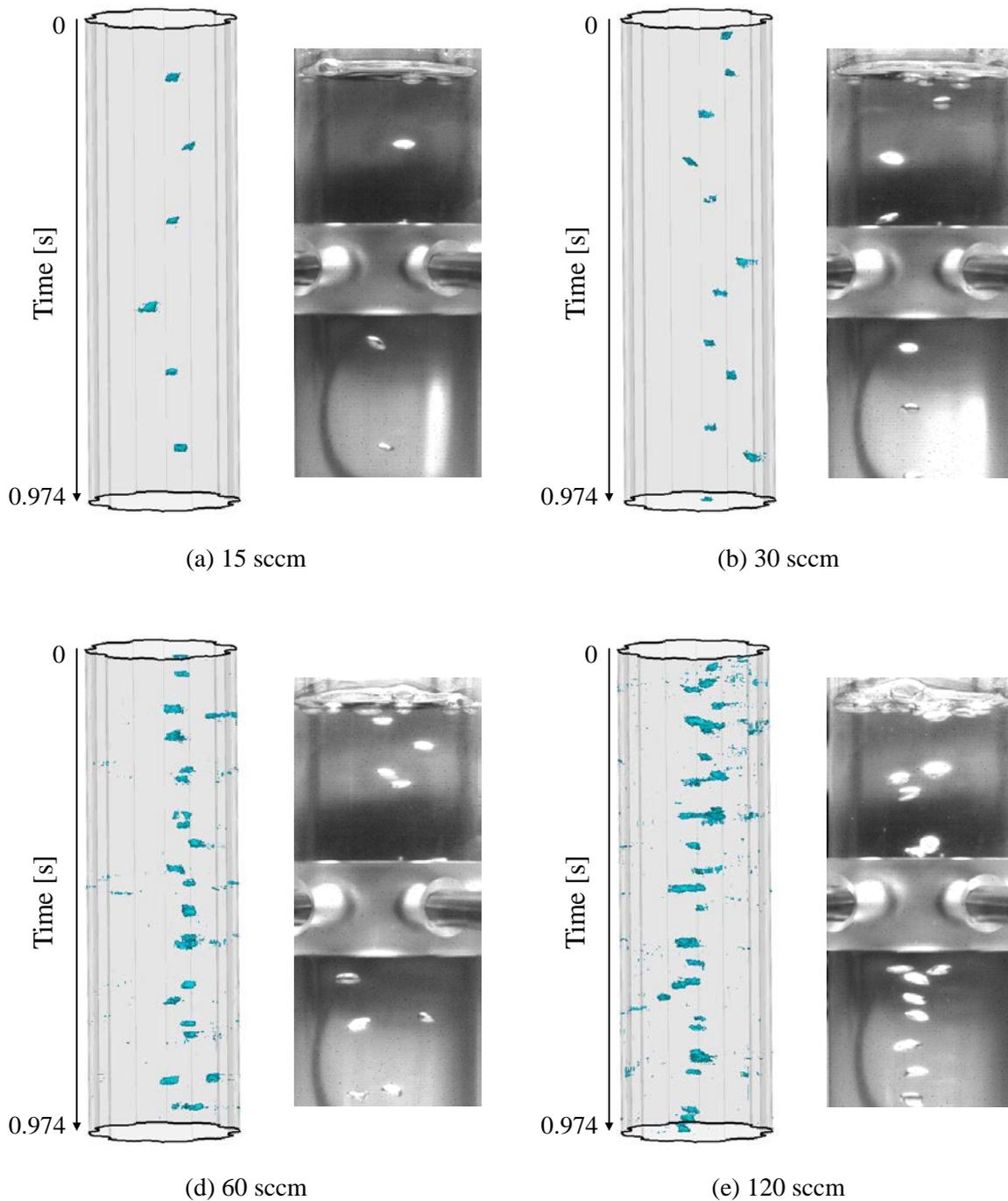


Fig. 16 Pseudo 3D image from UT measurements of a bubble column

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3 7. Conclusions

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A new UT system was proposed for detecting and studying the motion of bubble chains in a

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liquid. An ultrasonic transducer with a large divergence angle of  $110^\circ$  and vertical height of measuring

1 volume of approximately 4 mm was developed for use in reflection-mode tomography. Ultrasonic back-  
2 projection was used for the reconstruction of bubble shapes. In addition, the weight distribution function  
3 was applied to eliminate the artifacts caused by the liquid–gas interface. Furthermore, a time-series  
4 filtering method was shown to be appropriate to eliminate scattering noise in the tomography data. The  
5 UT system includes eight transducers to measure the two-phase flow in a container with an inner  
6 diameter of 50 mm. Because the pulse transmission interval is set to 0.125  $\mu$ s, a temporal resolution of  
7 1 ms is achieved. The system can detect cross-sectional images at frame rates up to 1,000 frames/s. A  
8 sphere moving at 0.7 m/s was successfully detected at 500 frames/s. The use of a restricted number of  
9 transducers limits the accuracy of the reconstructed cross-sectional images. However, the location of the  
10 bubbles can be qualitatively obtained from the pseudo 3D image. If more than 3 bubbles are located  
11 within the measurement volume, it is difficult to distinguish the bubbles and follow their outlines clearly.  
12 However, the system is capable for qualitative observations, such as motion of bubble chains and  
13 deformation of the bubble interface.

14 Because the velocity information is not included in the pseudo 3D image, there is no  
15 information about the bubble height. However, if the UT measurements are performed simultaneously  
16 on two planes with a small intervening distance between them, the velocity information can be obtained  
17 by analyzing the time offset in the cross-sectional images between both planes. Furthermore, UT can be  
18 used to evaluate bubble coalescence and bubble interaction if the inlet conditions are known.

19

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